

Cause and Impact of Low-Frequency Chirping Modes in DIII-D Hybrid Discharges

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C.C. Petty⁵, F. Turco⁶ and M. A. Van Zeeland⁵

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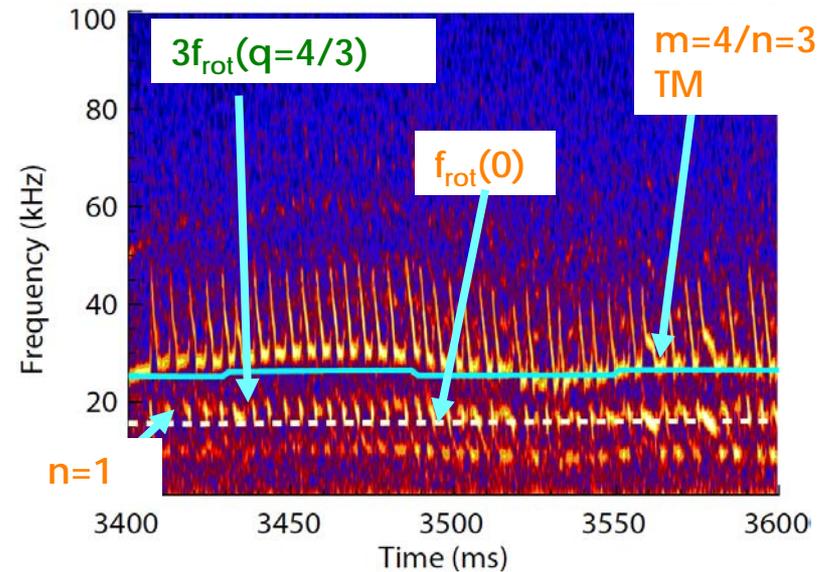
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³Dalian University of Technology

⁴Zhejiang University

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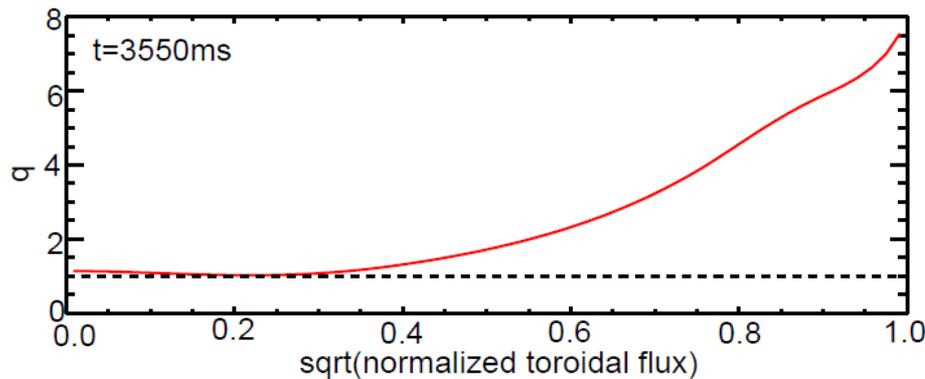
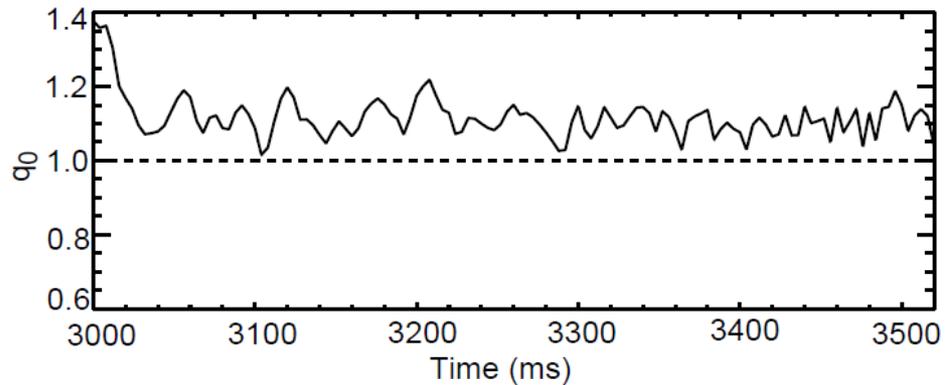
⁶Columbia University



16th Technical Meeting on Energetic Particles in Magnetic
Confinement Systems – Theory of Plasma Instabilities

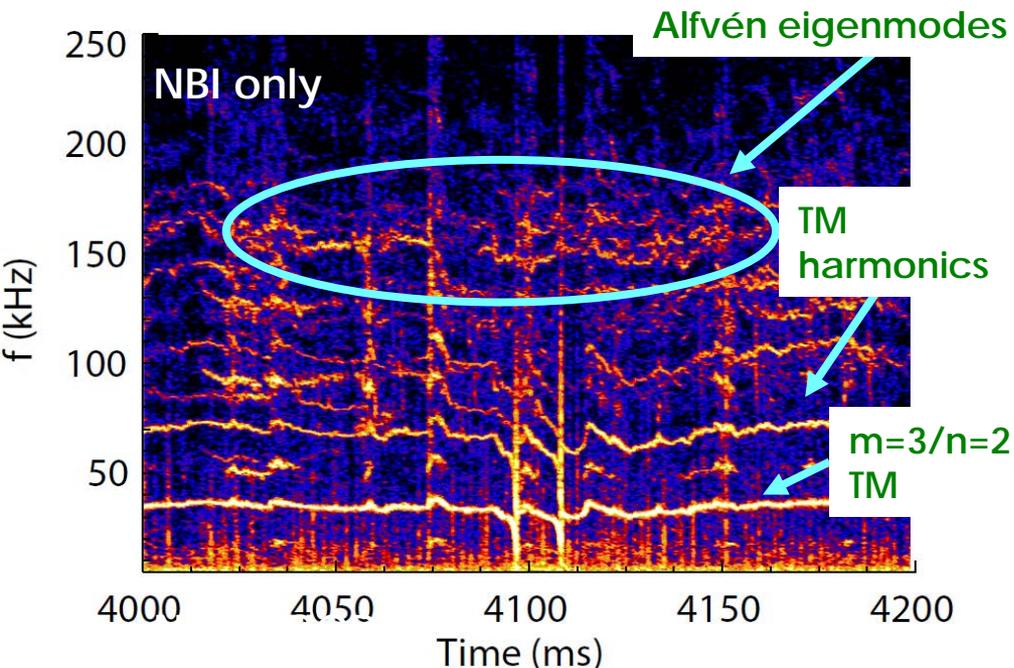
Shizuoka City, Japan
September 3-6, 2019

Significant Variations of Fast-ion Instabilities Observed in Hybrid Discharges with Electron Cyclotron (EC) Waves



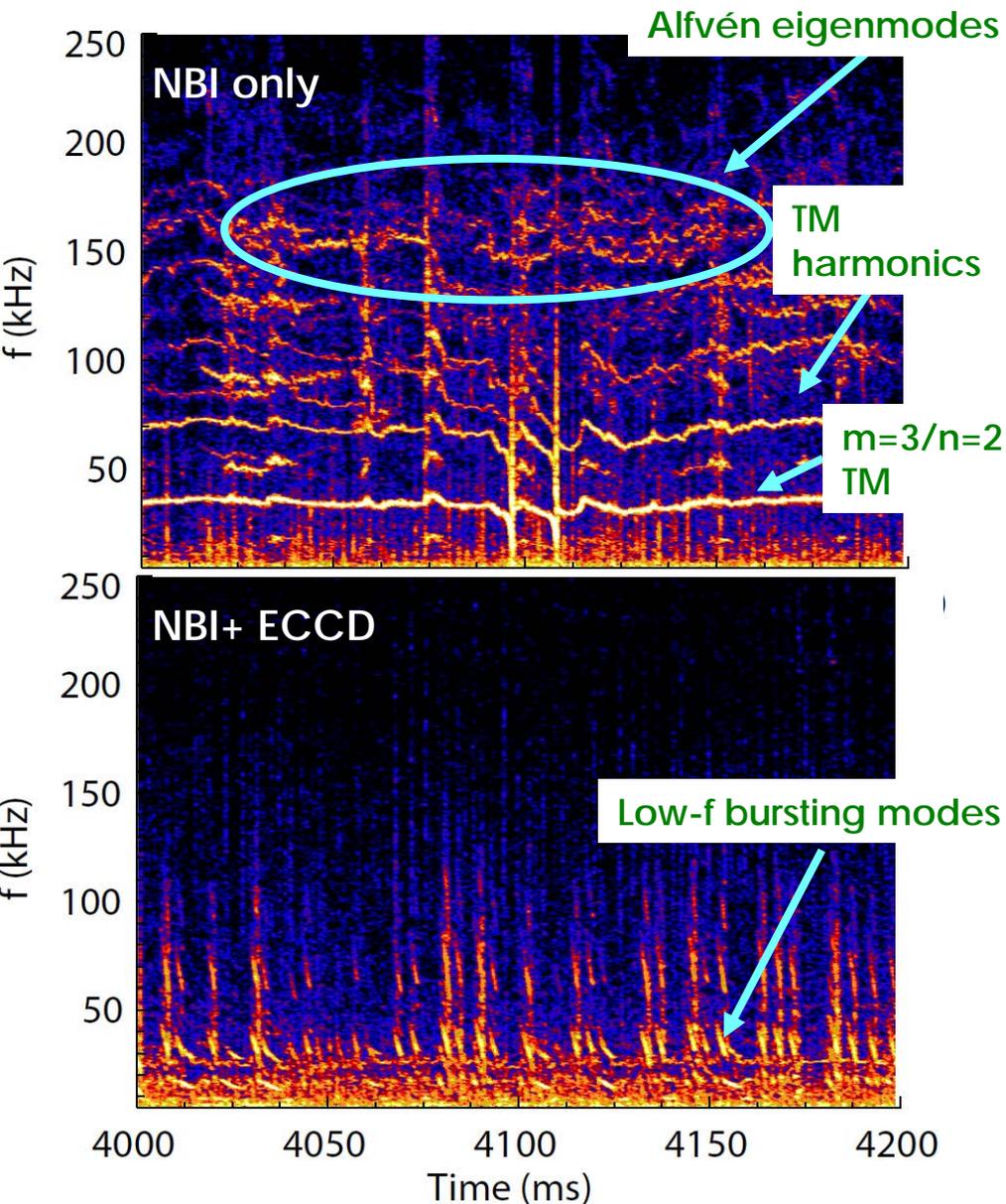
- Hybrid: long duration, high performance & steady H-mode; viable scenario for ITER operation
- Steady tearing mode (TM) often present; modest reduction in particle and energy confinement
- low magnetic shear in the core with q_0 close to unity

