

# DIAMAGNETIC MHD EQUATIONS FOR PLASMAS WITH FAST FLOW AND ITS APPLICATION TO ELM ANALYSIS IN JT-60U AND JET-ILW NOBUYUKI AIBA<sup>1)</sup>

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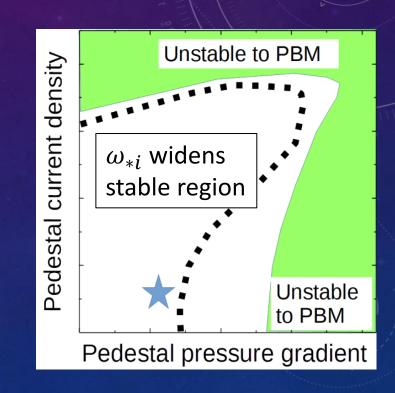
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### BACKGROUNDS



• Peeling-ballooning mode (PBM) with the toroidal mode number n is intermediate ( $\sim 30$ ) triggers the type-I ELM. [Snyder PoP2002 etc.]

- Results in JT-60U and JET-ILW imply higher-n modes sometimes trigger the ELM.[Aiba NF2011, Giroud PPCF2015 etc.]
- "Non-ideal" effects have impact on the stability to high-n MHD modes.
- Stable region becomes wider by the "ion diamagnetic drift  $(\omega_{*i})$ " effect analyzing with the stability condition[Tang NF1980 etc.]  $\gamma \geq 0.5\omega_{*i}$ .



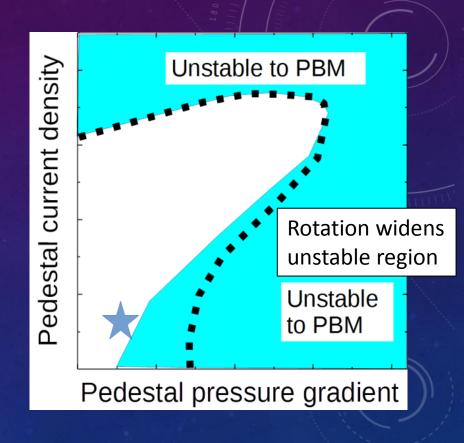


Discrepancy between experiments and numerical analyses becomes larger.

### ROTATION HAS DESTABILIZING EFFECTS ON MHD MODES



- Plasma rotation with shear can destabilize PBM.
   [Snyder NF2007, Aiba NF2009]
- This destabilization plays an important role on type-I ELM stability in JT-60U. [Aiba NF2010]
- Rotation can destabilize intermediate to high-n PBM.



How does rotation act on the PBM stability including the  $\omega_{*i}$  effect?

### DIAMAGNETIC MHD MODEL



#### Fluid models for ELM stability analysis

 $(v_E: \text{ExB drift vel. } v_{\text{thi}}: \text{ion thermal vel. }, \Omega_i: \text{Ion cyclotron freq. })$ 

#### Diamagnetic MHD model [Aiba PPCF2016]:

$$v_E/v_{thi} \sim O(\delta^{\alpha})$$
,  $\omega_0/\Omega_i \sim O(\delta^{1+\alpha})$ ,  $0 < \alpha < 0.5$ 

$$m_i N \left( \left( \frac{\partial}{\partial t} + (\mathbf{V}_{MHD} \cdot \nabla) \right) (\mathbf{V}_E + V_{\parallel} \mathbf{b}) + (\mathbf{V}_{*i} \cdot \nabla) \mathbf{V}_E \right) = \mathbf{J} \times \mathbf{B} - \nabla P.$$

$$\frac{\partial N}{\partial t} + (\boldsymbol{V}_{MHD} \cdot \nabla)N + N\nabla \cdot \boldsymbol{V}_{MHD} = 0,$$

$$\frac{\partial N}{\partial t} + (\mathbf{V}_{MHD} \cdot \nabla)N + N\nabla \cdot \mathbf{V}_{MHD} = 0,$$

$$\frac{\partial P}{\partial t} + (\mathbf{V}_{MHD} \cdot \nabla)P + \Gamma P\nabla \cdot \mathbf{V}_{MHD} = 0, \quad \mathbf{E} + \mathbf{V}_{MHD} \times \mathbf{B} = 0,$$

$$oldsymbol{V} = oldsymbol{V}_{MHD} + oldsymbol{V}_{*i} = oldsymbol{V}_E + oldsymbol{V}_{\parallel} oldsymbol{b}, \quad oldsymbol{V}_E = rac{oldsymbol{E} imes oldsymbol{B}}{B^2}, \quad oldsymbol{V}_{*i} = rac{oldsymbol{E} imes 
abla oldsymbol{V}_{p_i}}{eZNB^2},$$

