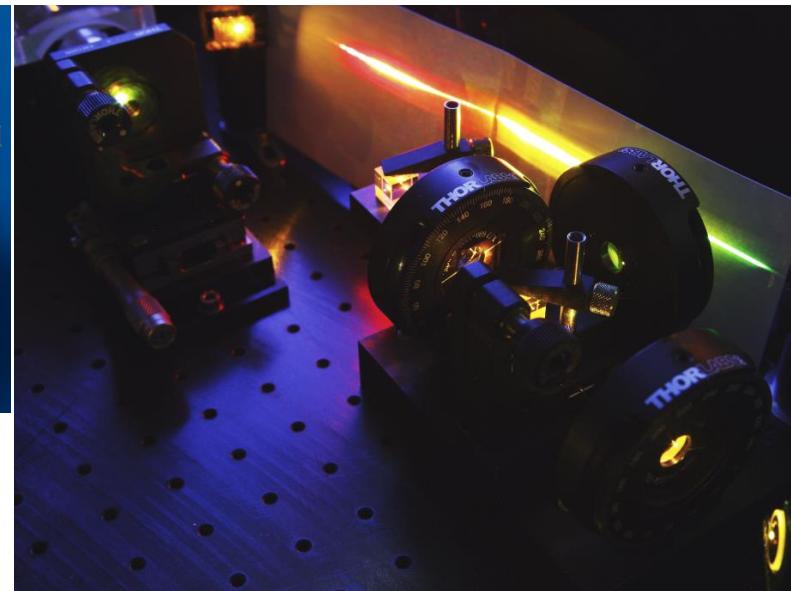


Charge Radii of Light Isotopes from Laser Spectroscopy of He-Like Atomic Systems



W. Nörtershäuser, P. Imgram, K. König, B. Maaß, P. Müller



Deutsche
Forschungsgemeinschaft



SFB 1245
Atomic Nuclei: From Fundamental
Interactions to Structure and Stars



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für Bildung
und Forschung

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für Wissenschaft und Kunst

Outline

Introduction

Motivation

Experimental Setup

Results

Summary and Outlook

Isotope Shift in a Nutshell

$$\delta\nu_{\text{IS}}^{AA'} = \nu^{A'} - \nu^A$$

$$\delta\nu_{\text{IS}}^{AA'} \approx K_{\text{MS}} \cdot \frac{M_{A'} - M_A}{M_A M_{A'}} + F \delta \langle r_c^2 \rangle^{AA'}$$

$$\delta \langle r_c^2 \rangle^{AA'} \approx \frac{1}{F} \left[\delta\nu_{\text{IS}}^{AA'} - K_{\text{MS}} \cdot \mu^{A'A} \right]$$

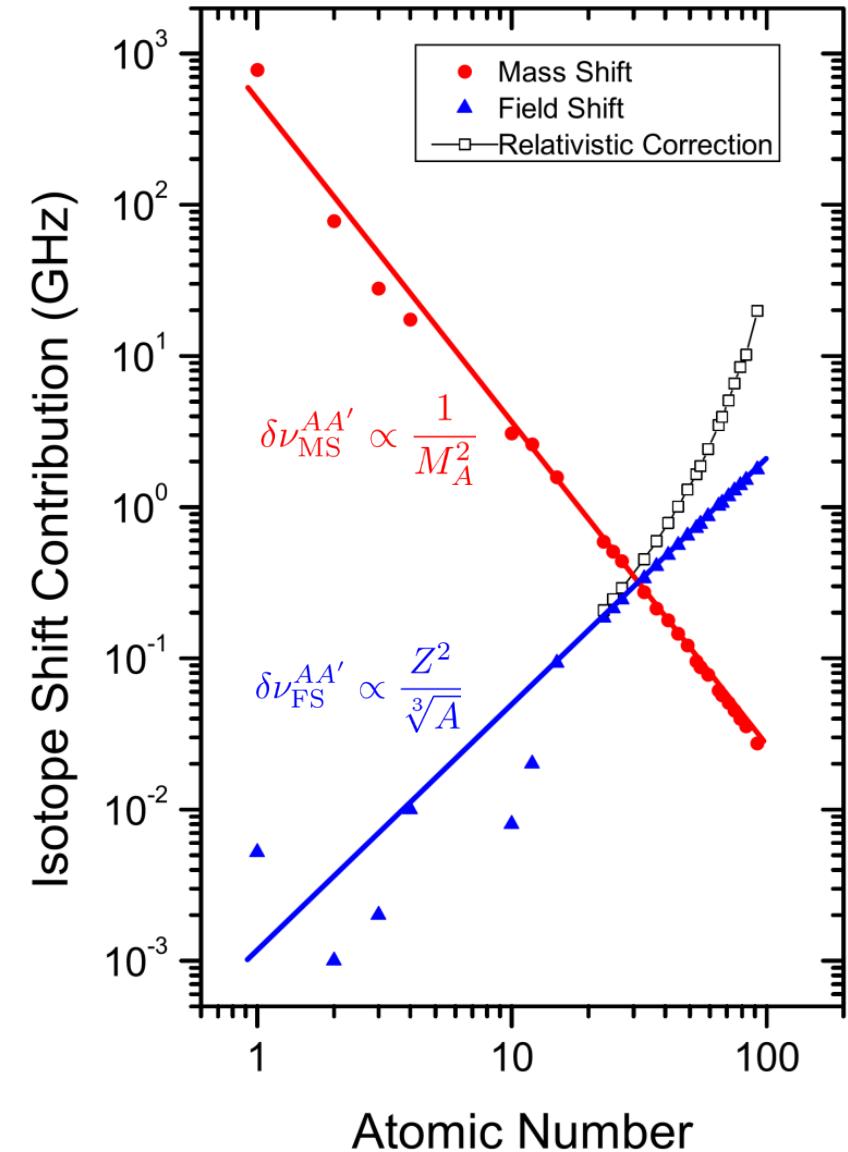
Requires knowledge of F and K_{MS} !

- ab initio NR-QED: up to 5-electron systems
- MCDHF, MBPT,
- King plot (requires ≥ 3 stable isotopes with known R_c)

How to get a radius ?

$$R_c(A) = \sqrt{\underbrace{R_c^2(A_{\text{ref}})}_{\text{Reference radius required from a different technique}} + \delta \langle r_c^2 \rangle^{A_{\text{ref}}, A}}$$

Reference radius required from a different technique



Nuclear Charge Radii

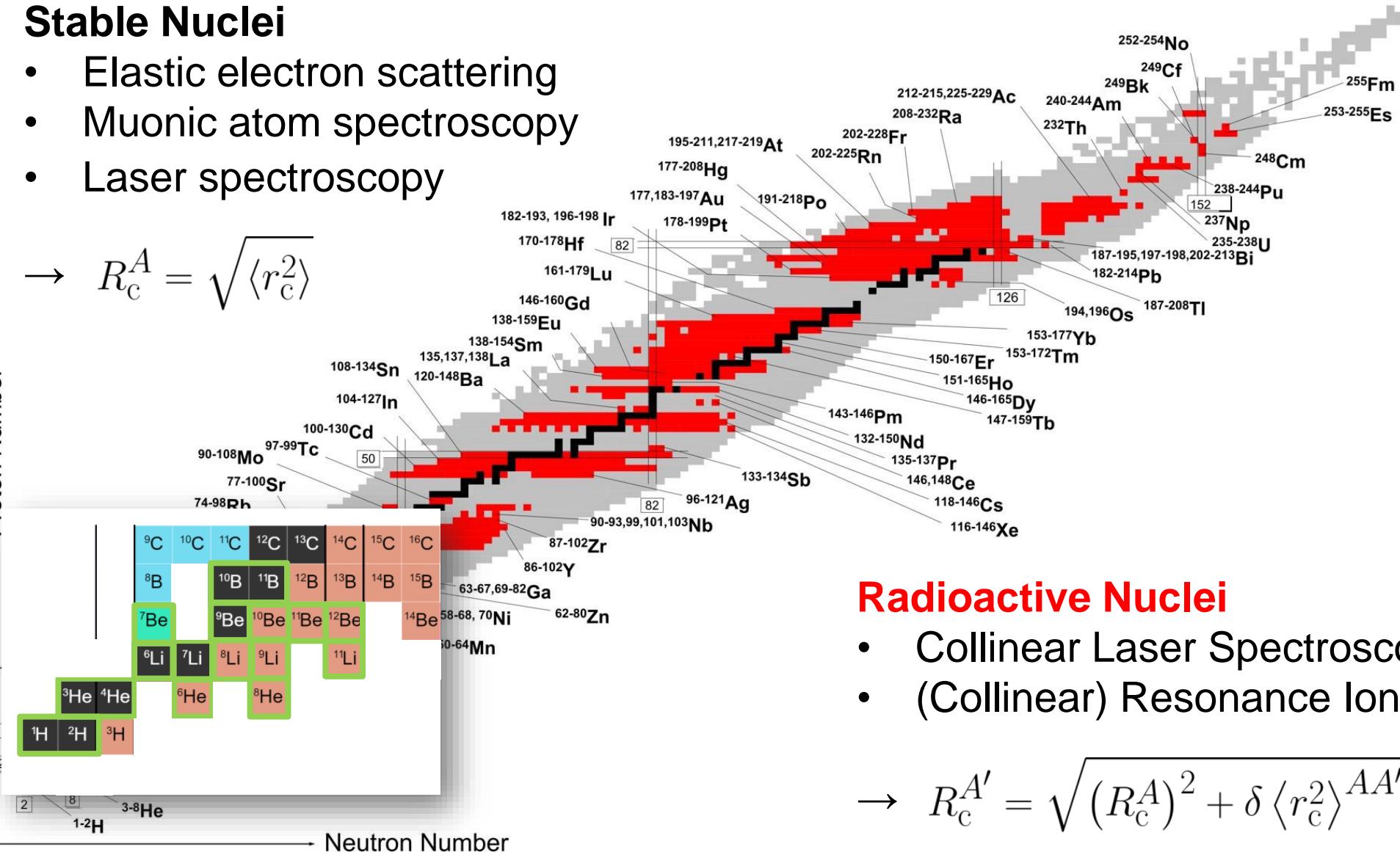
$$\left\langle r_c^2 \right\rangle = \frac{1}{Z} \int d^3r \ r^2 \rho_c(\vec{r})$$