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 - AEs could be TAE/EAE/BAE
 - D_f of 1.0-2.0 m²/s needed to match classical neutron rate

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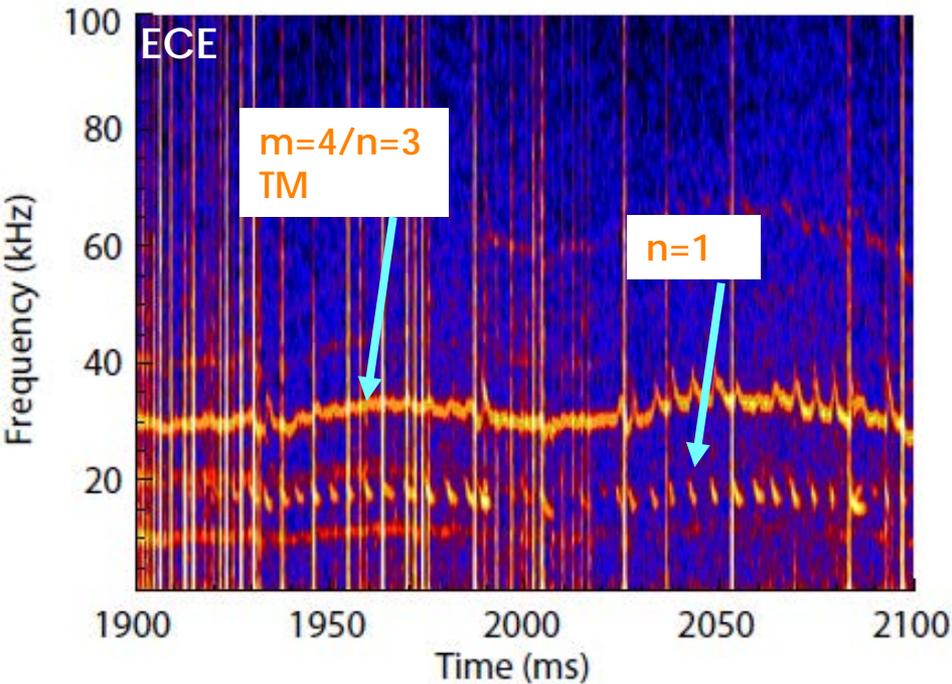
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 - AEs could be TAE/EAE/BAE
 - D_f of 1.0-2.0m²/s needed to match classical neutron rate
- With NBI and EC, AE activity often became weaker/suppressed; low-f bursting modes appear.
 - D_f of 0.5-1.0m²/s needed to match classical neutron rate

Outline

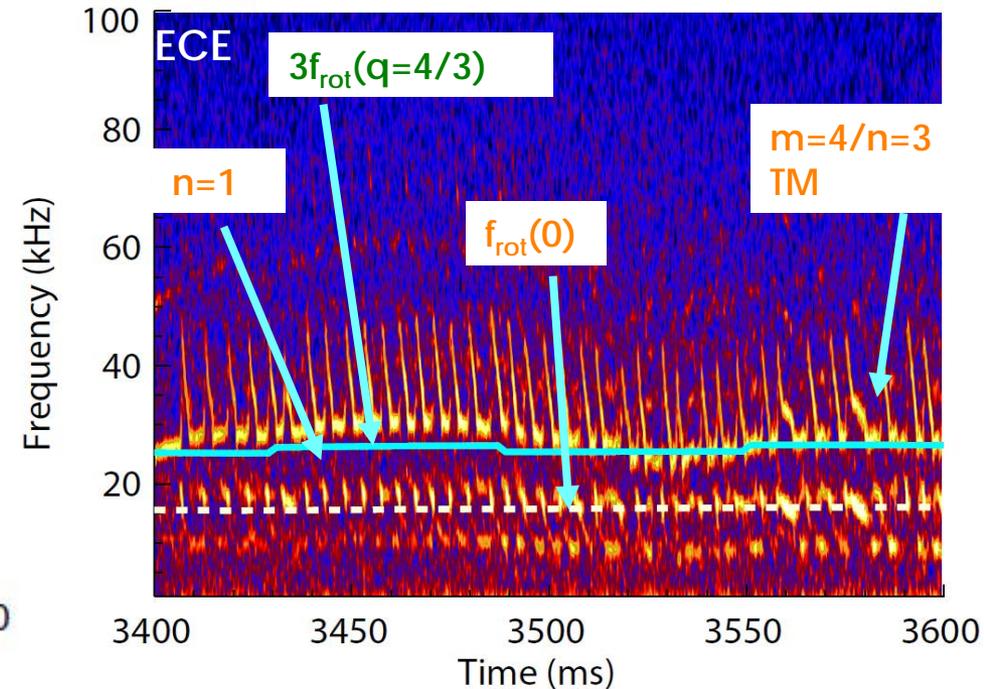
- **Experimental observations and database study**
 - With NBI + EC, AE → low-f bursting modes
 - low-f bursting modes are usually chirping TM; occasionally fishbones
- **Hypotheses and modelling for the instability transition**
 - Large (trapped) fast-ion population responsible for the transition
- **Impact and plausible reasons for low-f bursting modes**
 - Fast ion losses observed only when n=1 mode is large
 - TM & fishbones interplay through fast-ion channeling in phase space
- **Summary and future work**
- ❖ **Goal: understand fast-ion instabilities in hybrids & their interaction with TM to improve the plasma performance**

