

High fidelity simulations of fast ion power flux driven by 3D field perturbations on ITER

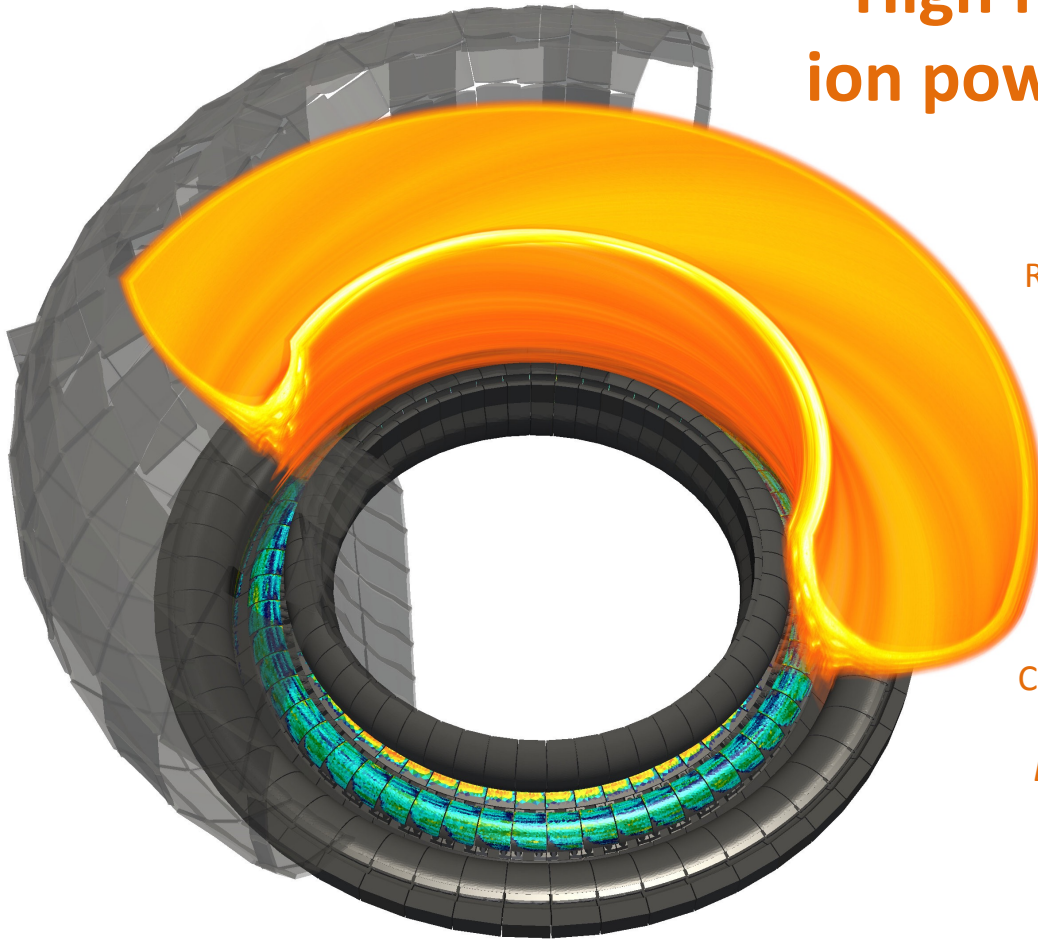
R J Akers¹, S Äkäslompolo², B Colling¹, J Hess¹, Y Liu¹,
S D Pinches³, K Särkimäki², M Singh³, A Turner¹,
J Varje²

¹CCFE, Culham Science Centre, Abingdon,
OX14 3dB, UK

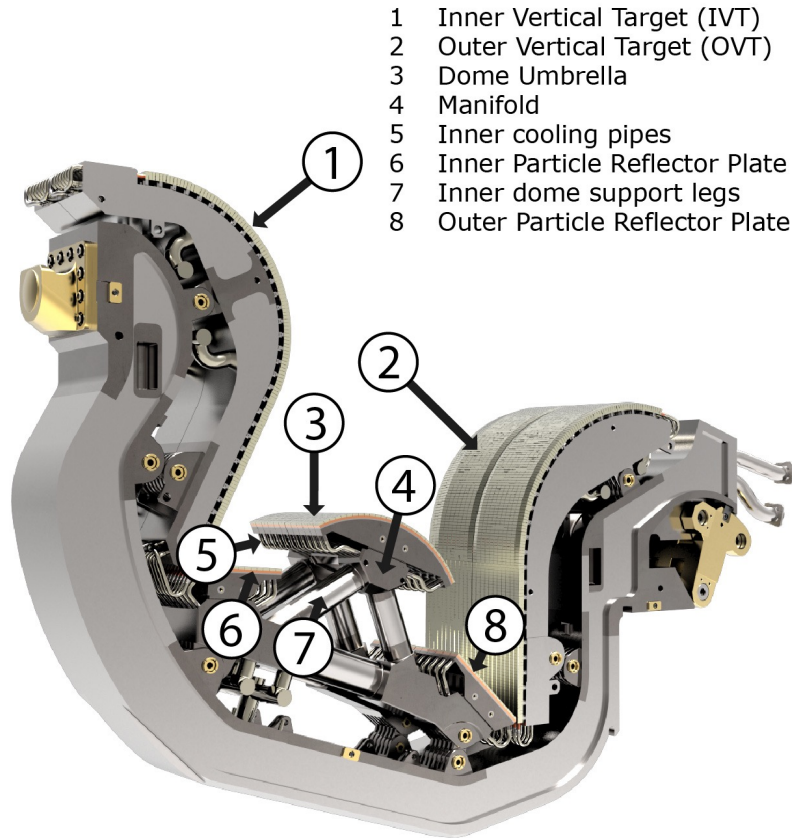
²Department of Applied Physics,
Aalto University, FI-0076 AALTO, Finland

³ITER Organization, Route de Vinon-sur-Verdon,
CS 90 046, 13067 St. Paul lez Durance Cedex, France.

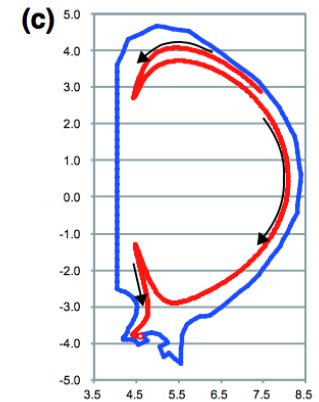
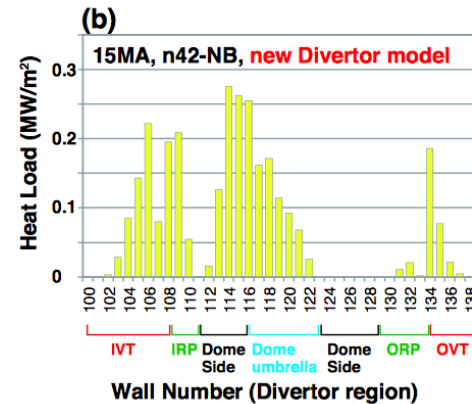
E-mail contact of main author: rob.akers@ukaea.uk



Code development motivated by problem posed FEC2012



T Oikawa et al., IAEA FEC 2012, paper ITR/P1-35.



0.2-0.3MW/m² (vacuum ECC field @90kAt)
(0.1MW/m² expected from thermal/radiative load)

Need:

- Accurate plasma response field
- High statistics
- Higher fidelity first wall model
- Gyro-motion

We have developed a new Monte Carlo code to solve this challenge:
LOCUST-gpu (the **L**orentz **O**rbital **C**ode for **U**se in **S**tellarators and **T**okamaks)

LOCUST-gpu solves the following equations using GPUs:

Lorentz equation of motion

$$m \frac{d\mathbf{v}}{dt} = q(\mathbf{v} \times \mathbf{B})$$

Based upon Boris pusher,
math light!