Stable Nuclei

- Elastic electron scattering
- Muonic atom spectroscopy
- Laser spectroscopy

$$\rightarrow R_c^A = \sqrt{\left\langle r_c^2 \right\rangle}$$

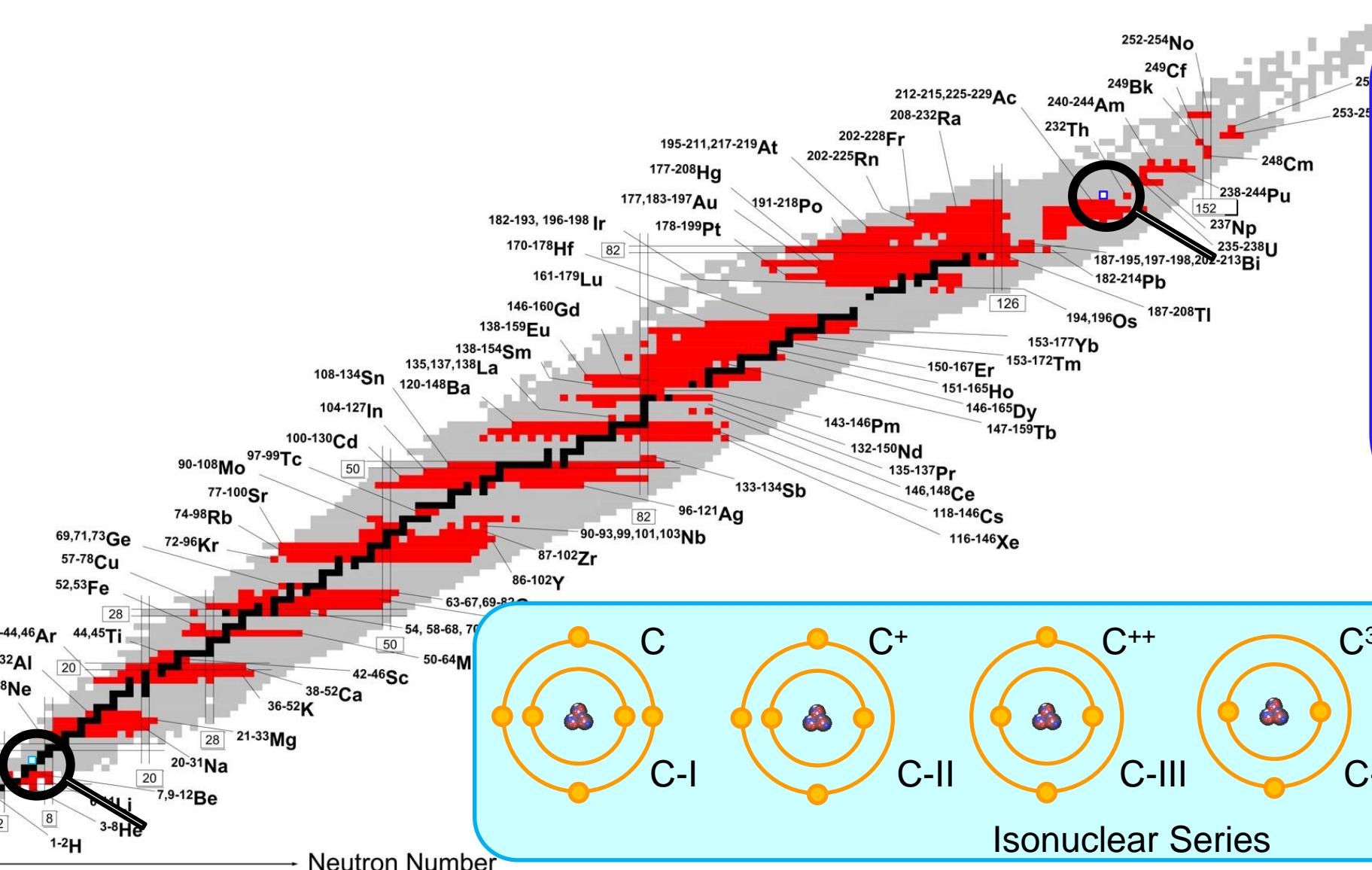
Proton Number



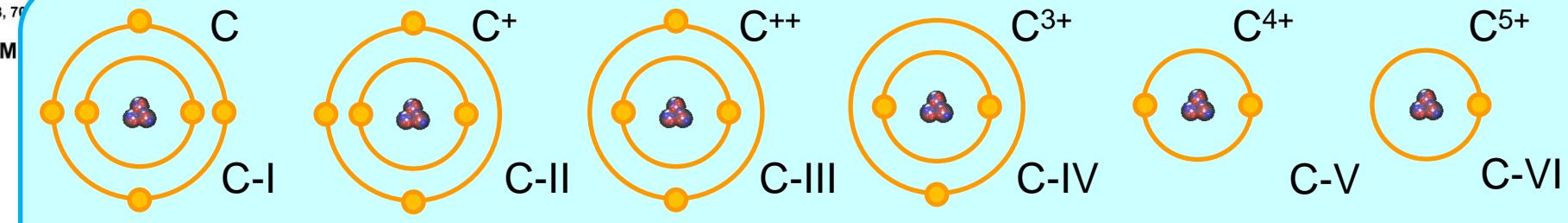
Additional Dimensions

Proton Number

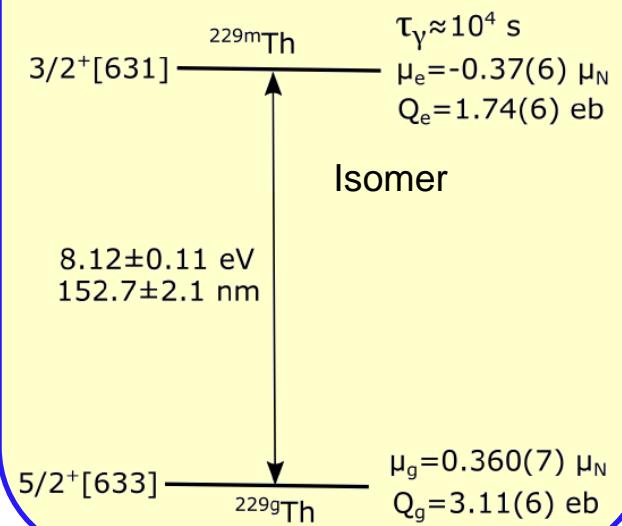
Neutron Number



Isonuclear Series

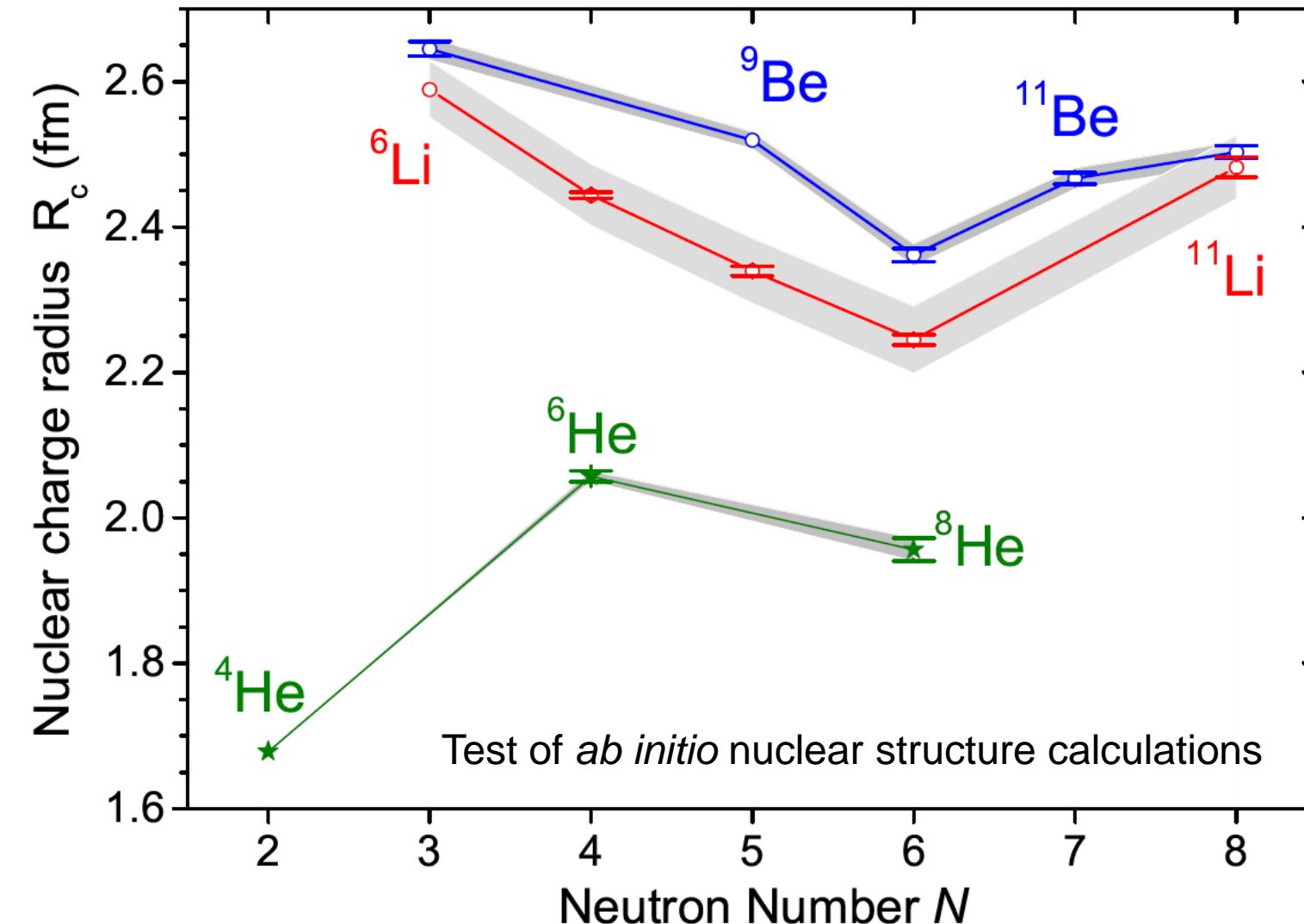


Excited Nuclear States



MOTIVATION

Nuclear Radii of the Lightest Isotopes



Error Bars: $\sigma(\delta v_{IS})$

A. Krieger *et al.*, PRL **108**, 142501 (2012)

R. Sanchez *et al.*, PRL **96**, 033002 (2006)

P. Müller *et al.*, PRL **99**, 252501 (2008)

Grey Regions: $\sigma(R_c)$

$$R_c(^9\text{Be}) = 2.519 (12) \text{ fm}$$

J.A. Jansen *et al.*, Nucl. Phys. A **188**, 337 (1972)

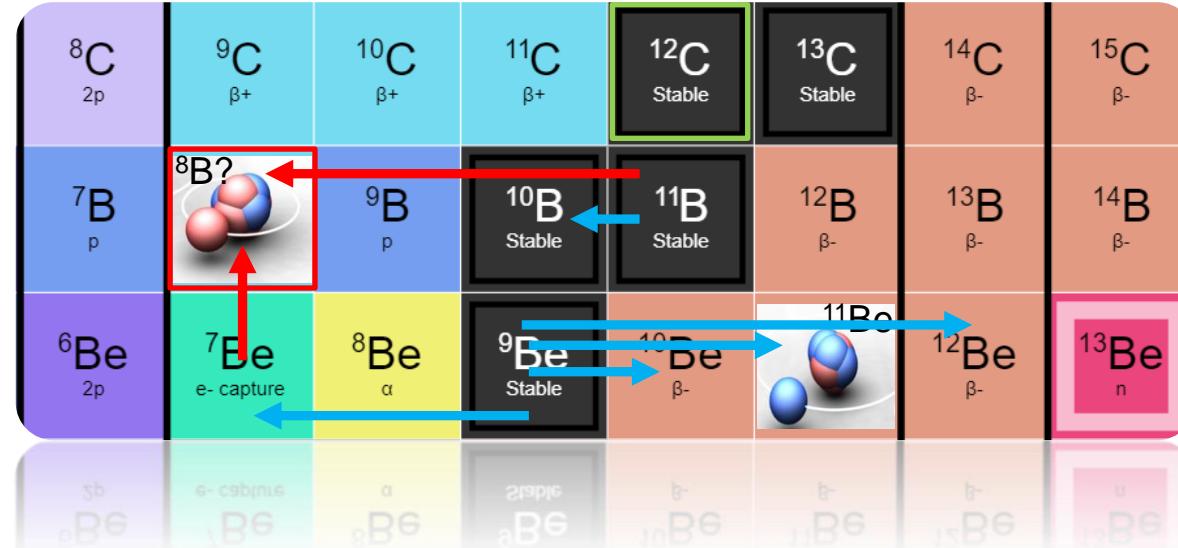
$$R_c(^6\text{Li}) = 2.589 (39) \text{ fm}$$

W. Nörtershäuser *et al.*, Phys. Rev. C **84**, 024307 (2011)

$$R_c(\alpha) = 1.678\,24(83) \text{ fm}$$

J.J. Krauth *et al.*, Nature **589**, 527 (2021)

The Proton-Halo Nucleus ${}^8\text{B}$



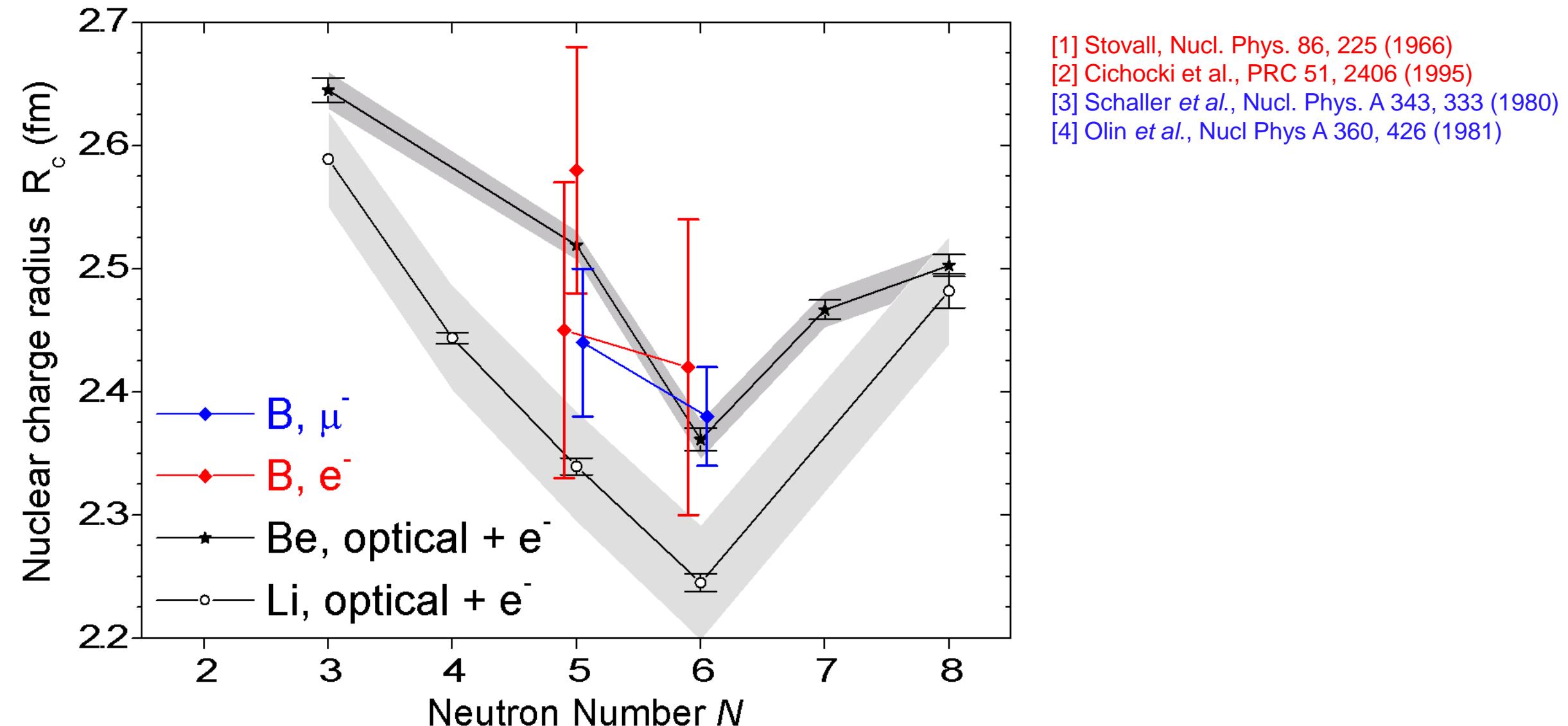
$$\delta\nu_{\text{IS}} - \delta\nu_{\text{MS}}^{\text{Theory}} \propto \delta\langle r_c^2 \rangle \longrightarrow R_c(A) = \sqrt{R_c^2(A_{\text{ref}}) + \delta\langle r_c^2 \rangle^{A_{\text{ref}}, A}}$$

