

Integration of Customized MHD Modeling into a Digital Engineering Workflow for Advanced Liquid Metal Blankets

Presenter: **Andrei Khodak**

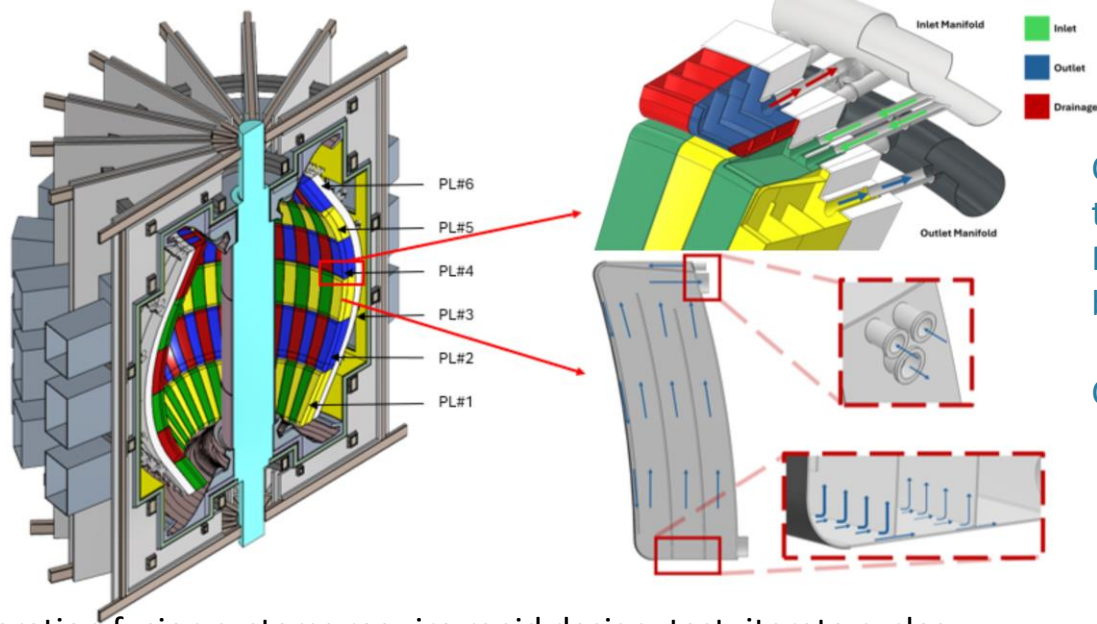
Collaborators:

Rajesh Maingi, Han Zhang Princeton Plasma Physics Laboratory

Colin Baus, Luigi Candido, Carli Smith, Jack Taylor, Bibake Uppal Kyoto Fusioneering

Work supported in part by the U.S. DOE INFUSE Program

Motivation



- Next-generation fusion systems require rapid design–test–iterate cycles
- Digital engineering offers unified workflows for design, simulation, and validation
- Liquid metal (LM) blankets present complex multi-physics challenges:
 - Strong magnetic fields
 - Complex 3D geometries
 - Coupled thermal, structural, and neutronic loads
- Need for scalable, high-fidelity MHD modeling integrated into engineering platforms

Outline

- Problem Set-up, Preparation and Meshing
- CFD Modeling at PPPL
- MHD
- Virtual Prototyping System
- Coupling
- Transient Flows
- Multiphysics Analysis

Outline

- Problem Set-up, Preparation and Meshing
- CFD Modeling at PPPL
- MHD
- Virtual Prototyping System
- Coupling
- Transient Flows
- Multiphysics Analysis

Problem Set-up



5

Dear Andrei,

As discussed, please find attached the outboard equatorial module of SCYLLA BB.

I also attach a picture showing the LiPb flow path.

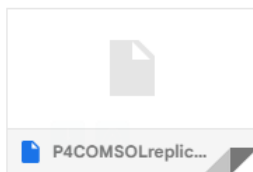
- Inlet temperature: 773.15 K
- Inlet flow rate: 80.46 kg/s
- Tungsten volumetric heating: 31 MW/m³
- Lithium Lead volumetric heating: $16.5119 \cdot \exp(-0.0538 \cdot y)$ MW/m³, y in cm
- Tungsten surface heat flux: 0.5 MW/m²


You should have all the data related to material properties. It would be interesting to see how the results change using a thermal conductivity for SiCf/SiC in the range 10-20 W/m/K, and the usual comparison with 0T/4T magnetic field. We can discuss also other sensitivity analyses. Let me know if you have any questions.

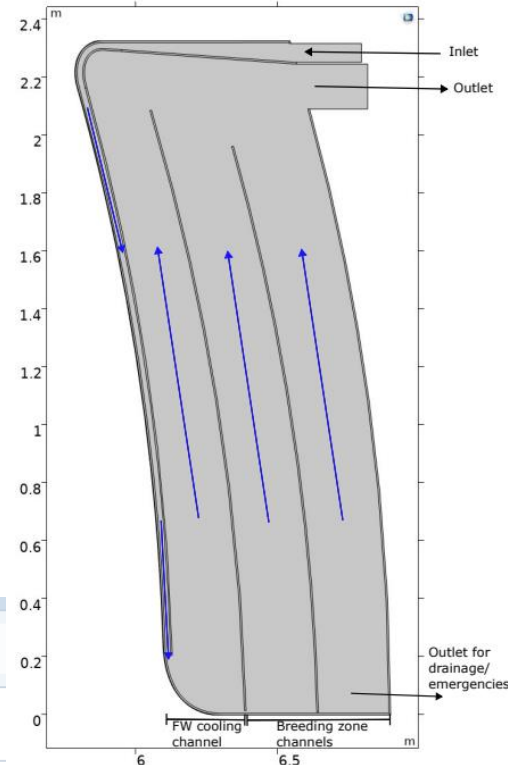
Best regards,

One attachment • Scanned by Gmail

KFA Workshop_files > user_files



Name	Date modified	Type
 P4COMSOLreplica	3/28/2025 1:49 PM	SldWorks 2021Application

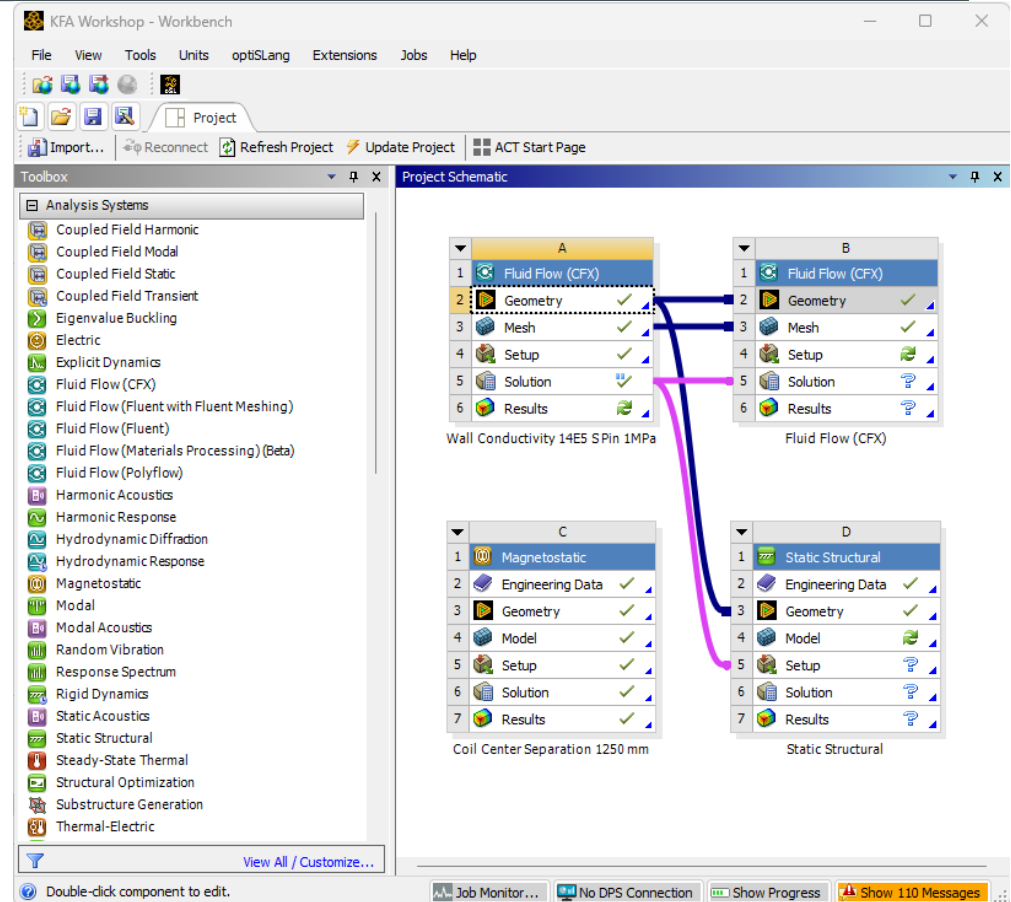


System Set-up



6

- Many problems can be coupled using drag and drop in Workbench
 - CFX geometry can be transferred directly to structural and another fluids problem
 - CFX mesh set-up can be transferred to another CFX problem
 - Temperature and pressure distribution can be transferred from CFX to static structural set-up
- Some couplings need to be done manually
- More info in ANSYS Workbench documentation

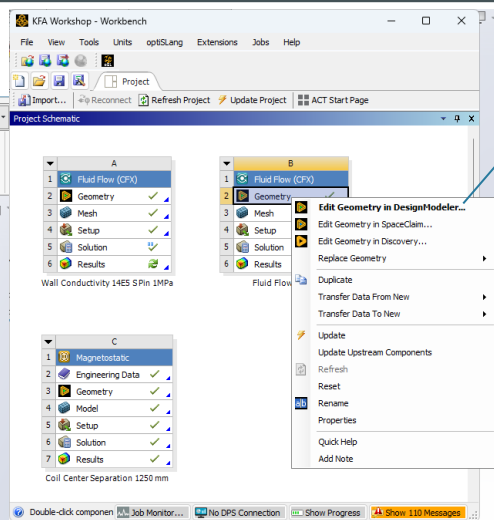
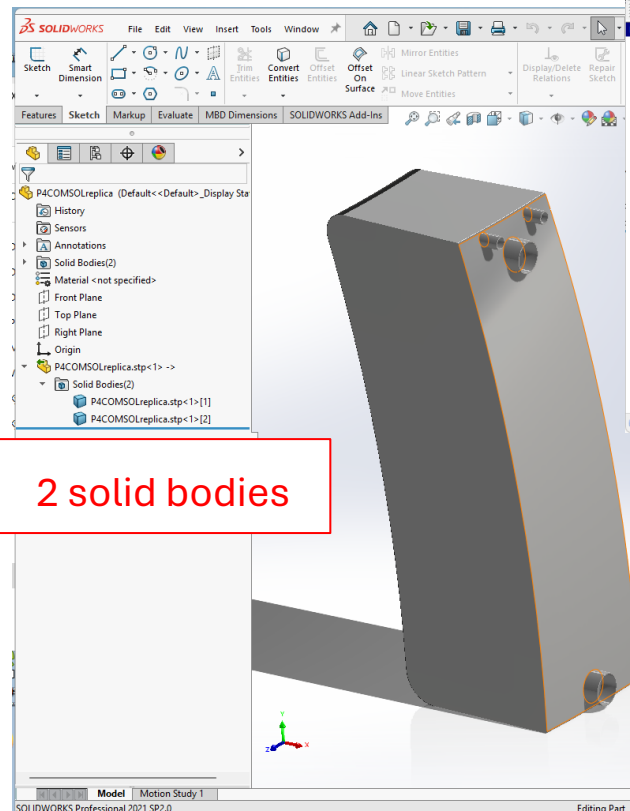


Geometry Input and Preparation

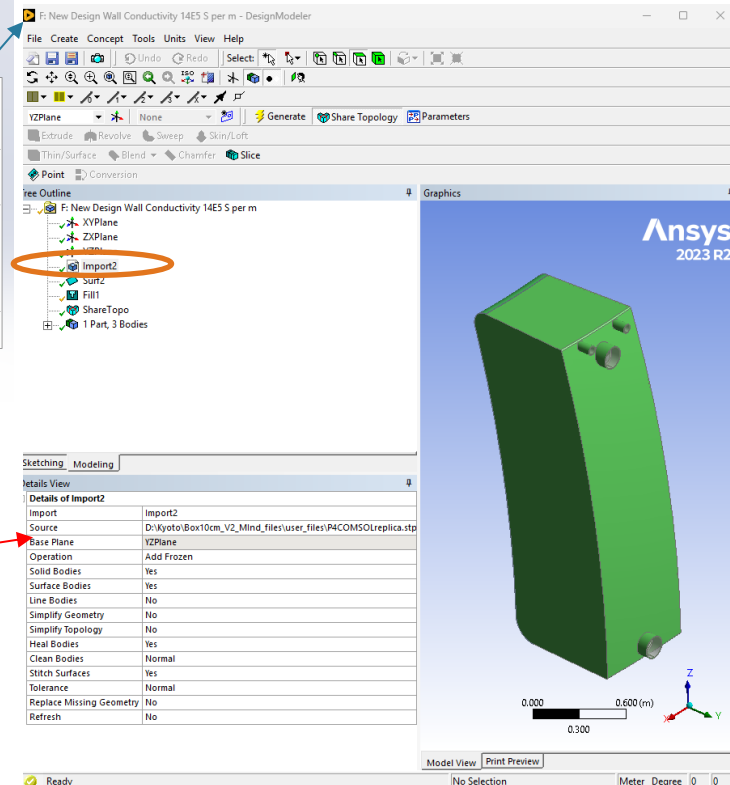


7

STEP file viewed in SolidWorks



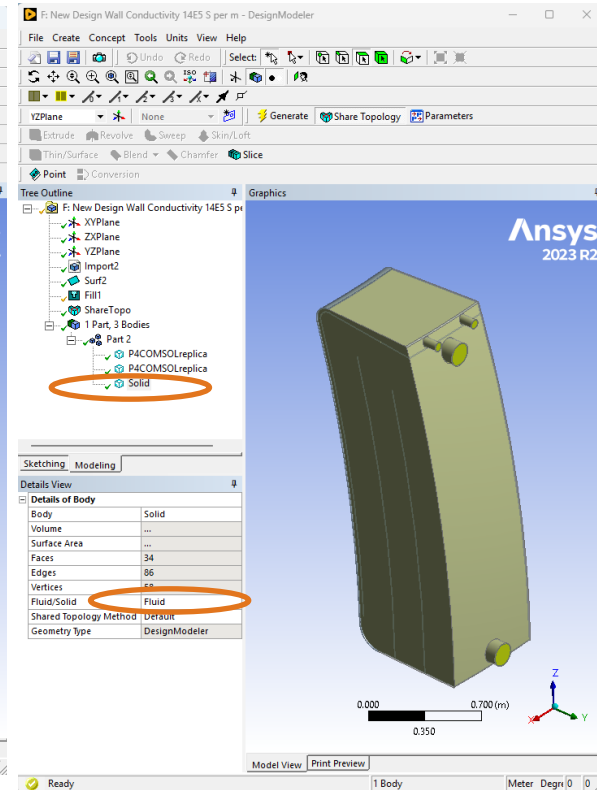
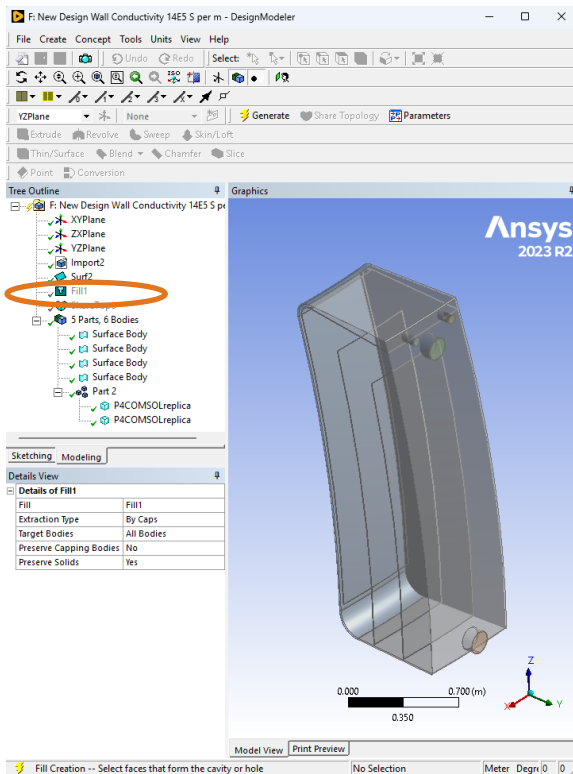
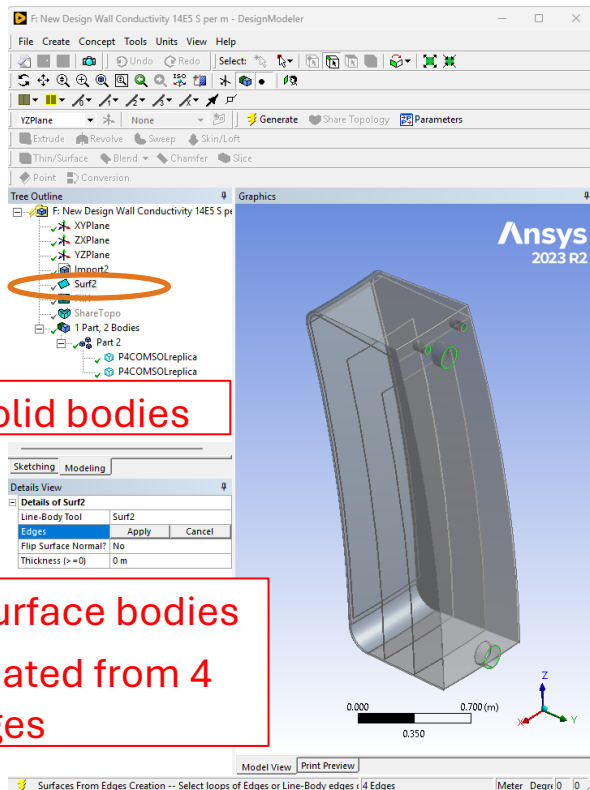
STEP file directly imported in Design Modeler