Guiding Centre equations

$$\dot{\chi} = \frac{qB}{m},$$

$$\dot{\mu} = 0,$$

$$\dot{\mathbf{v}}_{\parallel} = \frac{q}{m} \frac{\mathbf{B}^*}{B_{\parallel}^*} \cdot \mathbf{E}^*,$$

$$\dot{\mathbf{R}} = \mathbf{v}_{\parallel} \frac{\mathbf{B}^*}{B_{\parallel}^*} + \mathbf{E}^* \times \frac{\mathbf{b}}{B_{\parallel}^*},$$

$$\mathbf{E}^* = -\partial \mathbf{A}^* / \partial t - \nabla \Phi^*$$

$$\mathbf{B}^* = \nabla \times \mathbf{A}^*$$

$$\Phi^*(\mathbf{R}, \mu, t) = \Phi + \frac{\mu B}{q},$$

$$\mathbf{A}^*(\mathbf{R}, \mathbf{v}_{\parallel}, t) = \mathbf{A} + \frac{m \mathbf{v}_{\parallel} \mathbf{b}}{q}.$$

Based upon RKF45,
math heavy!

Collision operator

$$\begin{aligned} \Delta \xi &= -\nu \xi \Delta t + \delta_1 [(1 - \xi^2) \nu \Delta t]^{1/2}, \\ \Delta \epsilon &= -\sum_j 2\nu_{\epsilon,j} \Delta t \left[\epsilon - \left(\frac{3}{2} + \frac{\epsilon}{\nu_{\epsilon,j}} \frac{d\nu_{\epsilon,j}}{d\epsilon} \right) k_B T_j \right] \\ &\quad + \delta_2 \left(\sum_j 2k_B T_j \epsilon \nu_{\epsilon,j} \Delta t \right)^{1/2}, \end{aligned}$$

Time/spatial scale

Value (ITER 15MA H-mode,
1MeV D injection)

Gyro frequency

3.8×10^7 Hz

Field structure scale length

>2cm (poloidal plane)

Slowing down time

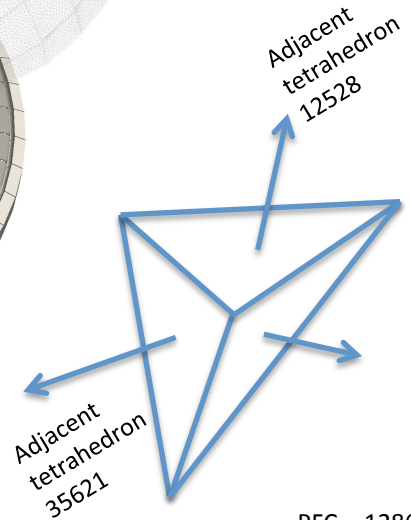
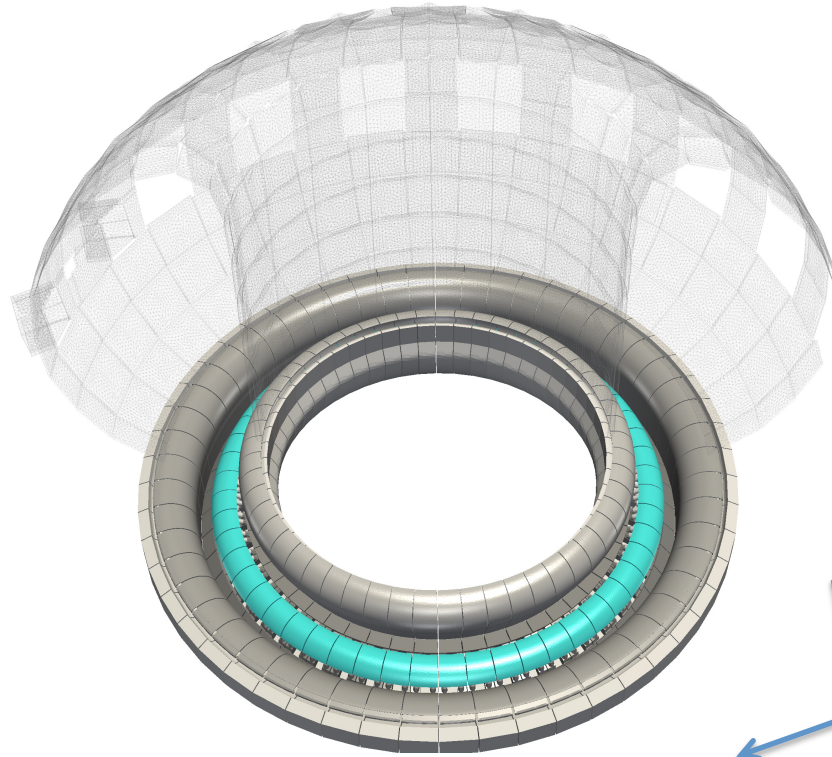
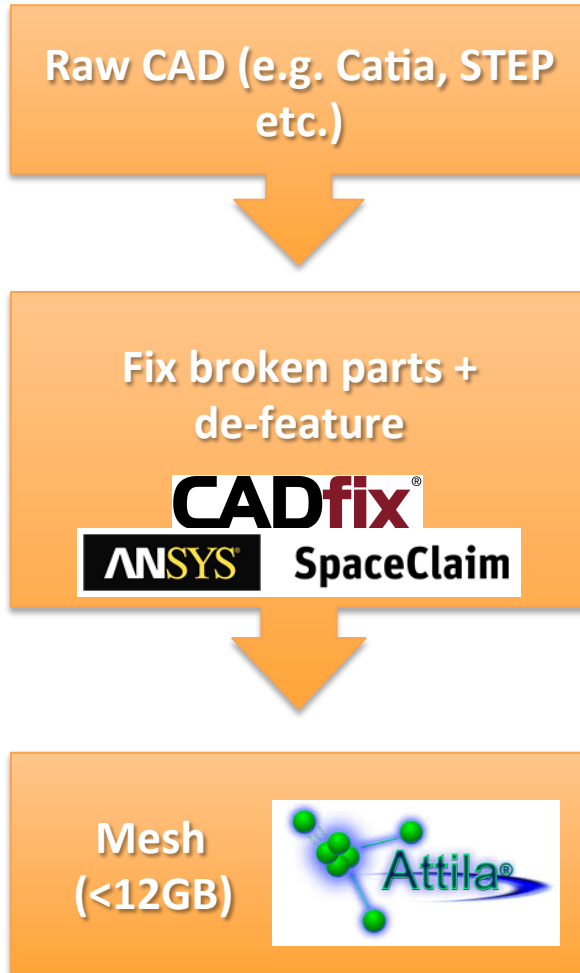
~1.5s (core born)

Choice of 9 tracking integrators.

Here we use **Boris**,
2ns time-step.

“Why is Boris Algorithm So Good?”
Hong Qin et. al., PPPL-4872, April 2013.

LOCUST-gpu deploys a detailed tetrahedral mesh

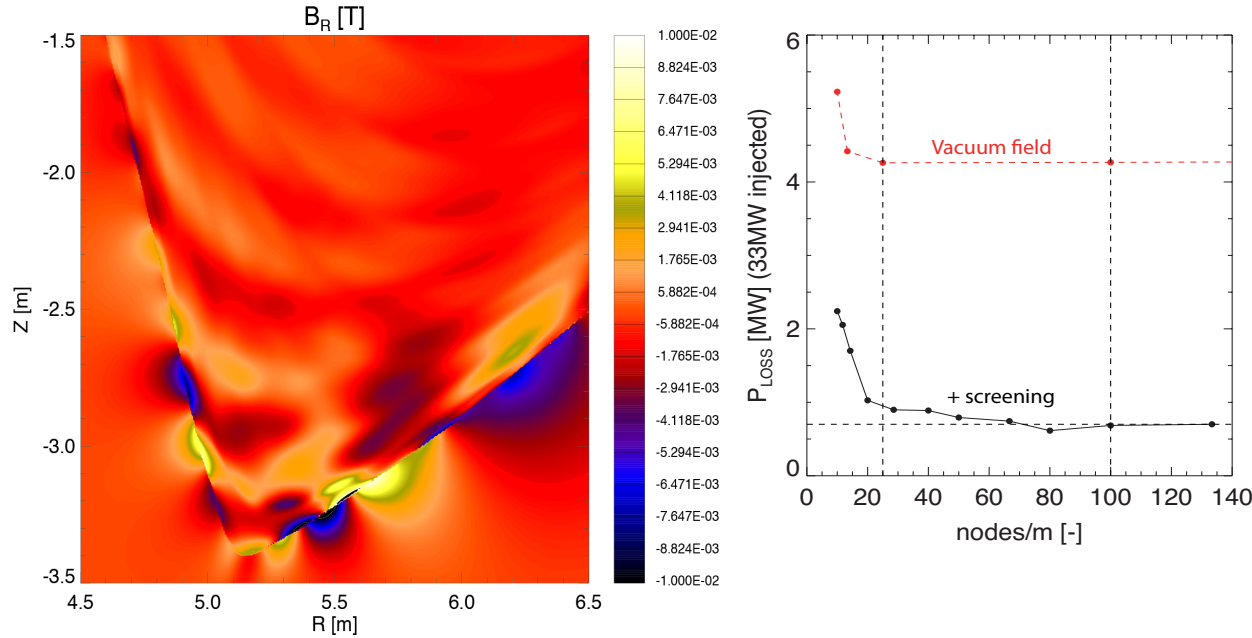


ITER LOCUST-gpu mesh

# tetrahedra	:	57570062
# nodes	:	17620565
# components	:	13
# surface triangles	:	2528454

Assous F., Degond P., Segre J.
Comput. Phys. Commun. 72,
1992, p105.