Low-Frequency Bursting Mode can be Chirping Tearing Mode (TM) or Fishbones

Early time



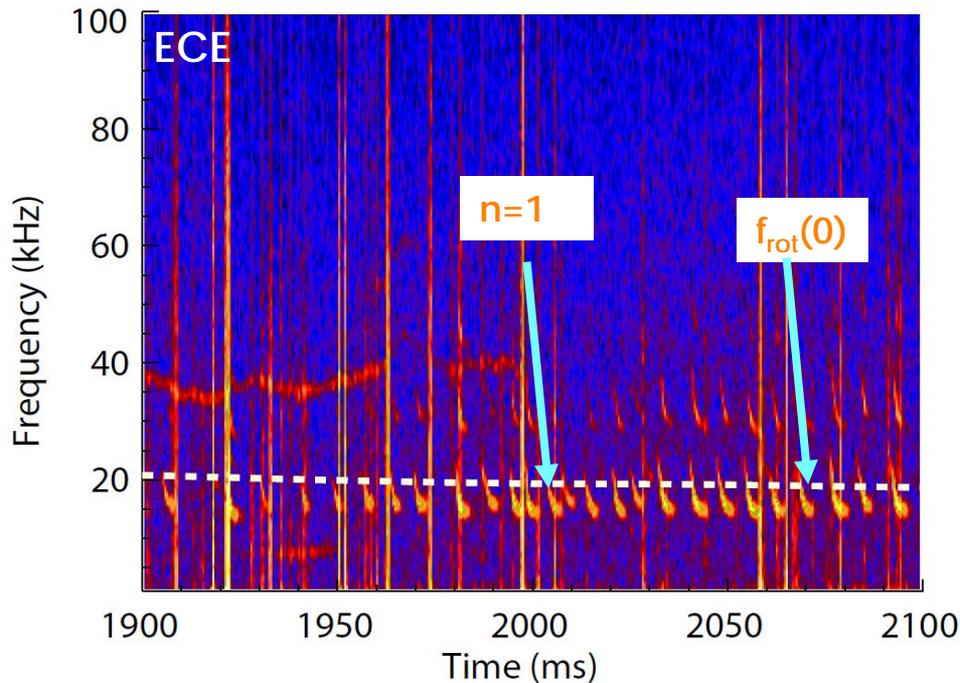
Later time



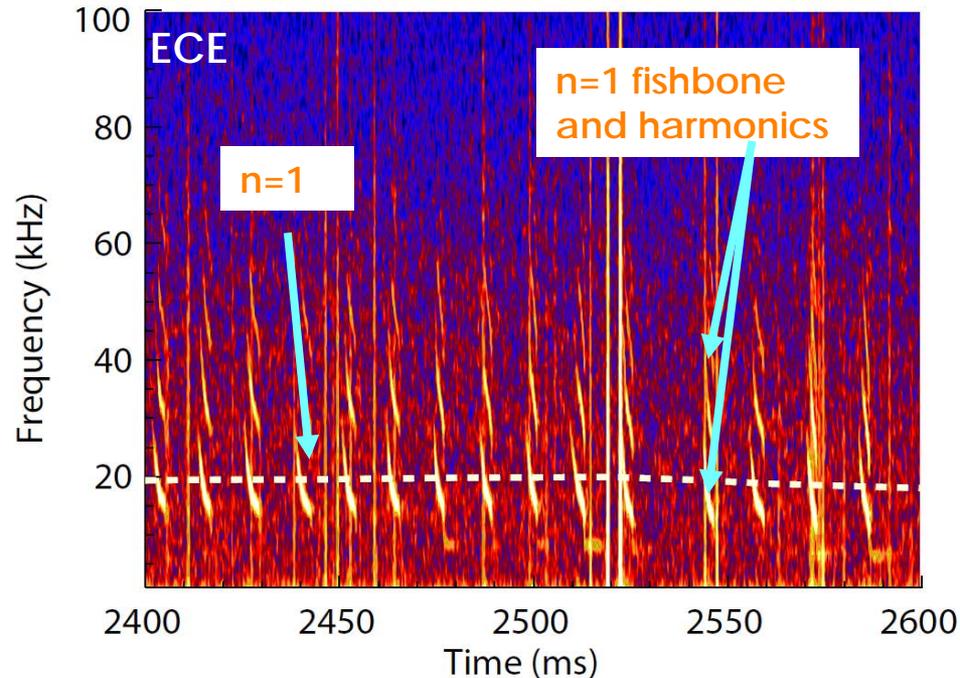
- NBI starts at 1500ms, EC starts at $t=1700$ ms, steady TM at 1725ms
- Fishbones appear at $t=1750$ ms, co-exist with steady TM
- $t > 2025$ ms, TM frequency abruptly jumps up and then chirps down within 1ms
- Note: $n=1$ mode can be very weak, sometimes only visible in magnetics

Low-Frequency Bursting Mode can be Chirping TM or Fishbones (Cont'd)

Early time

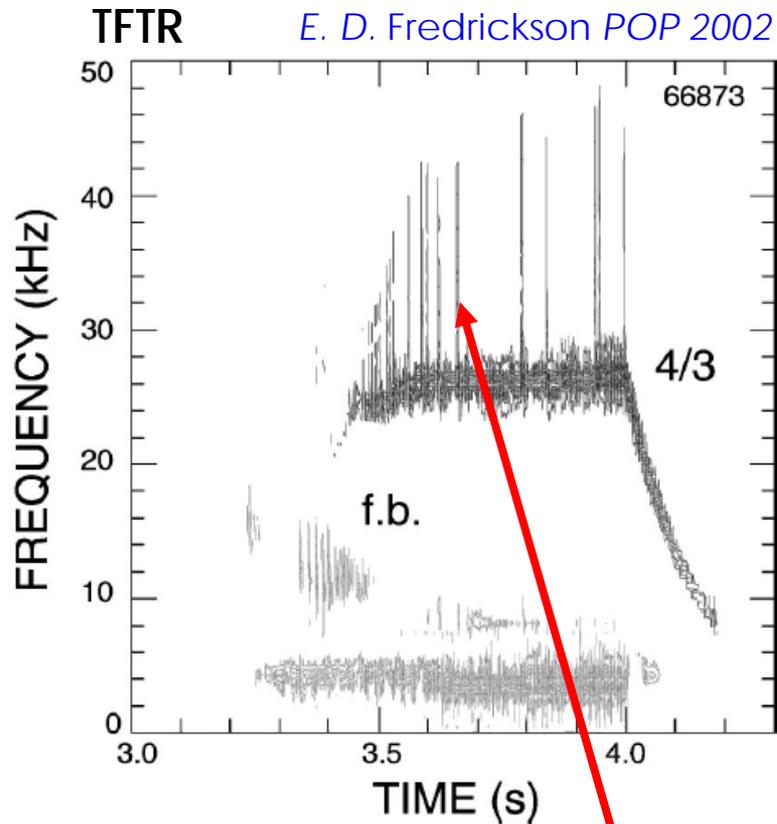


Later time



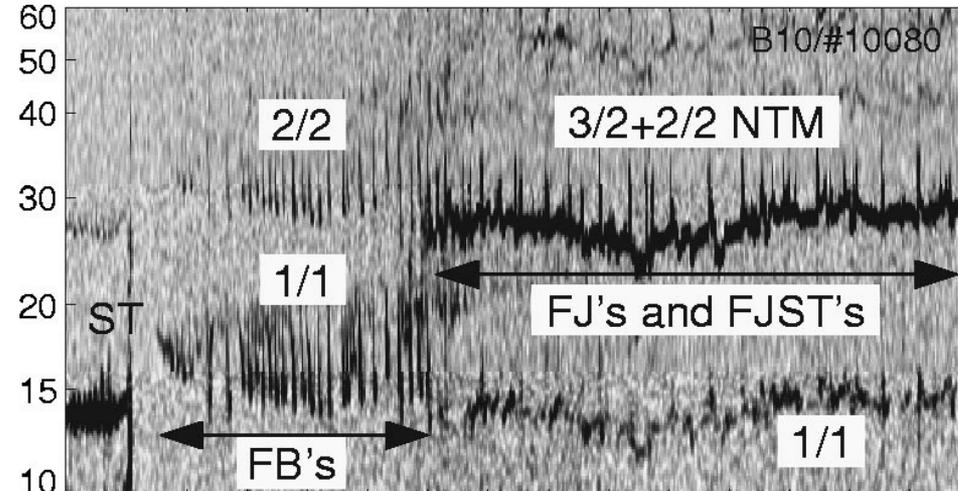
- TM and fishbones co-exist at the beginning, and then TM is suppressed (at $t=1960\text{ms}$). Harmonics of $n=1$ start to appear.
- Relatively rare in the database (3 shots only)

Chirping TM has been Observed on Other Facilities but not well Understood



- TFTR: NTM frequency jumps up and chirps down

S. Gunter NF 1999, Sesnic POP 2000



ASDEX-Upgrade

- ASDEX: Fishbones initiate NTM. Frequency jumps up and chirps down with a typical repetition frequency of fishbone
- Chirping TM was also observed in HL-2A (*Chen NF 2019*), EAST (*Li PPCF 2016*)

A Database is Built to Study the Cause of Variation of Instabilities in Hybrid Plasmas

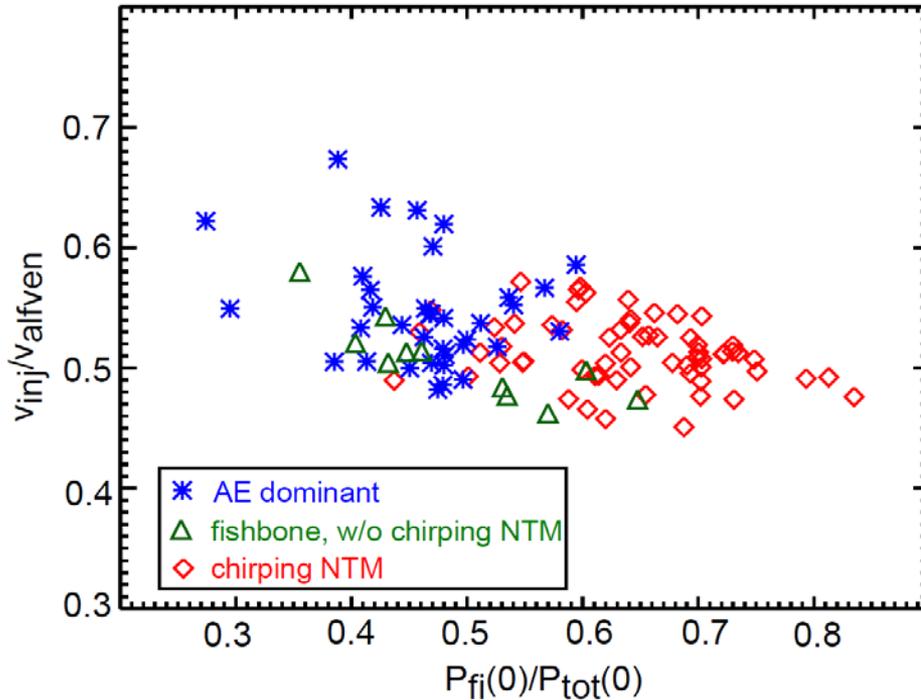
➤ Summary of observations

- **AEs:** in NBI-only or early phase of NBI+EC discharges
- **Low-f bursting modes:** 200-300 ms after EC; rare in low torque hybrids with counter-NBI or high-density hybrids.