N: number density, V: velocity, P: pressure,  $\Gamma$ : heat capacity ratio,

**E**: electric field, **B**: magnetic field, **I**: plasma current,  $b \equiv B/B$ ,

e: elementary charge,  $m_i$ : ion mass, Z: effective charge,  $p_i$ : ion pressure

N. Aiba, IAEA FEC2016, 21/Oct./2016

### EXTENDED FRIEMAN-ROTENBERG EQUATION



By introducing plasma displacement  $\xi$ , the derived basic equations can be linearized as follows; an "extended Frieman-Rotenberg equation".

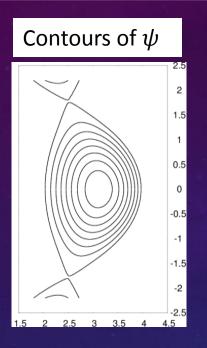
$$\rho_0 \frac{\partial^2 \xi}{\partial t^2} + 2\rho_0 (\mathbf{V}_{0,MHD} \cdot \nabla) \frac{\partial \xi}{\partial t} + \rho_0 (\mathbf{V}_{0,*i} \cdot \nabla) \frac{\partial \xi_{\perp}}{\partial t} = \mathbf{F}_{MHD} + \mathbf{F}_{*i},$$

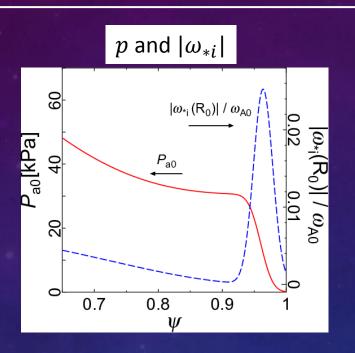
$$\begin{aligned} \boldsymbol{F}_{MHD} &= \boldsymbol{J}_{0} \times \boldsymbol{B}_{1} + (\nabla \times \boldsymbol{B}_{1}) \times \boldsymbol{B}_{0} - \nabla P_{1} \\ &+ \nabla \otimes \left[ \rho_{0} \boldsymbol{\xi} \otimes (\boldsymbol{V}_{0} \cdot \nabla) \boldsymbol{V}_{0,MHD} - \rho_{0} \boldsymbol{V}_{0} \otimes (\boldsymbol{V}_{0,MHD} \cdot \nabla) \boldsymbol{\xi} \right], \\ \boldsymbol{F}_{*i} &= \frac{\rho_{0}}{2eZ_{eff}N_{0}B_{0}^{2}} \{ (\nabla \cdot (\boldsymbol{\xi} \times \nabla P_{0})\boldsymbol{B}_{0} - (\boldsymbol{B}_{0} \cdot \nabla P_{0})\nabla \times \boldsymbol{\xi}) \cdot \nabla \} \boldsymbol{V}_{0,MHD,\perp} \\ &+ \nabla \otimes \left[ \rho_{0} \boldsymbol{\xi} \otimes (\boldsymbol{V}_{0,*i} \cdot \nabla) \boldsymbol{V}_{0,MHD} - \rho_{0} \boldsymbol{V}_{0,*i} \otimes (\boldsymbol{V}_{0,MHD} \cdot \nabla) \boldsymbol{\xi} \right], \end{aligned}$$
Assumptions 
$$\nabla \cdot \boldsymbol{\xi} = 0, \quad (\boldsymbol{B} \cdot \nabla) \boldsymbol{\xi} \ll 1$$

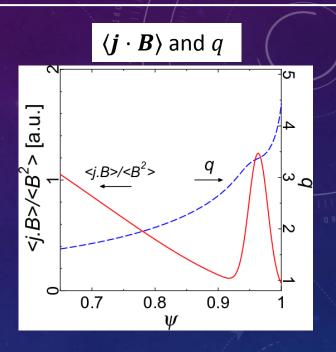
The MINERVA-DI code has been developed to solve this equation.