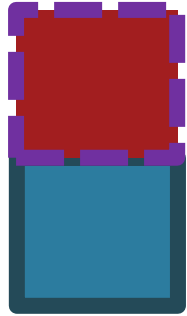
Lid surfaces created

Fluid volume is created by Fill operation

This operation also ensures that there are no leaks



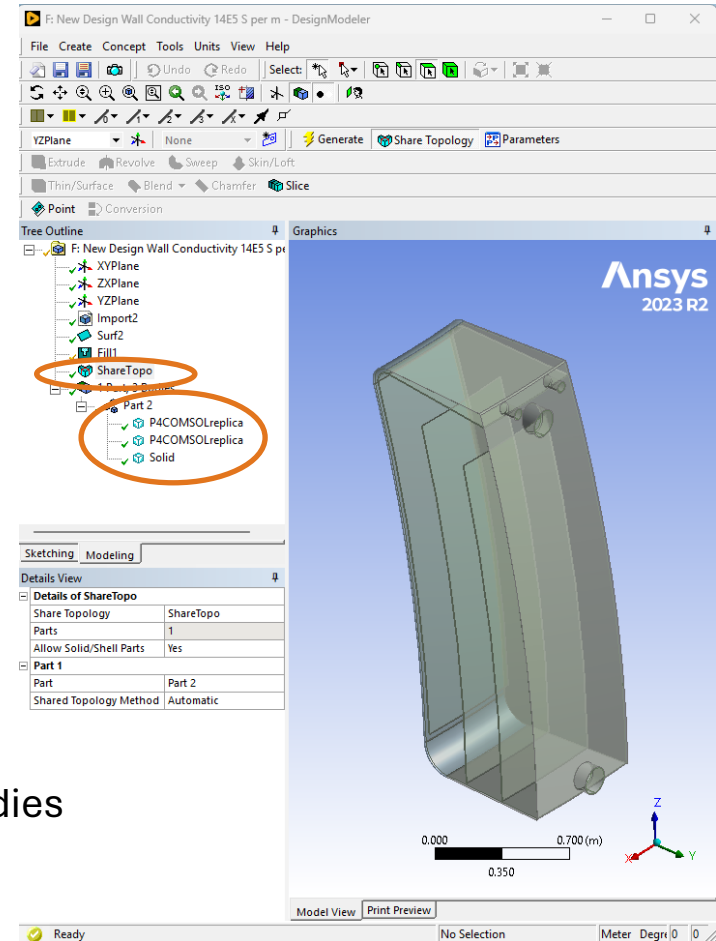
Share topology operation ensures that all bodies connected in one part will share the same surface



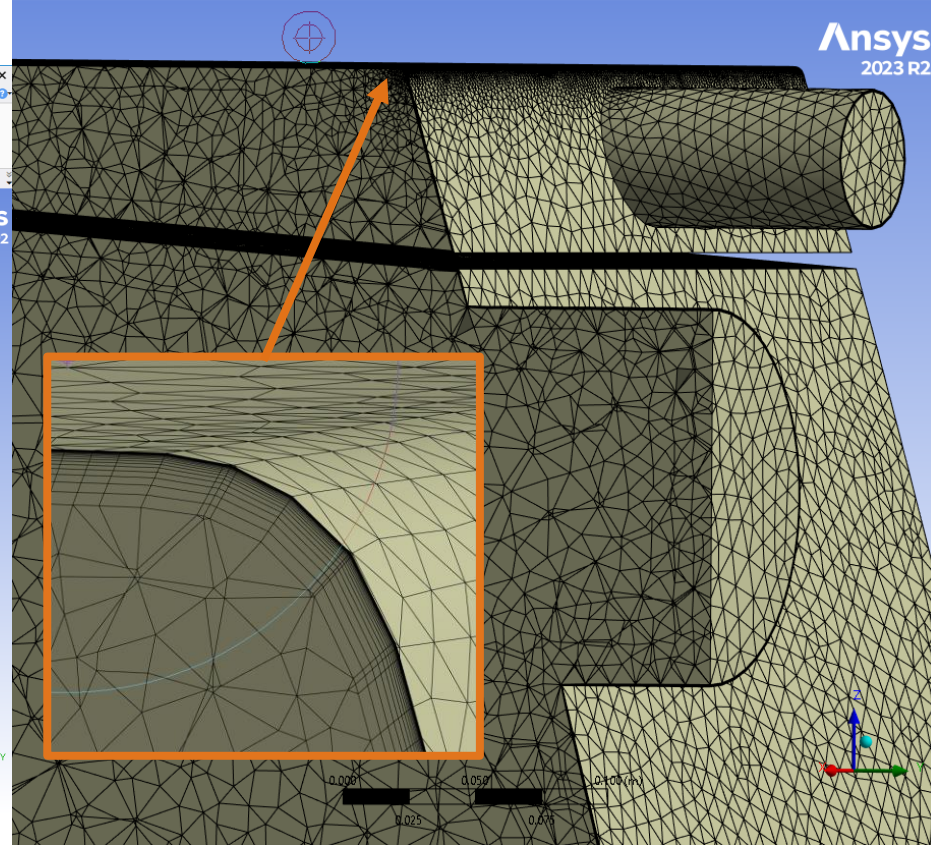
No share topology
Two coincident surface



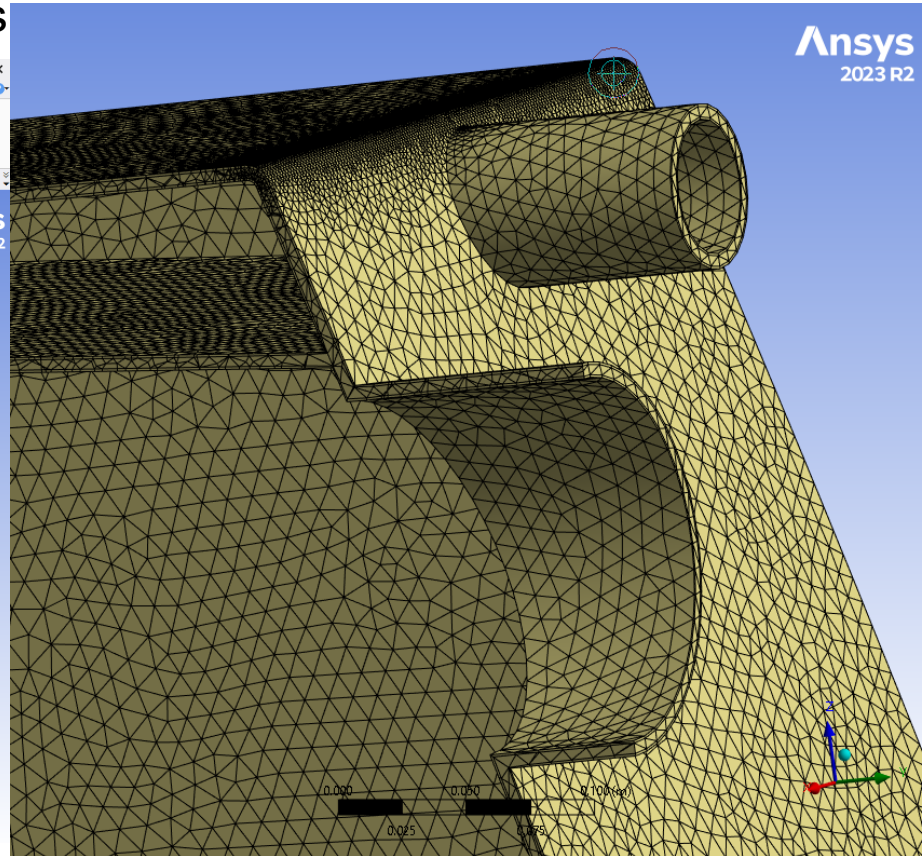
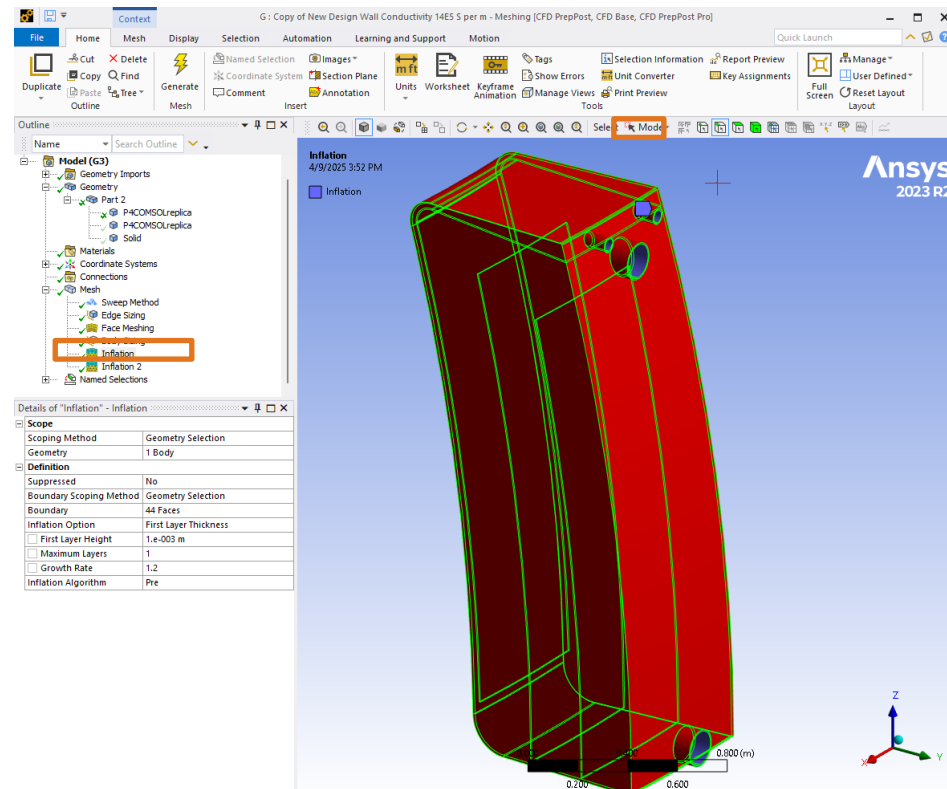
Share topology
One surface mutual for both bodies



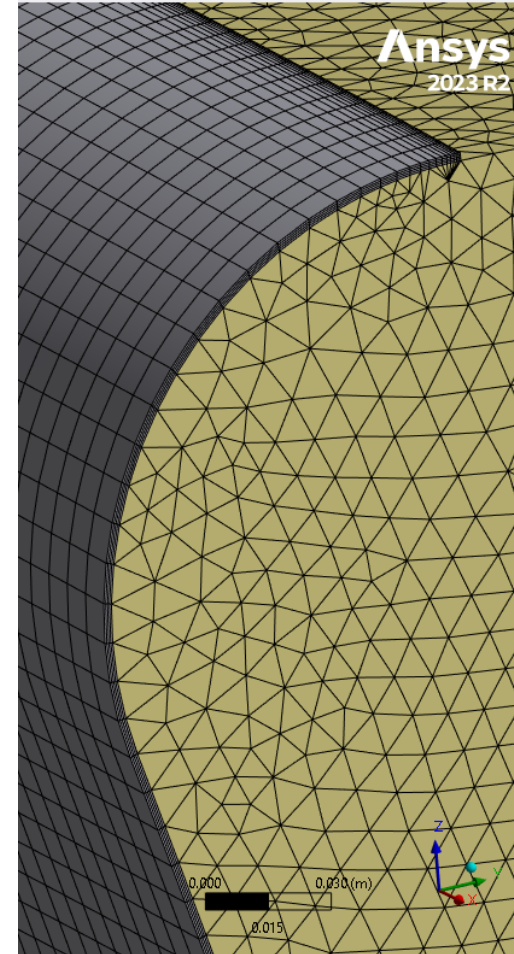
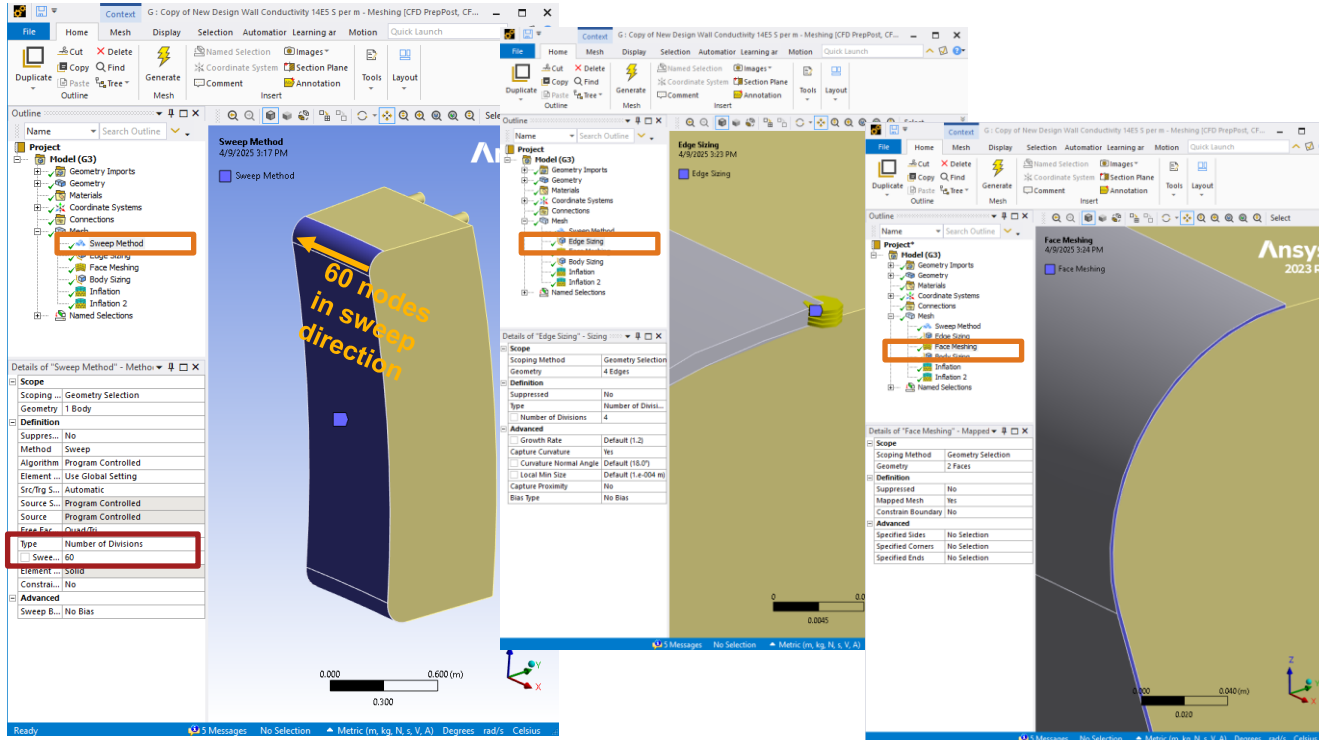
30 layers
Defined by first layer
and Growth Rate