Reference Radii required

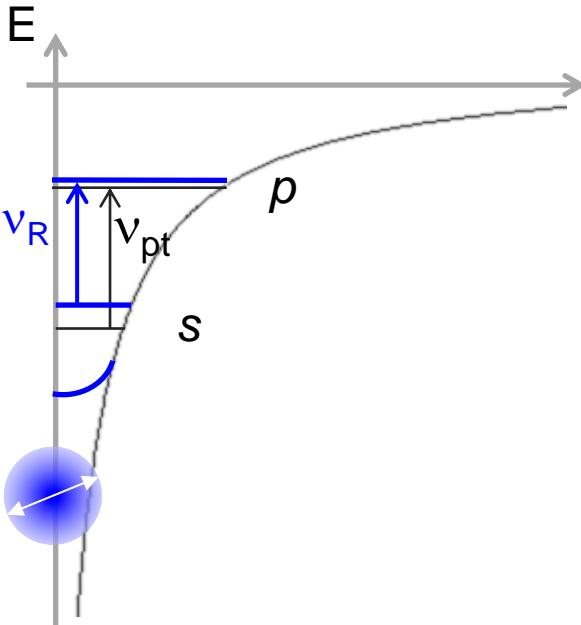
„Proton-halo size“: $R_c(\text{p}_{\text{halo}}) = R_c({}^8\text{B}) - R_c({}^7\text{Be})$

Conclusion: To gain information about the proton halo of ${}^8\text{B}$, we need reliable reference radii for Be and B **on equal footing** !

„Reference“ Radii of Boron



All-Optical Absolute Charge Radii



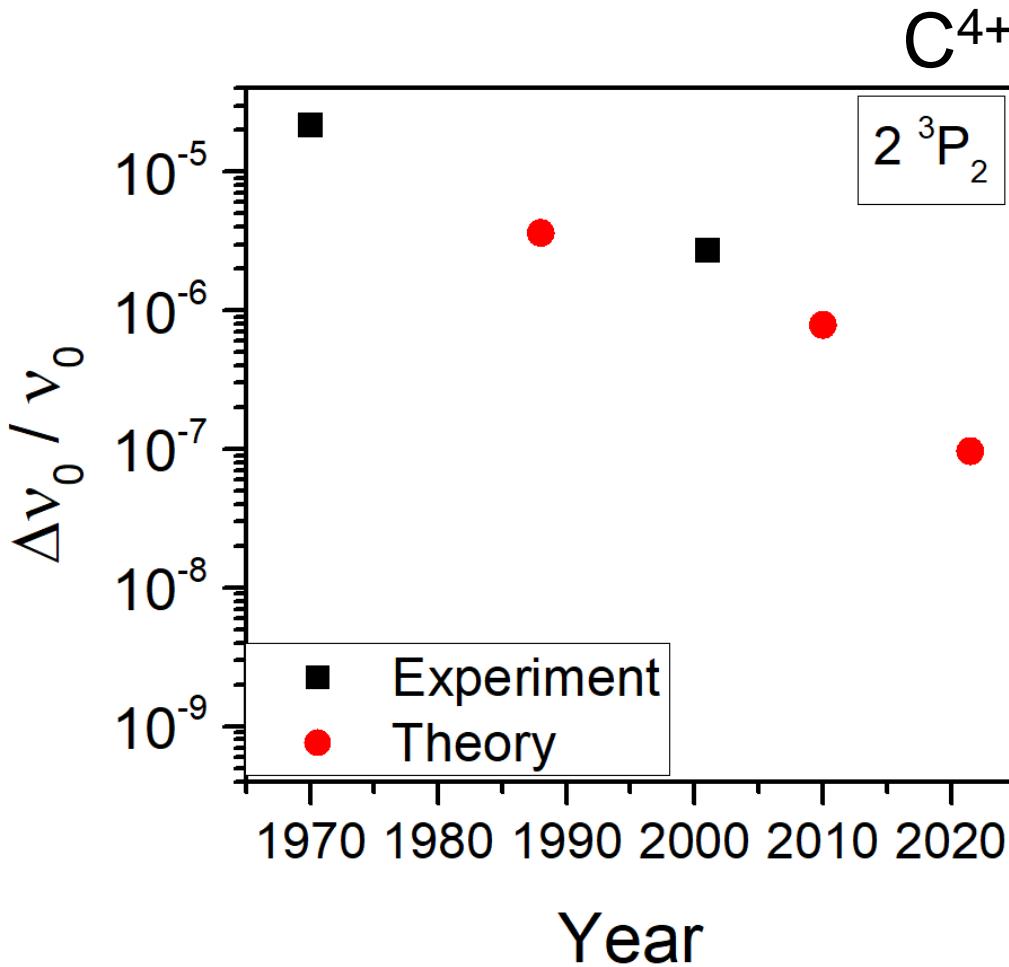
The diagram shows a plot of energy E versus radius r . A horizontal dashed line represents the point-like nucleus energy level. A solid curve represents the finite-size system energy levels. Two levels are shown: a higher one labeled p and a lower one labeled s . The vertical distance between these two levels is labeled ν_R . The vertical distance from the s level to the point-like nucleus level is labeled ν_{pt} .

$$\begin{aligned}\delta\nu_{FS} &= \nu_R - \nu_{pt} \\ &= -\frac{Ze^2}{6\varepsilon_0} \Delta |\Psi_e(0)|_{i \rightarrow f}^2 \times \langle r_c^2 \rangle \\ &\quad \underbrace{\qquad\qquad\qquad}_{\text{Electronic Factor}} \\ &= F_{i \rightarrow f} \langle r_c^2 \rangle\end{aligned}$$

- Measure **transition frequency** ν_R
- Compare with high precision atomic calculation for a point-like nucleus ν_{pt}
- Difference $\nu_R - \nu_{pt}$ is finite-size effect and **proportional to the ms charge radius**
- So far applied **only for H-like systems**, i.e., H, μ H and μ He
- Two-electron system requires elaborate QED calculations, which have been improved considerably

V.A. Yerokhin, V. Patkóš & K. Pachucki, PRA **98**, 032503 (2018)
V. Patkóš, V.A. Yerokhin & K. Pachucki, PRA **103**, 042809 (2021)
V.A. Yerokhin, V. Patkóš & K. Pachucki, PRA **106**, 022815 (2022)

Theory



Exp: S. Ozawa *et al.*, Phys. Scr. **T92**, 195 (2001)
Beam-foil spectroscopy

$$R_c(^{12}\text{C}) = 2.471(6) \text{ fm}$$

I. Sick, PLB 116, 212 (1982)

TABLE X. Comparison of theoretical and experimental $n = 2$ intrashell transition energies, in cm^{-1} .

Z	Theory	Experiment	Difference	Ref.
$2\ ^3S_1 - 2\ ^3P_0$				
5	35 393.6211 (49) 35 393.628 (14) ^a	35 393.627 (13)	-0.006 (13)	[47]
8	60 978.788 (27) 60 978.85 (14) ^a	60 978.44 (52)	0.35 (52)	[48]

V.A. Yerokhin, V. Patkóš & K. Pachucki, PRA **106**, 022815 (2022)

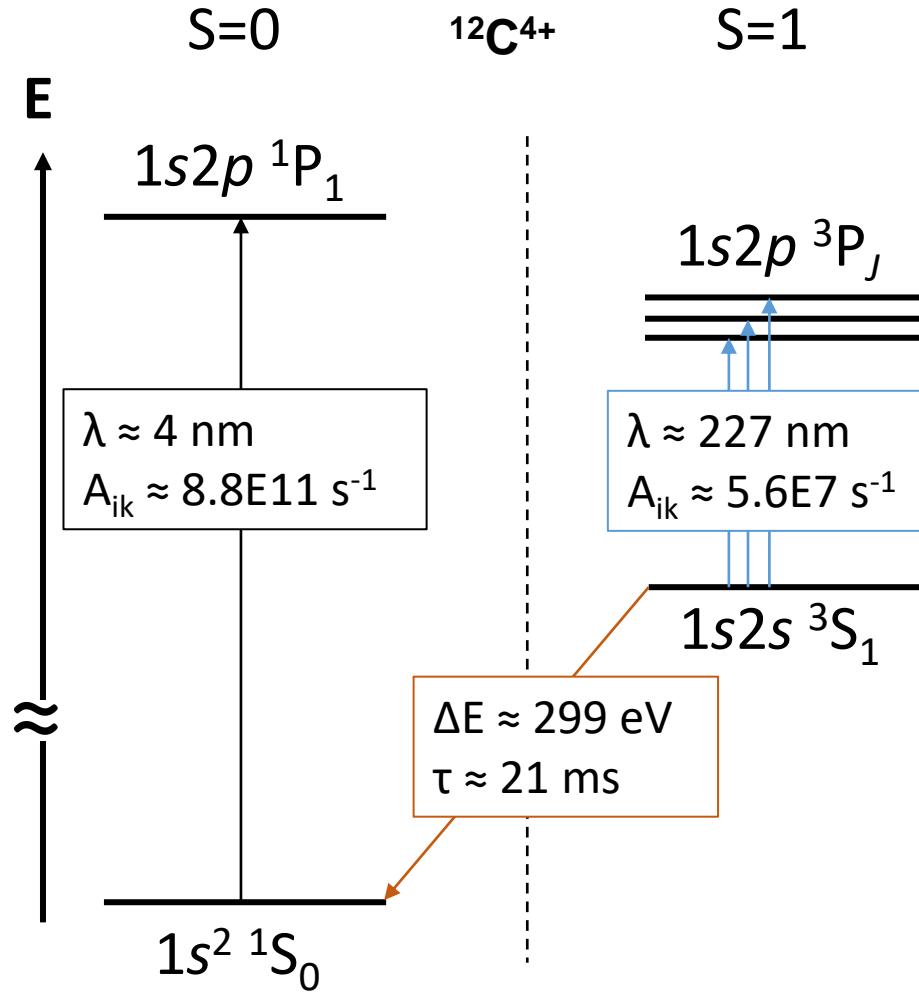
C ⁴⁺	$1s2s\ ^3S_1 \rightarrow 1s2p\ ^3P_2$	$1s2s\ ^3S_1 \rightarrow 1s2p\ ^3P_1$	$1s2s\ ^3S_1 \rightarrow 1s2p\ ^3P_0$
ΔE_p (eV)	5.45804678(53)	5.4412107(31)	5.4427592(11)
F ($\mu\text{eV}/\text{fm}^2$)	-0.875	-0.875	-0.874
ν_p (GHz)	1319749.83(13)	1315678.89(75)	1316053.32(27)
F (GHz/ fm^2)	0.2115	0.2115	0.2113