# PBM STABILITY WITH $\omega_{*i}$ IS ANALYZED IN A ROTATING TOKAMAK





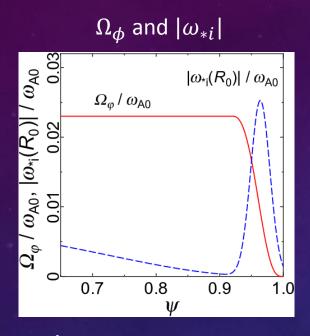


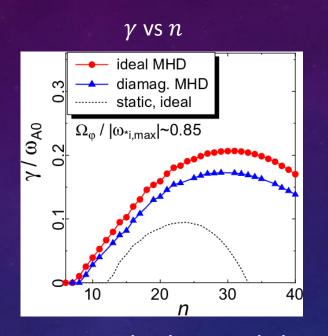


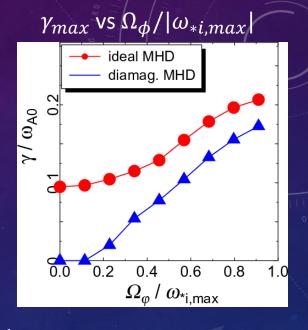
- PBM stability is analyzed in D-shaped (double-null) plasma.
- Density is assumed as  $N = 5.0 \times 10^{19} [1/m^3]$ .
- PBM stability is analyzed for  $1 \le n \le 40$ .

# ROTATION CAN MINIMIZE THE $\omega_{*i}$ EFFECT ON PBM









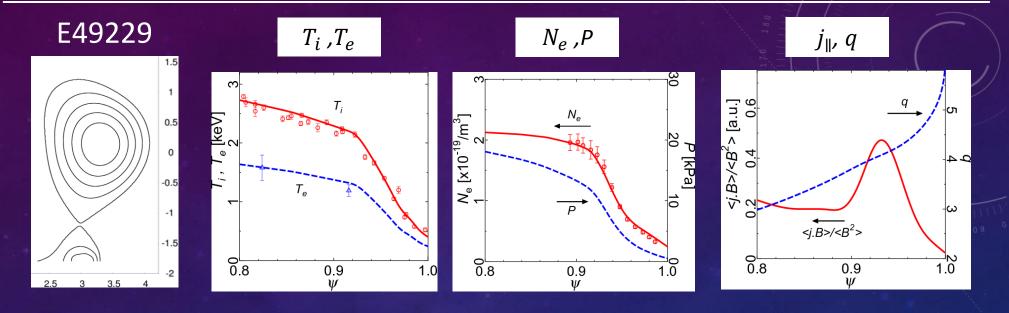
- Plasma rotation excites PBM, which is stabilized by  $\omega_{*i}$  in static case.
- The threshold rotation frequency  $\Omega_{\phi}$  is smaller than  $\omega_{*i}$ .
- When  $\Omega_{\phi}$  becomes comparable to  $\omega_{*i}$ , PBM stability is not affected so much by  $\omega_{*i}$



Plasma rotation minimizes the  $\omega_{*i}$  effect on PBM stability.

### TYPE-I ELMY H-MODE DISCHARGE IN JT-60U



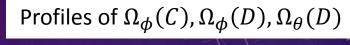


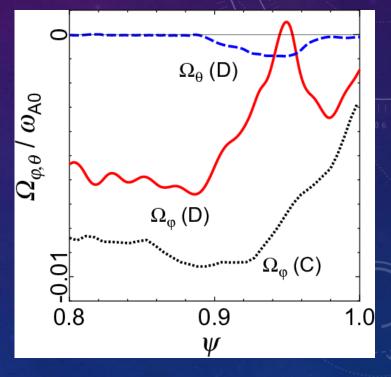
- Plasma profiles were measured with CXRS  $[T_i, \Omega_{\phi}(C)]$ , LiBP  $[n_e]$ , TS  $[T_e]$ ; note that  $T_e$  profile is assumed as  $T_e = 0.6T_i$ .
- Current density near pedestal is estimated as the bootstrap current  $j_{BS}$ .
- PBM stability is analyzed for  $1 \le n \le 40$ .