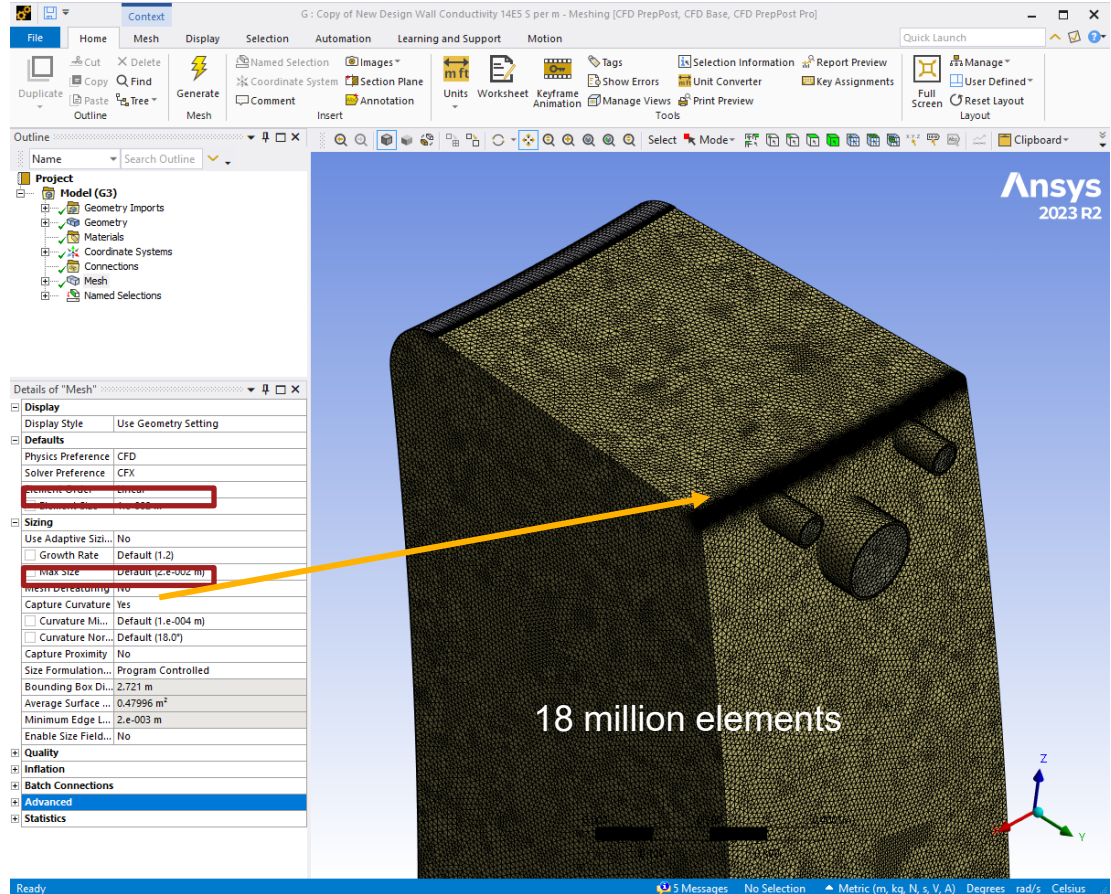
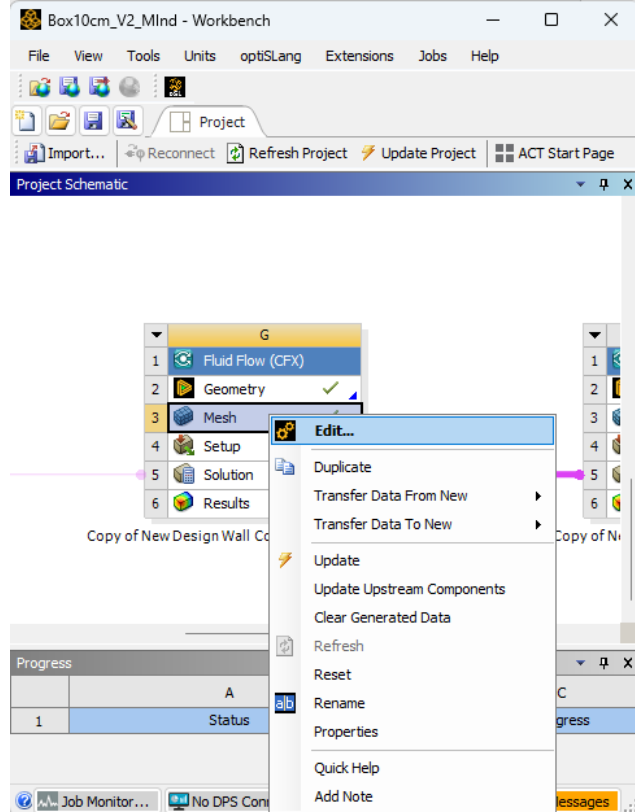
Inflation on solid bodies to make sure there are several elements through the thickness
Box mode can be used to select all surfaces



Sweep Meshing of Sweepable Geometry
 Not necessary can be abandoned to make meshing automatic
 Should be first meshing operation



Global Mesh Settings

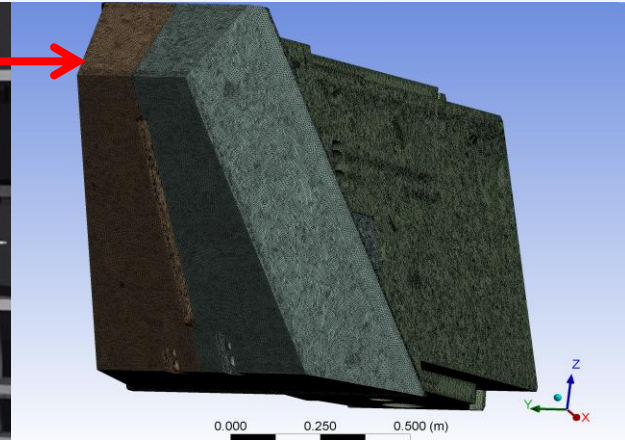
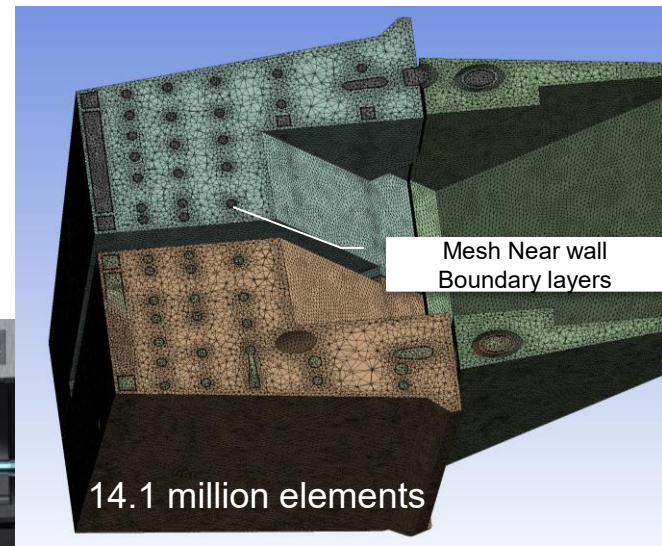
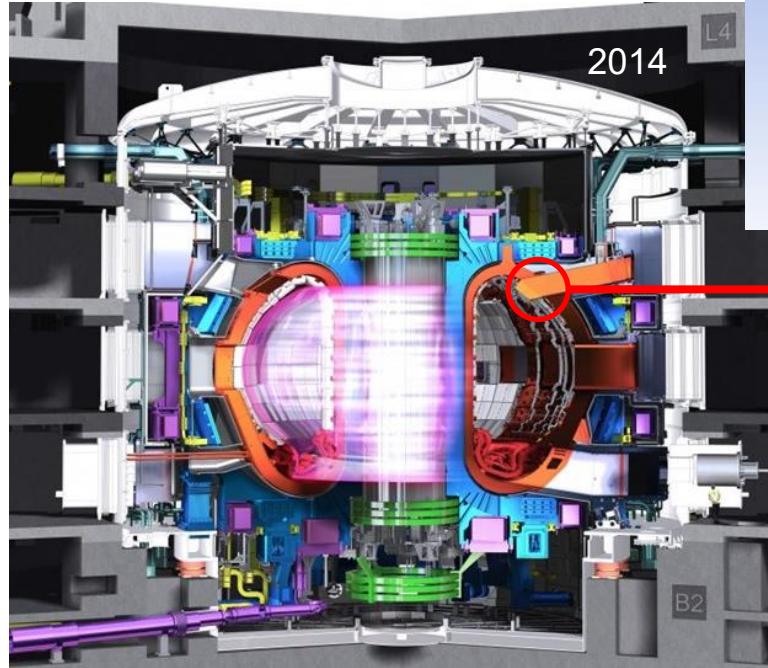


Outline

- Problem Set-up, Preparation and Meshing
- **CFD Modeling at PPPL**
- MHD
- Virtual Prototyping System
- Coupling
- Transient Flows
- Multiphysics Analysis

CFD analysis in PPPL

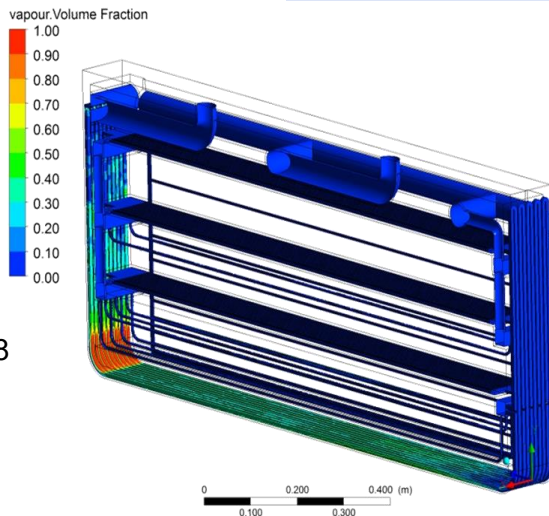
- The analysis of many fusion applications such as first wall blankets requires application of Computational Fluid Dynamics (CFD) methods.
- Highly customized version of ANSYS CFX is used at PPPL for thermal analysis of complex systems involving fluid flow and heat transfer in liquids and solids Virtual Prototyping of Liquid Metal Blanket Performance



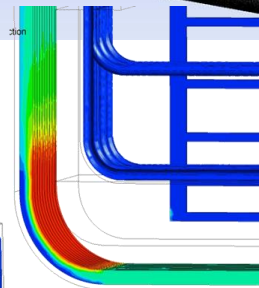
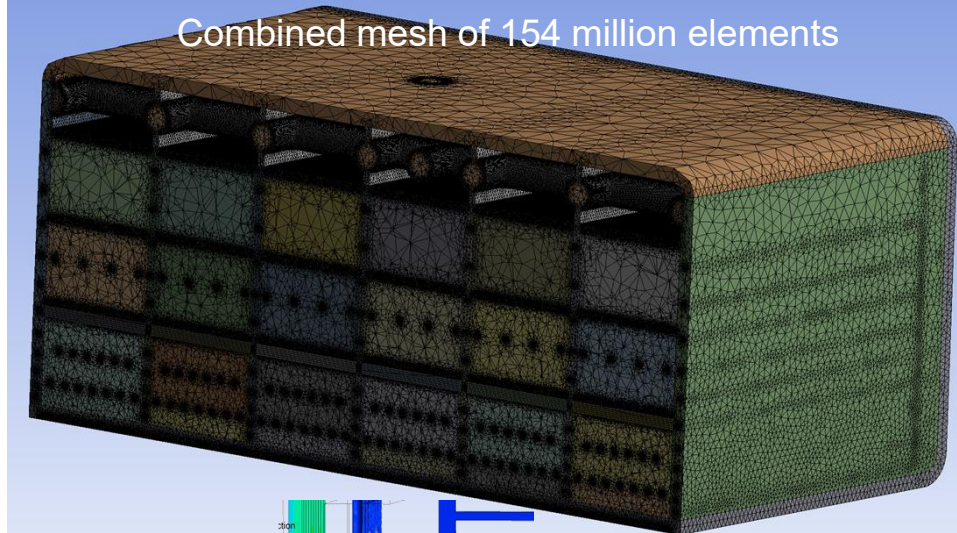
3D Two Phase Flow CFD

CFETR Pre-Superheated Blanket was performed using ANSYS CFX and included: 3D coolant flow analysis, external volumetric and surface heating effect, and two-phase wall boiling.

Khodak, et al. FST (2017).72(4), 628–633.
<https://doi.org/10.1080/15361055.2017.1350478>



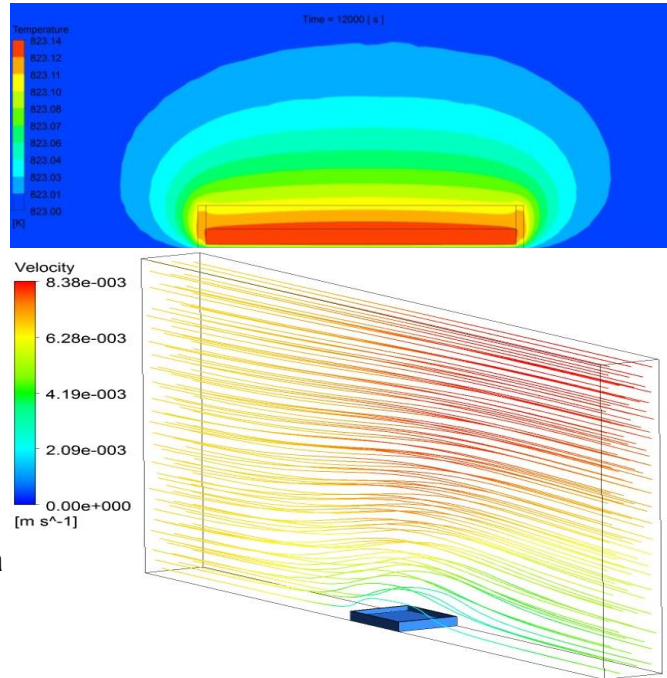
Combined mesh of 154 million elements



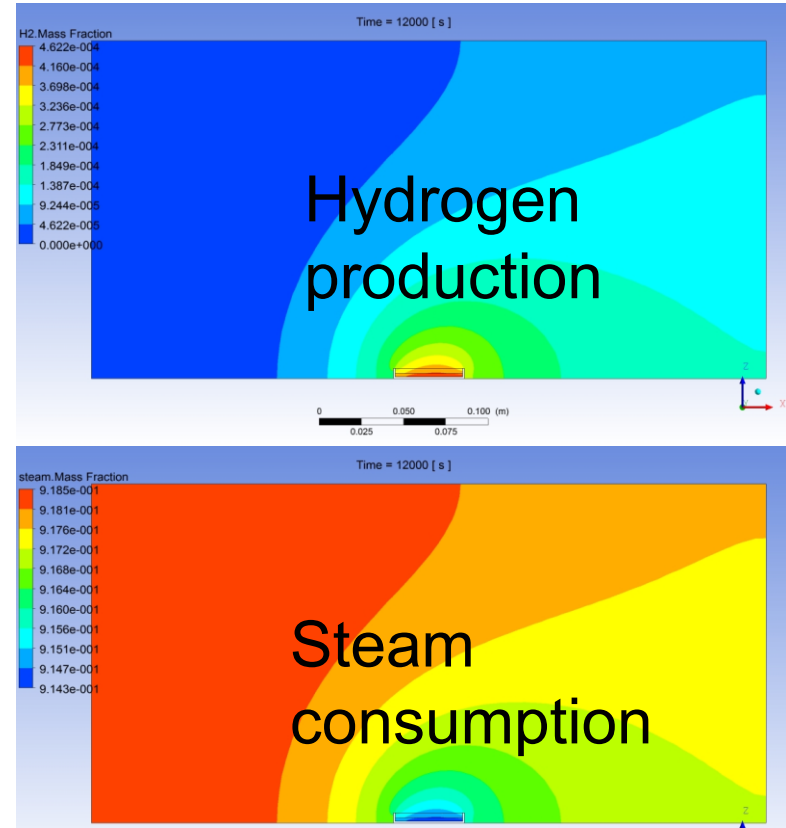
Blanket coolant
vapor volume
fraction distribution.

3D CFD with Chemical Reactions in Porous Media

Conjugated heat transfer approach is applied to calculate heat transfer in support structures as well as coolant flow, simultaneously with the porous medium steam flow in a blanket's granular beds.



