

# Dynamic method to study turbulence and turbulence transport

S. Inagaki, K. Ida<sup>1</sup>, S.-I. Itoh, K. Itoh<sup>1</sup>, T. Tokuzawa<sup>1</sup>, N. Tamura<sup>1</sup>, S. Kubo<sup>1</sup>,  
T. Shimosuma<sup>1</sup>, K. Tanaka<sup>1</sup>, H. Tsuchiya<sup>1</sup>, Y. Nagayama<sup>1</sup>, T. Kobayashi<sup>2</sup>, N. Kasuya,  
M. Sasaki, A. Fujisawa, Y. Kosuga<sup>3</sup>, K. Kamiya<sup>4</sup>, H. Yamada<sup>1</sup>, A. Komori<sup>1</sup> and LHD  
experiment group<sup>1</sup>

*Research Institute for Applied Mechanics, Kyushu University*

<sup>1</sup>*National Institute for Fusion Science*

<sup>2</sup>*Interdisciplinary Graduate School of Engineering Sciences, Kyushu University*

<sup>3</sup>*Institute for Advanced Study, Kyushu University*

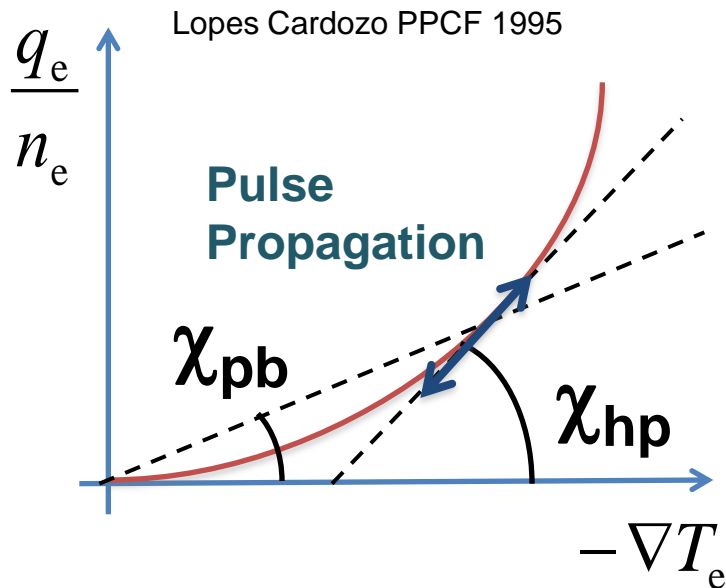
<sup>4</sup>*Japan Atomic Energy Agency*

# Revisiting heat pulse propagation analysis

## Discovery of the New Transport Relation on LHD

### Conventional Approach

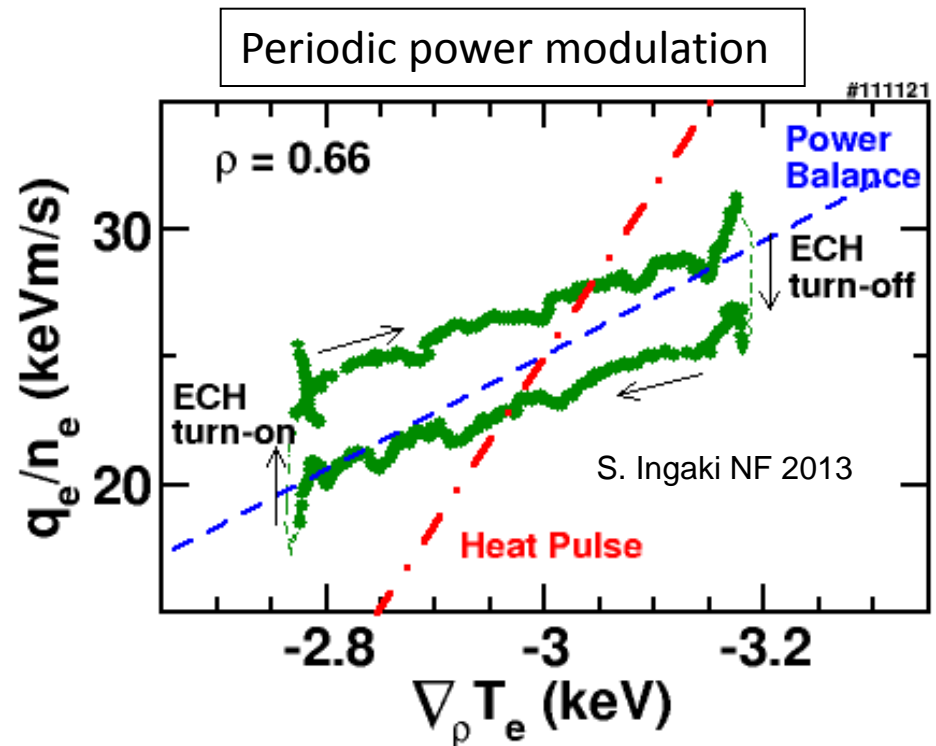
$$\chi_{hp} = \frac{-\partial q_e}{n_e \partial \nabla T_e} \neq \frac{-q_e}{n_e \nabla T_e} = \chi_{pb}$$



Single-Valued Function

One time-scale

### Conventional method has serious difficulty



Multiple-Valued Function  
(→ hysteresis)

Two time-scales

## Method to study turbulence transport

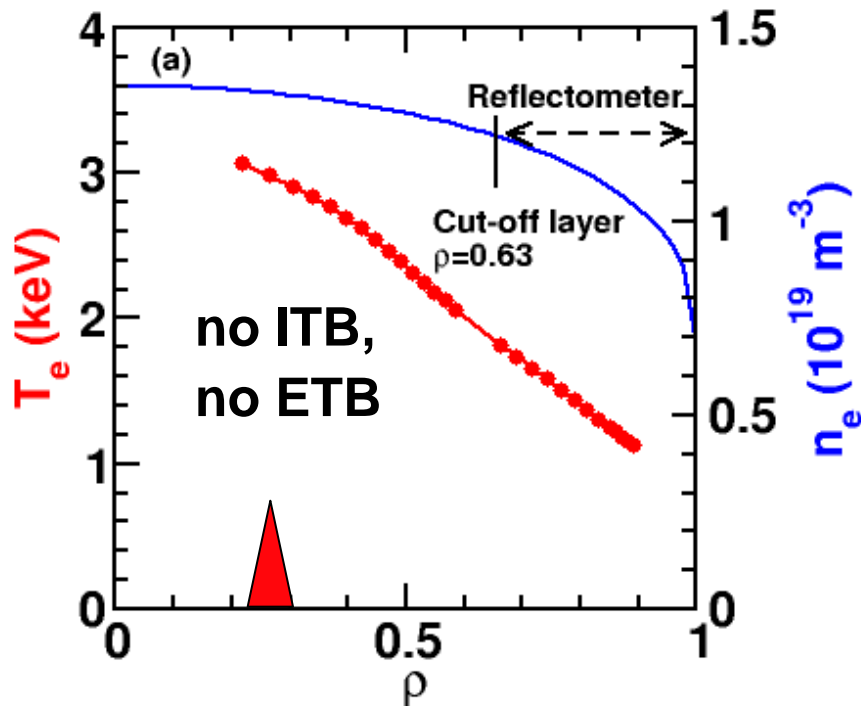
- Assessment of conventional method (What is  $\chi_{hp}$ ?).
- A simplified new approach to understand the transport with multiple-valued flux (hysteresis, barrier formation)