P. Imgram, Dissertation TU Darmstadt (2023)

P. Imgram, PRL **131** 243001 (2023)

Required accuracy for $\Delta R_c \leq 0.006$ fm: $\Delta\nu \leq 6$ MHz

The Case of $^{12}\text{C}^{4+}$



e^- scattering: $R_c(^{12}\text{C}) = 2.471(6) \text{ fm}$

I. Sick, PLB **116**, 212 (1982)

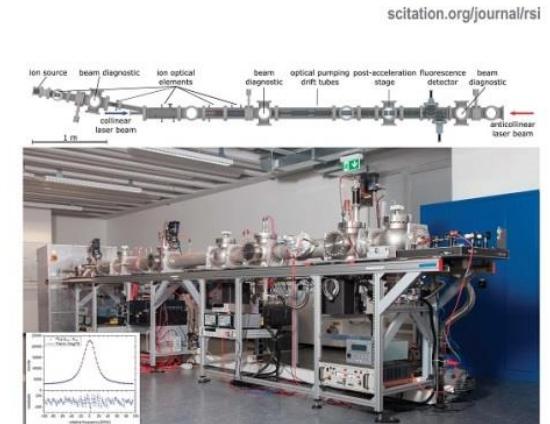
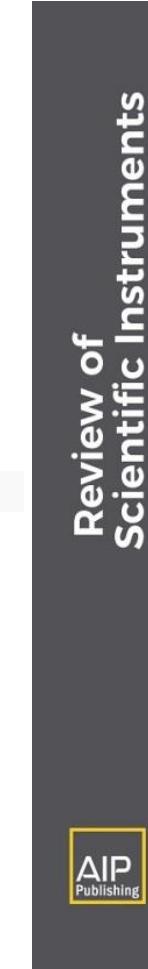
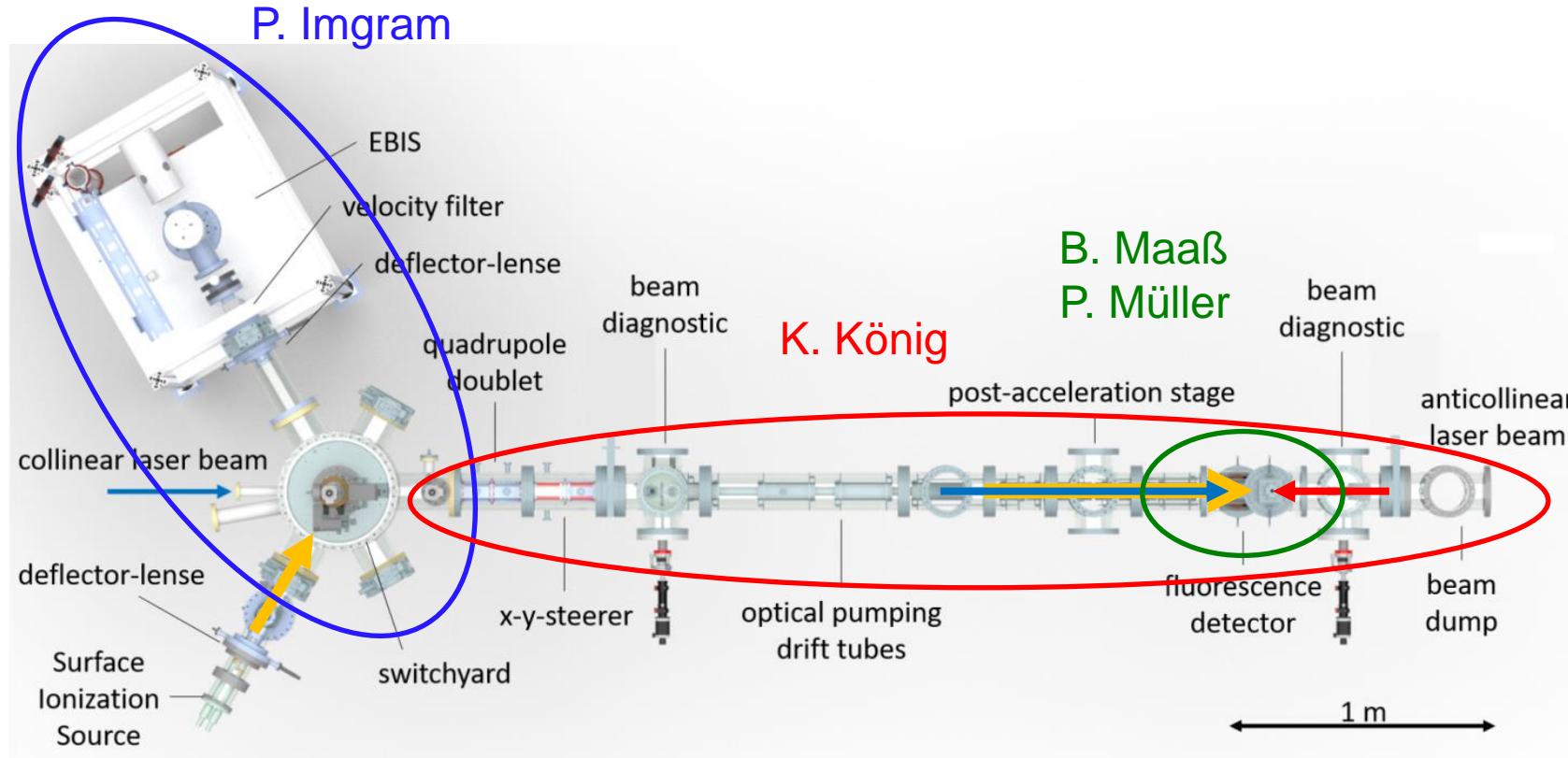
Muonic atoms: $R_c(^{12}\text{C}) = 2.4829(19) \text{ fm}$

W. Ruckstuhl *et al.*, NPA **430**, 685 (1984)

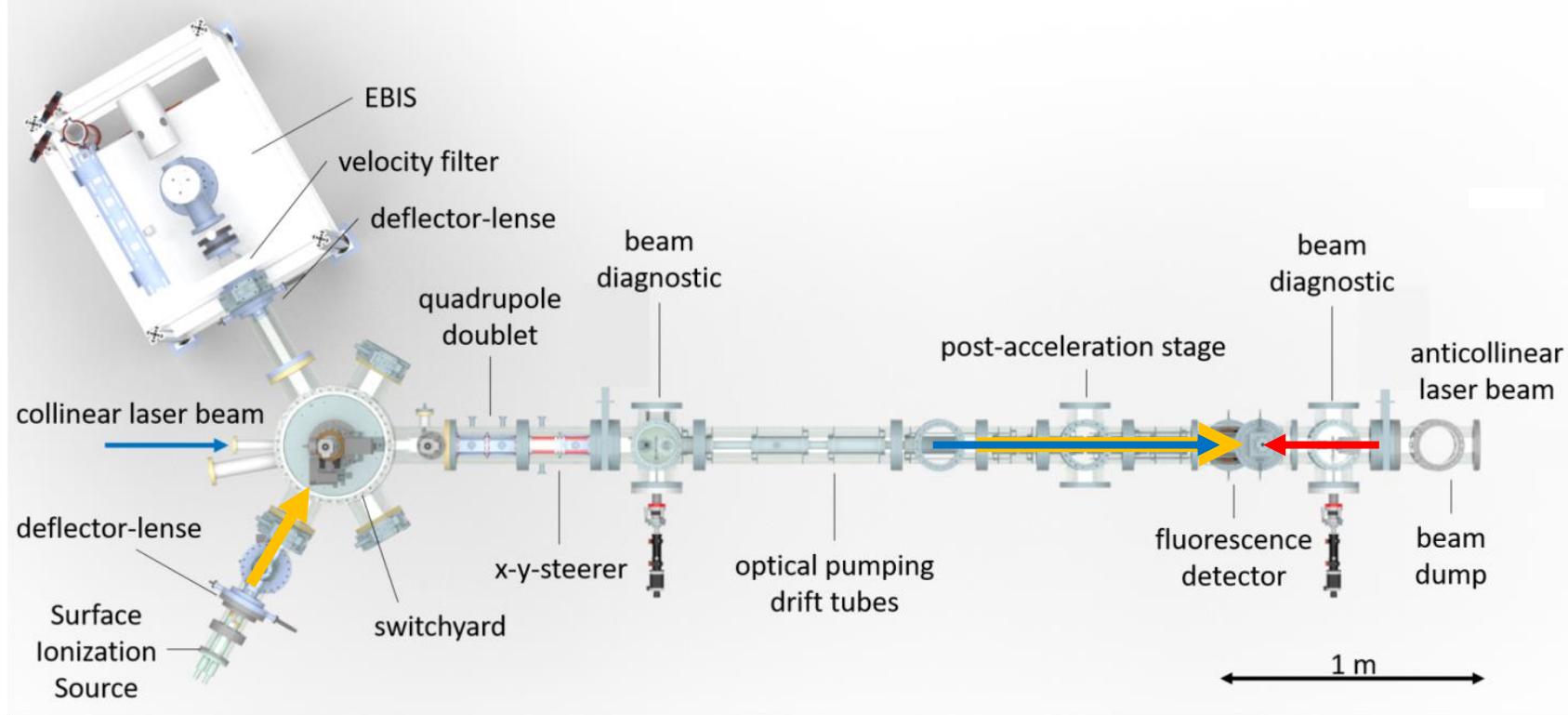
- Nuclear Charge Radius of ^{12}C well known
→ Test of Theory
- Easy to produce in an EBIS
- $\lambda \approx 227 \text{ nm} \rightarrow \text{Ti:Sa} \times 4$ stabilized to frequency comb
- $I = 0 \rightarrow$ no hyperfine-structure induced level mixing

EXPERIMENTAL SETUP

COALA = Collinear Apparatus for Laser Spectroscopy and Applied Physics



Measurement Scheme

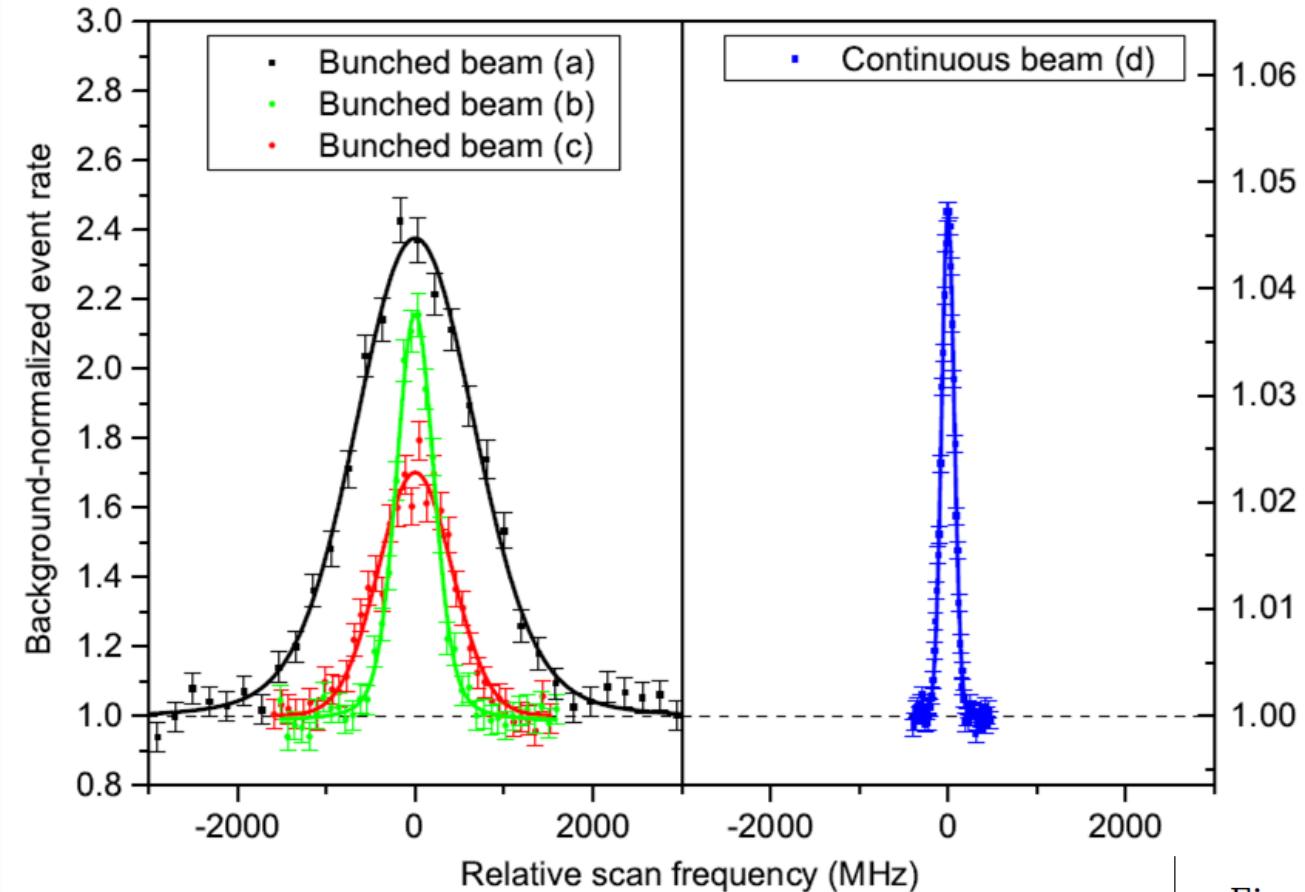


→ Measurement of v_0 instead of $\delta v^{A'A}$ removes uncertainties caused by the inaccurate knowledge of β (and γ).

$$\left. \begin{aligned} v_c &= v_0 \gamma (1 + \beta) \\ v_a &= v_0 \gamma (1 - \beta) \end{aligned} \right\} v_c \cdot v_a = v_0^2 \gamma^2 \cdot (1 + \beta)(1 - \beta) = v_0^2$$