# ROTATION PROFILE IS DETERMINED BASED ON THE NEOCLASSICAL THEORY



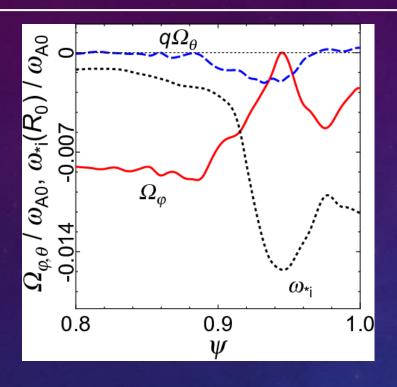
- Deuterium rotation profile is evaluated based on the neoclassical theory with MI by CHARROT code [Honda NF2013].
- CHARROT determines the profile by calculating radial electric field through radial force balance equation with measured  $\Omega_{\phi,imp}$ ,  $T_{imp}$ , and  $N_{imp}$  evaluated with  $Z_{eff}$ .
- Both toroidal and poloidal rotation are taken into account in the stability analysis; slow poloidal rotation is assumed.

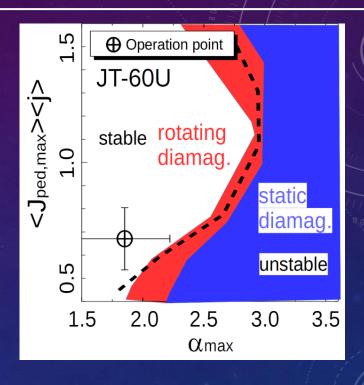




# PLASMA ROTATION COUNTERACTS $\omega_{*i}$ EFFECT ON PBM STABILITY BOUNDARY IN JT-60U



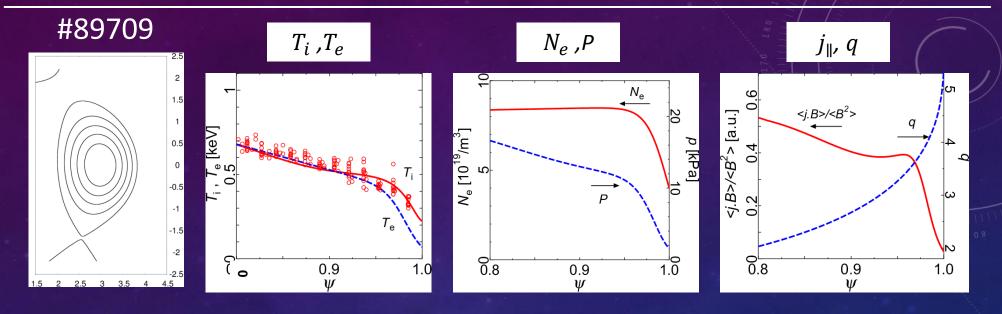




- Stabilizing effect due to  $\omega_{*i}$  pushes the stability boundary away from the operation point.
- Rotation realizes to bring back the boundary near the operation point.

### HOW ABOUT IN JET-ILW PLASMAS?

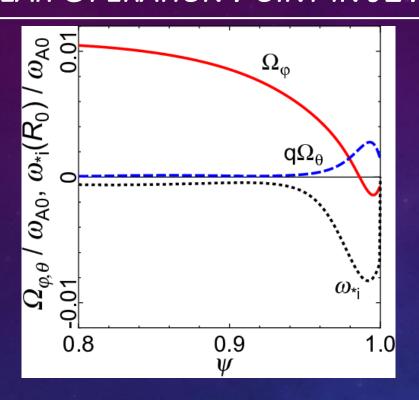


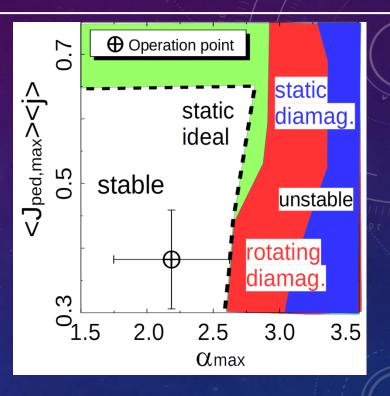


- Plasma profiles were measured with CXRS  $[T_i, \Omega_{\phi}(C)]$ , HRTS $[n_e, T_e]$ .
- Deuterium rotation and  $j_{BS}$  profiles are estimated with CHARROT.
- High density reduces  $j_{BS}$  due to increasing collisionality.
- The stability of  $2 \le n \le 100$  modes is analyzed numerically.