A. Khodak, et al.
IEEE Trans. Plasma
Sci, 46 (2018) 2332



Outline

- Problem Set-up, Preparation and Meshing
- CFD Modeling at PPPL
- **MHD**
- Virtual Prototyping System
- Coupling
- Transient Flows
- Multiphysics Analysis

CFD

$$\frac{\partial \rho}{\partial t} + \vec{\nabla} \cdot (\rho \vec{V}) = 0$$

$$\frac{\partial \rho \vec{V}}{\partial t} + \vec{\nabla} \cdot (\rho \vec{V} \vec{V}) = -\vec{\nabla} p + \vec{\nabla} \cdot (\boldsymbol{\tau}) + \rho \vec{g} + \vec{j} \times \vec{B} \quad \leftarrow \text{Lorentz Force}$$

$$\frac{\partial \rho c_p T}{\partial t} + \vec{\nabla} \cdot (\rho \vec{V} c_p T) = \vec{\nabla} \cdot (\lambda \vec{\nabla} T) + \boldsymbol{\tau} : \vec{\nabla} \vec{V} + \dot{h} + \vec{j} \cdot \vec{E} \quad \leftarrow \text{Joule Heat}$$

MHD

Electric Potential Formulation +1 PDE

Magnetic Induction Formulation +3 PDE
with Gauss law enforced +4 PDE

Magnetic Vector Potential Formulation +4 PDE
with gauge enforced +5 PDE

$$\left\{ \begin{array}{l} \frac{\partial \vec{B}}{\partial t} = -\vec{\nabla} \times \vec{E} \\ (\vec{E} + \vec{V} \times \vec{B}) = \frac{\vec{j}}{\sigma} \\ \vec{\nabla} \times \vec{H} = \vec{j} + \frac{1}{c^2} \frac{\partial \vec{E}}{\partial t} \\ \vec{\nabla} \cdot \vec{B} = 0 \end{array} \right.$$

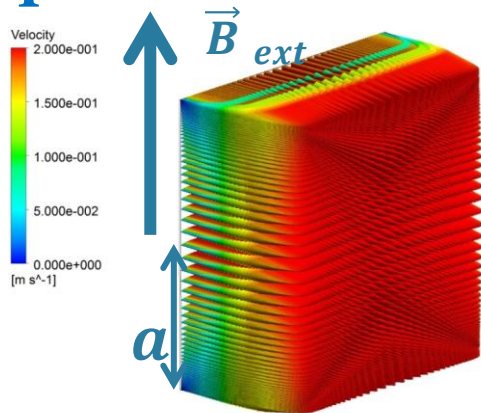
Maxwell-Faraday Equation

Ohm's Law

Ampere's Law

Gauss Law

Square Duct Flow Non-Conducting Wall



Fully developed flow of conducting Fluid subject to uniform transverse magnetic field
Smolentsev *et al.* (2014) case A1

Hartmann number

$$Ha = B_0 a \sqrt{\sigma / \rho \nu}$$

$$\rho = \text{const}$$

Flow rate

$$\tilde{Q} = \int_{-1}^1 d\tilde{y} \int_{-1}^1 \tilde{V} d\tilde{x} \quad \frac{\partial p}{\partial z} = \text{const}$$

$$\tilde{x} = \frac{x}{a} \quad \tilde{y} = \frac{y}{a} \quad \vec{V}_{\text{wall}} = 0$$

$$\vec{B}_{\text{wall}} = \vec{B}_{\text{ext}}$$

$$\tilde{V} = \frac{\rho \nu V}{a^2 \left(-\frac{\partial p}{\partial z} \right)} \quad \left(\frac{\partial \varphi}{\partial n} \right)_{\text{wall}} = 0$$

	Analytical Solution	Current Density in from Ampere's Law			Current Density from Ohm's Law		Size	Ratio
		Magnetic Induction Formulation	CFX Magnetic Vector Potential Formulation Modified	CFX Electric Potential Formulation Modified	CFX Magnetic Vector Potential Formulation	CFX Electric Potential Formulation		
Ha	Shercliff [7]	Equations (1,2,3,5,10)	Equations (1,2,3,15,18)	Equations (1,2,3,15,26)	Equations (1,2,3,15,18)	Equations (1,2,3,15)	N N⊥	R R⊥
500	7.679892E-03	0.0076799	0.0082639	0.0082697	0.0082172	0.0082166	100	100
		-0.00010%	-7.60437%	-7.67989%	-6.99629%	-6.98848%	100	100
			0.0076807	0.0076797	0.0076259	0.0076259	100	1000
			-0.01052%	0.00251%	0.70304%	0.70304%	100	1000
5000	7.902124E-04	0.00079031					100	100
		-0.01236%					100	100
			0.00078897	0.00078996	0.0007733	0.0007733	100	10000
			0.15722%	0.03194%	2.14023%	2.14023%	100	10000
50000	7.969391E-05	0.000079689	0.0000815				400	10000
		0.00616%	-2.26628%				400	10000
		0.00007969	0.000080431				800	10000
		0.00491%	-0.92490%				800	10000

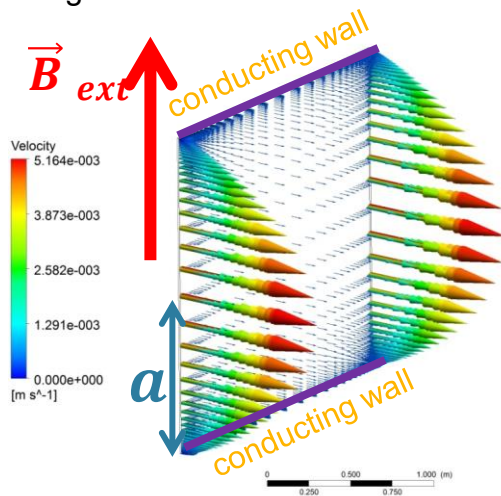
Analytical solution from Shercliff (1953) *Proc. Camb Phi. Soc.* 49, pp 136-144

Square Duct Flow with Conducting Walls

Two conducting walls perpendicular to the magnetic field direction.

Fully developed flow of conducting Fluid subject to uniform transverse magnetic field

Smolentsev *et al.* (2014) case A2



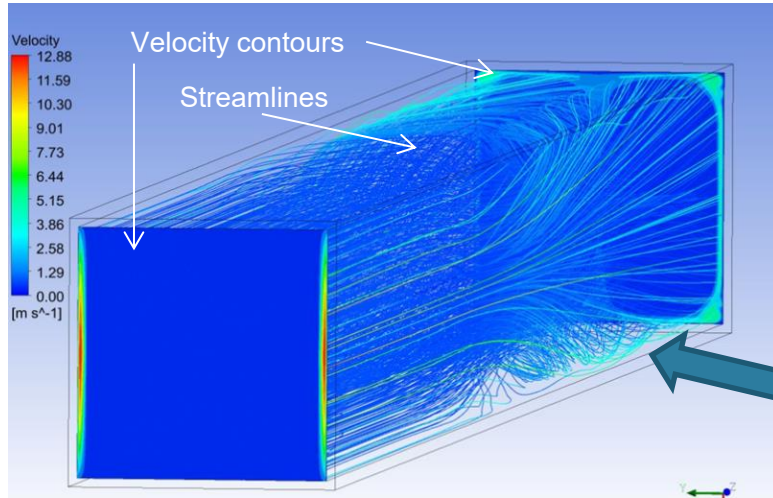
$$\begin{aligned} \vec{B}_{wall} &= \vec{B}_{ext} & \rho &= \text{const} \\ \vec{V}_{wall} &= 0 & \frac{\partial p}{\partial z} &= \text{const} \\ \left(\frac{\partial \phi}{\partial n}\right)_{wall} &= 0 & c_w &= 0.01 \end{aligned}$$

wall conductance

Ha	Analytical Solution	Current Density in from Ampere's Law			Current Density from Ohm's Law		Size	Ratio
		Magnetic Induction Formulation	CFX Magnetic Vector Potential Formulation Modified	CFX Electric Potential Formulation Modified	CFX Magnetic Vector Potential Formulation	CFX Electric Potential Formulation		
	Hunt [8]	Equations (1,2,3,5,10)	Equations (1,2,3,15,18)	Equations (1,2,3,15,26)	Equations (1,2,3,15,18)	Equations (1,2,3,15)	N N _⊥	R R _⊥
500	1.405351E-03	0.0014063	0.0082639	0.0082697	0.0082172	0.0082166	100	10000
		-0.06751%	-7.60437%	-7.67989%	-6.99629%	-6.98848%	100	10000
		0.0014063	0.0076807	0.0076797	0.0076259	0.0076259	200	10000
		-0.06751%	-0.01052%	0.00251%	0.70304%	0.70304%	200	10000
5000	1.907361E-05	0.00079031					100	100
		-0.01236%					100	100
			0.00078897	0.00078996	0.0007733	0.0007733	100	10000
			0.15722%	0.03194%	2.14023%	2.14023%	100	10000
50000	2.677874E-07	2.7223E-07	2.677E-07	2.6761E-07		2.2170E-07	400	10000
		-1.65899%	0.03265%	0.06626%		17.21046%	400	10000
		2.6942E-07	2.68346E-07	2.68363E-07		2.4338E-07	800	10000
		-0.60965%	-0.20858%	-0.21493%		9.11448%	800	10000

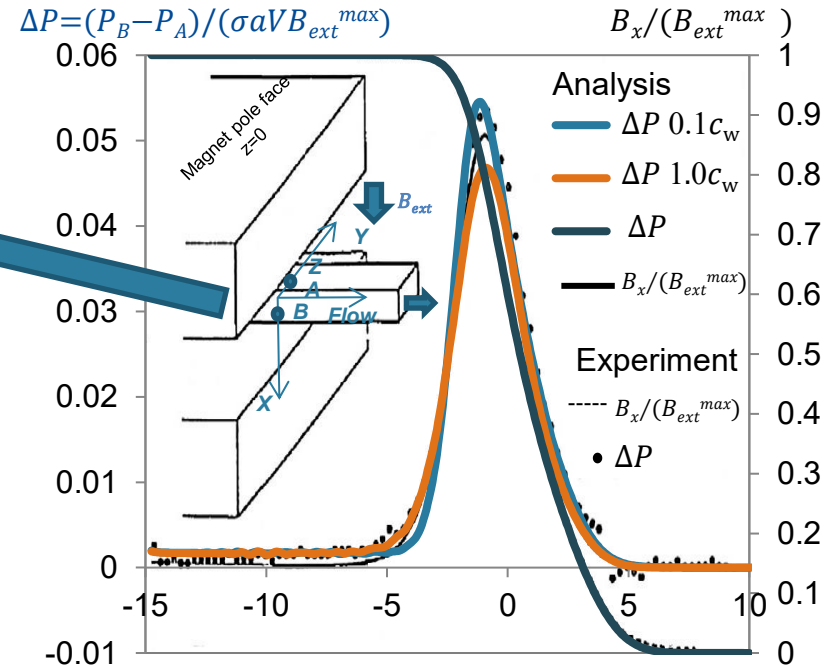
Analytical solution from Hunt (1965) *J. Fluid Mech.* 21, pp 577-590

3D MHD Analysis Channel with Fringe Field



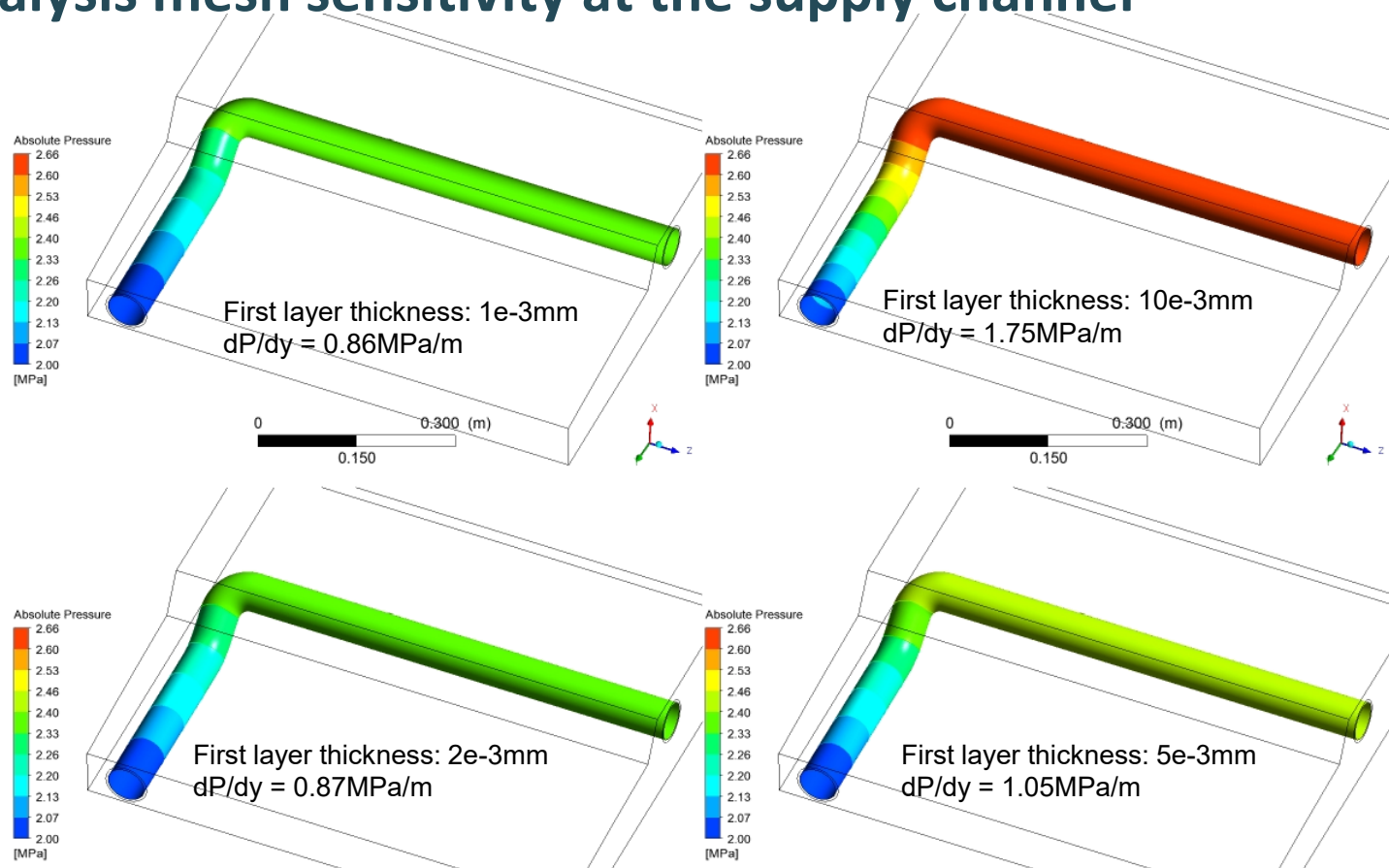
- ANSYS CFX adapted at PPPL for MHD problems using a magnetic induction approach¹
- Modified code tested against benchmarks relevant for fusion applications¹

3D Square Duct flow with Change in External Field
Cross-section pressure drop and magnetic field
distribution along the square duct
 $Ha=2900$, $N=Ha^2/Re=540$, $c_w=0.07$



DCLL blanket analysis mesh sensitivity at the supply channel

$B_z = 4 \text{ T}$
Diameter 60 mm
Wall Thickness 4mm
Flow 10 kg/s
Analytical Solution
 $dP/dy = 0.85 \text{ MPa/m}$

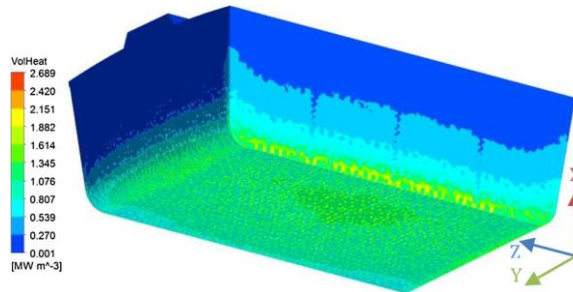


Virtual Prototyping of Liquid Metal Blanket Performance

24

- LM Blanket is a crucial element of the next step fusion device:
 - harvesting energy from fusion reaction
 - producing fuel for fusion reaction through tritium breeding
- PPPL possesses unique expertise in modeling of liquid metal blankets, including transient, electromagnetic, fluid, thermal and structural analysis, with three-dimensional nuclear loading
- Unique Features:

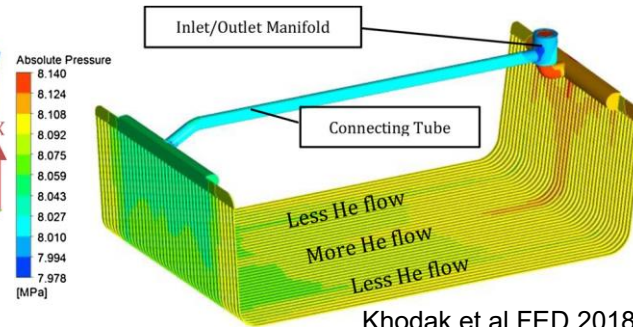
Neutronics code connection



Volumetric heat source imported from Attila.