## Method to observe multi-scale couplings of turbulence

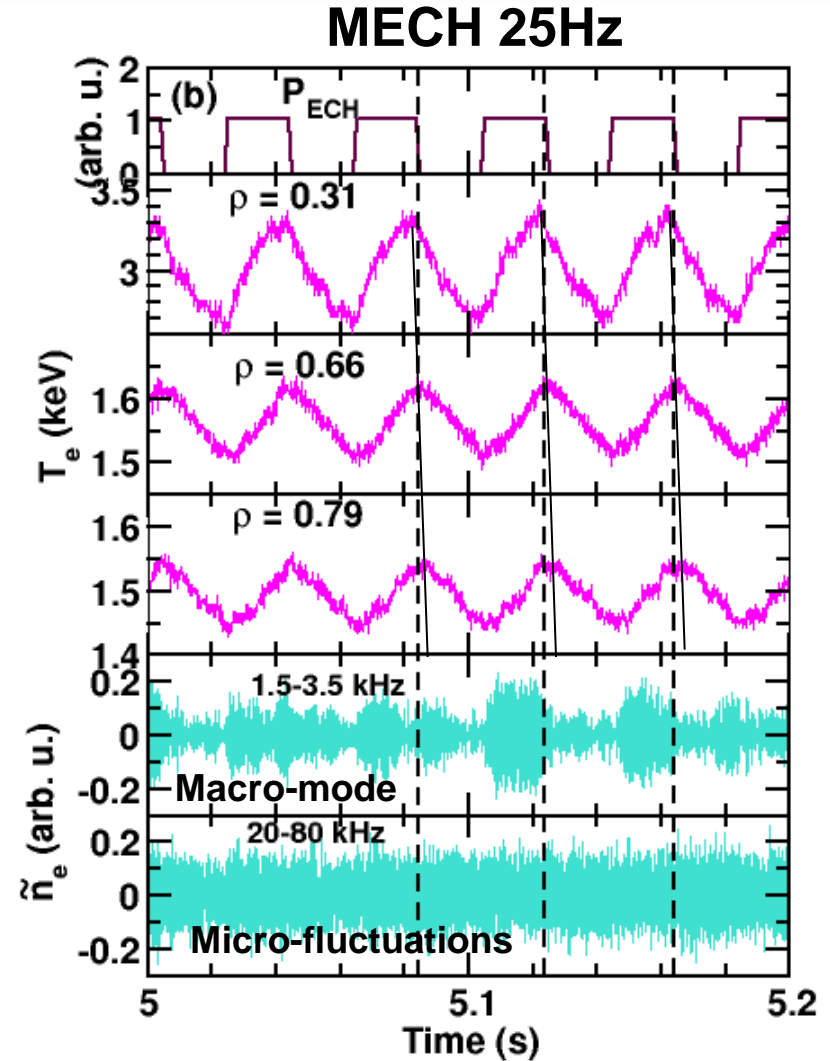
- Observation of coupling of micro-fluctuations at distant locations

# Exp. Set-up and Conditional Averaging

- Target plasma (NBI+MECH)
- Modulations of  $T_e$ ,  $\nabla T_e$  and fluctuation are observed simultaneously