# PLASMA ROTATION CAN BRING PBM STABILITY BOUNDARY NEAR OPERATION POINT IN JET-ILW







Plasma rotation minimizes the  $\omega_{*i}$  stabilizing effect on PBM, and brings back the boundary near the operation point.

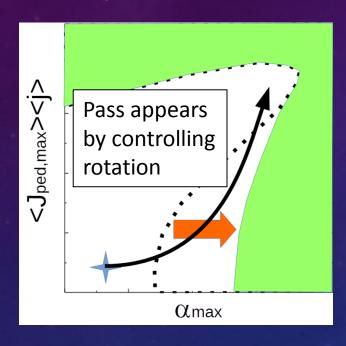


Rotation plays an important role on the ELM stability in JT-60U and JET-ILW.

### DISCUSSION FOR GETTING HIGH PEDESTAL ROBUSTLY IN ITER



Stability diagram determined with  $\omega_{*i}$  and rotation.



- Trajectory during pedestal build-up doesn't intersect with the stability boundary => O.K..
- In case trajectory intersects with the boundary, we have to consider how to avoid the situation as the JET-ILW case.
- To make the pass to the corner,
  - $\checkmark$  Increasing  $j_{ped}$  by reducing collisionality
  - ✓ Seeding low-Z impurity
    [Dunne EX/3-5, Giroud EX/P6-3]
  - ✓ Increasing core pressure [Urano EX/3-4, Chapman EX3-6]
  - ✓ Minimizing rotation [this work]

Predicting rotation and analyzing the pedestal stability with the rotation help to obtain high pedestal robustly in ITER.

### SUMMARY



- Diamagnetic MHD model has been developed to analyze ion diamagnetic drift effect on peeling-ballooning (PBM) stability in rotating plasmas.
- An extended Frieman-Rotenberg equation has been derived from the diamagnetic MHD model.
- MINERVA-DI code was developed to solve the equation.
- It is found that plasma rotation can minimize the ion diamagnetic drift  $(\omega_{*i})$  effect on PBM stability.
- Minimization of  $\omega_{*i}$  effect by rotation plays an important role on PBM stability in both JT-60U and JET-ILW.
- Stability analysis including  $\omega_{*i}$  and rotation helps to realize high pedestal performance robustly in ITER.

**APPENDIX** 



## APPROXIMATIONS USED FOR SIMPLIFYING THE DRIFT MHD MODEL



We simplify the model with Frieman-Rotenberg formalism. **Approximations:** 

In Faraday's law, non-ideal term is neglected.

$$\frac{\partial \boldsymbol{B}}{\partial t} = \nabla \times \boldsymbol{E} = -\nabla \times \left(\boldsymbol{V}_{MHD} \times \boldsymbol{B} + \frac{1}{eN} \nabla p_{e\parallel}\right)$$
This approximation can be justified when

- Rotation is enough slow compared to ion thermal velocity.
- Density N or temperature T is constant in a plasma
- Functional form of N is proportional to that of T.
- Magnetic field varies slowly  $\nabla \times (\boldsymbol{b}/B) \ll 1$ . This helps to change the continuity equation as follows.

$$\left. \frac{DN}{Dt} \right|_{MHD} + N\nabla \cdot \boldsymbol{V}_{MHD} = 0$$

### POLOIDAL ROTATION CAN AFFECT EDGE MHD STABILITY



Difference of the mode freq.  $n\omega$  from the Doppler-shifted freq.  $k \cdot v$  is essential for destabilizing edge MHD modes.[Aiba NF2011].

$$\mathbf{k} \cdot \mathbf{v} = -in\Omega_{\phi} + im\Omega_{\theta}$$

 $Ω_{\phi}$ : Toroidal rotation Freq., n: Toroidal mode num.,

 $\Omega_{\theta}$ : Poloidal Rotation freq. m: poloidal mode num.