➤ The database include

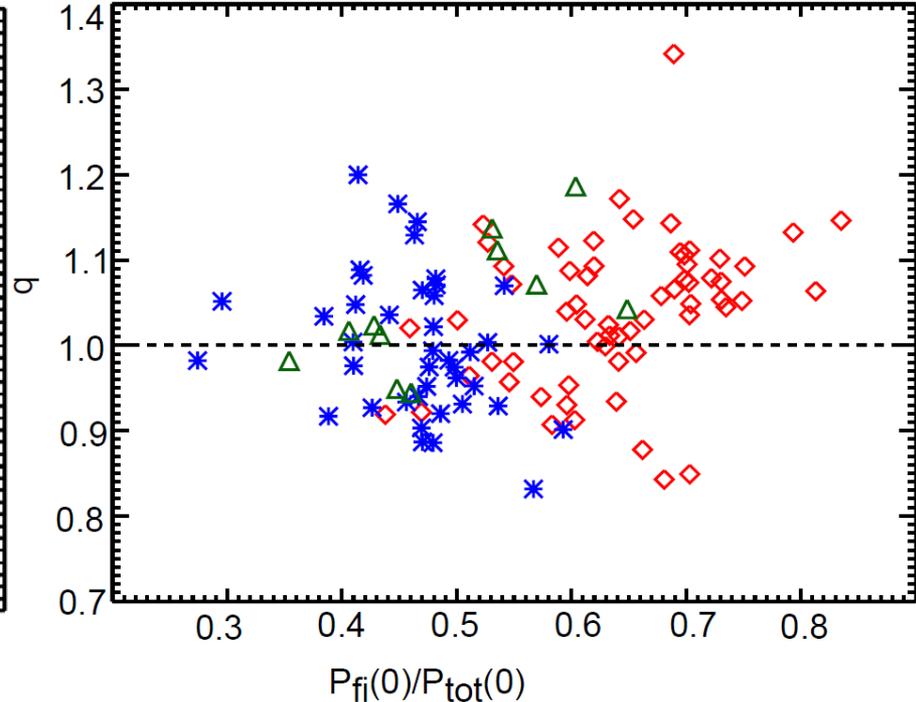
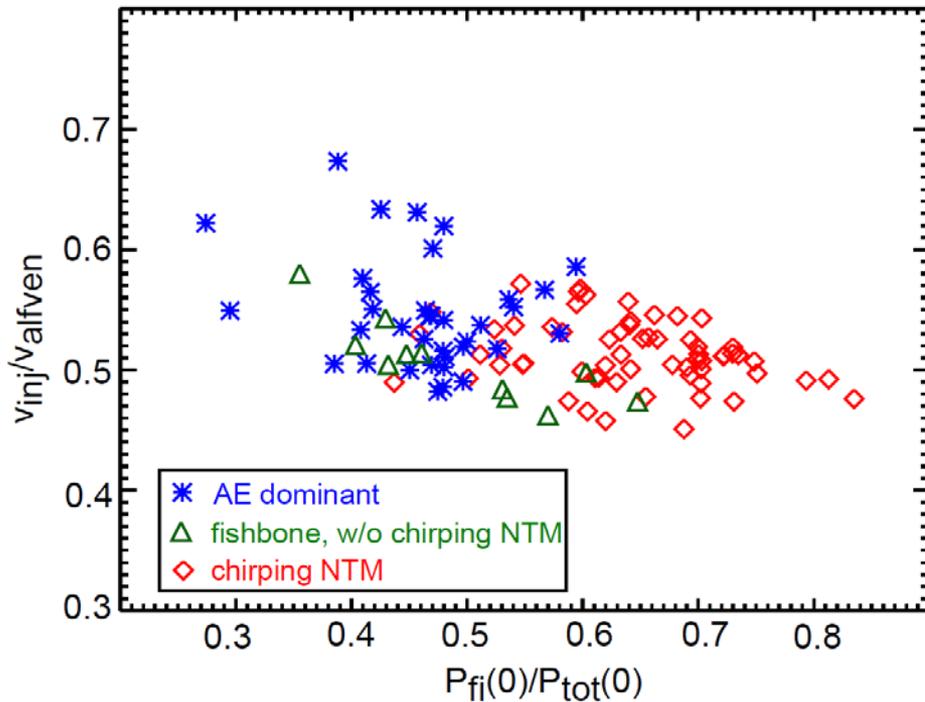
- 4-5 time slices per shot, totally 40 hybrid shots
- Flags for steady TM, chirping TM, fishbone, AE, ELM
- P_{NBI} , P_{EC} , q profile from efit02 with E_r correction
- Plasma/fast-ion pressure and beta, fast ion density ... are extracted from TRANSP runs that assume classical fast ion behavior

The Database Suggests that Occurrence of Low-Frequency Bursting Mode is Mainly due to Large Fast Ion Population



- AE: $P_{fi}(0)/P_{tot}(0) \sim 0.3-0.5$ and $v_{inj}/v_{alfven} > 0.6$
- Low-frequency bursting modes: $P_{fi}(0)/P_{tot}(0) > 0.5$ and $v_{inj}/v_{alfven} < 0.6$. Pure fishbones (w/o chirping NTM) seem in the transition region.

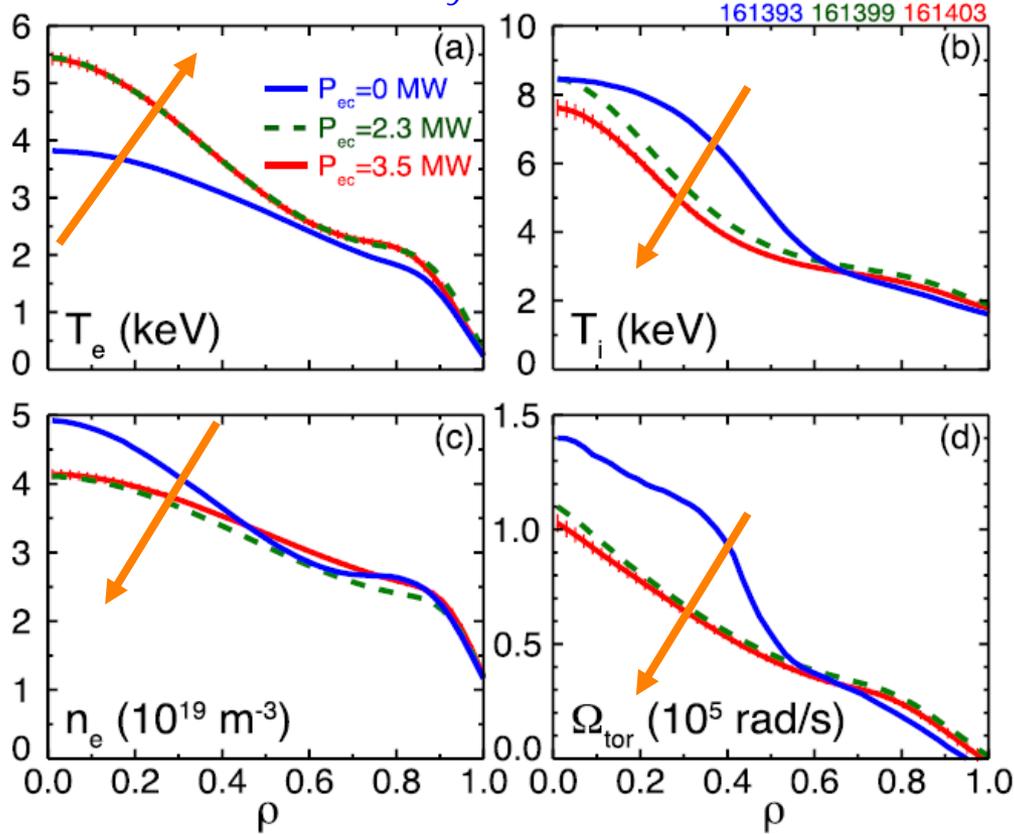
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- Not well separated by q_0

Plasma during ECCD/ECH Always Evolves toward Higher Electron Temperature and Lower Density

C. C. Petty NF 2017

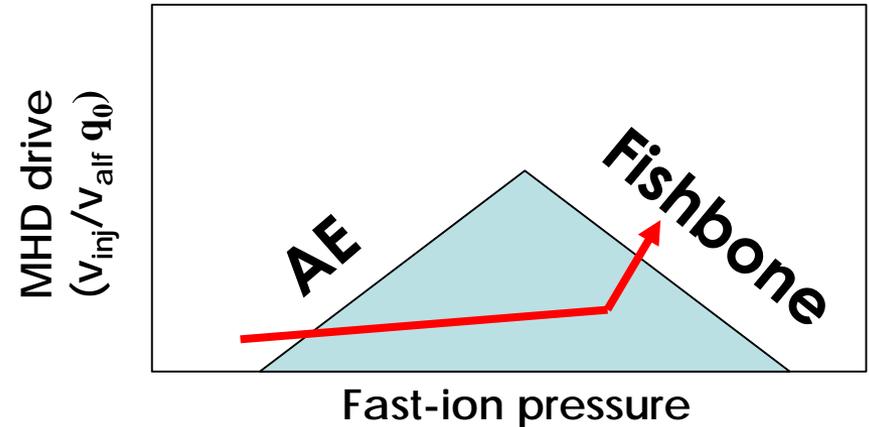


Higher temperature and lower density during EC phase result in an increase of fast-ion slowing-down time