LASER SPECTROSCOPY OPTIMIZATION AND RESULTS

Comparison of Pulsed and Continuous Extraction

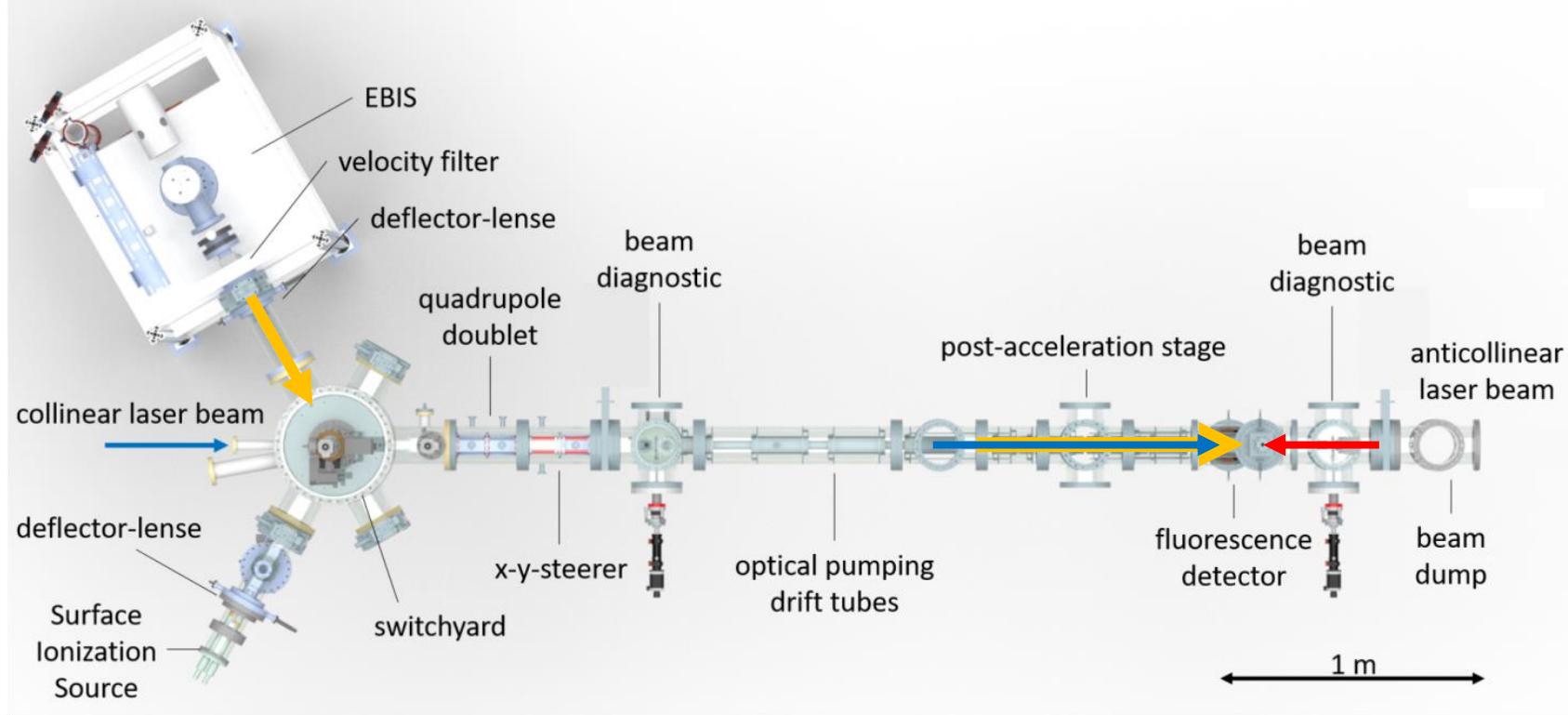


continuous extraction (leaky mode):

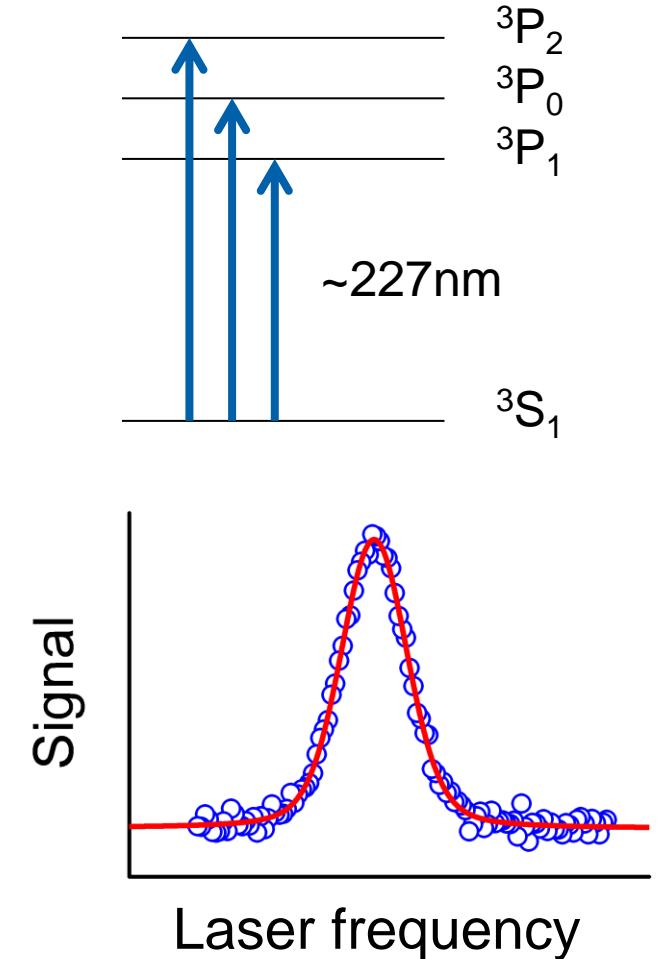
- good signal/noise ratio (similar to pulsed)
- smallest linewidth (gain factor 3)
- smallest statistical uncertainty for line centre

	Fig.	I_e / mA	$\Delta U_{\text{trap}} / \text{V}$	$p_{\text{gas}} / \text{mbar}$	$t_{\text{breed}} / \text{ms}$	SNR	FWHM / GHz	$\Delta\nu_{\text{center}} / \text{MHz}$
(a)	5.1/5.2	80	71	$6 \cdot 10^{-8}$	15	58	1.59(4)	16.6
(b)		25	26	$6 \cdot 10^{-8}$	15	51	0.50(1)	5.7
(c)	5.2	25	26	$2 \cdot 10^{-8}$	15	17	0.97(4)	17.8
(d)		80	171	$6 \cdot 10^{-8}$	leaky	59	0.168(2)	0.7

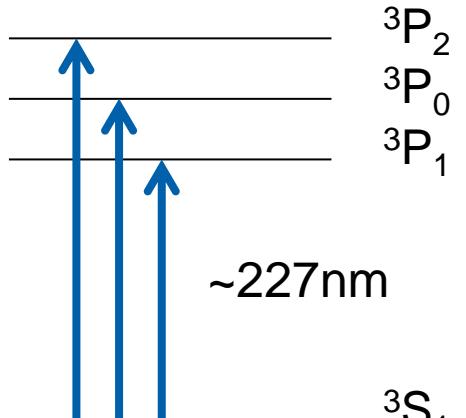
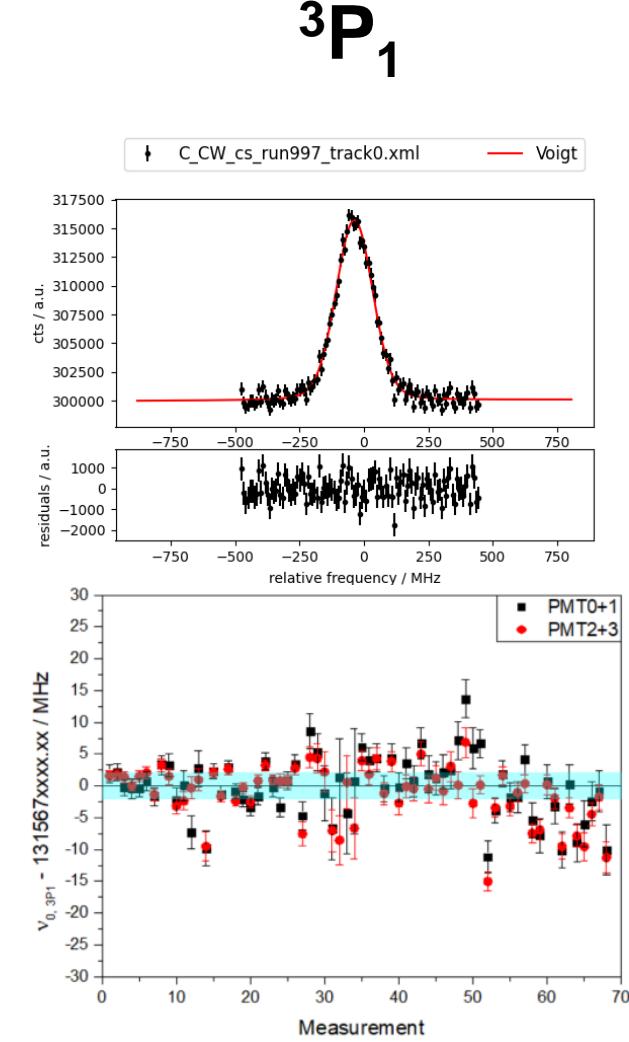
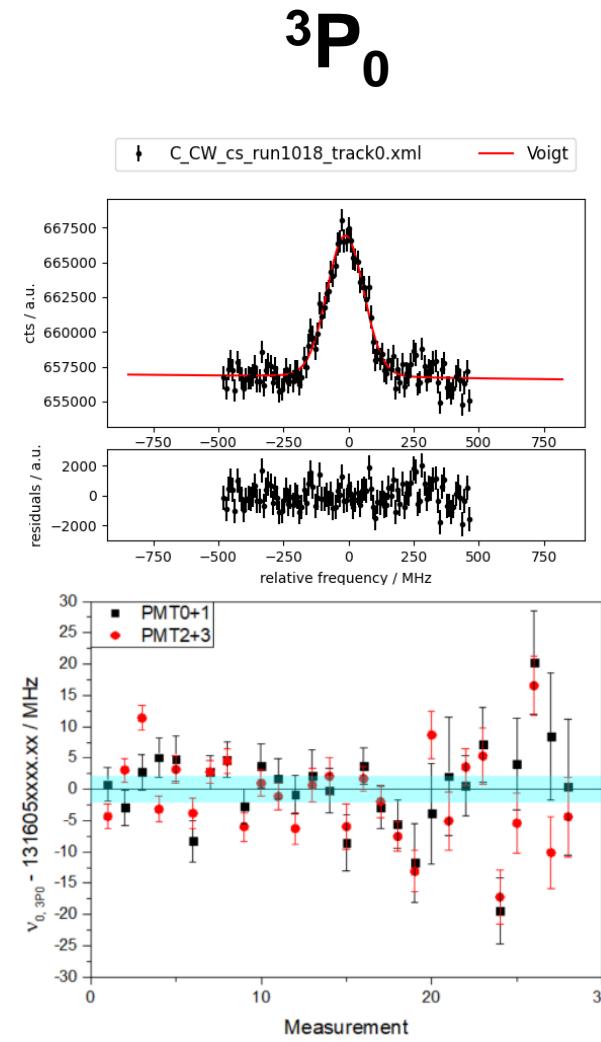
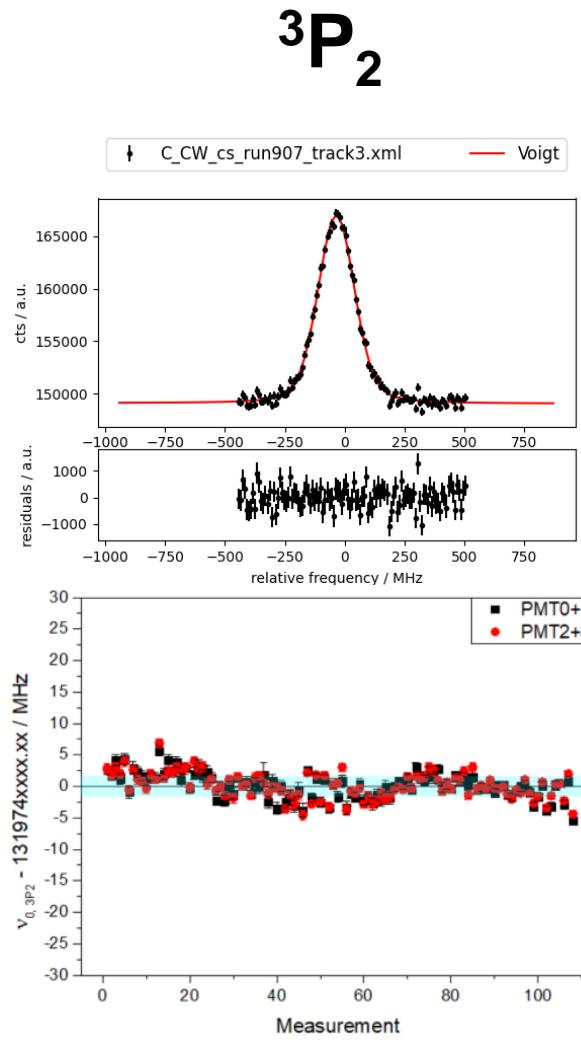
Laser spectroscopy of He-like ions