For the Fourier harmonics which satisfy m-nq=0,  $m\Omega_{\theta} \sim n\Omega_{\phi}$  even when  $v_{\theta}=(nr/mR)v_{\phi} \sim 0.1v_{\phi}$  if q=3 and  $R/r \sim 3.3$ .

$$= \iota \Omega_{\parallel}(\boldsymbol{k} \cdot \boldsymbol{B}/B) - \iota n \Omega_{E \times B}$$

 $\Omega_{\parallel}$ : Freq. parallel to  $\boldsymbol{B}$  $\Omega_{E\times B}$ : Freq. perp. to  $\boldsymbol{B}$ 

Near rational surfaces,  $\mathbf{k} \cdot \mathbf{v} \sim 0 \rightarrow \Omega_{E \times B}$  will be important.

MINERVA(-DI) can identify the poloidal rotation effect on MHD stability (at present, poloidal rotation effect on equilibrium is neglected.)

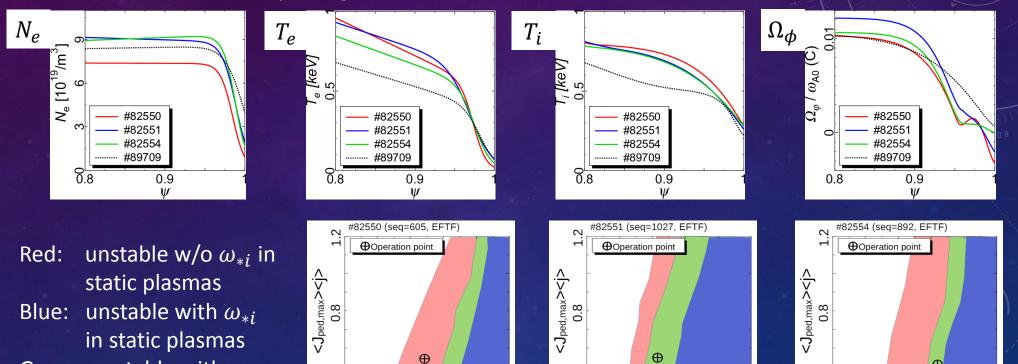


Re-evaluate stability diagram with not only  $\Omega_{\phi}$  but also  $\Omega_{\theta}$ .

# VALIDATION STUDY OF THE NEW MODEL FOR ELM STABILITY ANALYSIS IN JET-ILW



To confirm the validity of the new model for analyzing ELM stability in JET-ILW, stability diagrams were made in several shots.



In any cases, the diamagnetic MHD model is the best to obtain the boundary near the operation point.

TH/8-1 N. Alba, IAEA FEC2016, 21/Oct./2016

4.0 4.5

2.5

3.0

3.5

4.0 4.5

2.5

3.0

3.5

 $\alpha$ max

4.0 4.5

2.5

3.0

3.5

 $\alpha$ max

Green: unstable with  $\omega_{*i}$ 

in rotating plasmas

# SENSITIVITY STUDY OF STABILITY ON $T_i$ PROFILE (1)



The stability with  $\omega_{*i}$  and rotation is affected by  $T_i$  profile, because

1. increase of  $\omega_{*i}$  due to

$$\omega_{*i} = \frac{n}{e_i n_i} \frac{dp_i}{d\psi}.$$

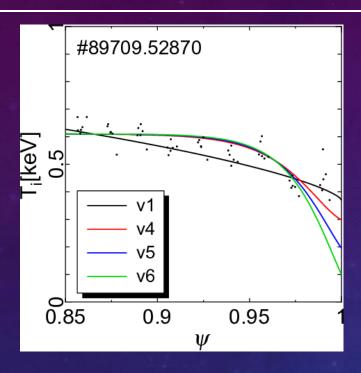
2. Increase of  $v_{ heta}$  due to neoclassical theory as

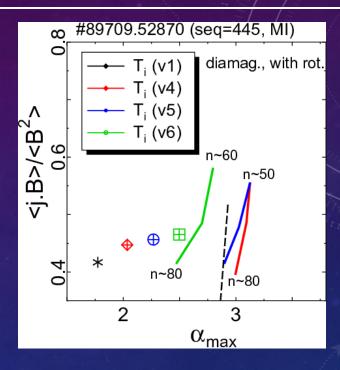
$$v_{\theta} \propto \frac{1}{Z_i} \frac{dT_i}{d\psi}.$$

Since  $\omega_{*i}$  stabilizes PBM but  $\Omega_{\theta}$  destabilizes it, it is necessary to understand the sensitivity of stability on  $T_i$  profile.