Two Fluid CFD analysis

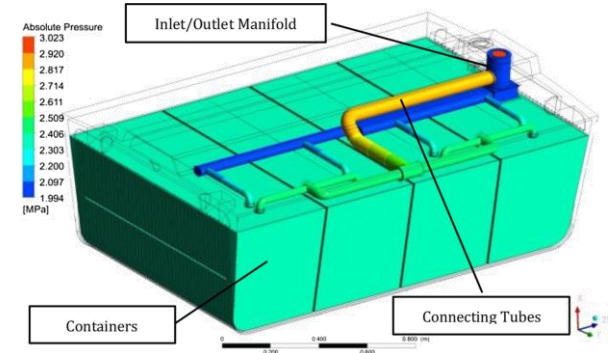
He coolant pressure distribution



Khodak et al FED 2018

Conjugate Heat Transfer

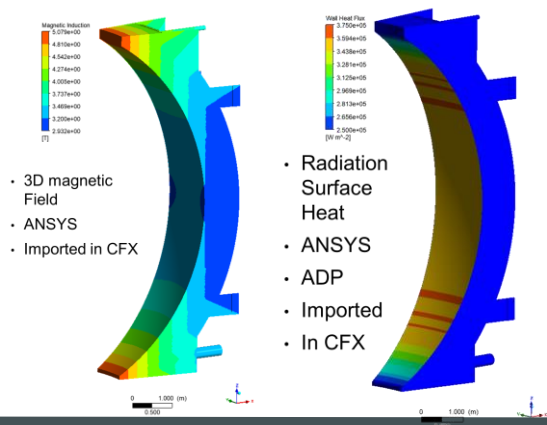
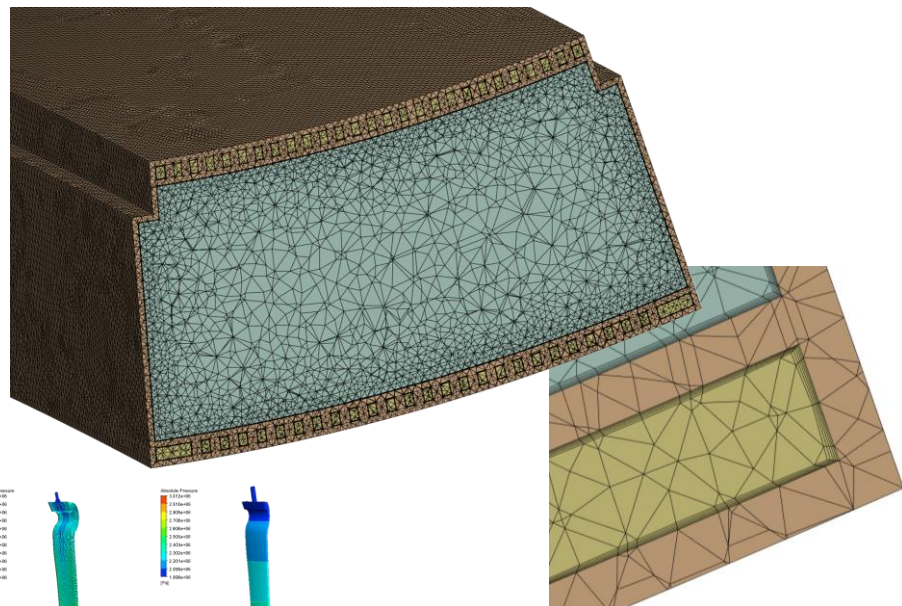
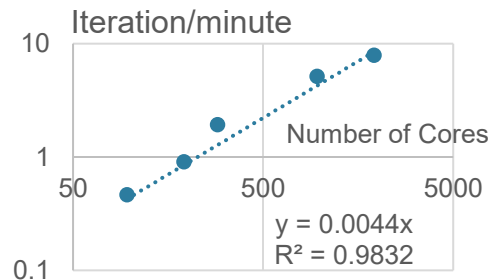
Pressure distribution in Li17PB



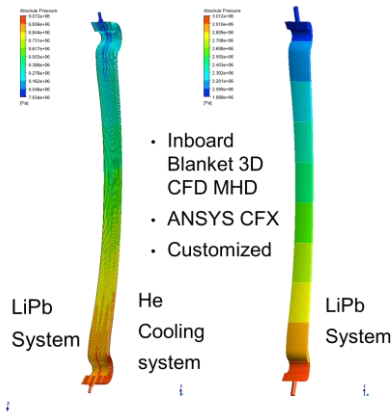
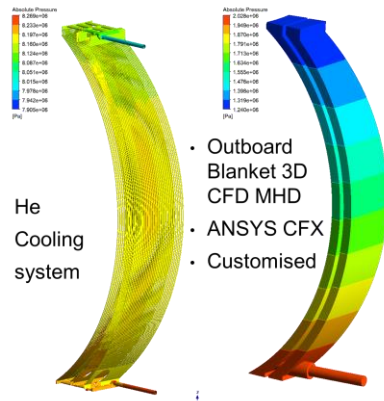
PPPL 3D MHD CFD analysis of STAR blanket using ANSYS CFX

- 3D CFD MHD Analysis
- Coupling with M3D-C1
- Automatic mesh Generation
- Massive parallel processing analysis on NERSC

- Parallelization study was performed using PPPL Stellar cluster
- The queue time increases for higher number of cores requested
- Study continues with higher number of cores, using exponential licensing structure of ANSYS



- Radiation Surface Heat
- ANSYS
- ADP
- Imported
- In CFX



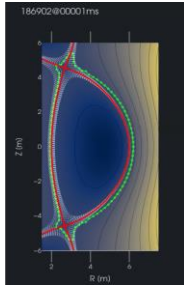
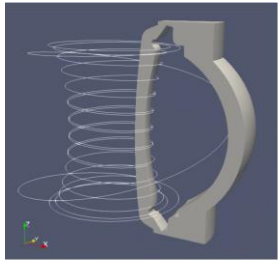
- Inboard Blanket 3D CFD MHD
- ANSYS CFX
- Customized

- Turbulent He flow analysis
- MHD Li Pb flow analysis
- Conjugate Heat Transfer

Outline

- Problem Set-up, Preparation and Meshing
- CFD Modeling at PPPL
- MHD
- **Virtual Prototyping System**
- Coupling
- Transient Flows
- Multiphysics Analysis

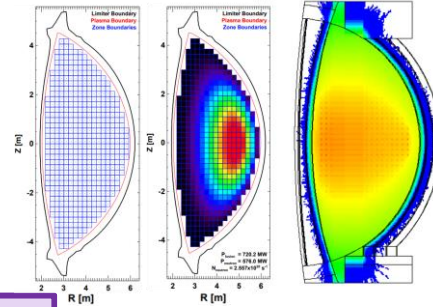
Virtual Prototyping System



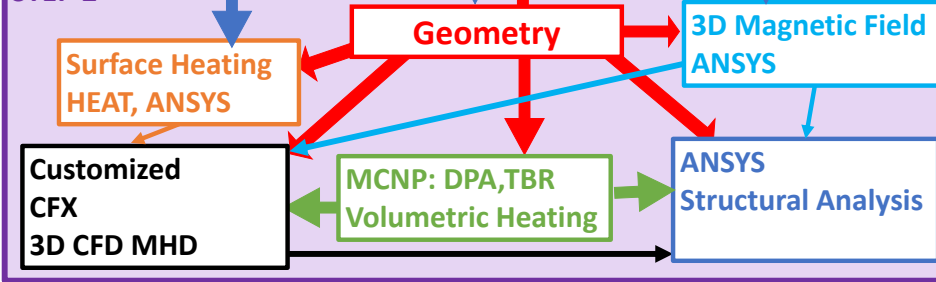
Magnetic field line trace from the blanket surface starting at midplane with the equilibrium used in HEAT

STEP 1

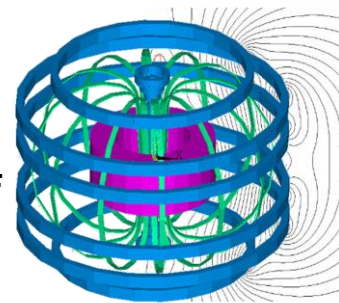
0D System Code PROCESS
2D Equilibrium Optimization ISOVER
2D Axisymmetric Set-up in MCNP
2D Axisymmetric Set-up for HEAT



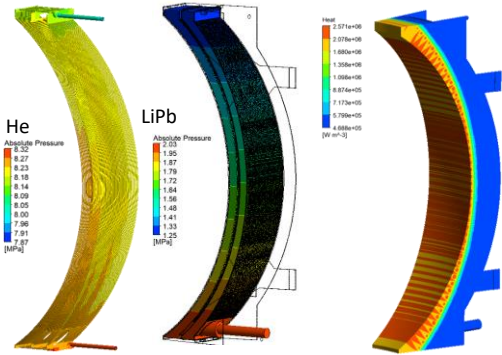
STEP 2



Neutron Source from ISOLVER Interpolated into MCNP



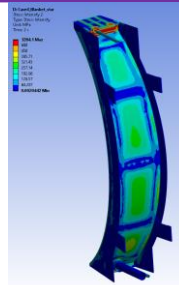
Axisymmetric magnetic field obtained using ISOLVER and PF and TF coils geometry used for 3D interpretation in ANSYS



Absolute pressure in He coolant (left) and Li-Pb (right) fluid zones of the Out-Board blanket

Volumetric heating from MCNP imported in CFX

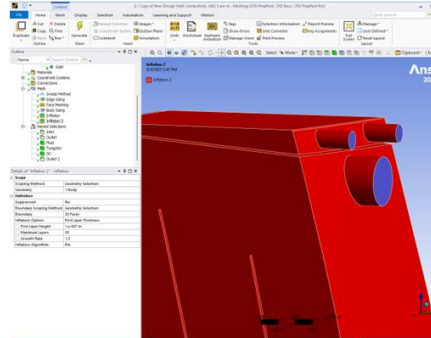
Stress Result under Pressure Load



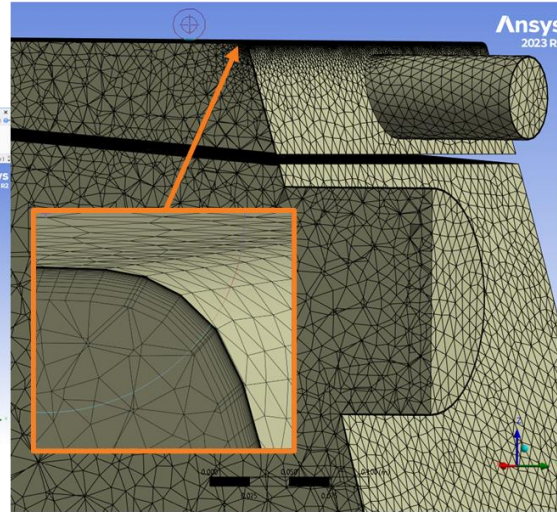
Automatic Meshing Procedure

Inflation on fluid domain is required for proper resolution of boundary layers

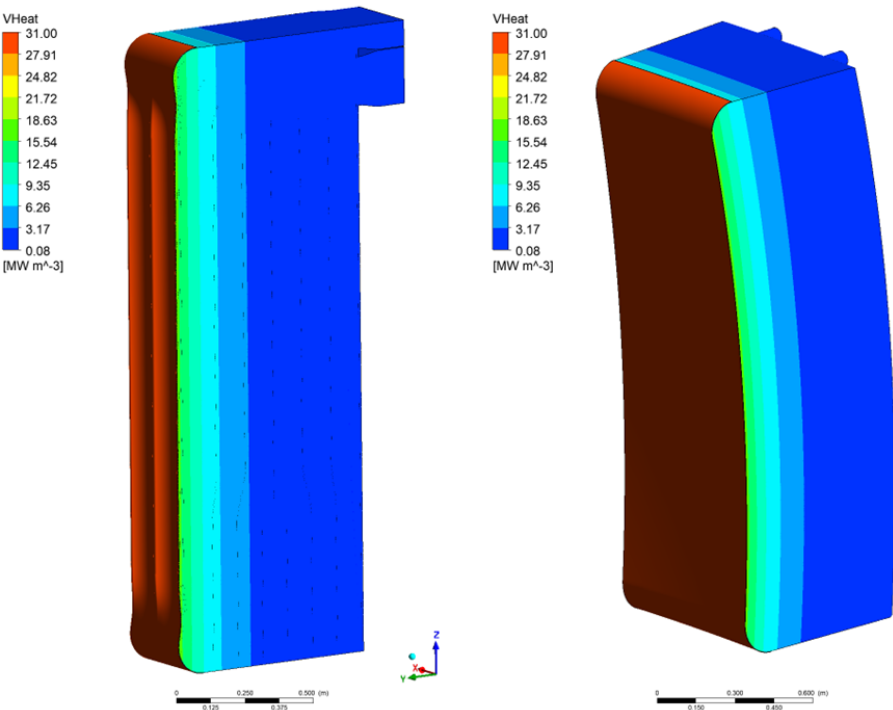
Box mode can be used to select all surfaces



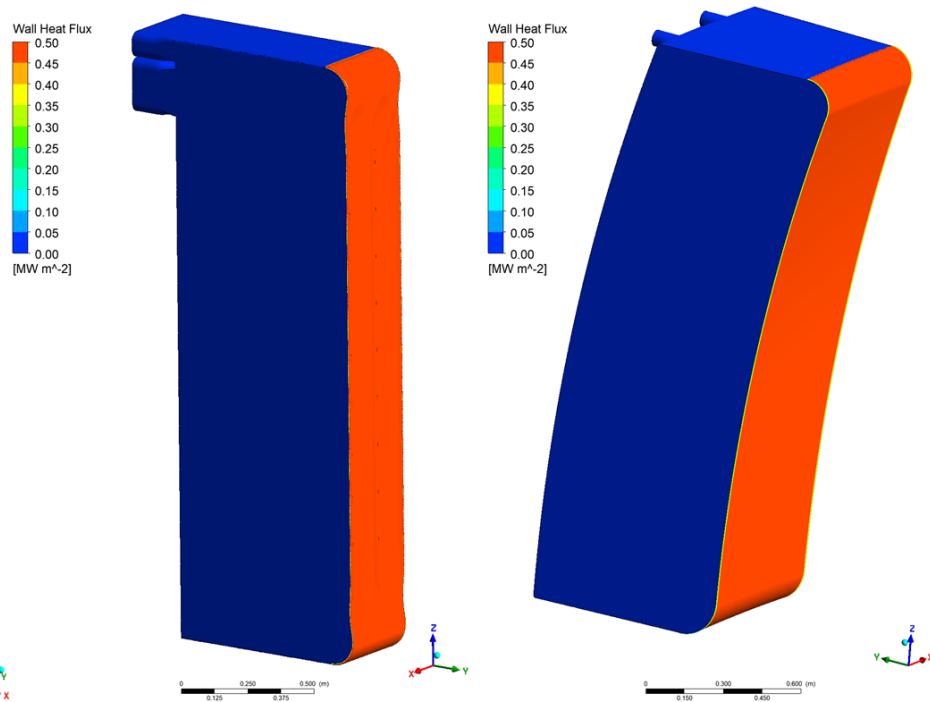
30 layers
Defined by first layer
and Growth Rate



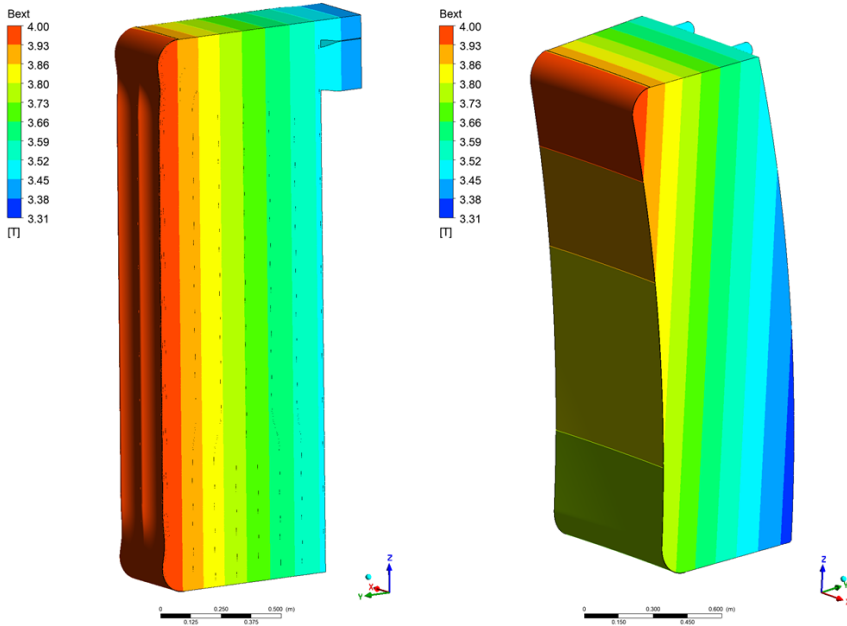
Volumetric Heating



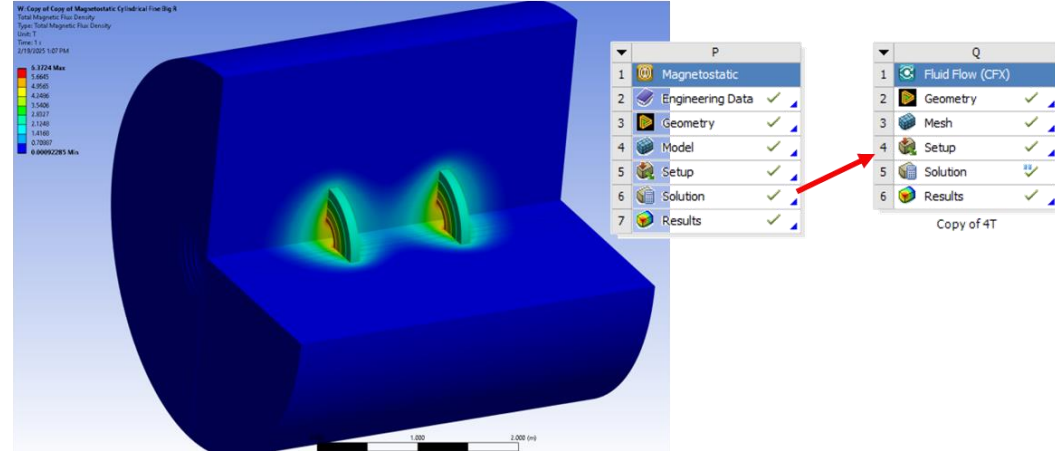
Surface Heating



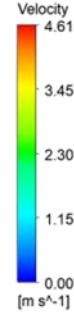
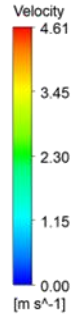
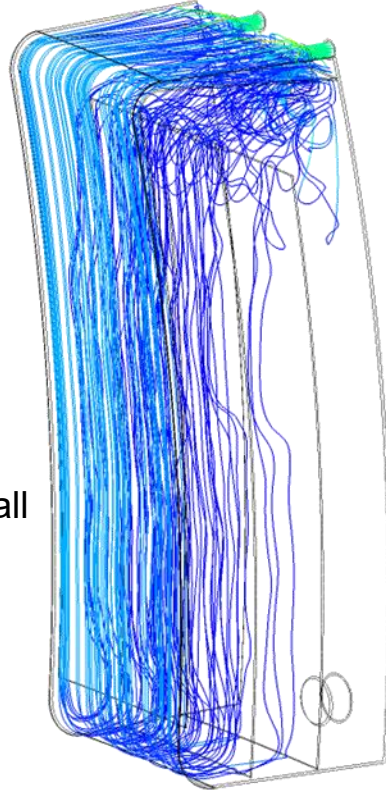
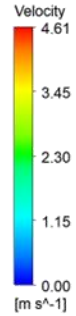
Magnetic Field