ECC field map built from MARS-F field components



$$\begin{aligned}
 \mathbf{B1}(s, \chi, \phi) &= \sum_{m=M1}^{M2} \mathbf{B1}(s, m) e^{im\chi + in\phi} \\
 \mathbf{B2}(sm, \chi, \phi) &= \sum_{m=M1}^{M2} \mathbf{B2}(sm, m) e^{im\chi + in\phi} \\
 \mathbf{B3}(sm, \chi, \phi) &= \sum_{m=M1}^{M2} \mathbf{B3}(sm, m) e^{im\chi + in\phi} \\
 B_R &= \frac{1}{J} \left(\mathbf{B1} \frac{\partial R}{\partial s} + \mathbf{B2} \frac{\partial R}{\partial \chi} \right) \\
 B_Z &= \frac{1}{J} \left(\mathbf{B1} \frac{\partial Z}{\partial s} + \mathbf{B2} \frac{\partial Z}{\partial \chi} \right) \\
 B_\phi &= \frac{1}{J} R \mathbf{B3} \\
 J &= \left(\frac{\partial R}{\partial s} \frac{\partial Z}{\partial \chi} - \frac{\partial R}{\partial \chi} \frac{\partial Z}{\partial s} \right) R
 \end{aligned}$$

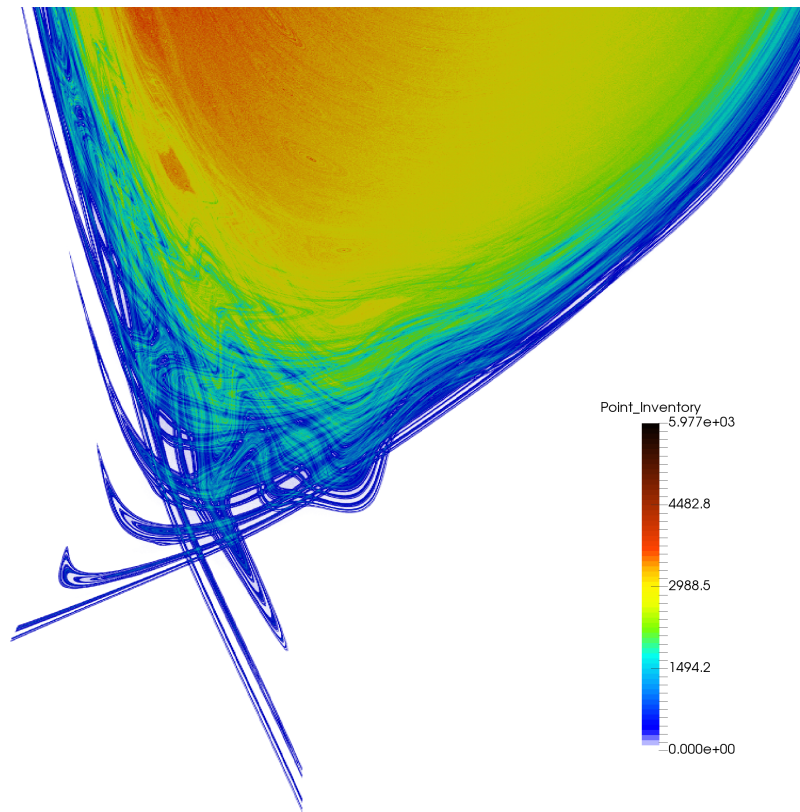
- Separate radial splines for $s < 1$ and $s > 1$.
- Large values of $M0=240$, $M1=-109$ & $M2=+109$ needed.
- LOCUST-gpu uses bi-cubic spline of ψ for 2D field and either tri-cubic spline or summation over toroidal Fourier harmonics using bi-cubic splines of the Real and Imaginary components of the field vectors for a given n .

$$\begin{aligned}
 R(s, \chi) &= \mathbf{RF}(s, 1) + 2\text{Re} \left[\sum_{m=2}^{M0} \mathbf{RF}(s, m) e^{i(m-1)\chi} \right] \\
 Z(s, \chi) &= \mathbf{ZF}(s, 1) + 2\text{Re} \left[\sum_{m=2}^{M0} \mathbf{ZF}(s, m) e^{i(m-1)\chi} \right]
 \end{aligned}$$

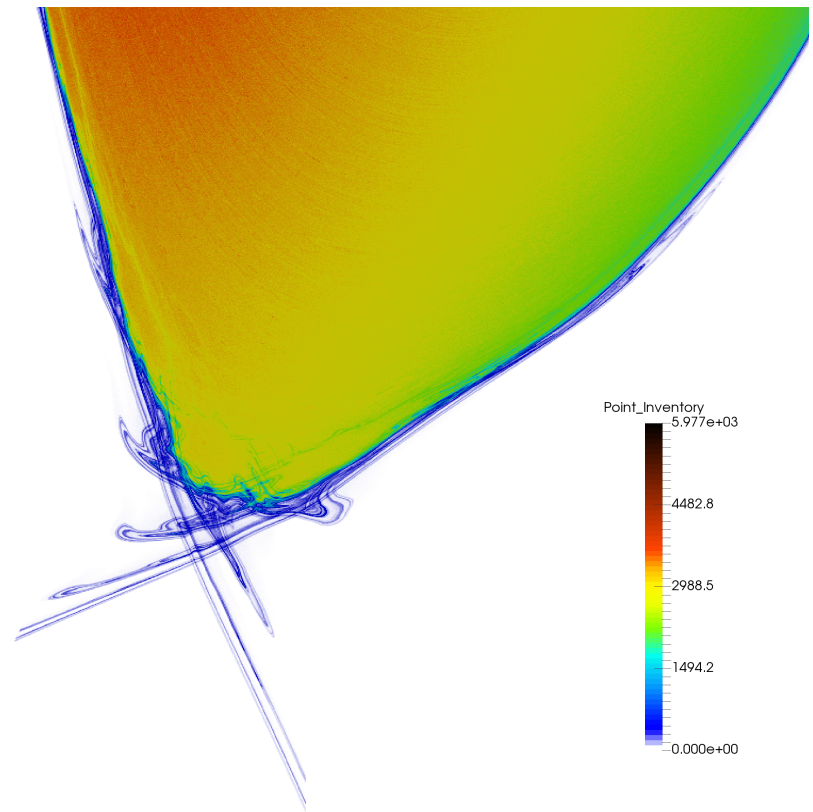
Chosen grid res: 0.5cm x 0.5cm

LOCUST-gpu can efficiently follow field lines as well as orbits...