no evidence of high-energy tail

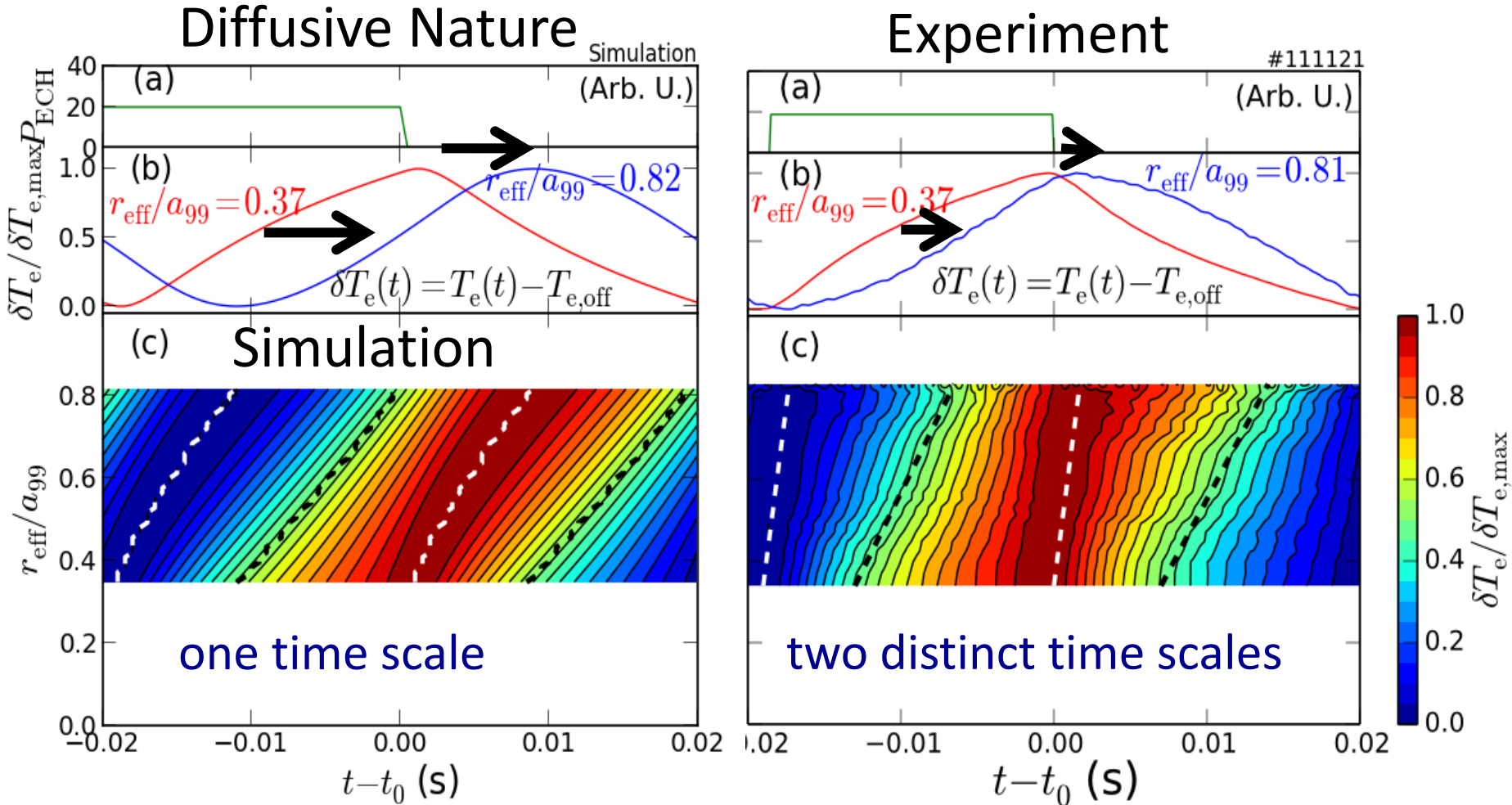


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Periodic temporal evolution of signals are precisely extracted.

# Precise spatiotemporal structure of heat pulse <sup>5</sup>

Conditional averaging technique is very powerful tool

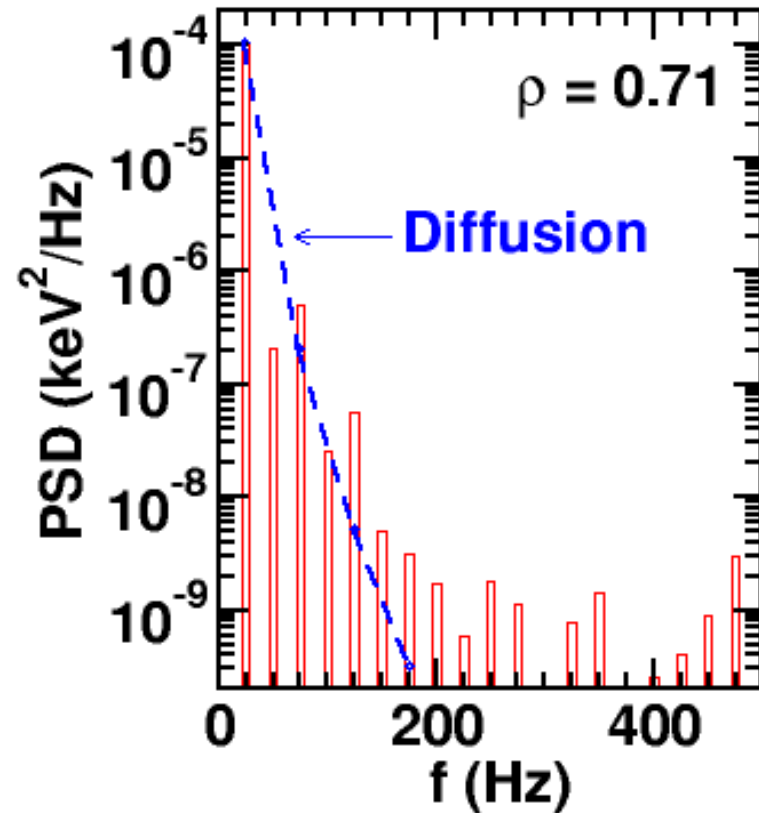
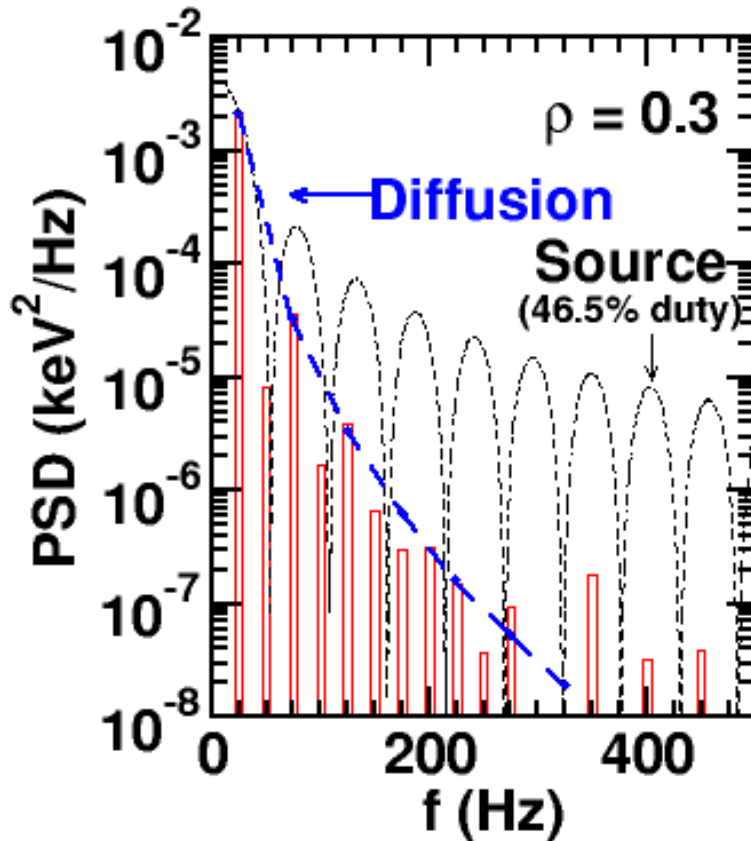


The conventional  $\chi_{\text{hp}}$  is flawed since it neglects two time scales in transient response.