- large (trapped) fast-ion population
- large drive for fishbones

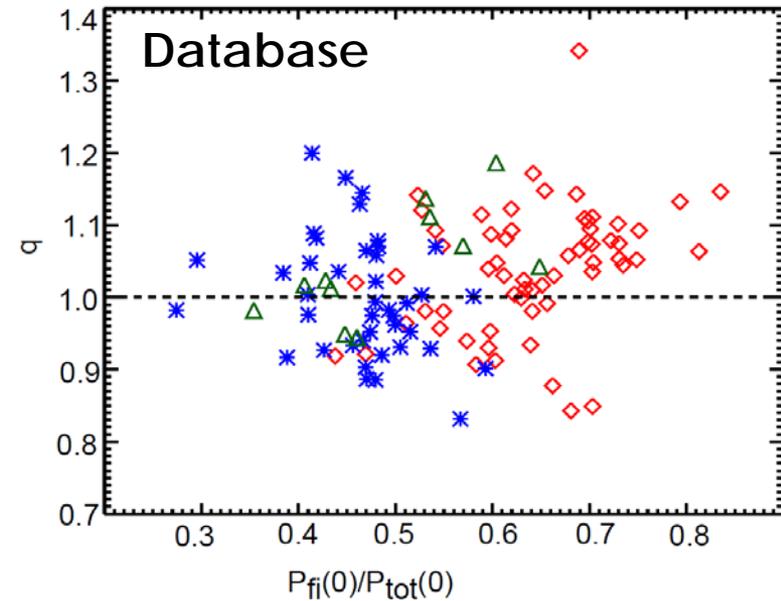
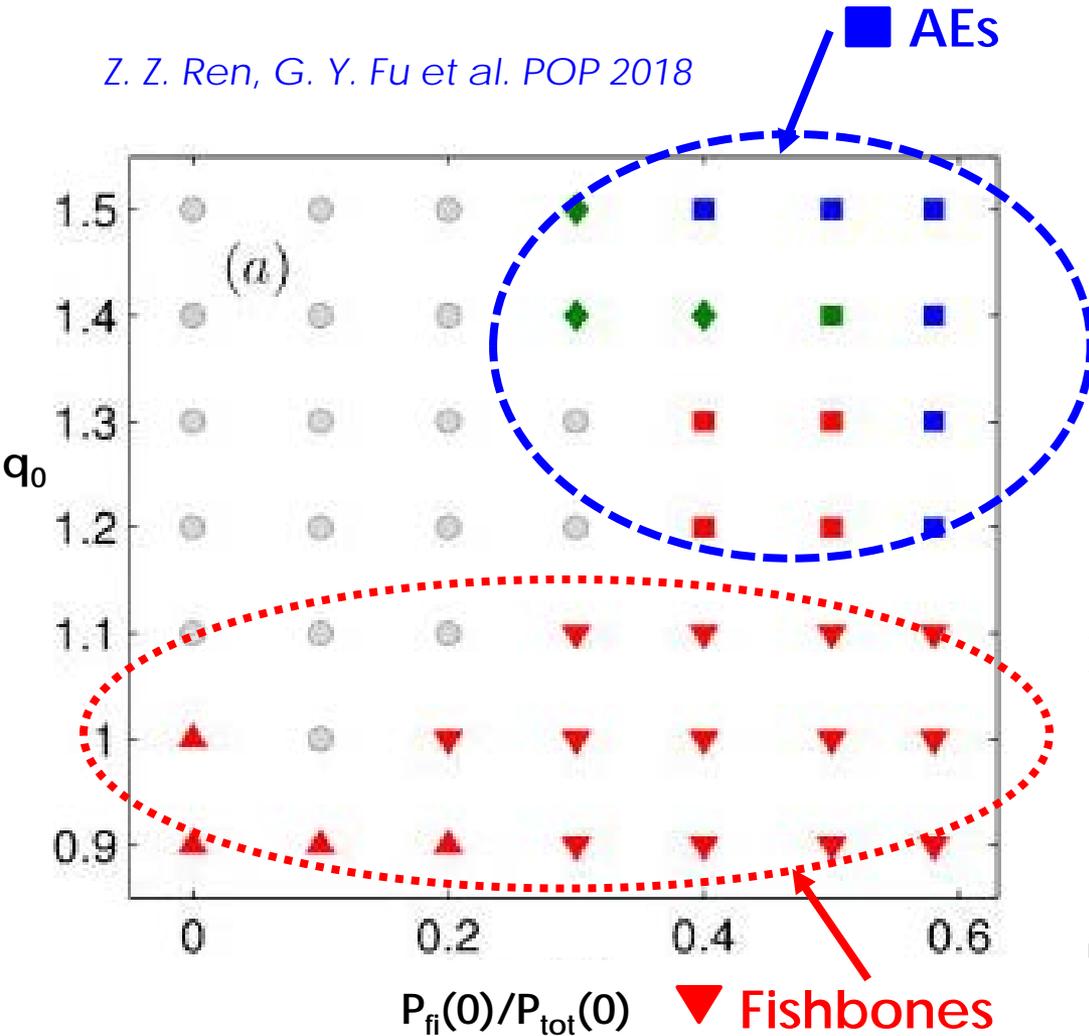
Our Hypotheses for the Transition from AE to Fishbones

- The increase of T_e & decrease in n_e during EC result in a rise of (trapped) fast-ion density, which makes fishbones most unstable.
- The gradual decrease of q_0 also facilitates the excitation of fishbones.
- Although the increase of fast-ion density also increases the drive of AEs, the increase of total plasma pressure and T_e can also increase the damping depending on the AE mode type.
- If unstable first, fast-ion transport induced by the fishbones may relax the gradients that would drive AEs.



Previous Kinetic/MHD Hybrid Simulations Shows the Transition of AEs to Fishbones could be due to q_0 Drop.

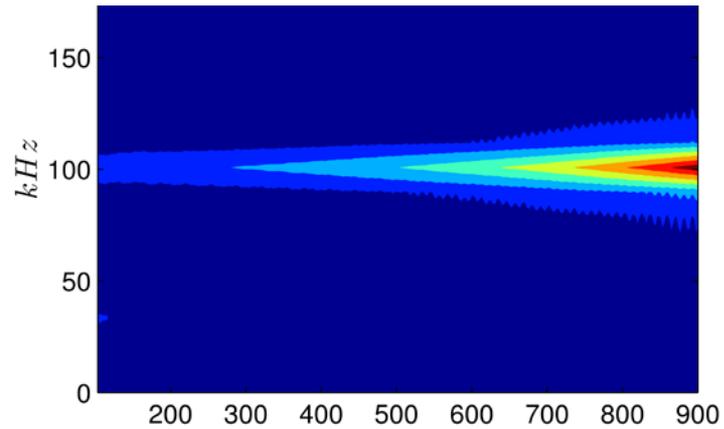
Z. Z. Ren, G. Y. Fu et al. POP 2018



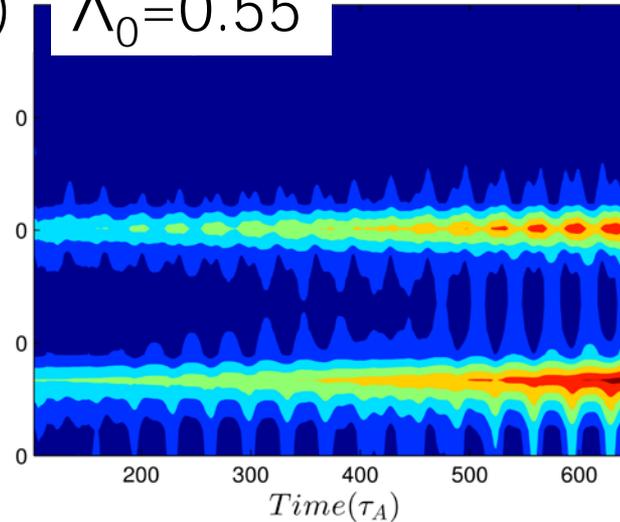
- This prediction is different from the database observation which suggests the transition from AEs to fishbone is because of large fast-ion population
- Note that in the simulations, q_0 and P_{fi}/P_{tot} scan is performed with fixed total pressure and fast ion pitch angle.