Colour rendered Poincare plots of the ITER homoclinic tangle

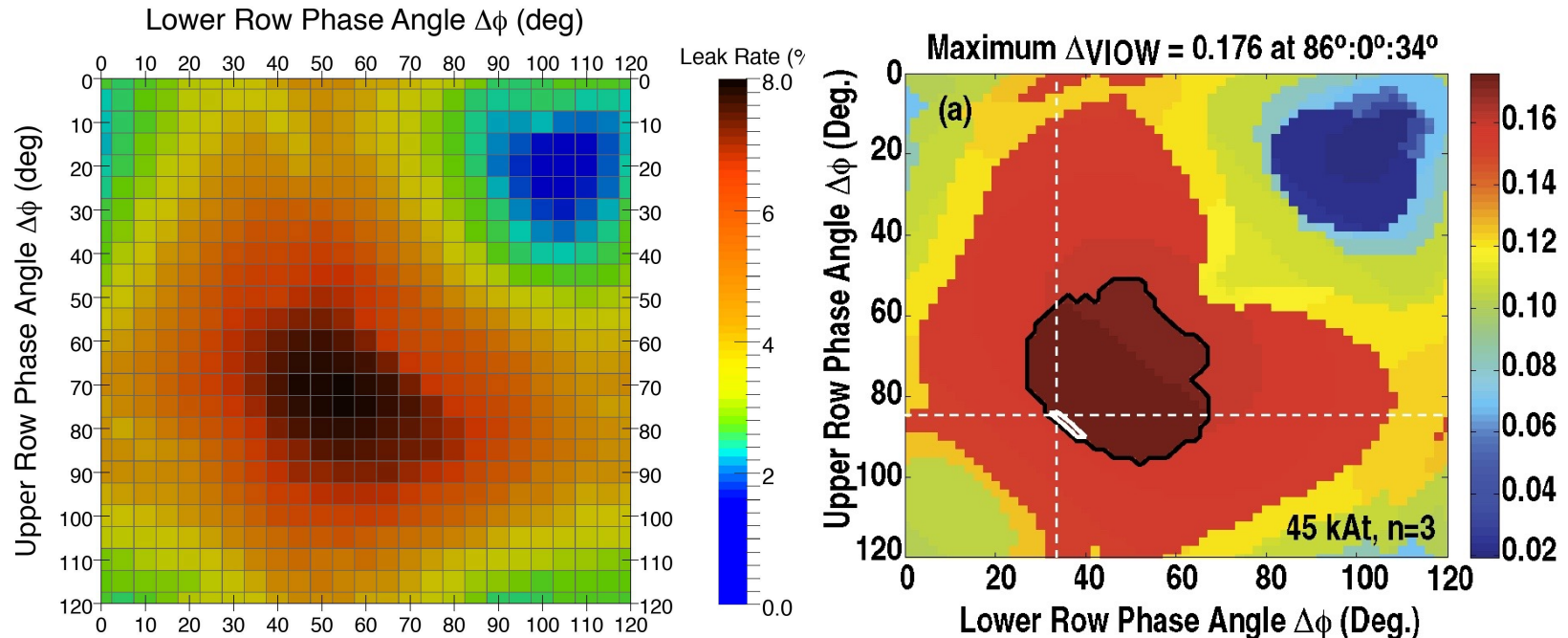


ITER 15MA baseline H-mode with
45kAt n=3 ECC (vacuum, incl. n=6 sideband)



ITER 15MA baseline H-mode with
45kAt n=3 ECC (incl. n=6 sideband &
plasma screening)

[86°,0°,34°] U,M,L phase settings generate close to maximum stochasticity for a given ECC drive current



T.E.Evans et al., IAEA FEC2012 paper ITR P1-25

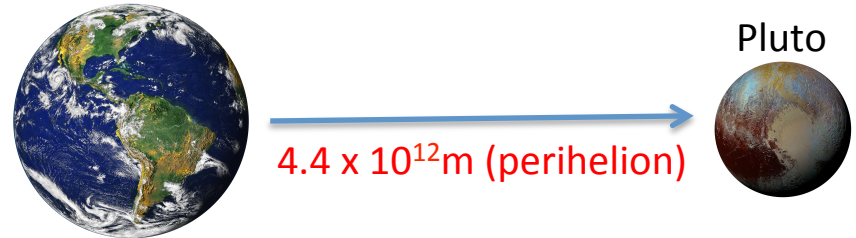
- MARS-F runs done for each coil set independently, separated into toroidal harmonics.
- Scan of field line leak rate vs. upper & lower coil set phase offset looks very similar to that of vacuum island overlap width.

Is our cooling pipe problem tractable?

In 24 hours, the 3 K80 nodes at CCFE can integrate up a distance (with 2cm resolution, 1MeV D + 2D field) of: $5.4 \times 10^{12}\text{m}$

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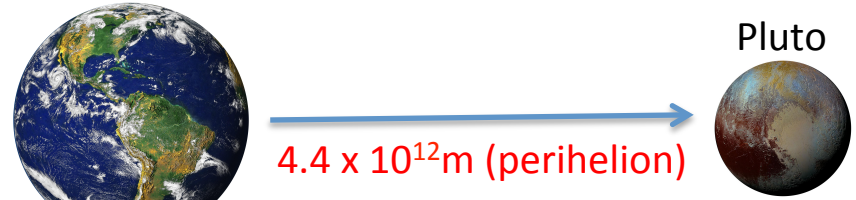


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For a 10% statistical error...
(very rough back of the envelope calculation):

100	markers per triangle
400	triangles “painted” area per pipe
12	pipes per cassette
54	cassettes
$\sim 1.0 \times 10^7 \text{m/s}$	“average” velocity over slowing down
$\sim 0.5 \text{s}$	Time to impact
50kW	Power deposited to pipes (0.15% injected)



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50kW	Power deposited to pipes (0.15% injected)

$$100 \times 400 \times 12 \times 54 \times 1.0 \times 10^7 \times 0.5 / (0.05 / 33.0) \\ = 8.6 \times 10^{16} \text{m} (\sim 9 \text{ light years})$$



$4.4 \times 10^{12}\text{m}$ (perihelion)

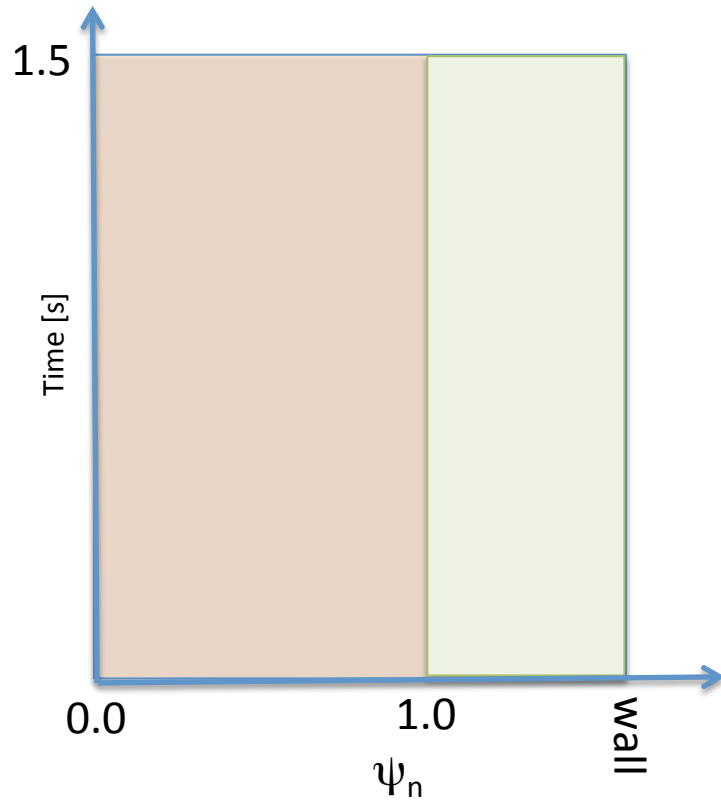


$4.014 \times 10^{16}\text{m}$



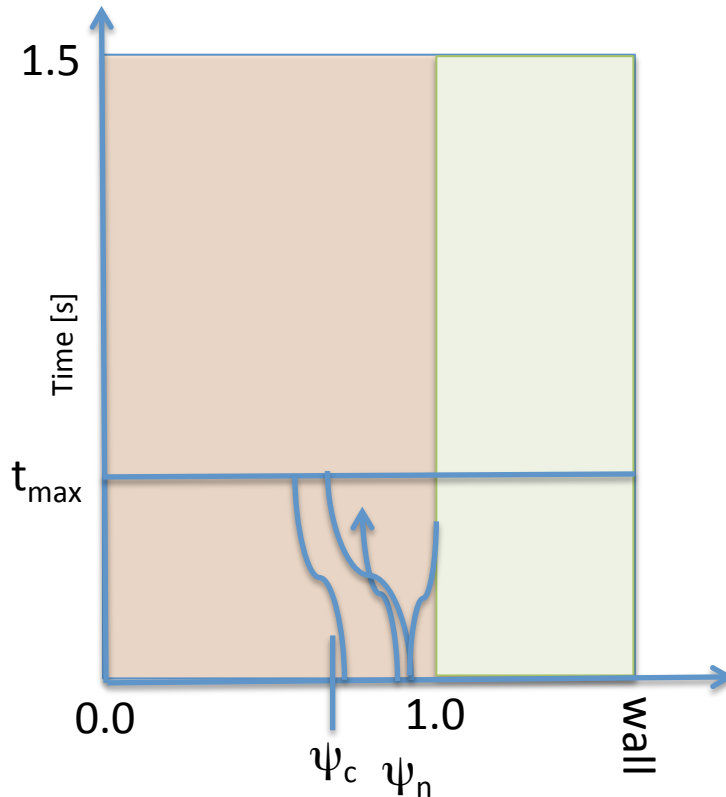
We are going to need some Monte Carlo "tricks".