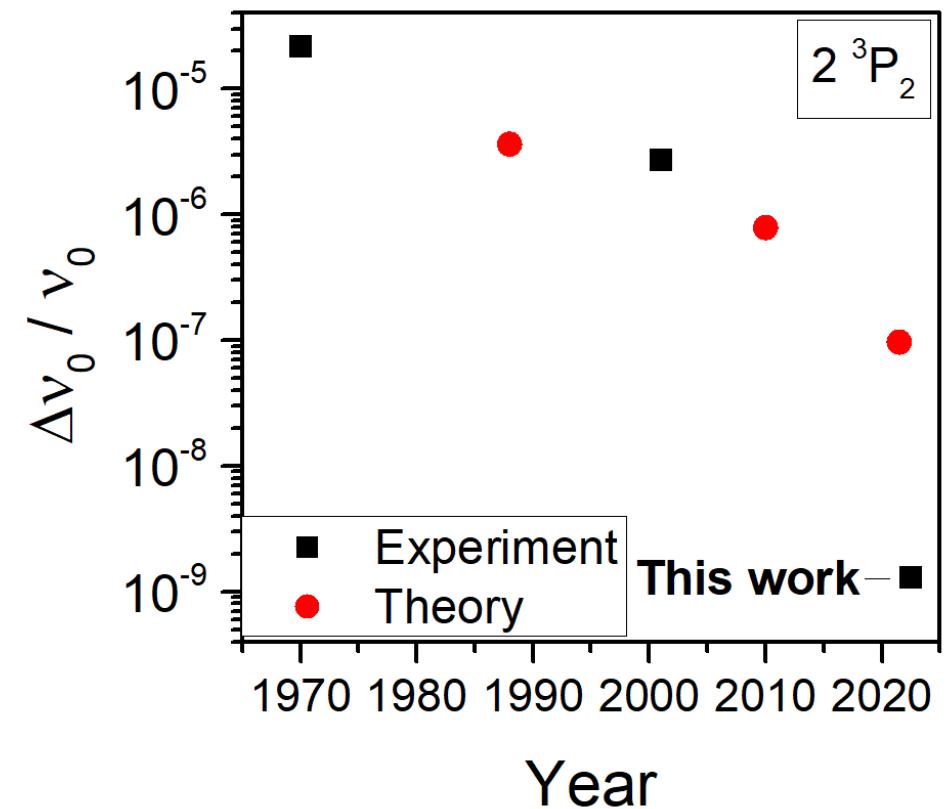
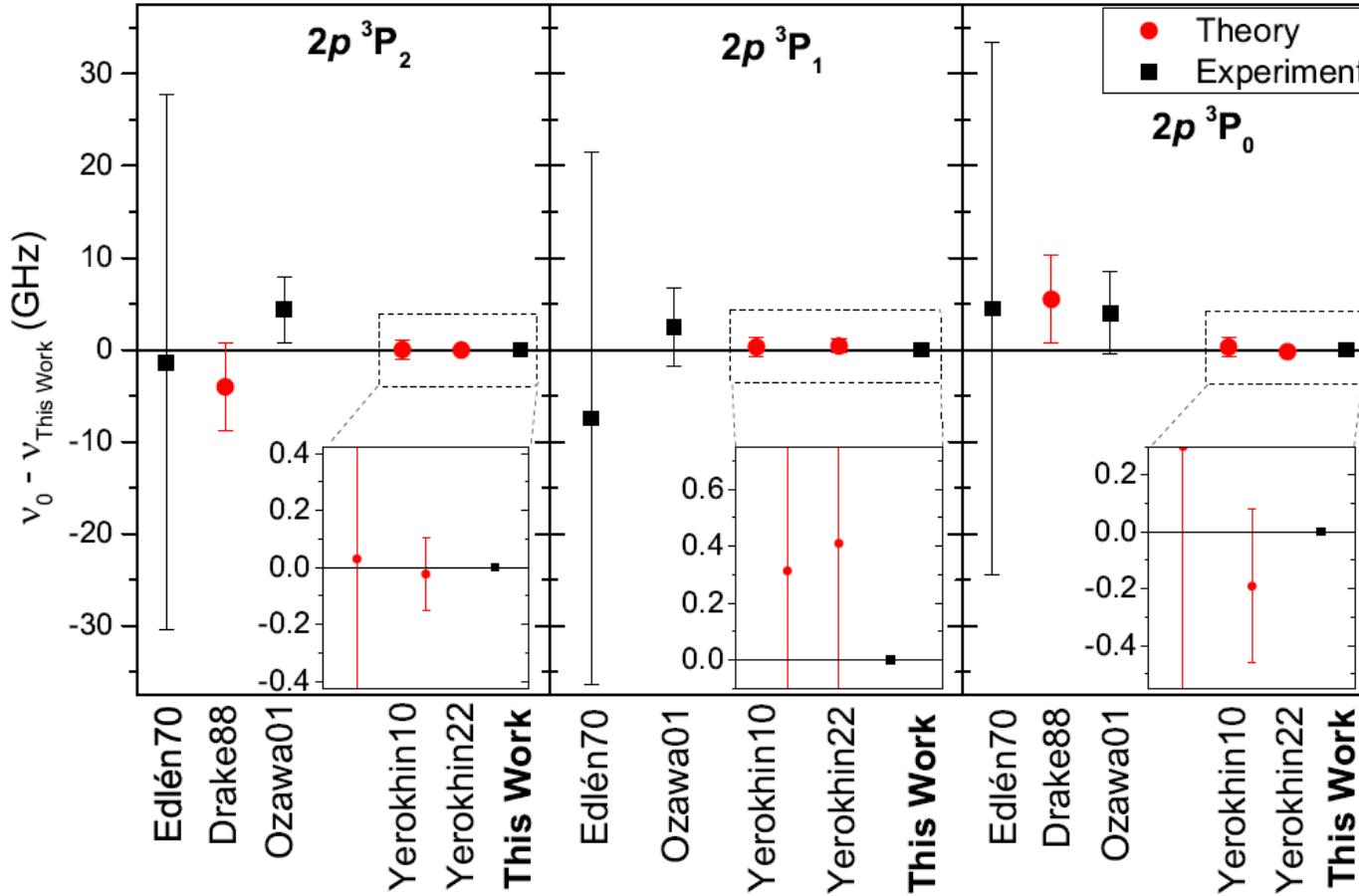
$$\left. \begin{aligned} v_c &= v_0 \gamma (1 + \beta) \\ v_a &= v_0 \gamma (1 - \beta) \end{aligned} \right\} \boxed{v_c \cdot v_a = v_0^2 \gamma^2 \cdot (1 + \beta)(1 - \beta) = v_0^2}$$



Laser spectroscopy results for $^{12}\text{C}^4+$



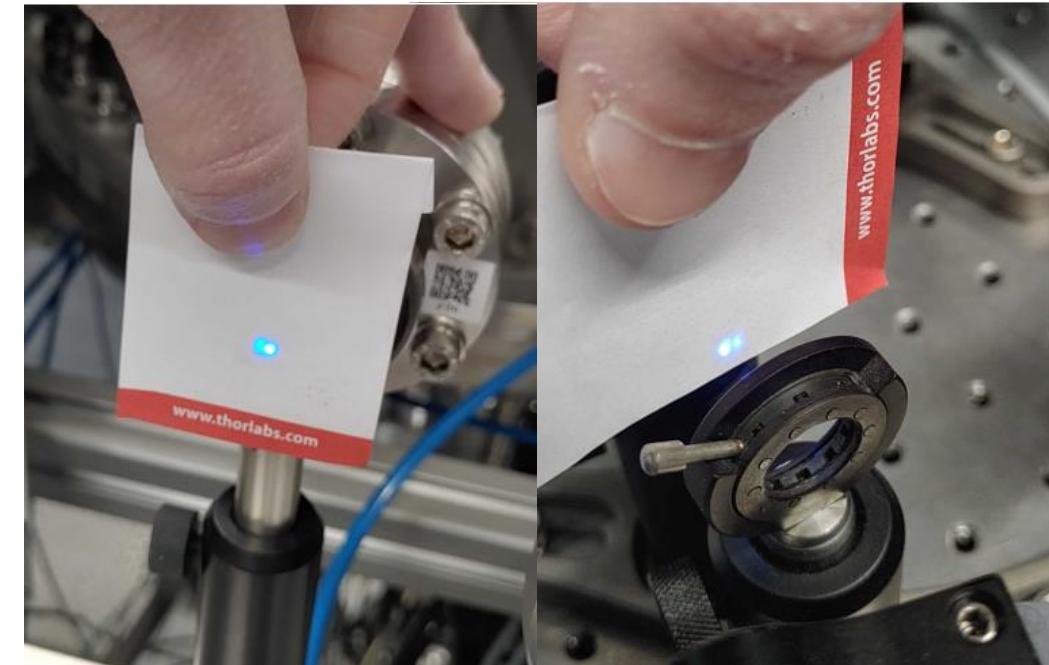
Transition Frequencies: Comparison to Literature



Uncertainty Budget and Fine Structure Splitting

TABLE IV. All investigated systematic uncertainties in MHz.
The main systematic uncertainty originates from the alignment of the two laser beams.

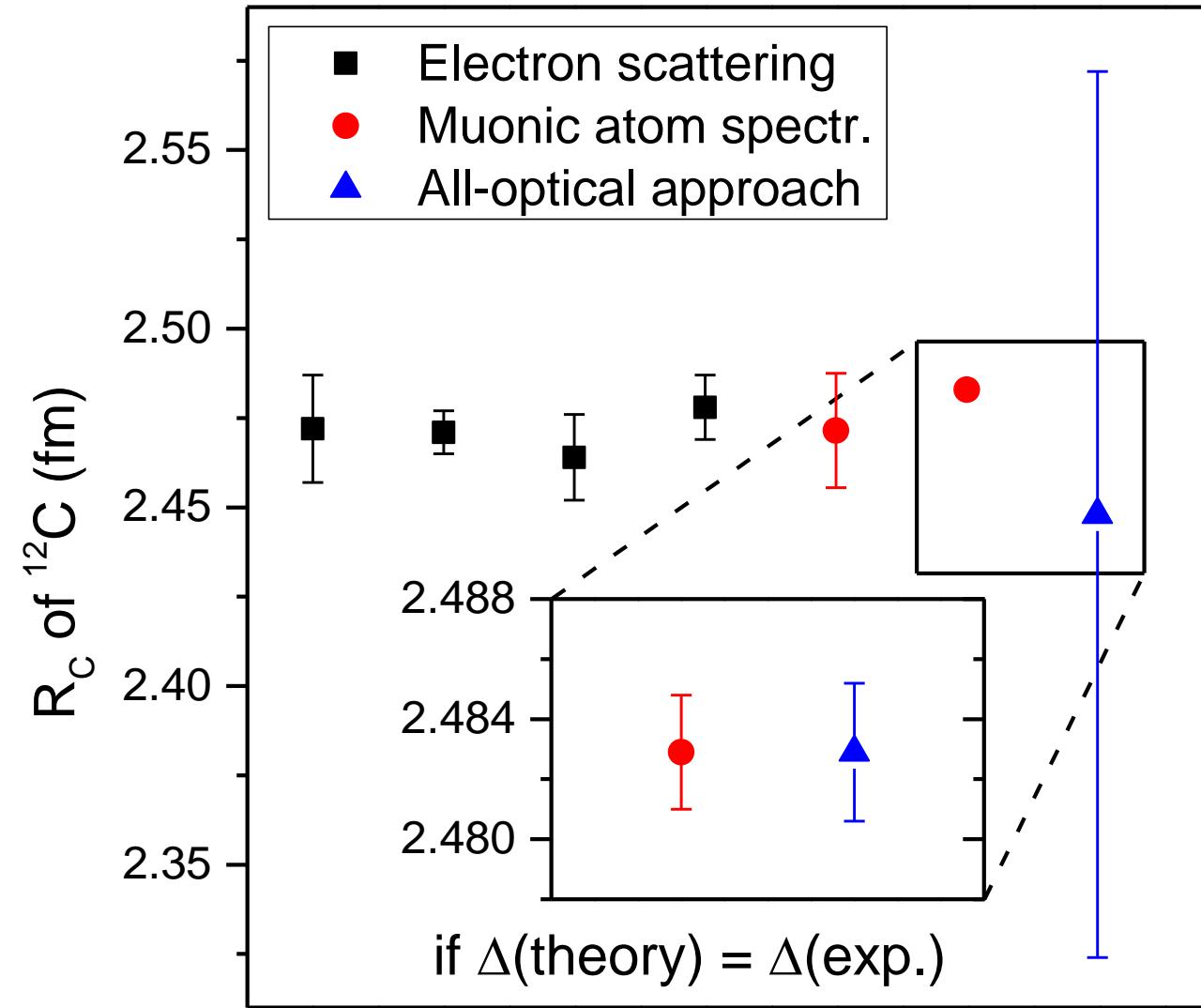
Uncertainty	
Line shape	<0.01
Start potential	0.01
Beam alignment	1.7
Photon recoil	<0.1
Scan voltage	<0.07
Laser polarization	0
Total	1.7



(J, J')	This work	Theory [52]	$m\alpha^{8+}$ contr.
(0, 1)	-375 026.5 (2.5)	-374 996.3 (48.0)	-30.2 (2.5)
(0, 2)	3 696 352.1 (2.5)	3 696 343.5 (10.0)	8.6 (2.5)

Relatively large contribution
of higher orders
⇒ may guide further QED
calculations