# SENSITIVITY STUDY OF STABILITY ON $T_i$ PROFILE (2)



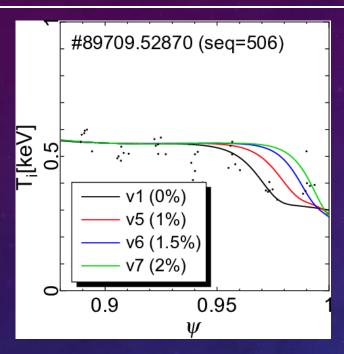


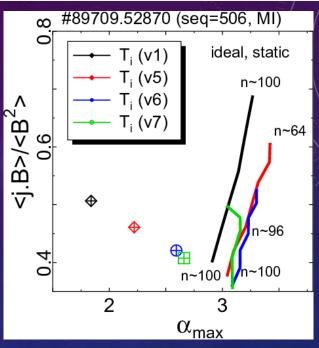


- Plasma toroidal rotation contributes to shift back the boundary to the lower  $\alpha_{max}$  side.
- In particular, with  $T_i$  (v6), the boundary moves close to the O.P. (within 10%).
- The stability is sensitive to  $T_i$  profile near very edge;  $T_{i,sep} = 200 \, \text{eV} \, (\text{v5}), \, 100 \, \text{eV} \, (\text{v6}).$

# SENSITIVITY STUDY OF STABILITY ON $T_i$ PROFILE (3)





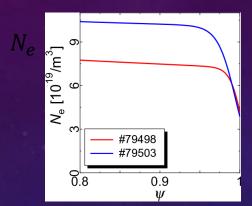


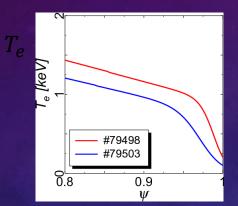
- By shifting the  $T_i$  profile outward, the  $\alpha_{max}$  value increases due to that both  $\frac{dT}{d\psi}$  and  $\frac{dn}{d\psi}$  become large at the same radial position.
- The stability boundaries with different  $T_i$  profiles are similar to each other, but the O.P. moves to higher  $\alpha_{max}$  side.
- => The difference between the O.P. and boundary becomes smaller as the  $T_i$  profile is shifted outward.

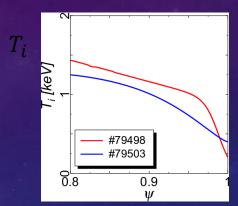
## ELM STABILITY ANALYSIS IN JET-C WITH NEW MODEL (1)

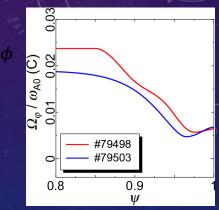


The difference in stability determined with conventional and new methods was confirmed in JET-C; stability in JET-C has been well-explained with conventional method.









#### Conventional method:

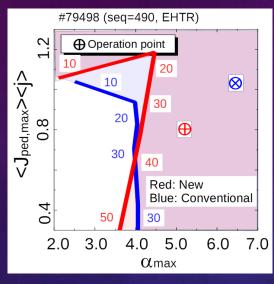
- Ideal stability in static plasma.
- Maximum n number analyzed is  $n_{max} = 30$ .
- Sauter model determines pedestal BS current with  $T_i = T_e$ .

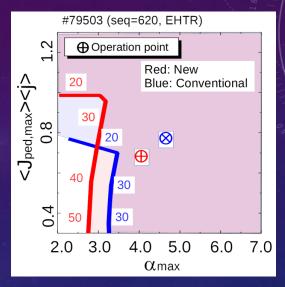
#### New method:

- Diamagnetic stability with  $\omega_{*i}$  and rotation.
- Maximum n number analyzed is  $n_{max} = 100$ .
- MI model determines pedestal BS current with measured  $T_i$ .

### ELM stability analysis in JET-C with new model (2)







New method agrees well with experiments, and shows the difference from the conventional method as follows.

- #79498 (low density)
  - ✓ boundary is similar to the conventional one.
  - ✓ operation point approaches to the boundary.
- #79503 (high density)
  - ✓ Boundary and operation point shift to lower  $\alpha_{max}$  side.