Monte Carlo Enhancement methods



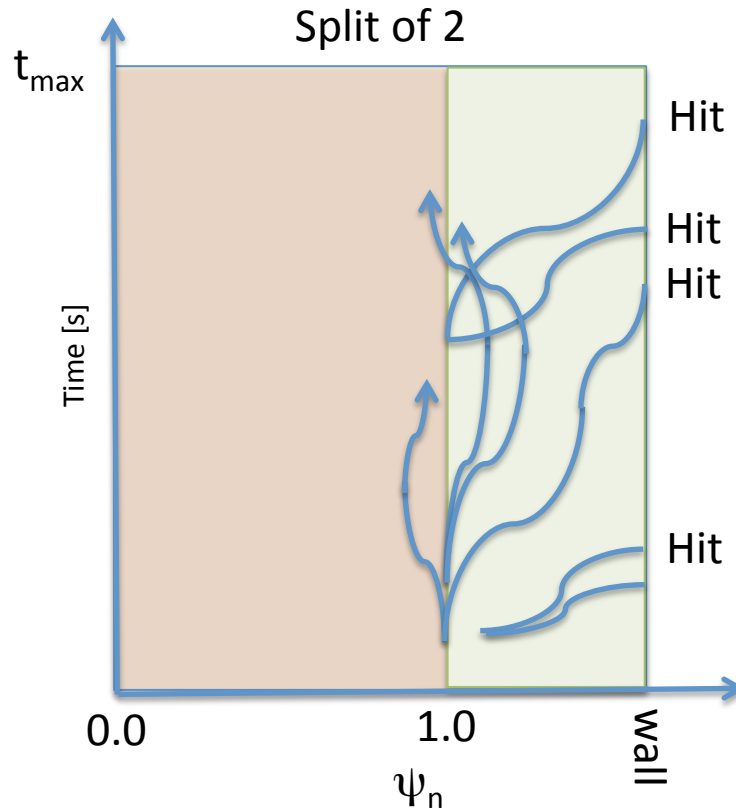
Tracking Stage 1

Stage 1: Track w/o PFC hit testing



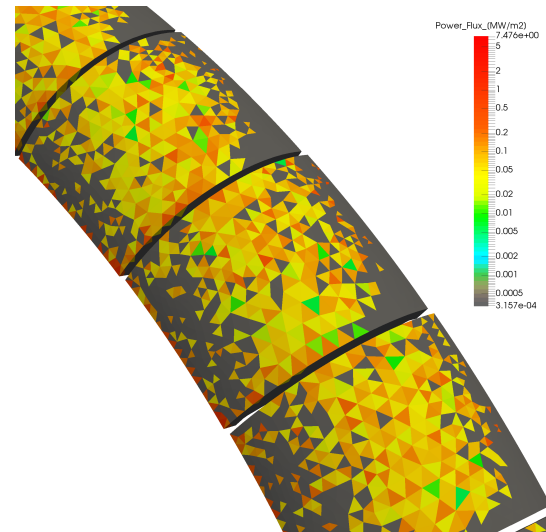
- **Reject markers** born inside $\psi_n = \psi_c$ (use a low stats run to determine ψ_c and also maximum tracking time)
- Follow markers inside $\psi_n = 1$ until they cross the separatrix (when they do, **cache** them) or until they thermalize or reach $t_{\max}$.
- Every n kernel calls, **cache all the marker state parameters**, keeping m copies.

Tracking Stage 2

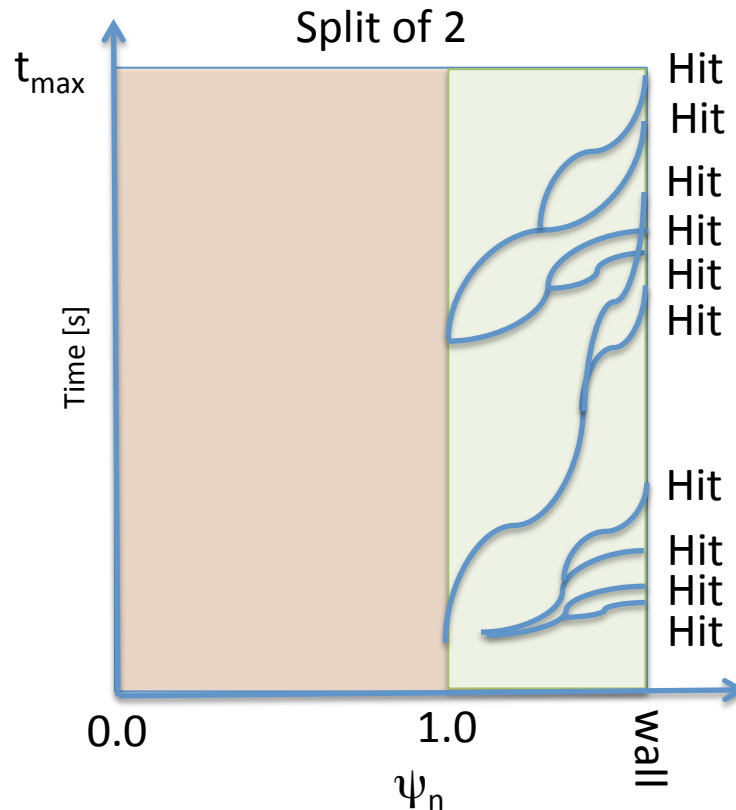


Stage 2: Track with PFC hit testing

- “Split” markers that were either born outside the separatrix or were cached from stage 1 until they hit the wall, are thermalized or reach $t_{\max}$.

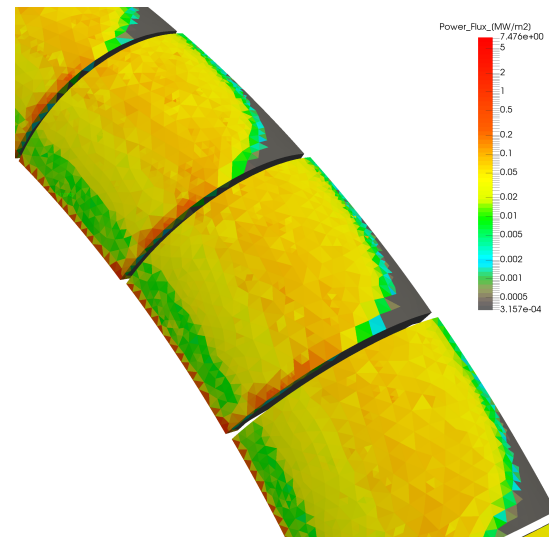


Tracking Stage 3



Stage 3: Step markers which hit wall back in time

- Use marker state cache to step markers which hit wall **back in time** and “massively split” them to form a new ensemble.



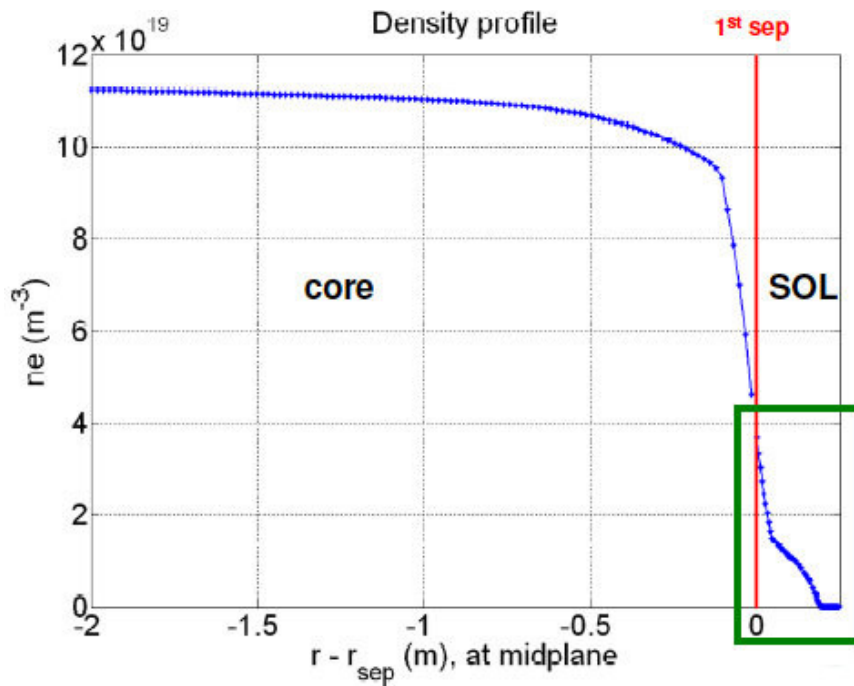
Stepping back $\sim 0.2-0.4\text{ms}$ sufficient for collisions to smear out markers and produce smooth maps.