3D external magnetic field
Coupling with Magnetostatic analysis
Coil Center Separation 1250 mm



Velocity Streamlines



Electric
Potential
Model
SiCf/SiC wall
Laminar

Magnetic
Induction
Model
SiCf/SiC wall
Laminar

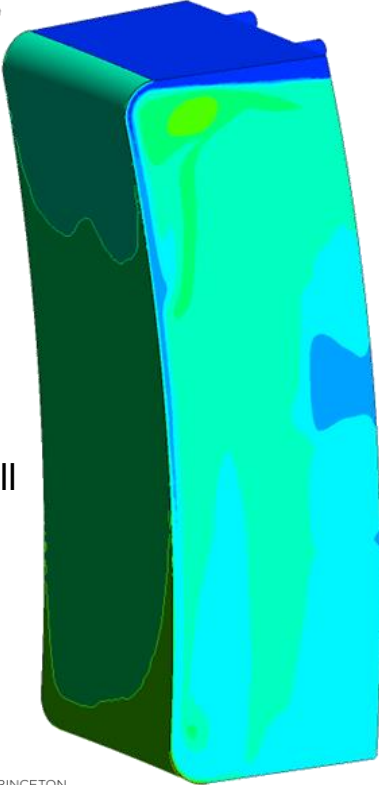
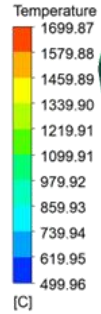
No MHD
Turbulent
Buoyancy

Max V_{LiPb}
4.57 m/s

Max V_{LiPb}
4.61 m/s

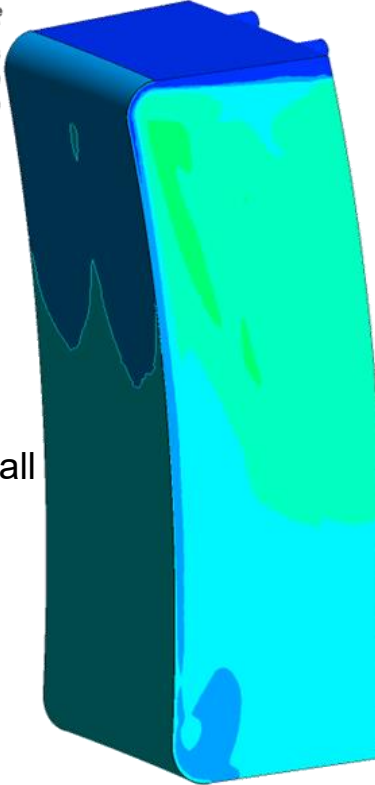
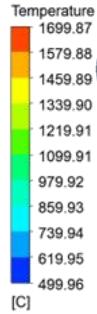
Max V_{LiPb}
2.15 m/s

Temperature Distribution



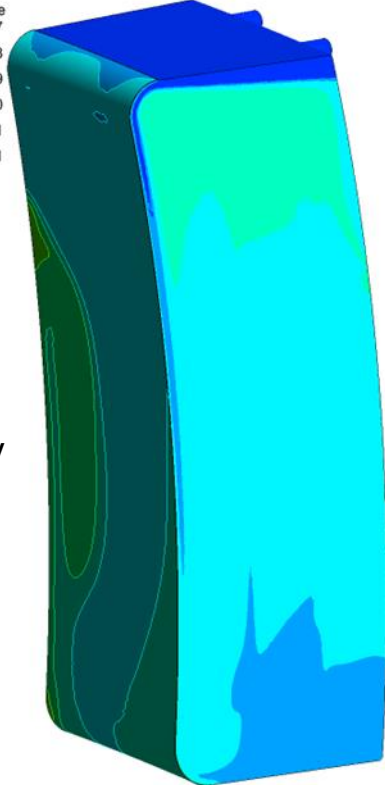
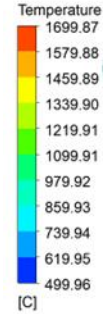
Electric
Potential
Model
SiCf/SiC wall
Laminar

Max T
1270.42 C



Magnetic
Induction
Model
SiCf/SiC wall
Laminar

Max T
1046.78 C



No MHD
Turbulent
Buoyancy

Max T
1156.2 C

Outline

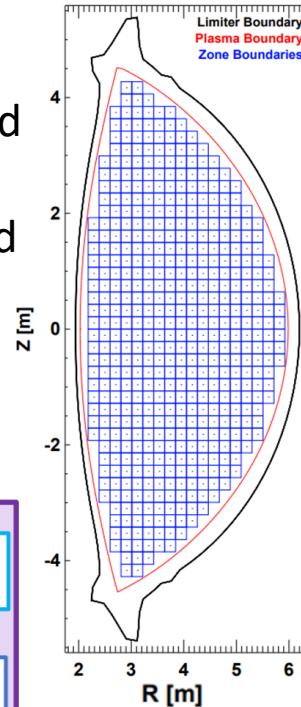
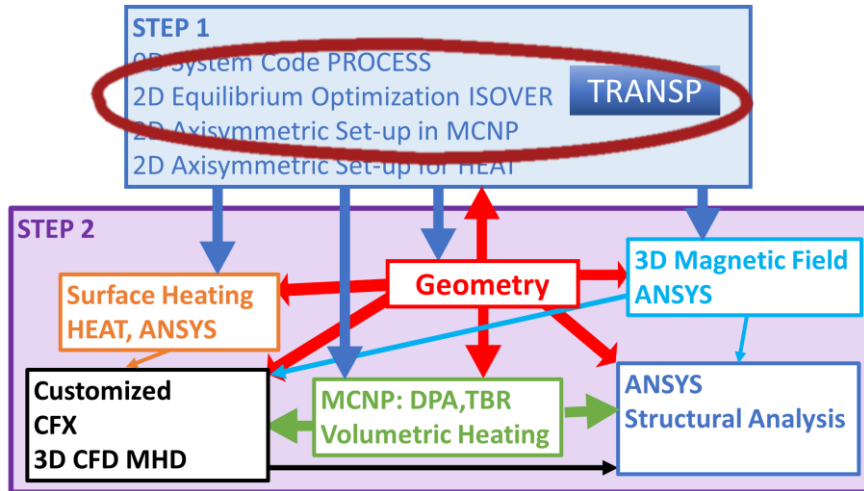
- Problem Set-up, Preparation and Meshing
- CFD Modeling at PPPL
- MHD
- Virtual Prototyping System
- **Coupling**
- Transient Flows
- Multiphysics Analysis

Neutron Source Interpolation for Neutronics Code MCNP

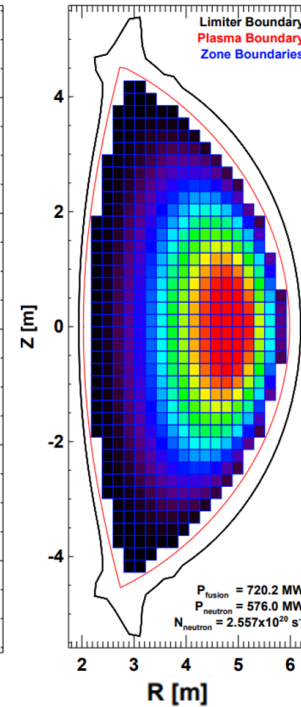


34

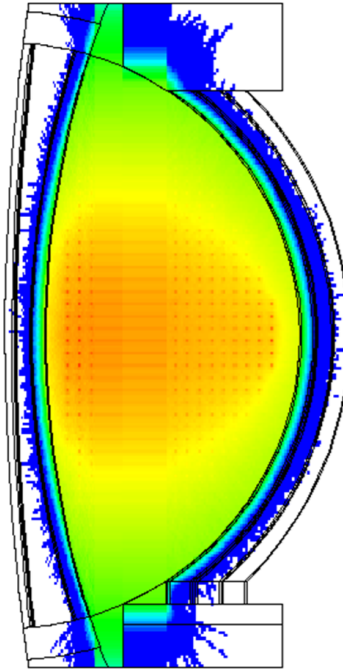
- Automatic spatial NS distribution transfer from ISOLVER to MCNP
- Connection to TRANSP can be achieved in a similar manner
- IMAS interface connection can be used



R,Z grid and plasma zone boundaries defined in iSOLVER



Neutron power density profile mapped onto the R,Z grid for import into MCNP

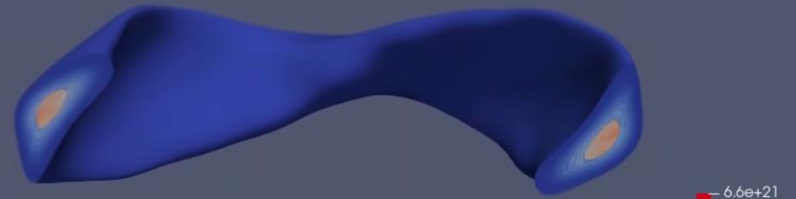


Relative intensity of neutrons born in MCNP model visualized by plotting neutron flux ($E > 13.99 \text{ MeV}$)

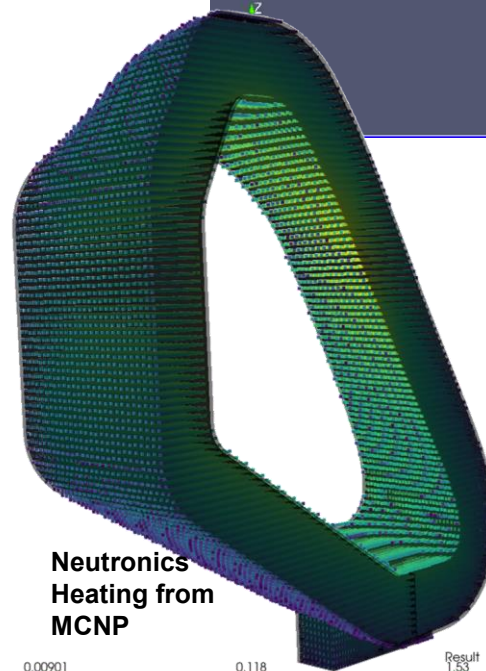
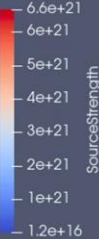
Stellarator Blanket Analysis

3D Neutronics Heating Import

- Nuclear Analysis is completed using MCNP6.2
- Python scripts used to convert MCNP output to importable mesh tallies
- MCNP Cylindrical Mesh tally was used to acquire the nuclear heating
- Multiplication factor for heating was calculated per unit volume for a 2800MW plasma



3D Stellarator neutronics source
Obtained using parastell



Neutronics
Heating from
MCNP

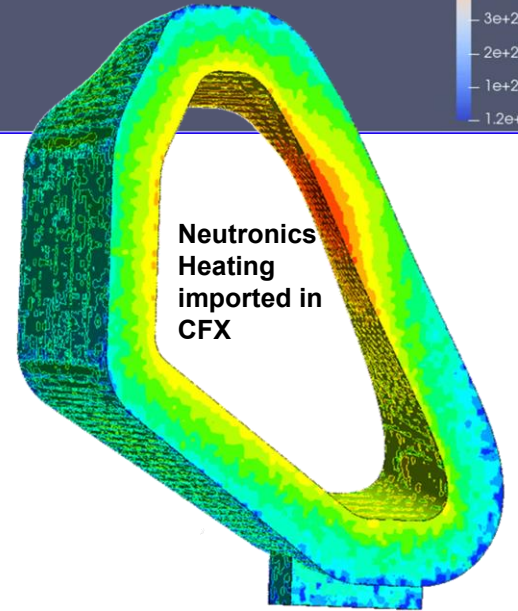
0.00901

0.118

Result
1.53

20.0

261.



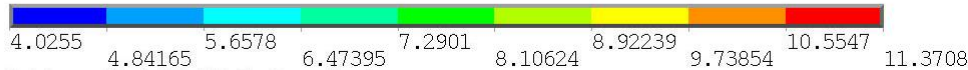
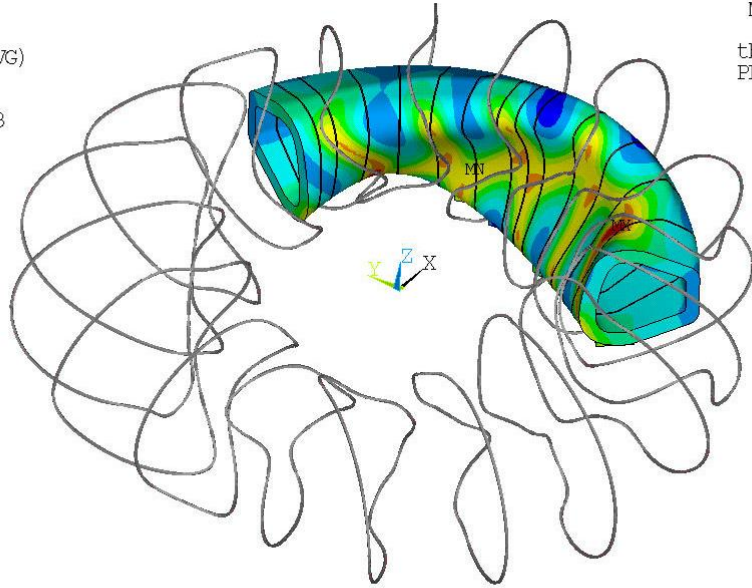
Neutronics
Heating
imported in
CFX

Stellarator Blanket Analysis

3D Magnetic Field

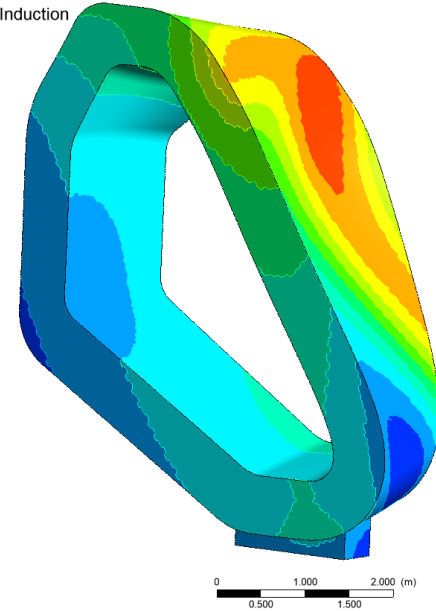
STEP=1
SUB =1
TIME=1
BSUM (AVG)
RSYS=0
SMN =4.0255
SMX =11.3708