# Higher harmonics in the heat pulse propagation<sup>6</sup>

The two-time scale feature should appear in the response of extremely-higher harmonics

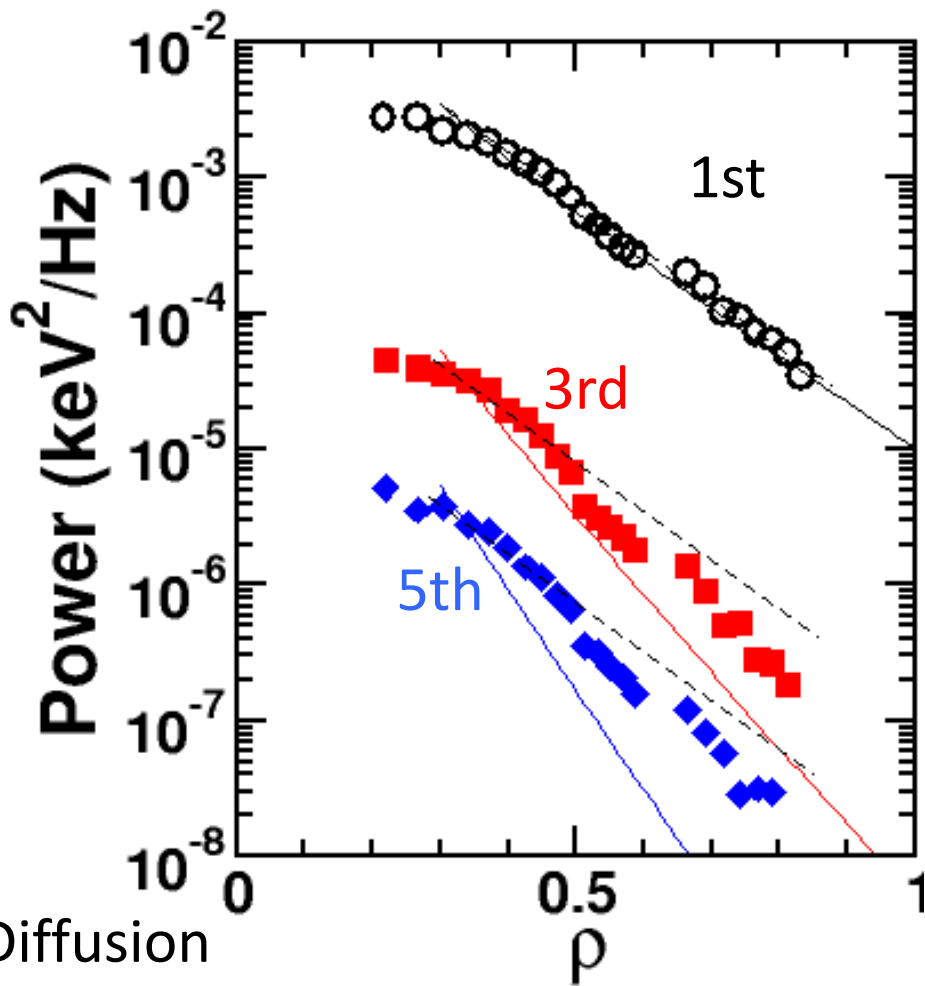
(Conditional Averaged)



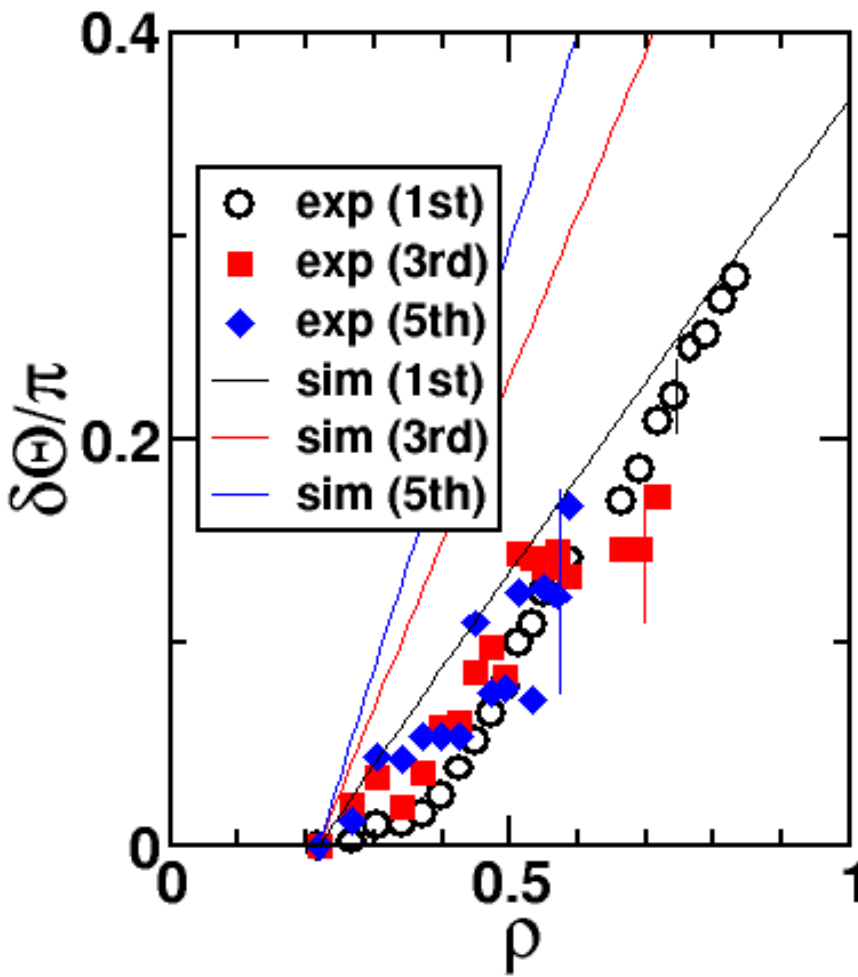
More-than 10th harmonics are observed even far away from source