Caveat: Must step far enough back in t to prevent problems with shadow areas. Power accounting maintained by normalizing newly collected power from siblings to their parent marker.

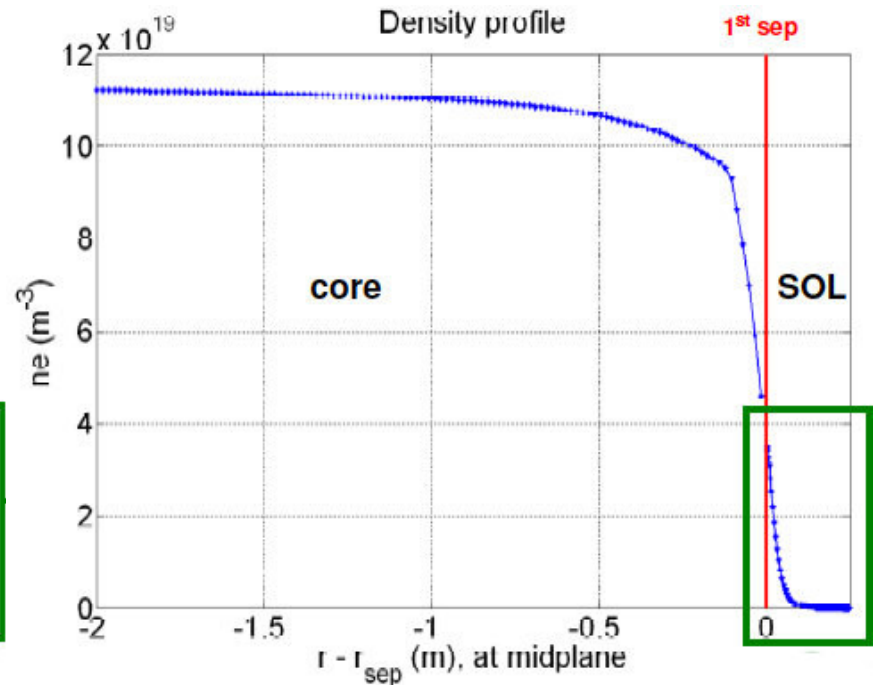
Results: Location dependent losses

15MA baseline H-mode, 1 beam on-axis, 1 off-axis. (33MW D injection) n=3 ECC (including n=6 sideband)

ITER_D_33Y59M – v2.3



High Density SOL (H)



Low Density SOL (L)

Results: Location dependent losses

2D field:

- Losses are negligible for low density SOL.
- 0.26MW (0.8%) loss, mainly prompt to 1st wall and OVT for high density SOL.

LOCUST-gpu: Bicubic spline ECC field (n=3 + n=6 sideband)

I _c [kAt]	Plasma Response ?	n _c (SOL) High/Low [MW]	1 st wall [MW]	Dome Umbrella [MW]	Inner Support legs [MW]	Outer PRP [MW]	Inner Cooling pipes [MW]	OVT [MW]	IVT [MW]	
0	-	L	0.0032±0.0004	0.0062±0.0006	0.00007±0.00006	0.0004±0.0001	0.000±0.000	0.0081±0.0004	0.00118±0.00005	→ 0.01MW (0.04%)
45	✗	L	0.0038±0.0008	0.216±0.004	0.0085±0.0007	0.0029±0.0004	0.0227±0.0013	0.296±0.003	0.591±0.004	
45	✓	L	0.0036±0.0005	0.078±0.001	0.0032±0.0004	0.0028±0.0002	0.0069±0.0004	0.0486±0.0008	0.0206±0.0006	
90	✗	L	0.0076±0.0011	0.962±0.012	0.044±0.002	0.0091±0.0013	0.156±0.004	1.251±0.011	1.821±0.016	
90	✓	L	0.0077±0.0006	0.262±0.003	0.0197±0.0007	0.0104±0.0008	0.043±0.001	0.239±0.002	0.146±0.002	
0	-	H	0.109	0.0472±0.0018	0.0002±0.0001	0.0049±0.0004	0.0001±0.0001	0.108	0.0025±0.0003	→ 0.26MW (0.8%)
45	✗	H	0.111±0.004	0.295±0.004	0.0087±0.0010	0.0116±0.0009	0.0239±0.0018	0.461±0.006	0.573±0.005	
45	✓	H	0.113±0.003	0.171±0.003	0.0029±0.0003	0.0118±0.0006	0.0067±0.0005	0.180±0.002	0.0211±0.0007	
90	✗	H	0.128±0.002	1.049±0.006	0.0477±0.0015	0.0151±0.0005	0.151±0.002	1.454±0.008	1.808±0.008	
90	✓	H	0.128±0.004	0.357±0.005	0.019±0.001	0.0173±0.0007	0.049±0.001	0.414±0.005	0.149±0.002	

Results: Location dependent losses

45kAt vacuum ECC field:

- Losses to dome umbrella increase to 0.2(L)-0.3(H)MW
- Losses to OVT increase by 0.3(L)-0.35(H)MW
- Losses to IVT increase by ~0.6MW (similar for both Low and High density SOL)
- 1st wall losses don't increase very much (prompt, poorly confined orbits in SOL)

LOCUST-gpu: Bicubic spline ECC field (n=3 + n=6 sideband)

I _c [kAt]	Plasma Response ?	n _c (SOL) High/Low [MW]	1 st wall [MW]	Dome Umbrella [MW]	Inner Support legs [MW]	Outer PRP [MW]	Inner Cooling pipes [MW]	OVT [MW]	IVT [MW]	
0	-	L	0.0032±0.0004	0.0062±0.0006	0.00007±0.00006	0.0004±0.0001	0.000±0.000	0.0081±0.0004	0.00118±0.00005	
45	✗	L	0.0038±0.0008	0.216	0.0085±0.0007	0.0029±0.0004	0.0227±0.0013	0.296	0.591	➡ 1.11MW (3.4%)
45	✓	L	0.0036±0.0005	0.078±0.001	0.0032±0.0004	0.0028±0.0002	0.0069±0.0004	0.0486±0.0008	0.0206±0.0006	
90	✗	L	0.0076±0.0011	0.962±0.012	0.044±0.002	0.0091±0.0013	0.156±0.004	1.251±0.011	1.821±0.016	
90	✓	L	0.0077±0.0006	0.262±0.003	0.0197±0.0007	0.0104±0.0008	0.043±0.001	0.239±0.002	0.146±0.002	
0	-	H	0.109	0.0472±0.0018	0.0002±0.0001	0.0049±0.0004	0.0001±0.0001	0.108±0.002	0.0025±0.0003	
45	✗	H	0.111	0.295	0.0087±0.0010	0.0116±0.0009	0.0239±0.0018	0.461	0.573	➡ 1.47MW (4.5%)
45	✓	H	0.113	0.171±0.003	0.0029±0.0003	0.0118±0.0006	0.0067±0.0005	0.180±0.002	0.0211±0.0007	
90	✗	H	0.128	1.049±0.006	0.0477±0.0015	0.0151±0.0005	0.151±0.002	1.454±0.008	1.808±0.008	
90	✓	H	0.128	0.357±0.005	0.019±0.001	0.0173±0.0007	0.049±0.001	0.414±0.005	0.149±0.002	

Results: Location dependent losses

45kAt ECC field incl. plasma screening (MARS-F):

- For low density SOL, losses reduce dramatically down to ~0.5%.
- High density SOL – losses reduce by 2/3 to 1.5% (DU, OVT, IVT). Prompt loss to wall and OVT remain.
- Under dome cooling pipes – power flux still negligible.