Simulations Show that Either AE or Fishbones can be Destabilized Depending on Passing/Trapped Particle Fraction

$\Lambda_0=0.5$ (more passing ptcls)



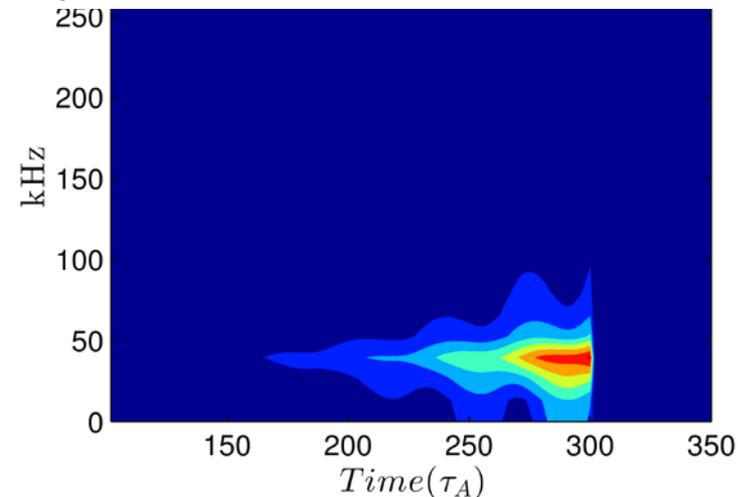
$\Lambda_0=0.55$



Kinetic/MHD M3D-K
hybrid simulations
by Z. Z Ren, G.Y. Fu

$$\Lambda_0 = \mu B_0 / E$$

$\Lambda_0=0.6$ (more trapped ptcls)



Small variation (more trapped particles) of pitch angle in the fast-ion distribution can cause the transition from AE to fishbones.

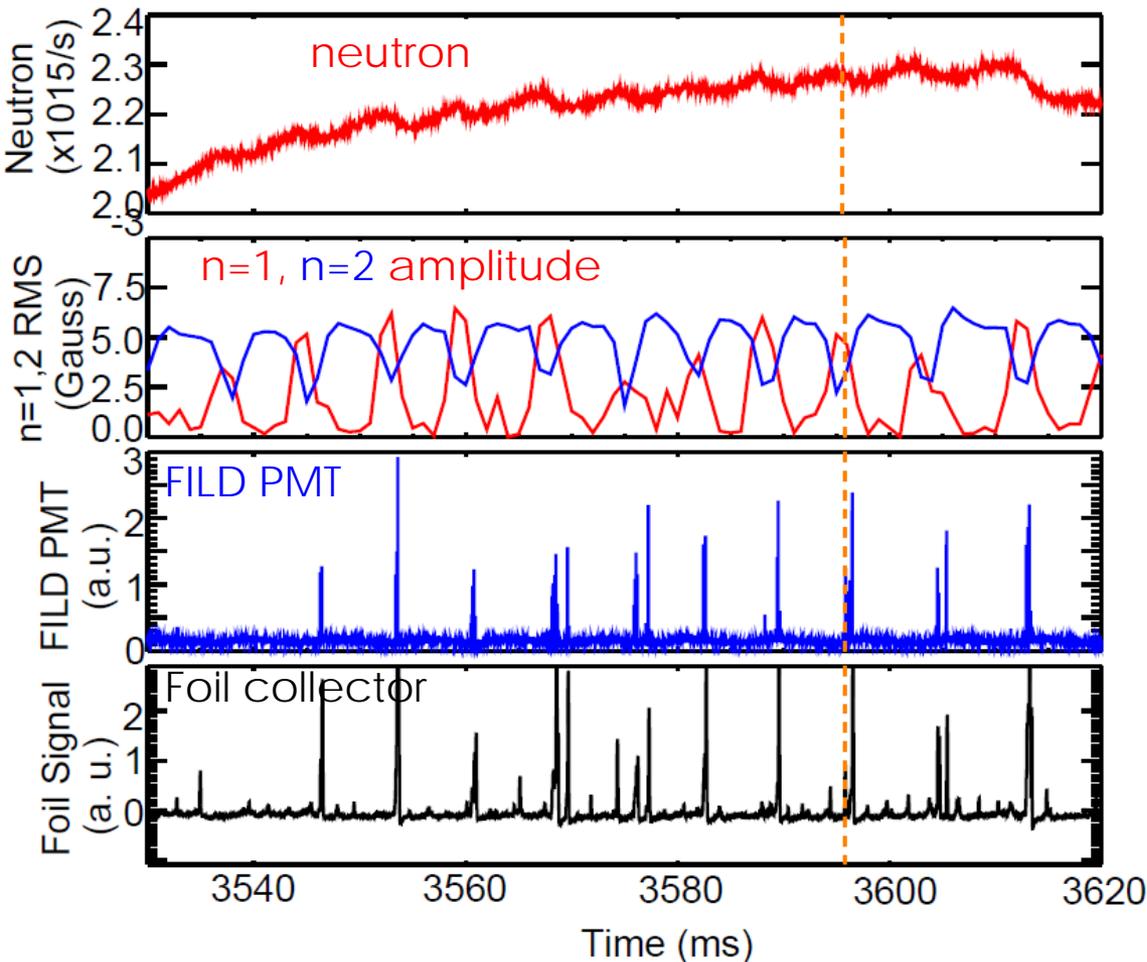
(Note: tearing mode is not included in the simulations.)

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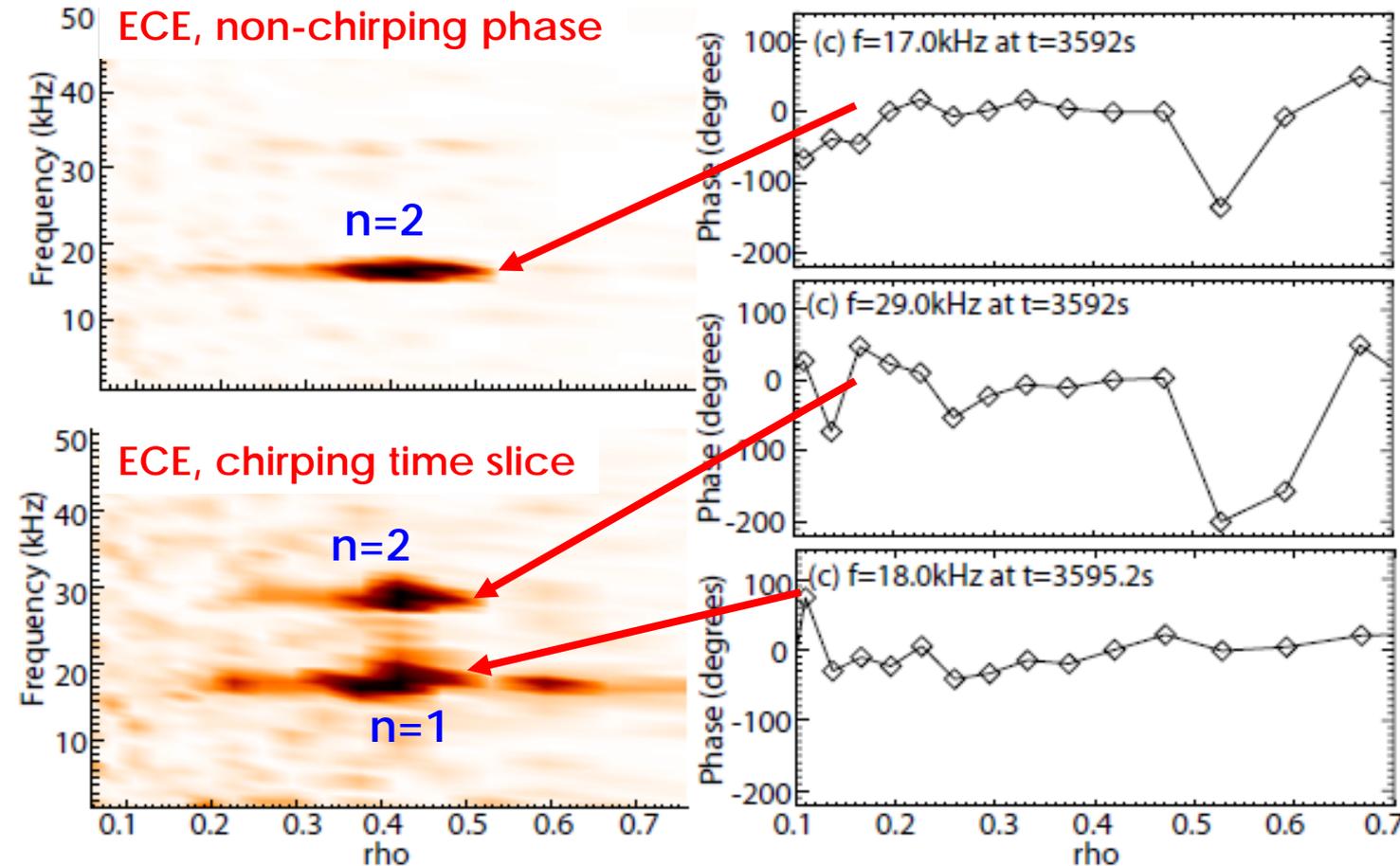
Low-Frequency Busting Mode Sometimes Cause Fast Ion Losses

161410: **chirping NTM** with $n=2$



- For all **fishbone** cases, fast ion losses are observed in the signals of PMT of FILD system and foil collector. Neutron rate drops 2-3%.
- For **chirping TM** cases, fast ion losses are only observed when the $n=1$ mode amplitude is large (1/4 of all chirping cases)
- In most chirping NTM cases with relatively weak $n=1$ mode, no obvious drops in neutron emission; no spikes in fast ion loss and D_a measurements.