MAR 6 2024
14:50:52
tbs7-coolant
PLOT NO. 1



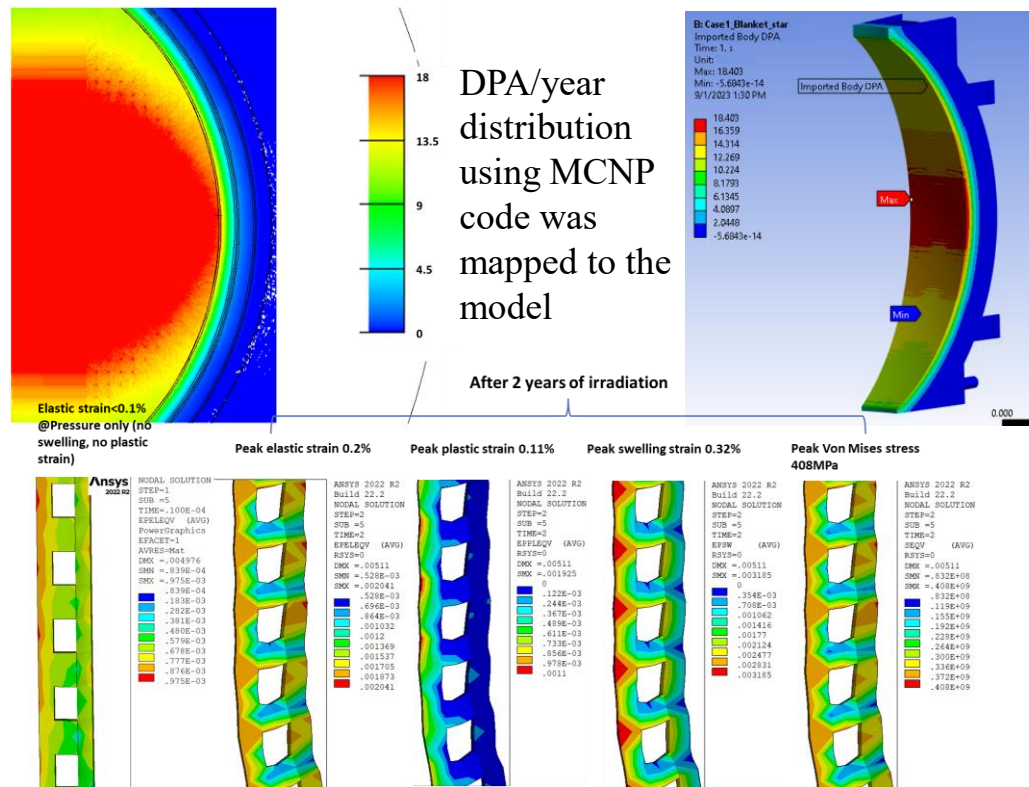
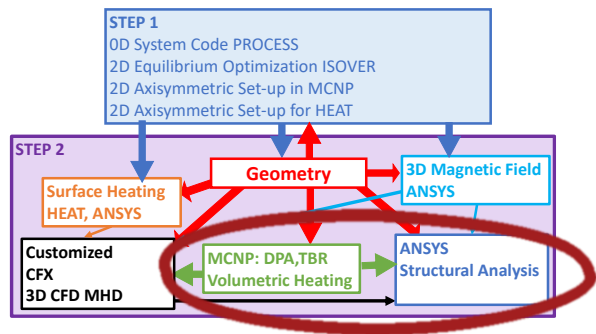
Magnetic Induction
[T]

11.6
10.6
9.7
8.8
8.0
7.3
6.7
6.1
5.6
5.1
4.7



Magnetic Field

Structural Analysis 3D Neutronic Swelling Model



- Neutronics Swelling and Hardening are introduced in ANSYS ADPL using User Defined Functions for Properties
- DPA values are imported from MCNP

H.Zhang et al. IEEE TPS 2024

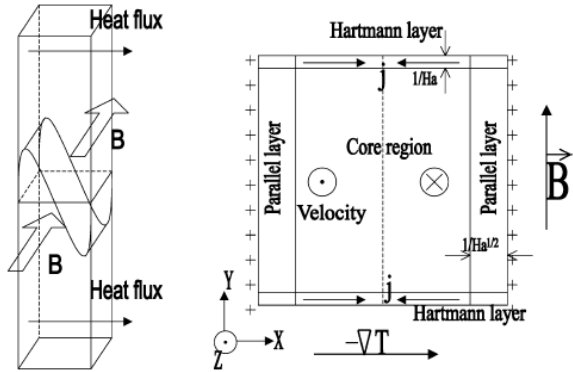
Outline

- Problem Set-up, Preparation and Meshing
- CFD Modeling at PPPL
- MHD
- Virtual Prototyping System
- Coupling
- **Transient Flows**
- Multiphysics Analysis

Natural Convection

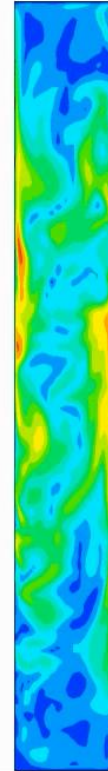


39



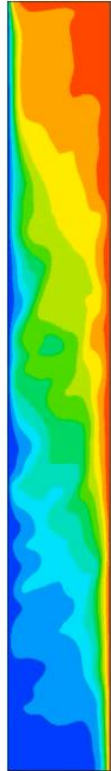
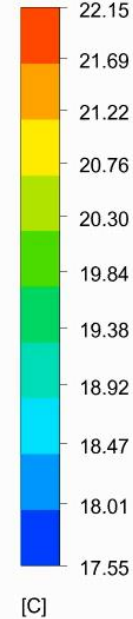
Time = 200 [s]

Velocity

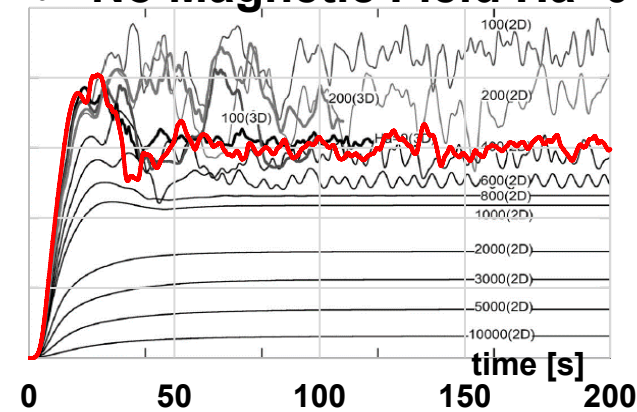


Time = 200 [s]

Temperature



No Magnetic Field $Ha=0$

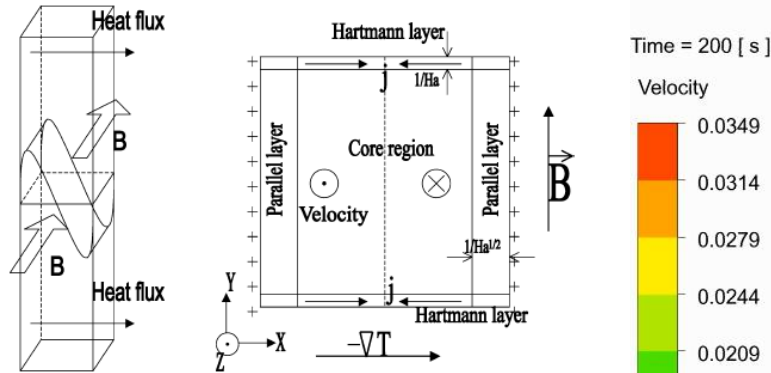


Experimental and Numerical Data Authie et al 2003

Natural Convection with MHD

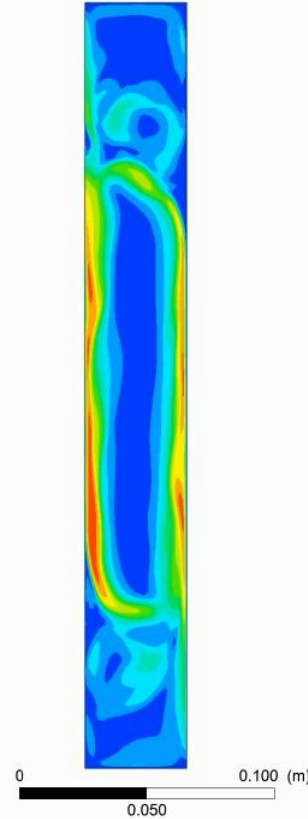
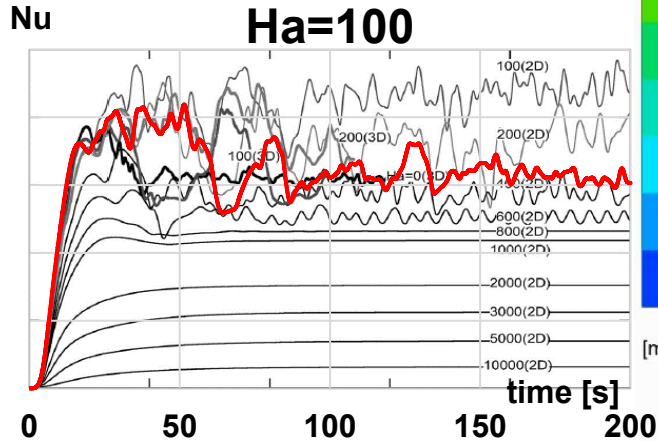
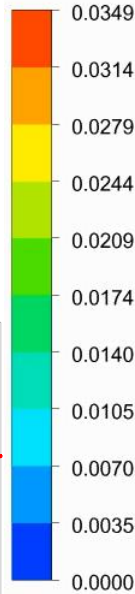


40



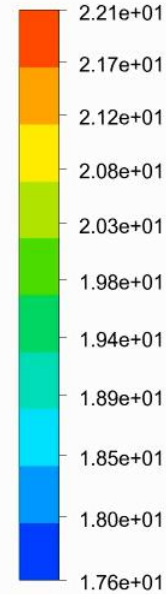
Time = 200 [s]

Velocity

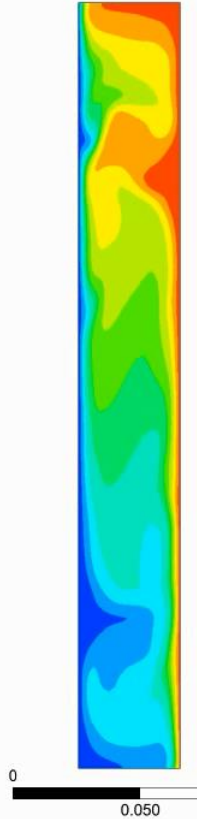


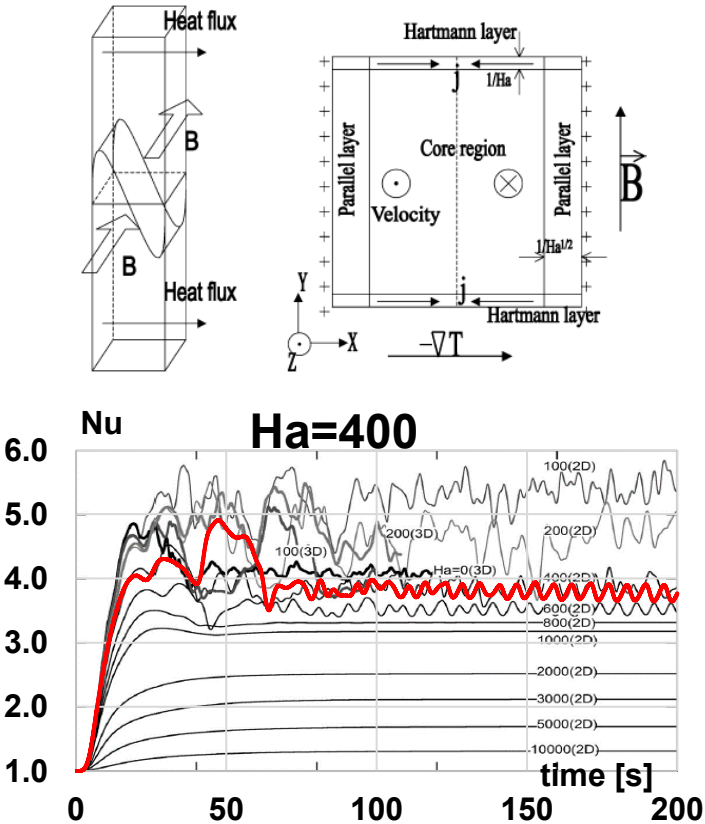
Time = 200 [s]

Temperature



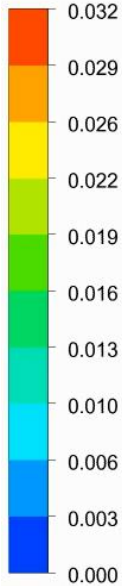
[C]



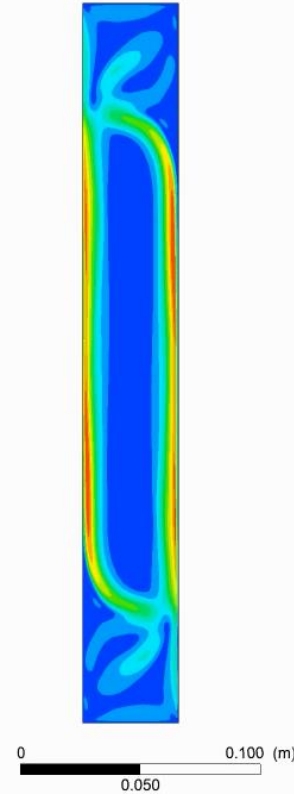


Time = 200 [s]

Velocity

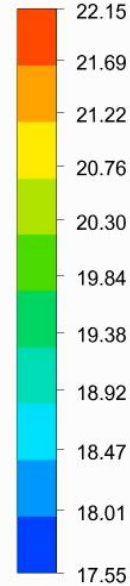


[m s⁻¹]

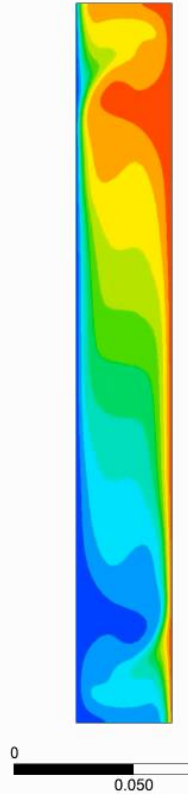


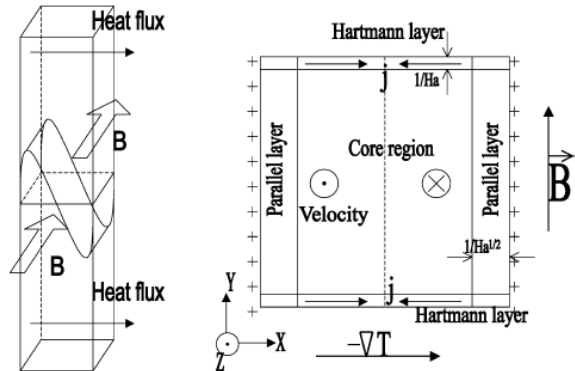
Time = 200 [s]

Temperature



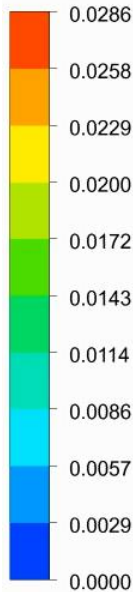
[C]





Time = 200 [s]

Velocity

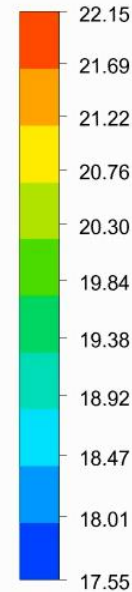


[m s⁻¹]

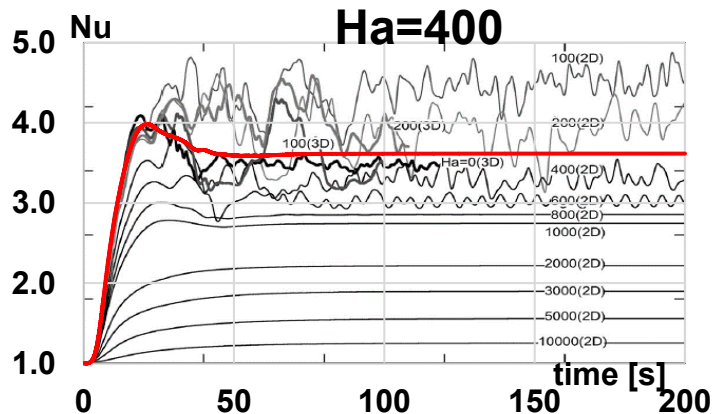
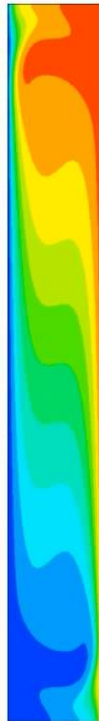


Time = 200 [s]

Temperature



[°C]



Experimental and Numerical Data Authie et al 2003

PPPL Magnetic Induction Formulation in ANSYS CFX

- Magnetic Induction MHD formulation was introduced in customized version of CFD code
- Transient MHD model was validated using analytical solution
- Customized code allows transient 3D MHD analysis in complex geometries

CFD
User Defined Sources

$$\frac{\partial \rho}{\partial t} + \vec{\nabla} \cdot (\rho \vec{V}) = 0$$

$$\frac{\partial \rho \vec{V}}{\partial t} + \vec{\nabla} \cdot (\rho \vec{V} \vec{V}) = -\vec{\nabla} p + \vec{\nabla} \cdot (\tau) + \rho \vec{g} + \vec{j} \times \vec{B}$$