LOCUST-gpu: Bicubic spline ECC field (n=3 + n=6 sideband)

I _c [kAt]	Plasma Response ?	n _c (SOL) High/Low [MW]	1 st wall [MW]	Dome Umbrella [MW]	Inner Support legs [MW]	Outer PRP [MW]	Inner Cooling pipes [MW]	OVT [MW]	IVT [MW]	
0	-	L	0.0032± 0.0004	0.0062± 0.0006	0.00007± 0.00006	0.0004± 0.0001	0.000± 0.000	0.0081± 0.0004	0.00118± 0.00005	
45	✗	L	0.0038± 0.0008	0.216± 0.004	0.0085± 0.0007	0.0029± 0.0004	0.0227	0.296± 0.003	0.591± 0.004	➡ 1.11MW (3.4%)
45	✓	L	0.0036± 0.0005	0.078± 0.001	0.0032± 0.0004	0.0028± 0.0002	0.0069	0.0486± 0.0008	0.0206± 0.0006	➡ 0.15MW (0.5%)
90	✗	L	0.0076± 0.0011	0.962± 0.012	0.044± 0.002	0.0091± 0.0013	0.156± 0.004	1.251± 0.011	1.821± 0.016	
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0	-	H	0.109± 0.003	0.0472± 0.0018	0.0002± 0.0001	0.0049± 0.0004	0.0001± 0.0001	0.108± 0.002	0.0025± 0.0003	
45	✗	H	0.111	0.295	0.0087± 0.0010	0.0116± 0.0009	0.0239	0.461	0.573	➡ 1.47MW (4.5%)
45	✓	H	0.113	0.171	0.0029± 0.0003	0.0118± 0.0006	0.0067	0.180	0.021	➡ 0.50MW (1.5%)
90	✗	H	0.128± 0.002	1.049± 0.006	0.0477± 0.0015	0.0151± 0.0005	0.151± 0.002	1.454± 0.008	1.808± 0.008	
90	✓	H	0.128± 0.004	0.357± 0.005	0.019± 0.001	0.0173± 0.0007	0.049± 0.001	0.414± 0.005	0.149± 0.002	

Results: Location dependent losses

90kAt vacuum ECC field:

- Losses increase dramatically compared with 45kAt (by >3MW for L and similar for H SOL)
- Losses are mainly to dome umbrella, OVT and IVT
- Divertor under-dome cooling pipes hit ~150kW (spread over an area of order 1m – but not uniformly)

LOCUST-gpu: Bicubic spline ECC field (n=3 + n=6 sideband)

I _c [kAt]	Plasma Response ?	n _e (SOL) High/Low [MW]	1 st wall [MW]	Dome Umbrella [MW]	Inner Support legs [MW]	Outer PRP [MW]	Inner Cooling pipes [MW]	OVT [MW]	IVT [MW]	
0	-	L	0.0032± 0.0004	0.0062± 0.0006	0.00007± 0.00006	0.0004± 0.0001	0.000± 0.000	0.0081± 0.0004	0.00118± 0.00005	
45	✗	L	0.0038± 0.0008	0.216	0.0085± 0.0007	0.0029± 0.0004	0.0227± 0.0013	0.296	0.591	→ 1.11MW (3.4%)
45	✓	L	0.0036± 0.0005	0.078± 0.001	0.0032± 0.0004	0.0028± 0.0002	0.0069± 0.0004	0.0486± 0.0008	0.0206± 0.0006	
90	✗	L	0.0076± 0.0011	0.962	0.044± 0.002	0.0091± 0.0013	0.156	1.251	1.821	→ 4.3MW (13%)
90	✓	L	0.0077± 0.0006	0.262± 0.003	0.0197± 0.0007	0.0104± 0.0008	0.043± 0.001	0.239± 0.002	0.146± 0.002	
0	-	H	0.109± 0.003	0.0472± 0.0018	0.0002± 0.0001	0.0049± 0.0004	0.0001± 0.0001	0.108± 0.002	0.0025± 0.0003	
45	✗	H	0.111± 0.004	0.295	0.0087± 0.0010	0.0116± 0.0009	0.0239± 0.0018	0.461	0.573	→ 1.47MW (4.5%)
45	✓	H	0.113± 0.003	0.171± 0.003	0.0029± 0.0003	0.0118± 0.0006	0.0067± 0.0005	0.180± 0.002	0.0211± 0.0007	
90	✗	H	0.128± 0.002	1.049	0.0477± 0.0015	0.0151± 0.0005	0.151	1.454	1.808	→ 4.7MW (14%)
90	✓	H	0.128± 0.004	0.357± 0.005	0.019± 0.001	0.0173± 0.0007	0.049± 0.001	0.414± 0.005	0.149± 0.002	

Results: Location dependent losses

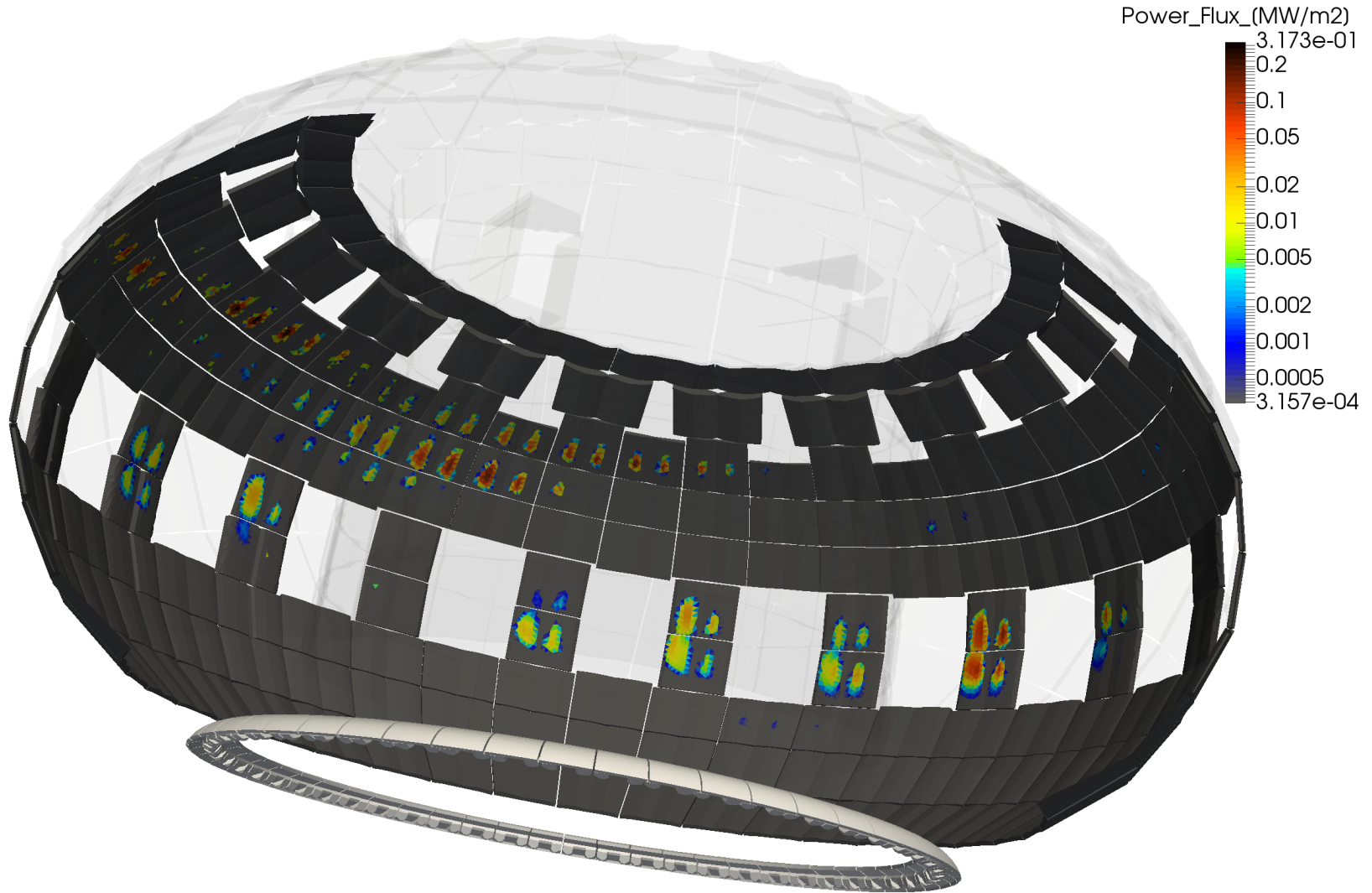
90kAt ECC field incl. plasma screening (MARS-F):

- Sharp rise in Dome umbrella, OVT and IVT losses relative to 45kAt.
- Plasma response effective at reducing losses (by over $\frac{3}{4}$) (reduction to DU, OVT and IVT).
- Screening reduces losses to the under dome cooling pipes by factor 3.