TM is Confirmed by its Phase Variation and Mode Frequency; n=1 Mode has Constant Phase



➤ The $n=2$ mode has a 180° phase change near the rational surface.

➤ $n=2$ mode frequency is close to the rotation frequency at the rational surface.

Overlapping of Resonance Conditions may Cause Mode Coupling between TM and Fishbones

Wave-particle resonance condition:

$$\omega - n\omega_{\xi} + (m+l)\omega_{\theta} = 0$$

toroidal transit freq poloidal transit freq

Drift harmonic

Annotations: "wave mode #s" points to n ; "toroidal transit freq" points to ω_{ξ} ; "poloidal transit freq" points to ω_{θ} ; "Drift harmonic" points to $(m+l)$.

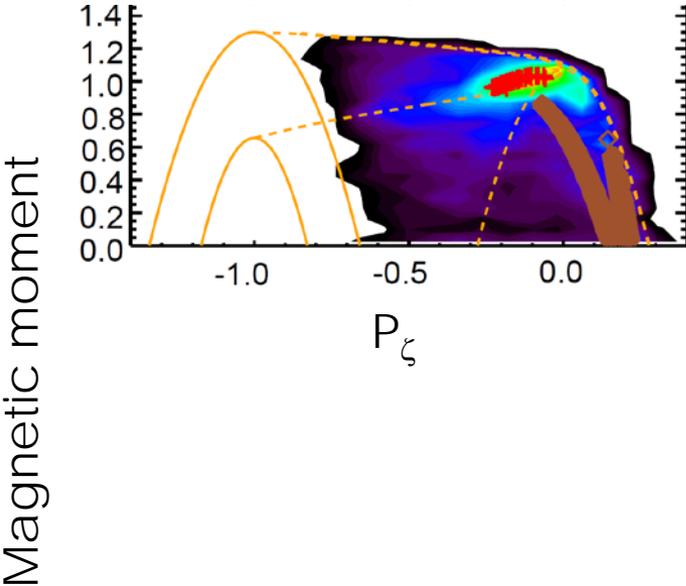
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toroidal transit freq Drift harmonic
poloidal transit freq

E=30keV, steady NTM f=18kHz



Symbols:
 possible orbits
 that can
 resonant with
 fishbones or TM.

- p=m+l=0
- p=m+l=1
- p=m+l=2

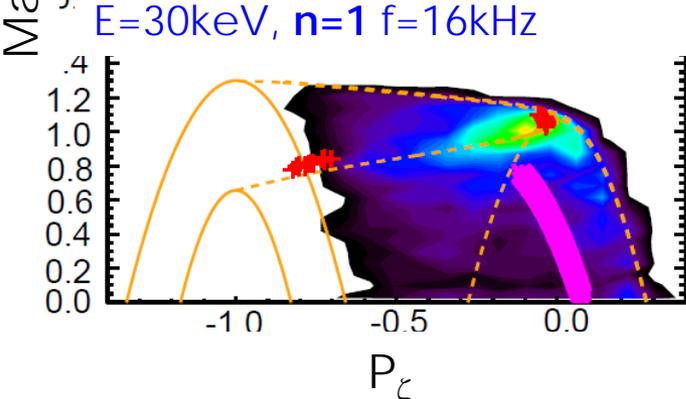
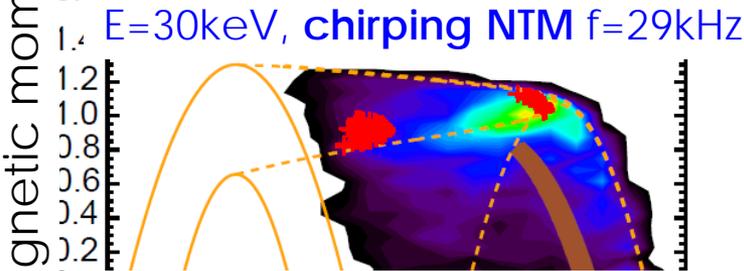
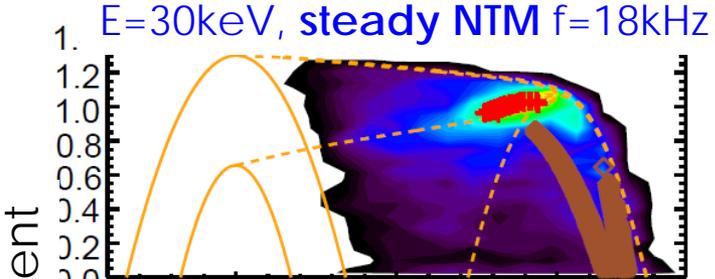
Contour:
 classical fast-ion
 distribution from
 TRANSP.

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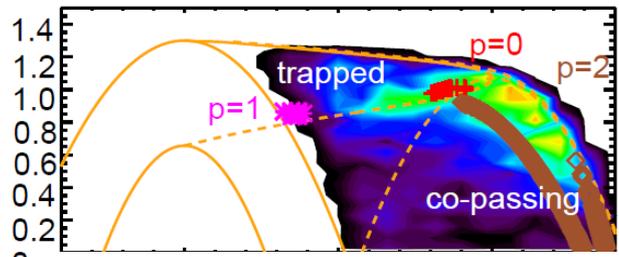
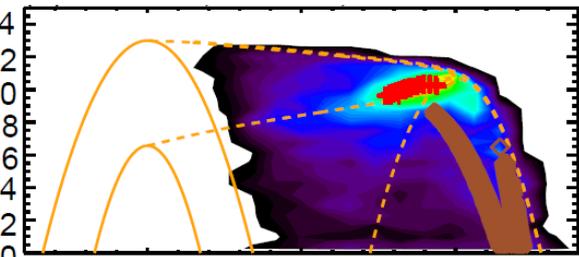
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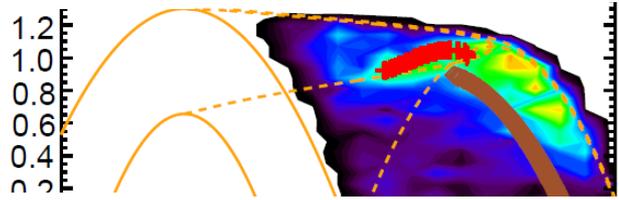
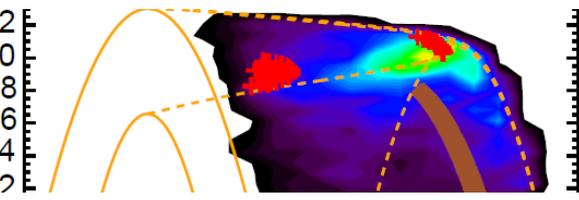
E=30keV, steady NTM f=18kHz

E=70keV, steady NTM f=18kHz



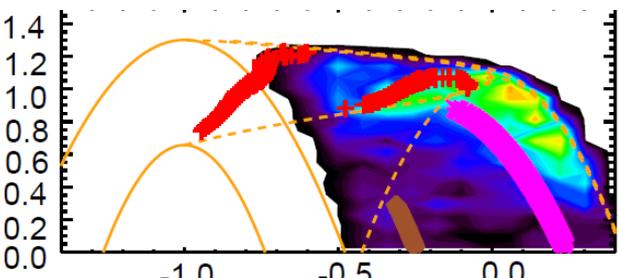
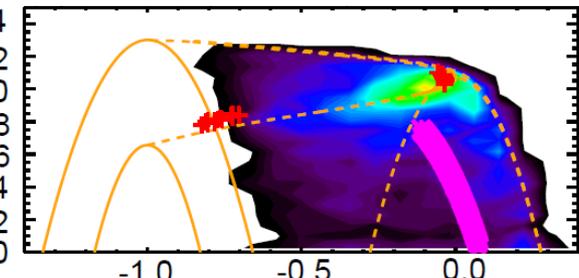
E=30keV, chirping NTM f=29kHz

E=70keV, chirping NTM f=29kHz



E=30keV, n=1 f=16kHz

E=70keV, n=1 f=16kHz



Symbols:
 possible orbits that can resonant with fishbones or TM.