# Features of Higher harmonics

Weaker decay in amplitude



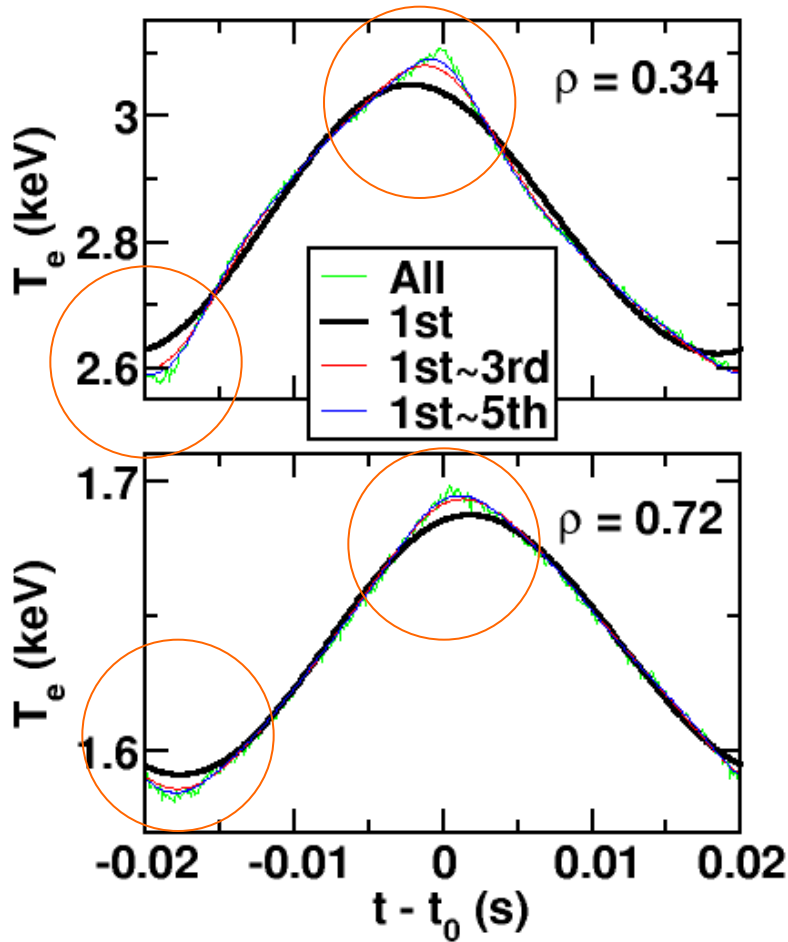
Faster propagation



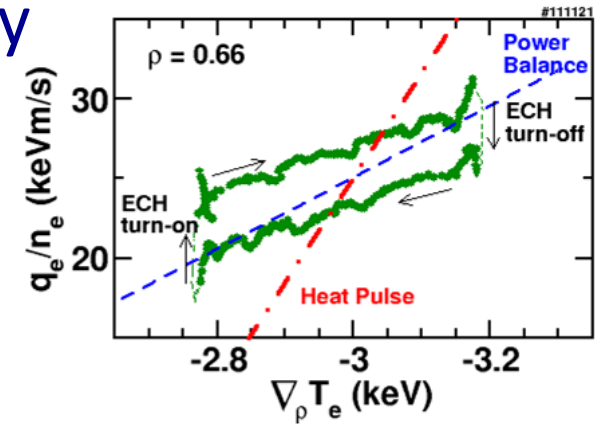
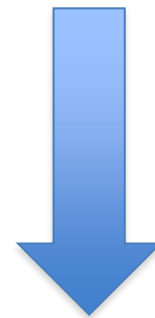
$$\frac{1}{A} \frac{\partial A}{\partial r} \sim \frac{1}{Q} \frac{\partial Q}{\partial r} \mu \sqrt{m}$$

Observations far from diffusive nature

# Higher harmonics in the heat pulse propagation<sup>8</sup>



Fundamental mode can not catch the response around turn-on/off of ECH power where  $q_e$  changes discontinuously



To describe a discontinuous function, higher harmonics is essential

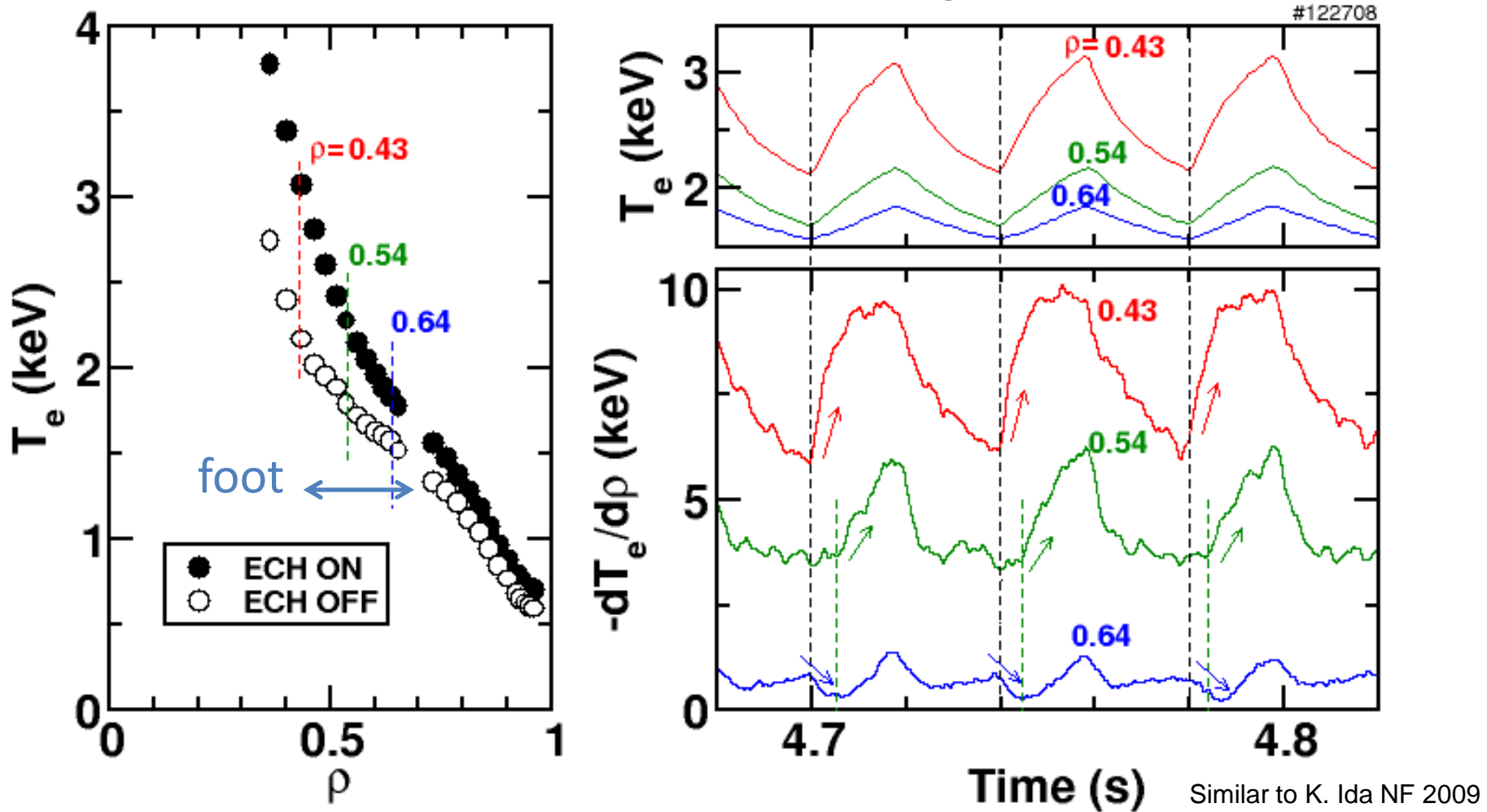
Higher harmonics should be more routinely checked to clarify the transport with multiple-valued flux