First all-optical nuclear charge radius of ^{12}C



→ more work needed for competitive all-optical R_C

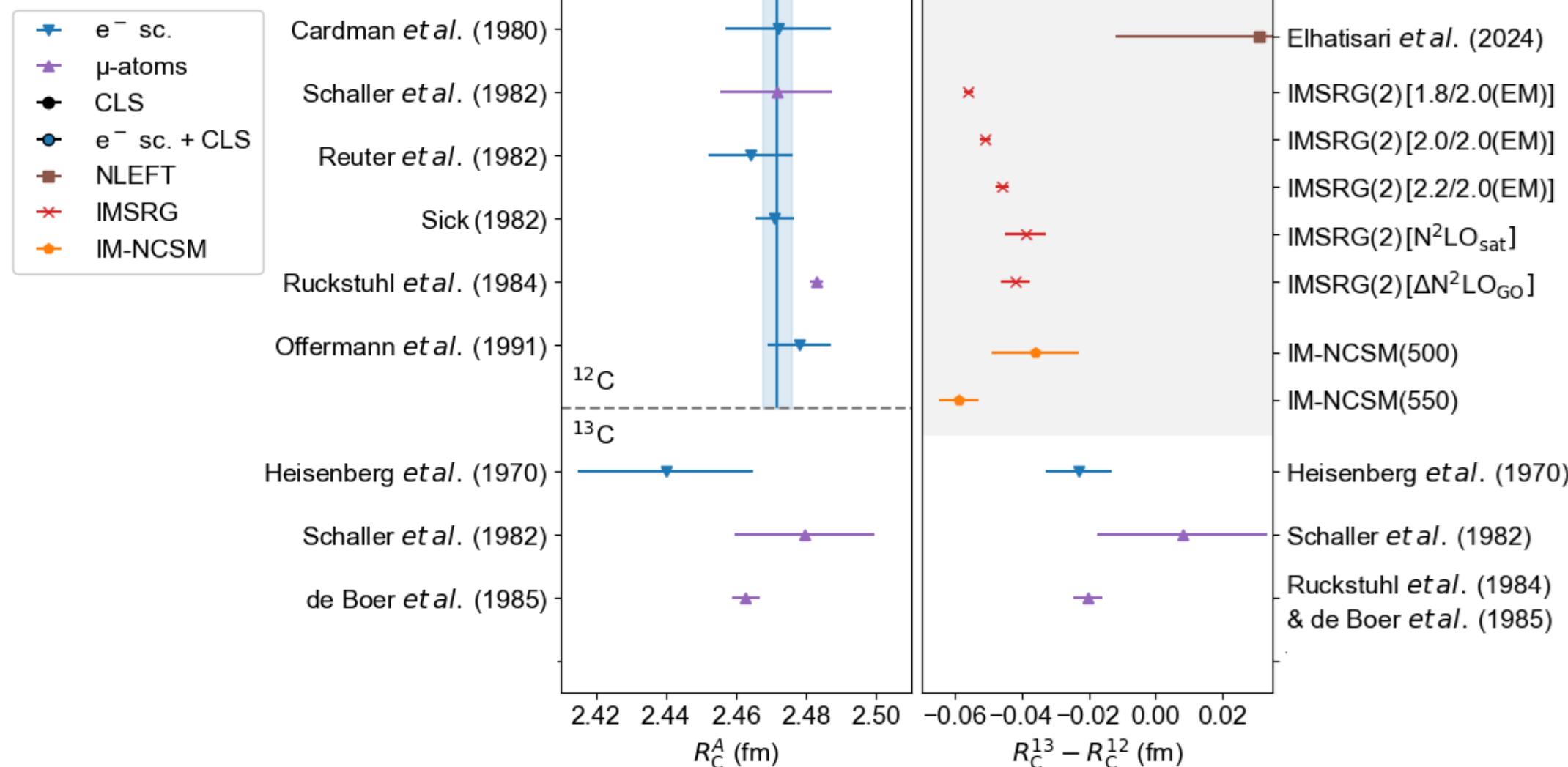
If **theory gets better by two orders of magnitude**, we are **competitive** with the most precise **muonic atom results**.

→ may resolve the discrepancies between muonic and elastic electron scattering results

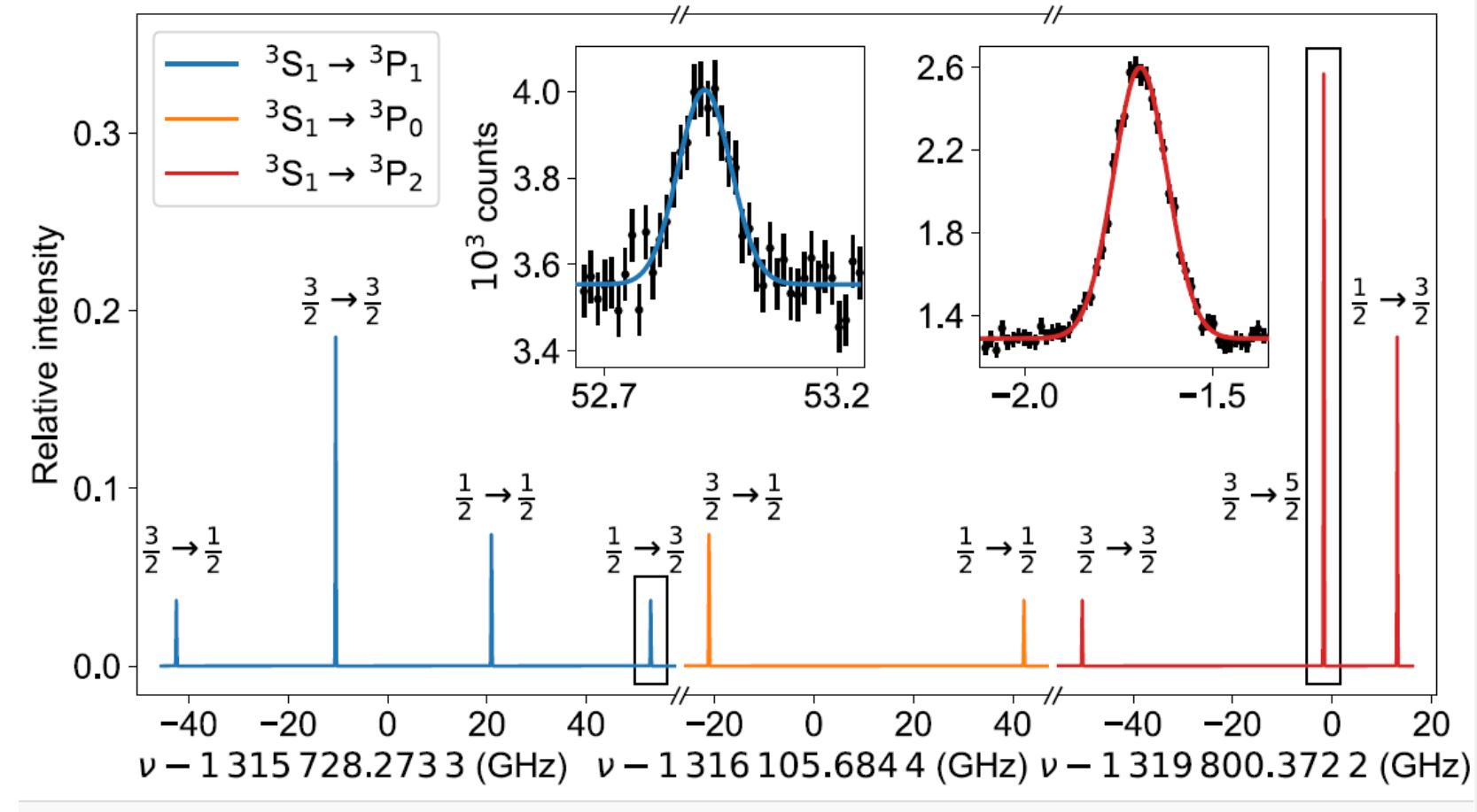
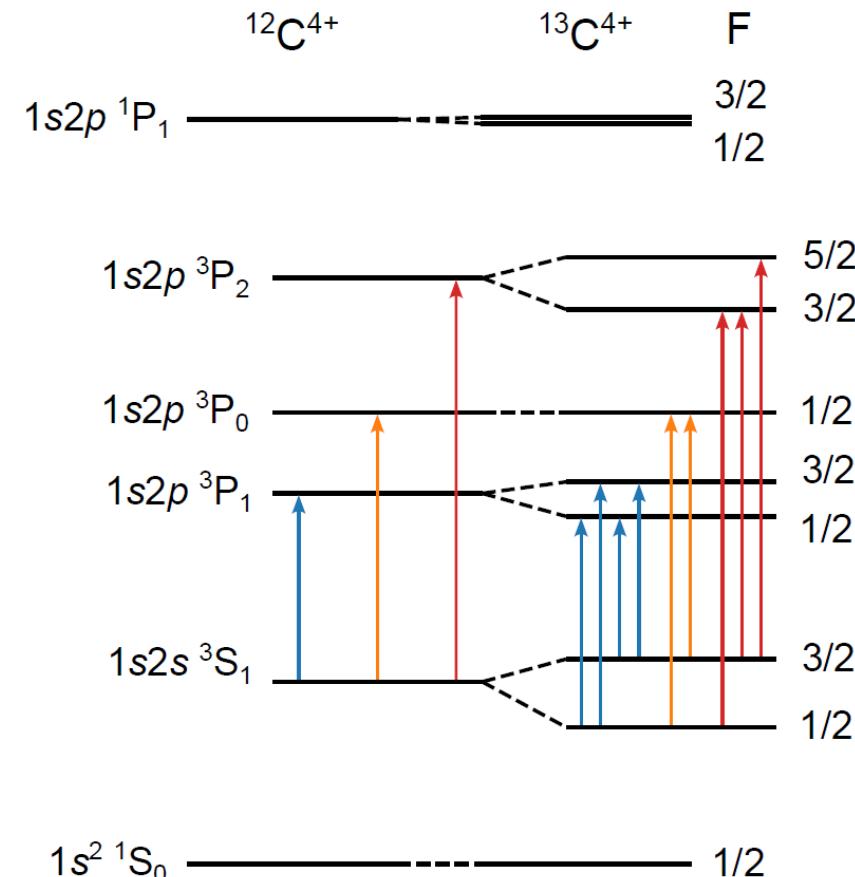
First high-precision laser spectroscopy in C isotope chain

→ starting point for regular isotope shift measurements to extract $\delta\langle r^2 \rangle$ of ^{13}C and ^{14}C

Motivation for ^{13}C

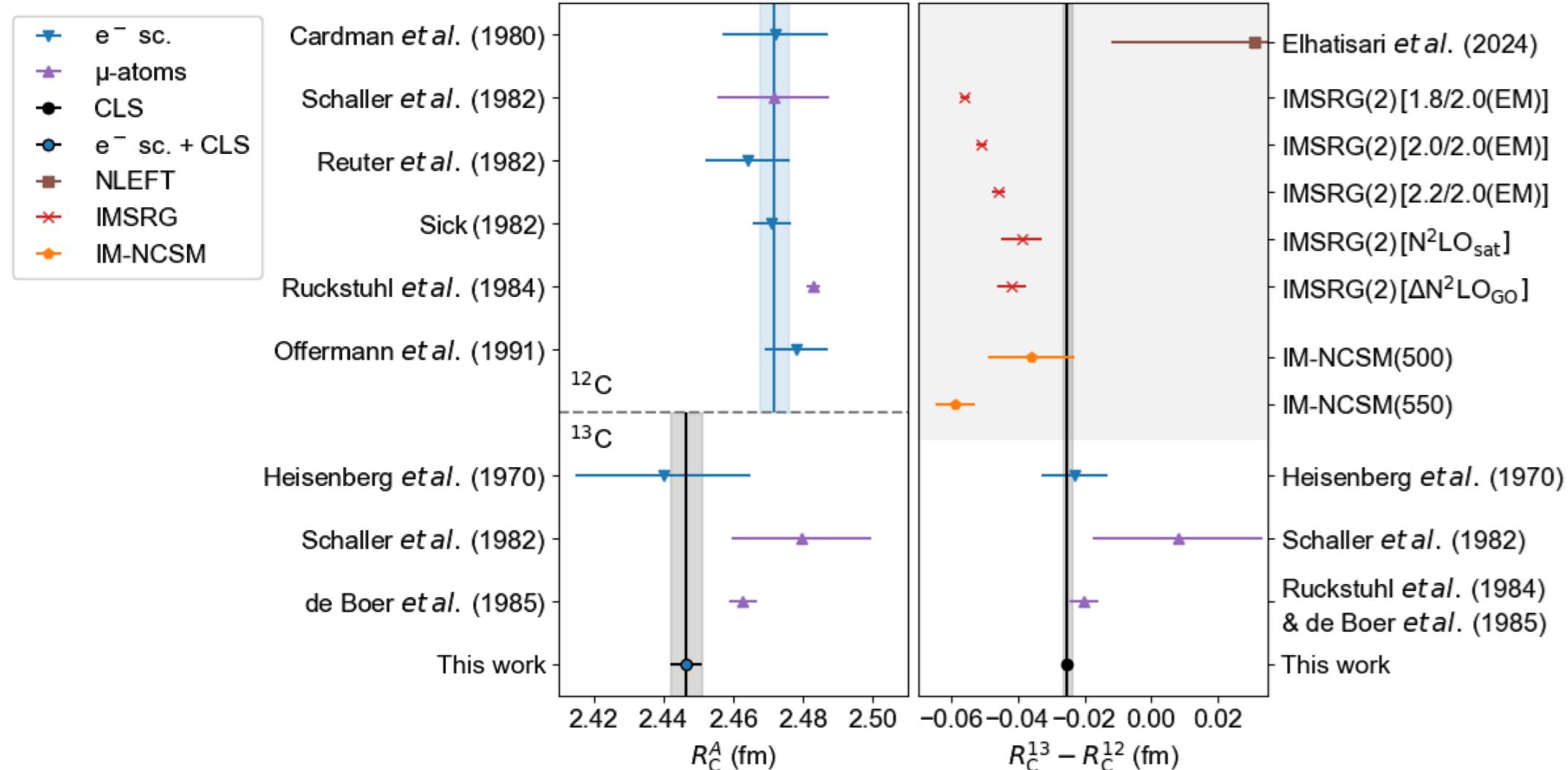


Spectrum of ^{13}C

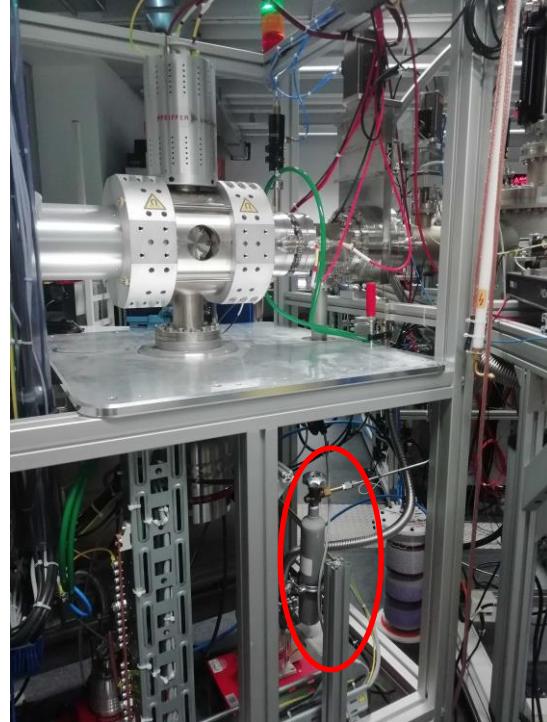


Mixed HFS calculated using matrix elements from
Johnson et al., Phys. Rev. A 55, 2728 (1997)