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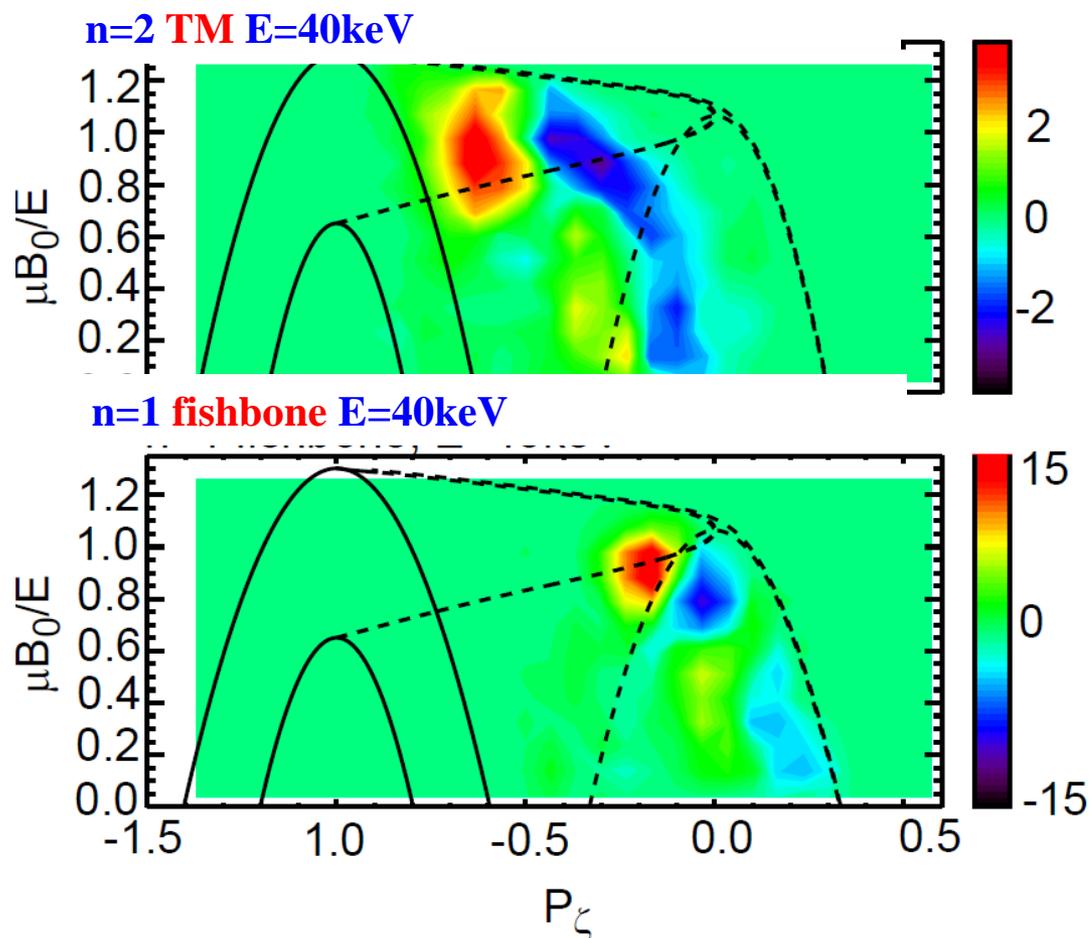
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Magnetic moment

Toroidal canonical angular momentum P_{ζ}

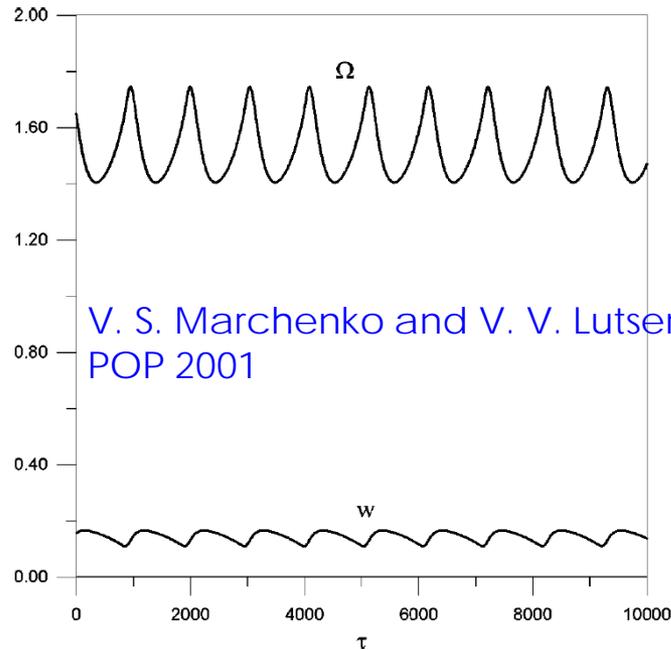
"Kick" Model* Simulations Suggest that n=2 TM and n=1 Fishbone can Interplay through Fast-ion Channeling in Phase-Space

Power flowing from fast ions to fishbone or TM



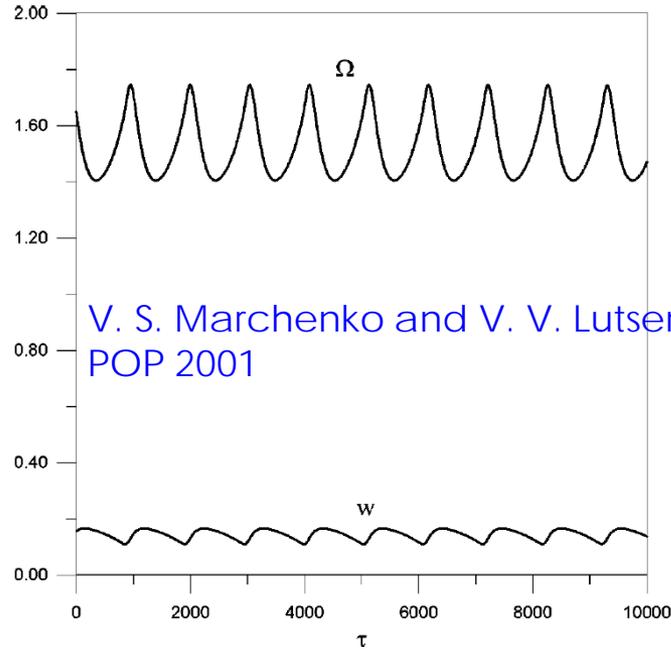
The resonance of trapped fast ions with TM can weaken the drive for fishbones.

Plausible Reasons for the NTM Island Width Modulation and Frequency Chirping



- **Theory I: resonance with precessing trapped particles** → change fast-ion deposition rate in the resonance region → generate a toroidal torque to accelerate island
- The resonant torque modulates the NTM frequency and amplitude through the **polarization current term**

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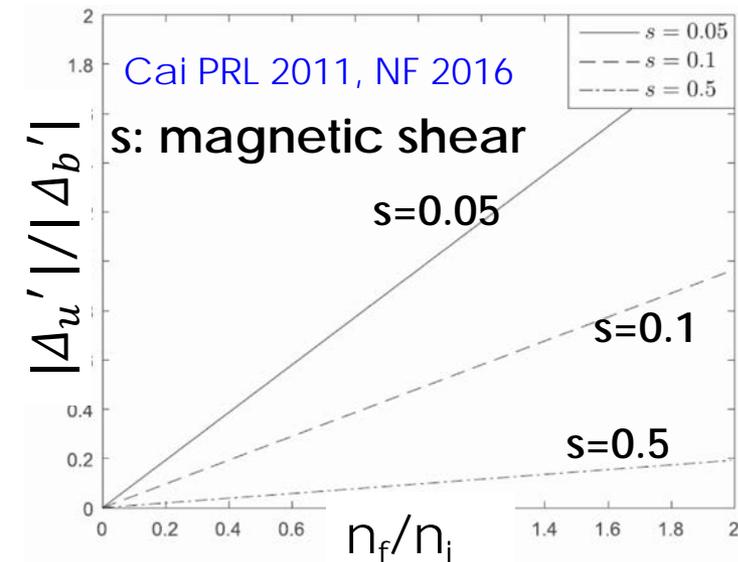
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- **Theory II: extra fast ion contribution term in the modified Rutherford equation**

$$\frac{8\pi}{\eta c^2} I_1 \frac{dw}{dt} = \Delta_u' + \Delta_b' + \Delta_i' + \Delta_u',$$

$$\Delta_u' = -G_3 \left(\frac{r}{sL_n} \right)^2 \frac{\beta_\theta}{w} \frac{\omega'}{\omega_{*i}} \frac{n_h}{n_i} \frac{L_n}{L_h}$$

- This effect depends on TM propagation freq, magnetic share and fast-ion density gradient.
- The effect is more significant with weak magnetic shear & high fast-ion density. It may suppress NTM under certain conditions.



Summary and Future Work

➤ Observations and database study

- With NBI+EC, AE activity is suppressed & replaced by low-f chirping mode
- The database suggests: (i) low-f chirping modes occur when $P_{fi}(0)/P_{tot}(0) > 0.5$
(ii) The q profile change plays a weaker role.
- Low-f chirping mode is often chirping NTM and occasionally fishbones.
- Chirping NTMs do not always cause significant fast ion losses. Only when n=1 amplitude is large, small neutron drop(2-3%) & fast ion losses are observed.

➤ Modelling

- Simulations suggest that increase of trapped fast ions can cause the transition from AE to low-frequency mode.
- Resonance conditions and “kick” model simulations show that TM and fishbone can interplay through fast-ion channeling in phase space.
- Island width & frequency modulation may be explained by (1) resonance of TM with trapped particles, (2) cross-field current by resonant fast ions

- **Future work:** (1) self-consistent simulations include fast ions, NTM and fishbones.
(2) measurements of response fast ions in phase space (passing vs trapped); island rotation direction and frequency evolution;...