Lorentz Force

$$\frac{\partial \rho c_p T}{\partial t} + \vec{\nabla} \cdot (\rho \vec{V} c_p T) = \vec{\nabla} \cdot (\lambda \vec{\nabla} T) + \tau : \vec{\nabla} \vec{V} + \dot{h} + \vec{j} \cdot \vec{E}$$

Joule Heat

MHD
Magnetic Induction Equation

$$\frac{\partial \vec{B}}{\partial t} = -\vec{\nabla} \times \vec{E}$$

Maxwell-Faraday Equation

$$\frac{\partial \vec{B}}{\partial t} = \vec{\nabla} \times (\vec{V} \times \vec{B}) - \vec{\nabla} \times \left(\frac{\vec{V} \times \vec{B}}{\mu \sigma} \right)$$

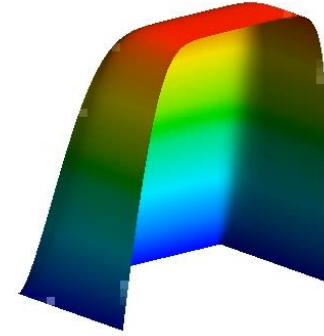
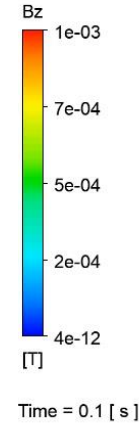
Ohm's Law

$$\vec{\nabla} \times \vec{B} = \mu \vec{j} + \frac{\mu}{\mu_0} \frac{1}{\sigma} \frac{\partial \vec{E}}{\partial t}$$

Ampere's Law

Introduced using:
User defined scalars
User defined transport equations
Gauss law enforced using additional $\vec{\nabla} \cdot \vec{B}$ cleaning procedure

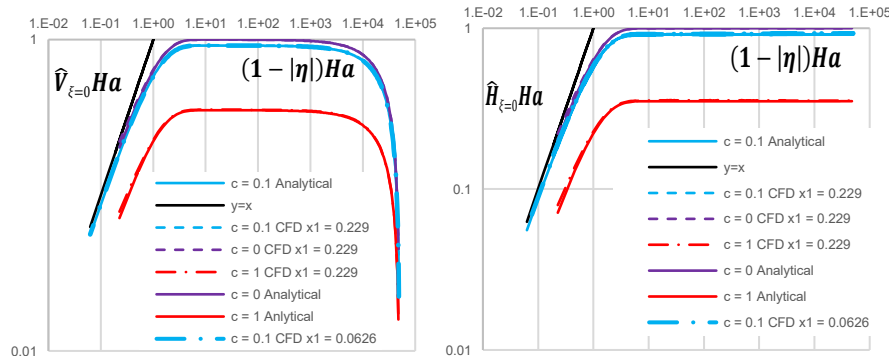
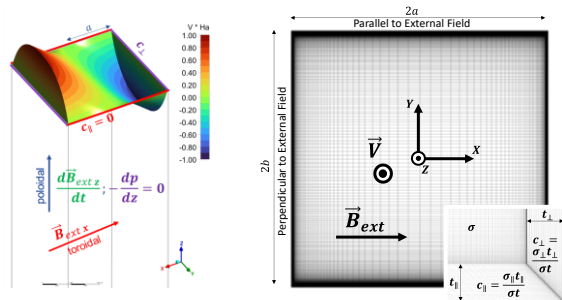
Linear Magnetic Low Frequency



Validation

Analytical solution by Khodak (PAMIR 2024)
Problem proposed by Smolentsev (FED 2024)
Steady state insulated walls parallel to magnetic field

Velocity and induced field profiles at $Ha = 50000$



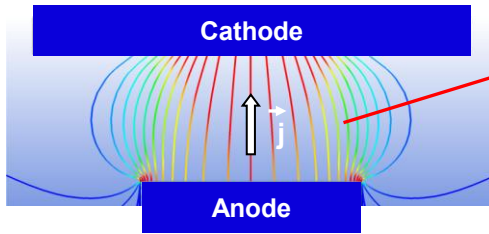
Outline

- Problem Set-up, Preparation and Meshing
- CFD Modeling at PPPL
- MHD
- Virtual Prototyping System
- Coupling
- Transient Flows
- **Multiphysics Analysis**

Universal computational platform for simulation of interacting solids, fluids, gases, and highly collisional plasma

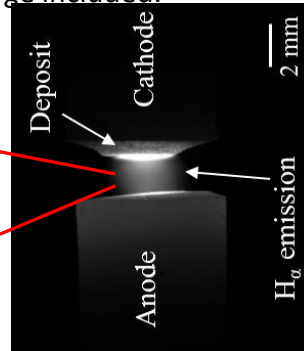
- Customized 3D CFD code from ANSYS
- MHD simulations for high Hartman numbers
- Self-Consistent model of atmospheric arc discharge included.

Electric current streamlines:

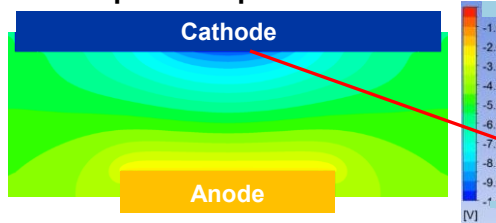


Arc contraction

Arc channel



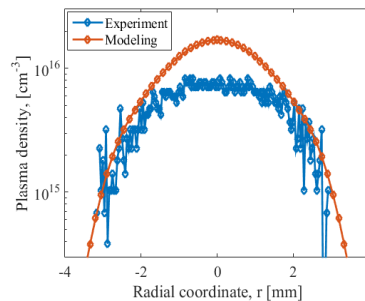
Electric potential profile:



Non-uniform potential distribution along the cathode tip

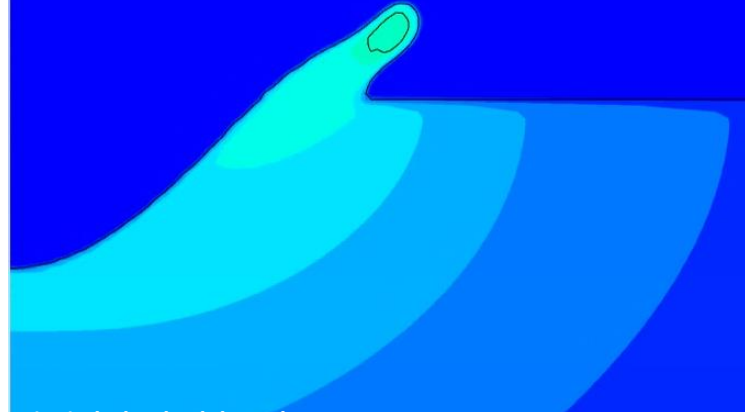
J. Chen, et al, Physics of Plasmas 2020

Middle plane plasma density profile:

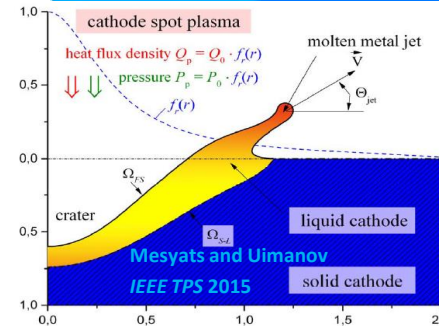


3-phase transient analysis

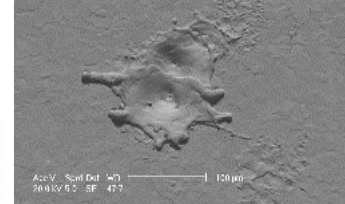
Unipolar act impact cavity development



Vignitchuk, Khodak et al NME 2020



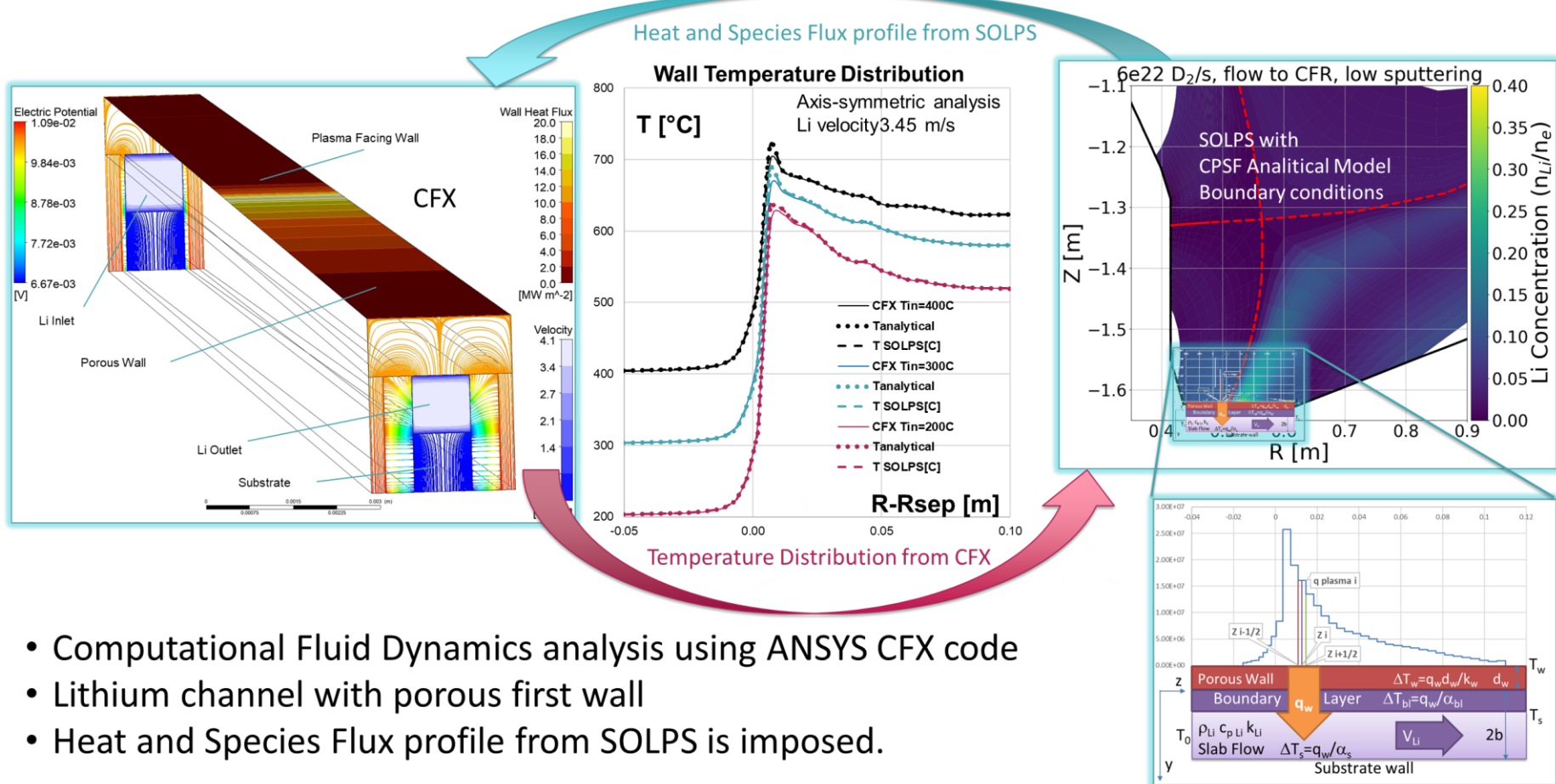
Khimchenko ITER 2019



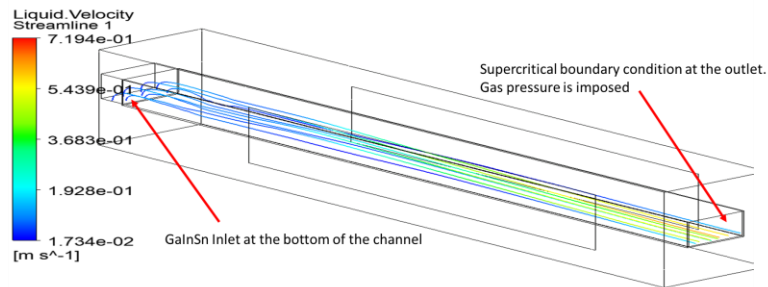
Coupled SOLPS 3D CFD MHD model



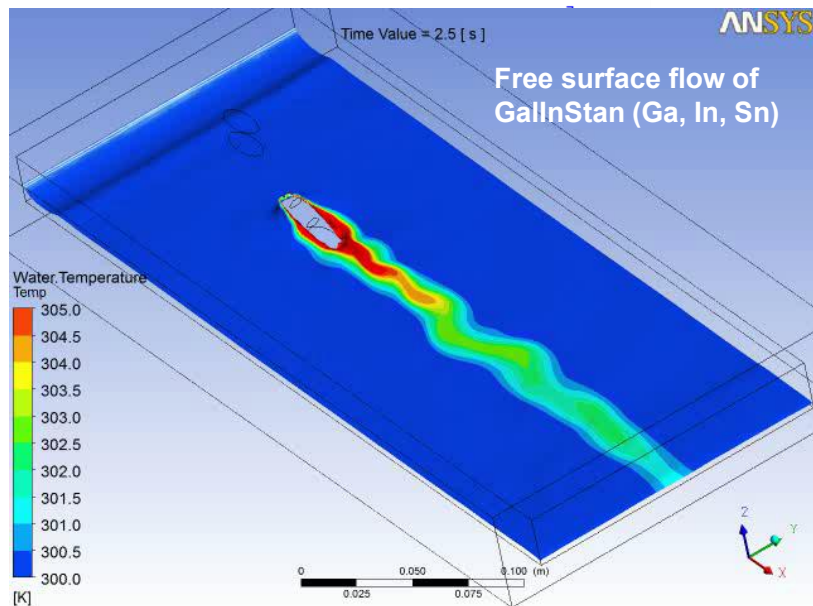
46



- Computational Fluid Dynamics analysis using ANSYS CFX code
- Lithium channel with porous first wall
- Heat and Species Flux profile from SOLPS is imposed.

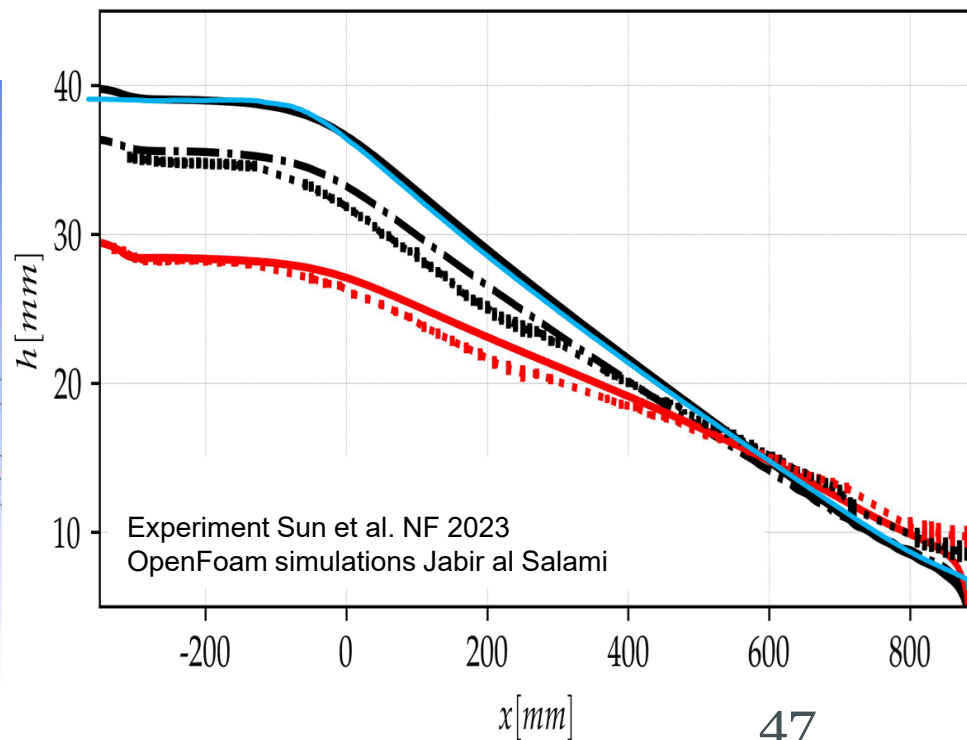


CFX Simulation GallSn level is not imposed both at the inlet and at the outlet



Validation of the free surface MHD codes

- Simulation 0.3T
- - - Simulation 0.3T (without corner)
- Simulation 0.2T
- Experiment 0.3T
- Experiment 0.2T
- Simulation CFX 0.3T



Summary

High-field MHD capabilities were implemented in the ANSYS CFX code and validated using a variety of steady-state and transient test cases.

The code forms the foundation of a Virtual Prototyping System for fusion device components, enabling fully multi-physics modeling and coupling with plasma-edge simulation tools.

This system has been successfully applied to the analysis and design optimization of liquid-metal blankets.