# Heat pulse propagation during ITB transition

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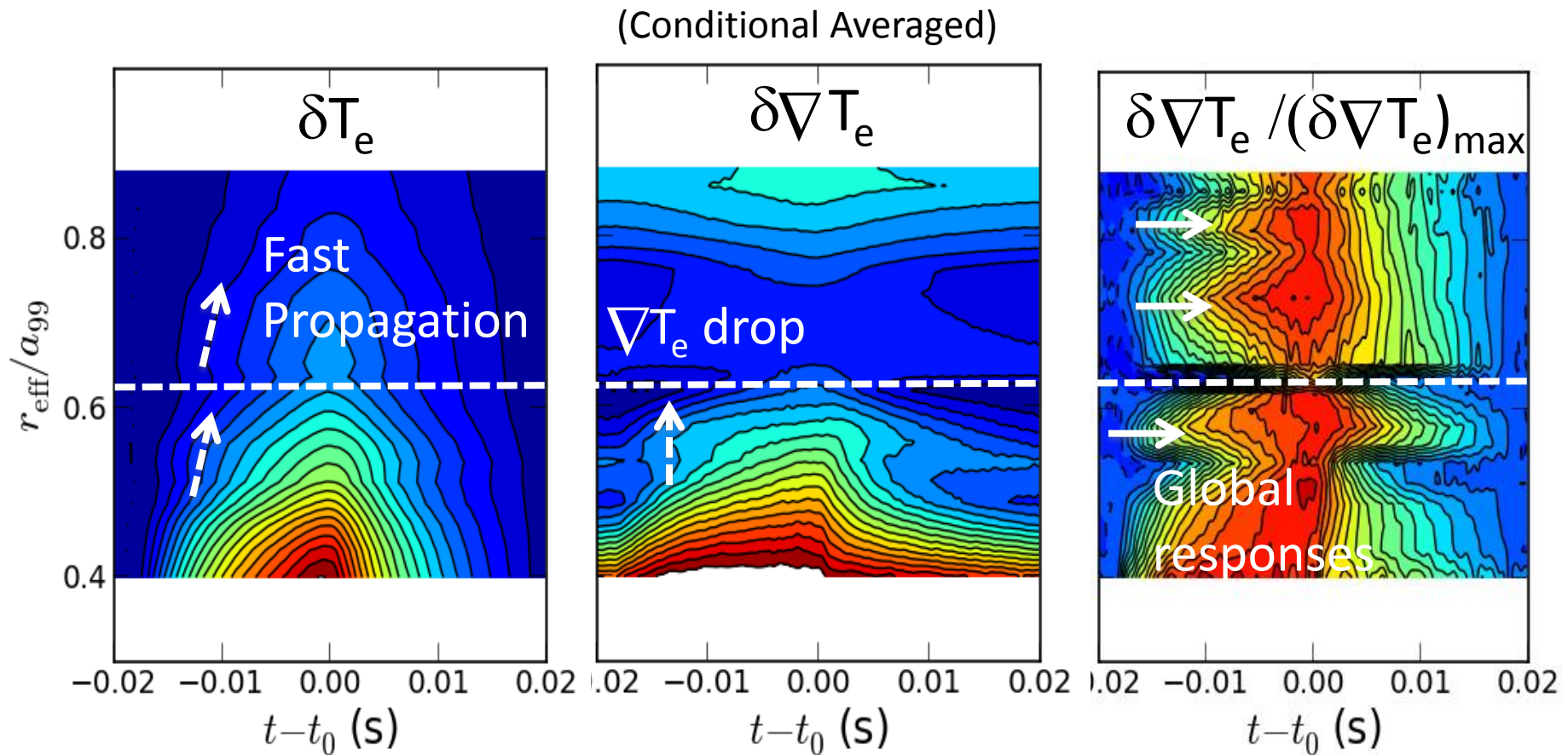
- ECH modulation experiment near the ITB transition
- The ITB foot shifts back and forth during ECH modulation



Delayed rises and simultaneous drops are observed

# Mixed time-scale phenomena

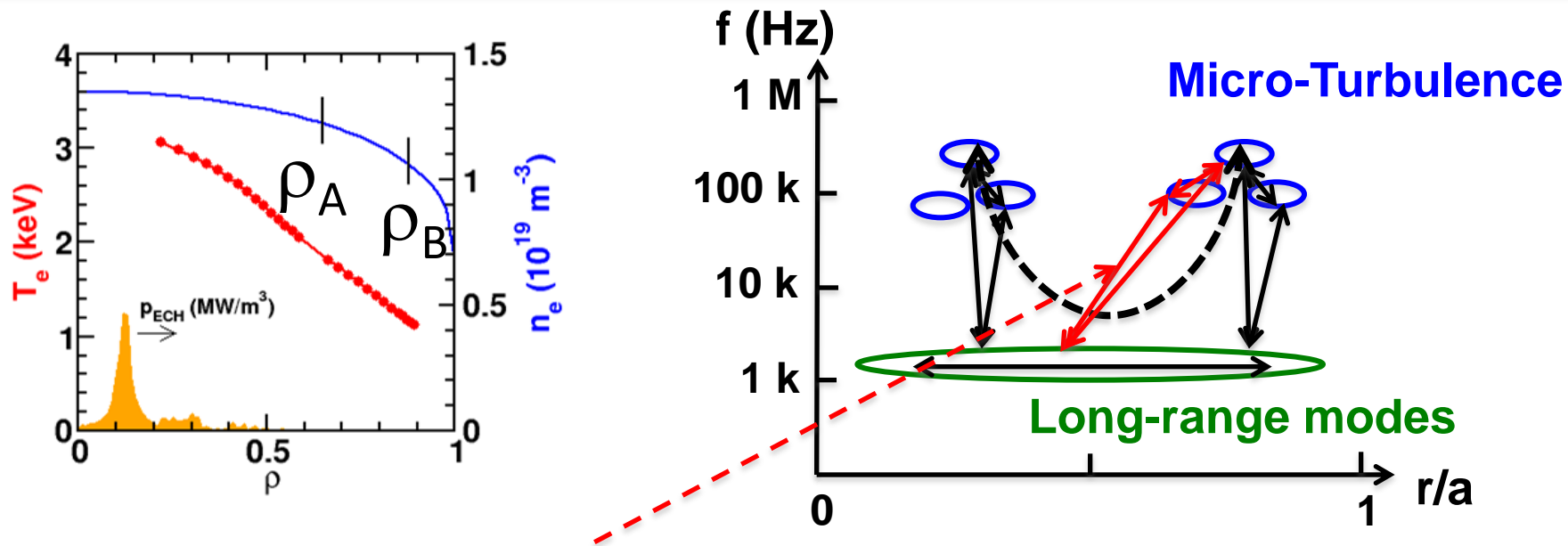
- Three or four dynamics combined
- Fast propagation, Displacement of ITB front, Global (non-local) response in  $\nabla T_e$