LOCUST-gpu: Bicubic spline ECC field (n=3 + n=6 sideband)

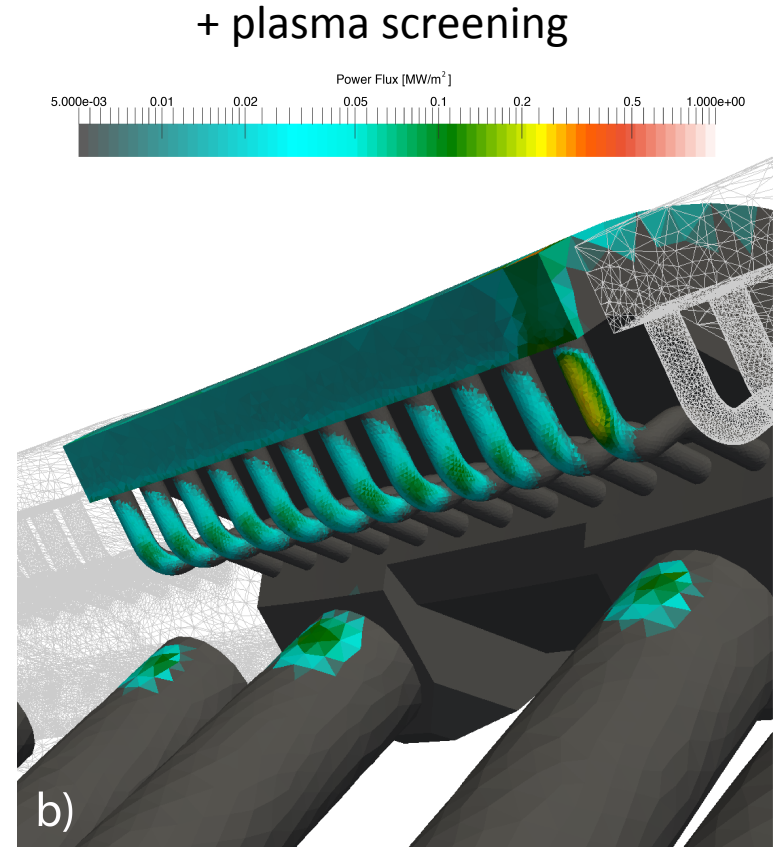
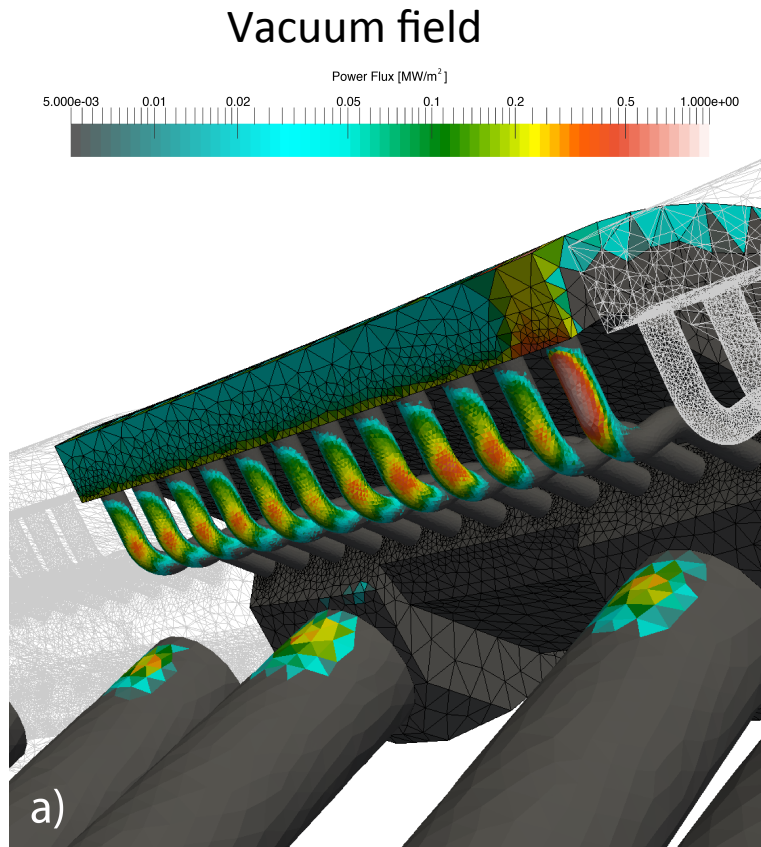
I _c [kAt]	Plasma Response ?	n _e (SOL) High/Low [MW]	1 st wall [MW]	Dome Umbrella [MW]	Inner Support legs [MW]	Outer PRP [MW]	Inner Cooling pipes [MW]	OVT [MW]	IVT [MW]	
0	-	L	0.0032± 0.0004	0.0062± 0.0006	0.00007± 0.00006	0.0004± 0.0001	0.000± 0.000	0.0081± 0.0004	0.00118± 0.00005	
45	✗	L	0.0038± 0.0008	0.216± 0.004	0.0085± 0.0007	0.0029± 0.0004	0.0227± 0.0013	0.296± 0.003	0.591± 0.004	
45	✓	L	0.0036± 0.0005	0.078	0.0032± 0.0004	0.0028± 0.0002	0.0069± 0.0004	0.049	0.021	
90	✗	L	0.0076± 0.0011	0.962	0.044± 0.002	0.0091± 0.0013	0.156	1.251	1.821	➡ 4.3MW (13%)
90	✓	L	0.0077± 0.0006	0.262	0.0197± 0.0007	0.0104± 0.0008	0.043	0.239	0.146	➡ 0.74MW (2.2%)
0	-	H	0.109± 0.003	0.0472± 0.0018	0.0002± 0.0001	0.0049± 0.0004	0.0001± 0.0001	0.108± 0.002	0.0025± 0.0003	
45	✗	H	0.111± 0.004	0.295± 0.004	0.0087± 0.0010	0.0116± 0.0009	0.0239± 0.0018	0.461± 0.006	0.573± 0.005	
45	✓	H	0.113± 0.003	0.171	0.0029± 0.0003	0.0118± 0.0006	0.0067± 0.0005	0.180	0.021	
90	✗	H	0.128± 0.002	1.049	0.0477± 0.0015	0.0151± 0.0005	0.151	1.454	1.808	➡ 4.7MW (14%)
90	✓	H	0.128± 0.004	0.357	0.019± 0.001	0.0173± 0.0007	0.049	0.414	0.149	➡ 1.17MW (3.5%)

Results: Prompt losses from high density SOL



High density SOL: **~0.1MW** of loss to first wall – power flux well below **2MW/m²** Beryllium limit

Results: Cooling pipe assembly power loading (90kAt)



- Gaps between cassettes mean that the end most pipe and edge of each cassette dome take an increased load, by roughly a factor of two (gap~1 missing pipe).
- For vacuum field, flux to pipes broadly consistent with OFMC $0.2\text{-}0.3\text{MW/m}^2$.
- With plasma screening, power flux to the end most pipe reduced from $\sim 0.7\text{MW/m}^2$ to $\sim 0.2\text{MW/m}^2$, close to the expected level for thermal/radiative load.

Summary – concluding remarks & future work

- To address an important engineering question, requiring the coupling of fast ion physics to a detailed model of the ITER divertor, we have developed the **LOCUST-gpu** code for ITER conditions.
- LOCUST can model the power flux to the ITER under-dome sub structure, which occupies a small wetted area ($\sim 1\text{m}^2$) but takes appreciable flux ($\sim 0.2\text{MW}/\text{m}^2$) even though the loss to the components is $<1\%$ of injected HNB power.
- We have improved the mapping of MARS-F data to cylindrical coordinates, and now deploy a fine resolution mesh to capture structure in the plasma response ($0.5\text{cm} \times 0.5\text{cm}$ in R,Z).
- Scans now need to be extended to more ITER scenarios (in particular, lower plasma current than the 15MA baseline H-mode) and more n's, phase settings etc.
- More field structure needs to be included (with low numerical divergence), in particular, the TF ripple field, TBMs and Fe inserts.

Thank you