The Nuclear Charge Radius of ^{13}C

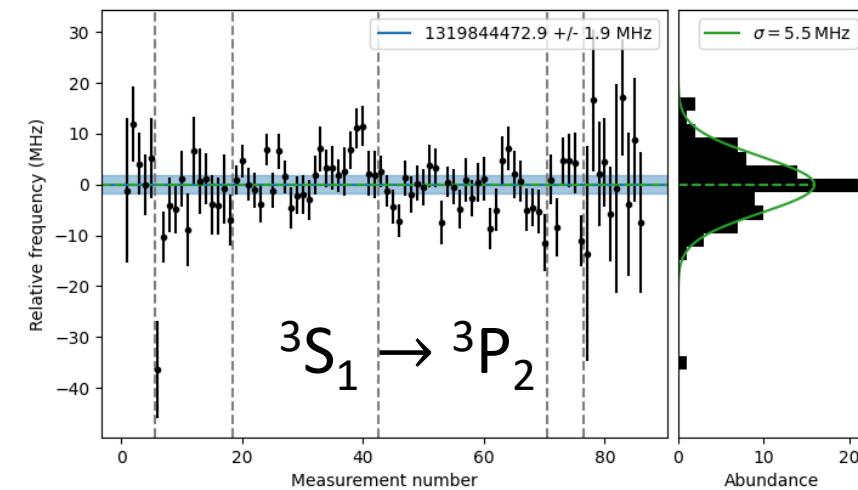
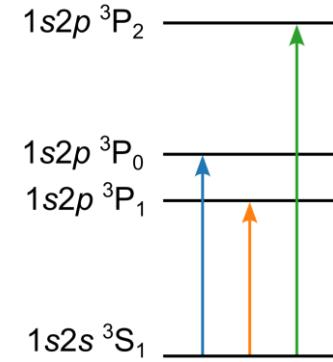
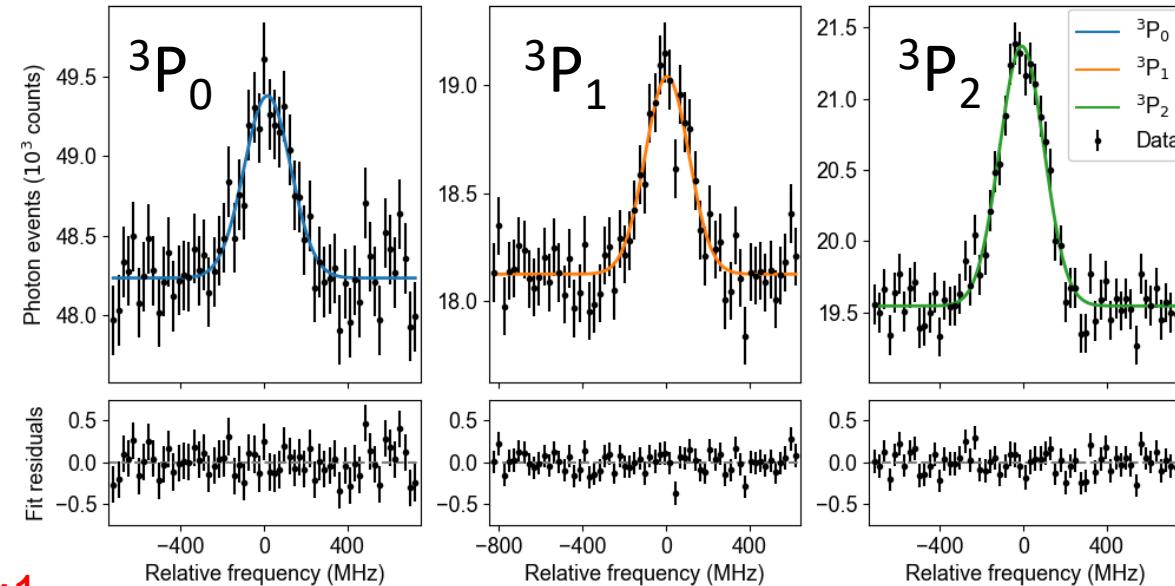


Measurements of ^{14}C



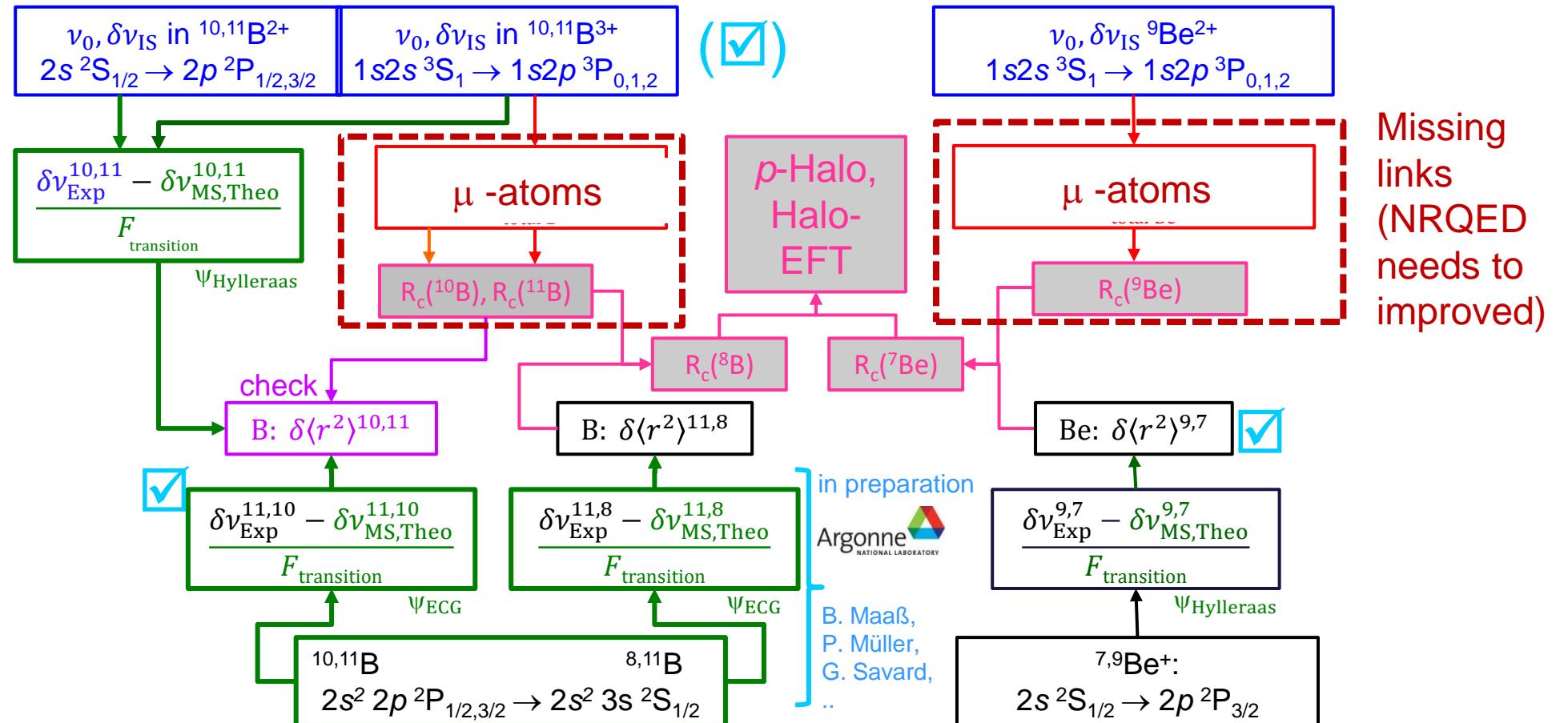
$^{14}\text{CO}_2 : ^{12}\text{CO}_2 = 1:1$
 1.4 l, 50 mbar,
 2 mmol ^{14}C , 50 mCi

- Determination of the $^3\text{S}_1 \rightarrow ^3\text{P}_J$ transition frequencies in $^{14}\text{C}^{4+}$ on a 2-MHz precision level
- Extraction of the differential nuclear charge radius $\delta\langle r^2 \rangle^{12,14}$ from the isotope shifts
- Additional check of theory: Splitting Isotope Shift



Analysis
ongoing ...
stay tuned

Measurement of the Proton-Halo of ${}^8\text{B}$



Experimental data, multiply charged

Experimental data: neutral or singly charged

Conventional mass-shift calculations

Theory of He-like systems

Consistency Checks

Goal

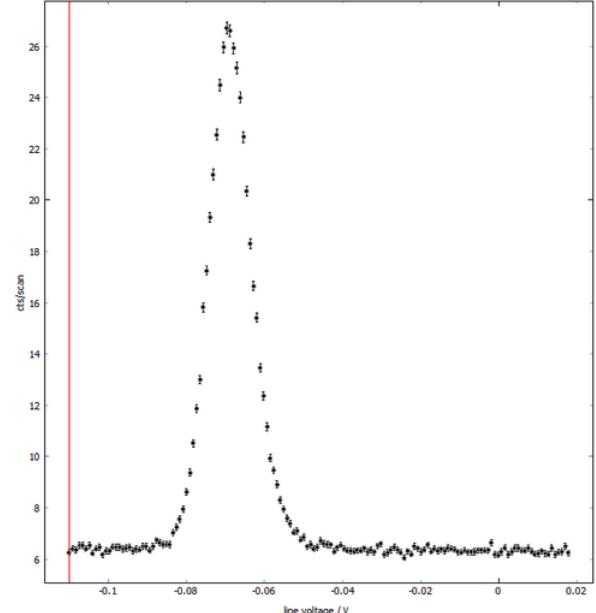
Outlook

Atomic structure theory (NR-QED calculations)

- Remaining uncertainty originating from **neglected higher order terms** (ma^{8+})
→ Measured fine-structure splitting in $^{12}\text{C}^{4+}$ will **benchmark new calculations**
- This will **improve** the extraction of α from fine-structure measurements in He & (hopefully) as well the all-optical nuclear charge radius determination
- For Boron a factor 3 in improvement would already be sufficient

He-like ions at COALA

- Measurement of $^{14}\text{C}^{4+}$ already completed
→ TBP
- $^{10,11}\text{B}^{3+}$ ongoing
@ 280 nm
- $^{10,11}\text{B}^{2+,0}$
- @ 206 nm, 250 nm until June 2025
- $^9\text{Be}^{2+}$ in 2025
→ Feeding of Be^+ into EBIS needs further development



Far-Reach: Measurements on Short-Lived Isotopes (LOI INTC-I-265)



Physics cases:

- ${}^7\text{Be}^{2+}$ (QP moment & Zemach radius)
→ influence in ${}^7\text{Be}(p, \gamma){}^8\text{B}$ reaction rate
- ${}^8\text{B}^{2+,3+}$ (QP moment & CR)
→ consistency check or even improvement to Argonne experiment
- ${}^{12,13,14}\text{B}^{2+,3+}$ (CR & moments)
→ Radii across N=8 shell closure, important benchmarks for nuclear ab-initio calc.
- ${}^{15,16}\text{C}^{4+}$ (CR & moments)
→ similar to B

	$\tau(2 {}^3S_1)$	$\lambda(2 {}^3S \rightarrow 2 {}^3P)$
He	2.2 h	1082 nm
Li^+	50 s	548 nm
Be^{2+}	1.8 s	372 nm
B^{3+}	150 ms	282 nm
C^{4+}	21 ms	227 nm
N^{5+}	3.9 ms	190 nm

But first: Consider and find the most efficient way to produce the ions and populate the 3S_1 state → LOI

Thank you!