ITB transition is involved with multi-mechanisms

# Method to observe multi-scale couplings of turbulence

Non-locality of turbulence is one of the important keys to understand the multiple-valued flux (hysteresis and two time-scale response)



## Non-Local Bi-Coherence

$$b_{nl}^2(f_1, f_2) = \frac{\left| \left\langle F^*(f_3, r_A) f(f_1, r_B) f(f_2, r_B) \right\rangle \right|^2}{\left\langle |F(f_3, r_A)|^2 \right\rangle \left\langle |f(f_1, r_B) f(f_2, r_B)|^2 \right\rangle}$$

$\phi(f_1, \rho_B), \phi(f_2, \rho_B)$ : Fluctuations at  $\rho_B$

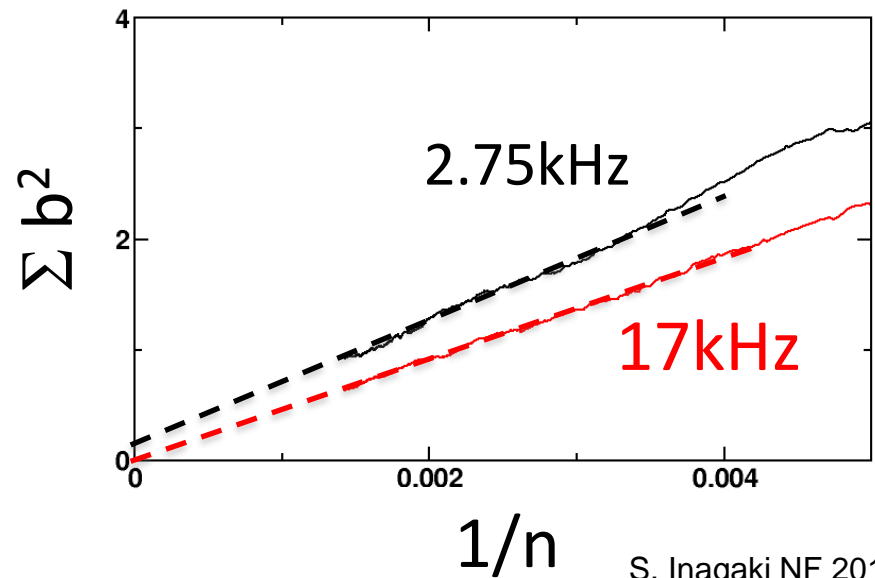
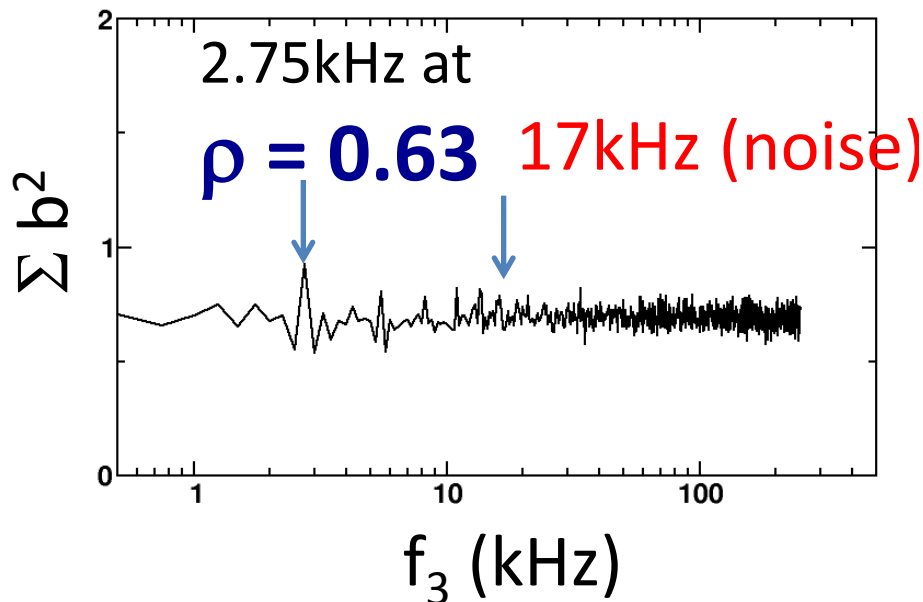
$\Phi(f_3, \rho_A)$ : Fluctuations at  $\rho_A$

$\rho_B - \rho_A \gg$  correlation length of micro-modes

# Non-Local Micro-Global Coupling

- Summed bi-coherence shows a peak at 2.75 kHz
- The summed bi-coherence converges to 0.2 (~1/10 of the local summed bi-coherence)

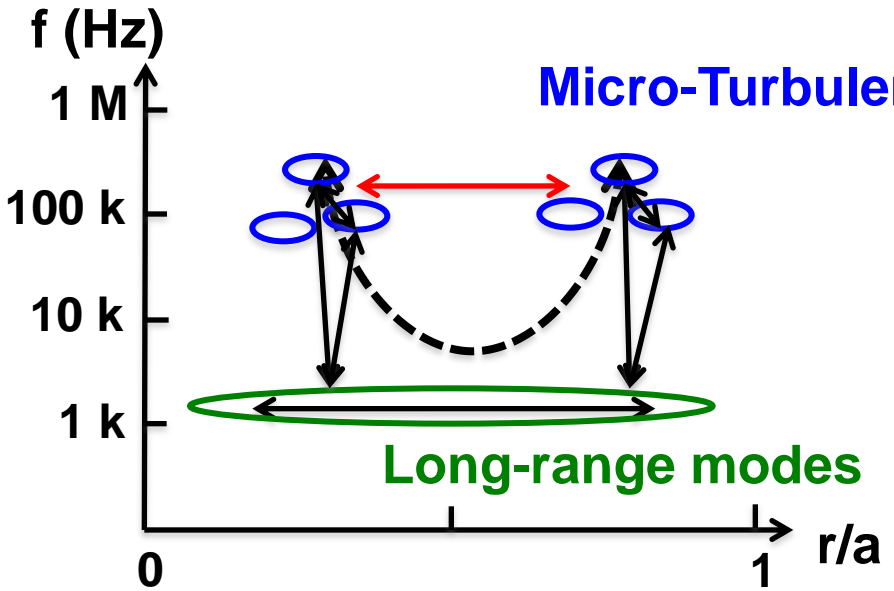
150 kHz <  $f_1$  < 250 kHz at  $\rho = 0.88$



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Global fluctuation(2.75 kHz) at  $\rho_A = 0.63$  non-locally couples with micro-fluctuations (150-250 kHz) at  $\rho_B = 0.88$

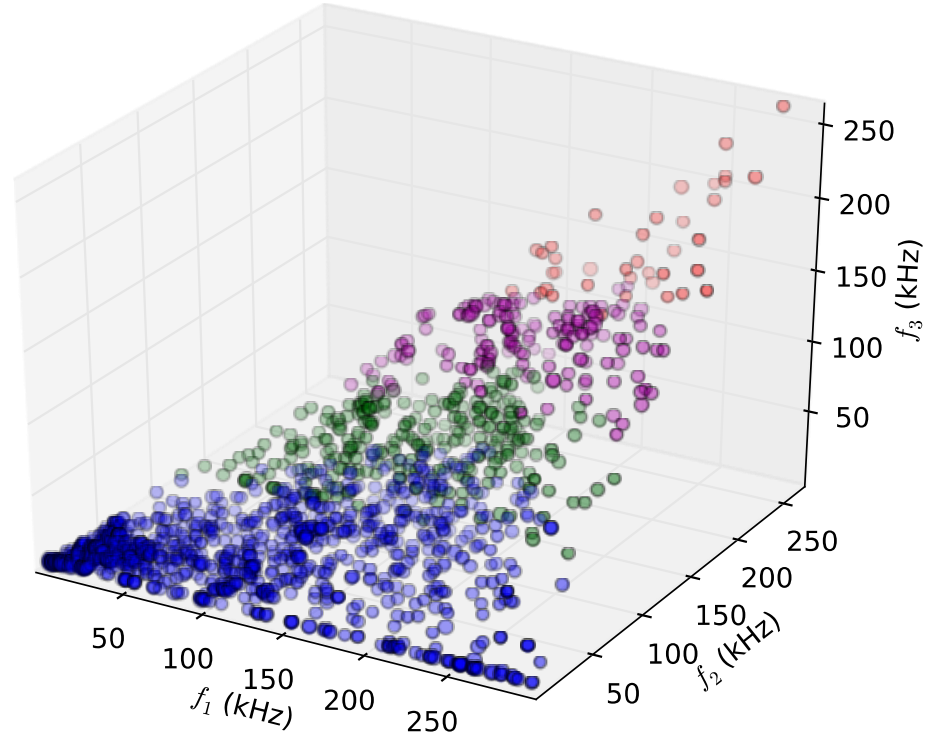
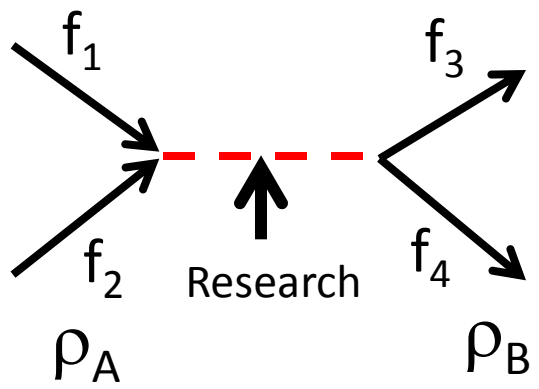
# Tri-Coherence analysis is just started



$$\gamma_{\text{tri}}^2 > 0.1$$

4-Wave coupling between distant locations

$$f_1 + f_2 = f_3 + f_4$$



Tri-coherence at two distant locations is calculated

This study established methods for analyzing (i) heat transport dynamics beyond Fick's law and (ii) 'non-local' coupling of micro-fluctuations.

- Conditional averaging technique is very useful to understand the transport with multiple-valued flux

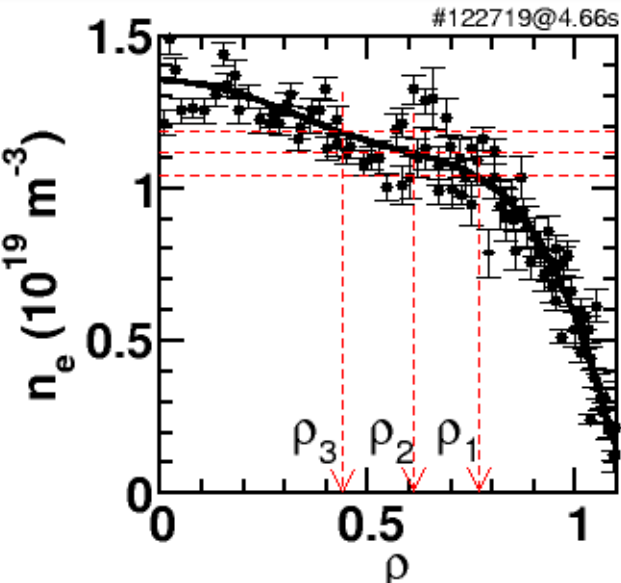
Hysteresis in transport = two-time scale response  
= Slow decay and fast propagation of the higher harmonics

Identification of three or four time-scale responses in the ITB plasma

- Non-local bi-/tri-spectrum analysis allows us to study the non-local coupling between micro-fluctuations

**These results are beneficial for understanding of the plasma dynamics in future fusion reactors.**

# Non-Local Micro-Micro Coupling



Tri-coherence suggests

- Micro-fluctuations ( $>50$  kHz) at two different locations are coupled
- Global-fluctuations ( $<10$  kHz) are involved

Like-scale couplings e.g.  $102\text{kHz} + 101\text{kHz} \rightarrow 99\text{kHz} + 103\text{kHz}$

$< 10 \text{ kHz}$                        $< 10 \text{ kHz}$

