



中国科学技术大学
University of Science and Technology of China



Simulation study of the grassy ELM cycles within Edge Plasma Coupling Simulation framework

Minyou YE¹, Shifeng MAO¹, Tianyuan LIU¹, Taihao HUANG¹
Tianyang XIA², Qingquan YANG², Xin LIN², Guosheng XU²

¹*University of Science and Technology of China*

²*Institute of Plasma Physics, CAS*

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**Fifth IAEA Technical Meeting
on Divertor Concepts**



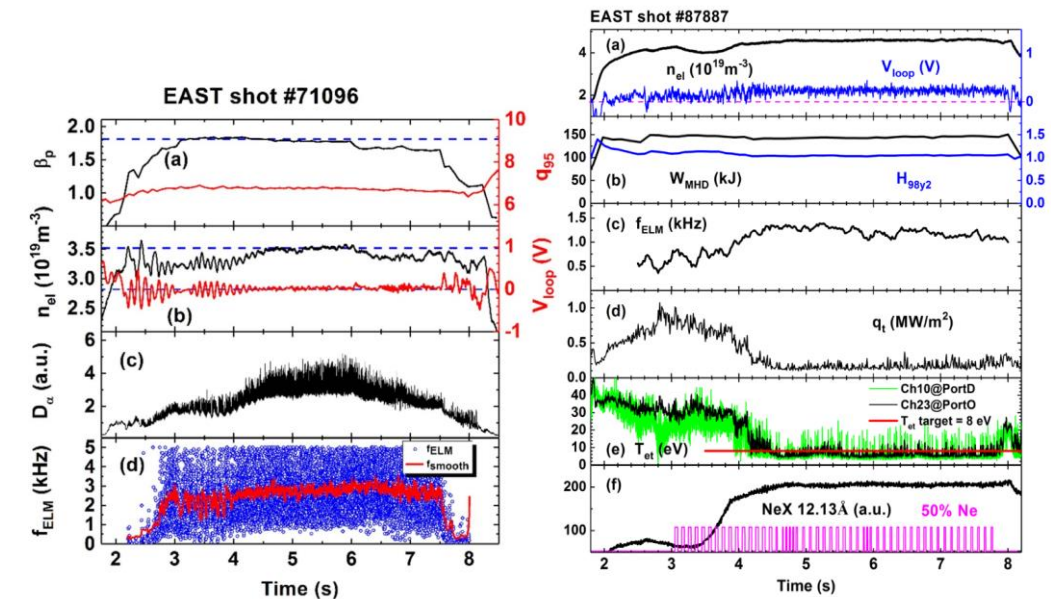
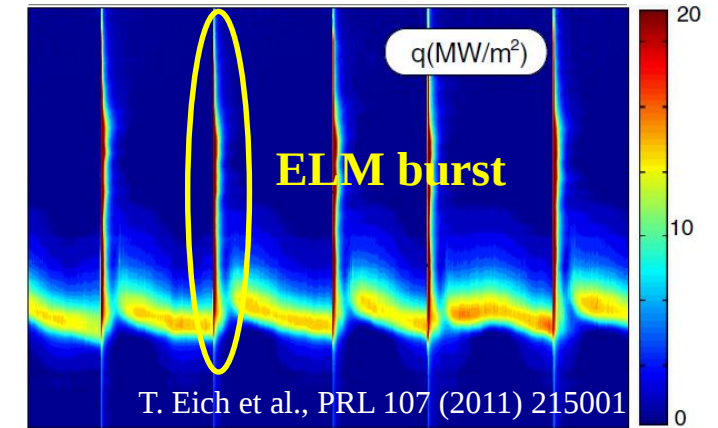
Outline



- **Motivation**
- **Edge plasma coupling simulation framework (EPCS)**
- **Time-dependent simulation for grassy ELM cycles**
- **Impurity seeding: simultaneous detachment/ELM mitigation**
- **Conclusion**

Motivation

- Divertor is subjected to **huge heat load**, including both the **transient heat load due to ELMs** and **steady-state heat load** in between ELMs
- For fusion reactor, steady-state operation requires
 - High confinement plasma – fusion gain
 - Small/no ELM – control the transient heat load
 - Detachment – reduce the (steady-state) heat load
- On EAST tokamak (also AUG, JET, DIII-D...)
 - High-performance grassy ELM regime accessed
 - Detachment and small ELM simultaneously achieved by impurity seeding

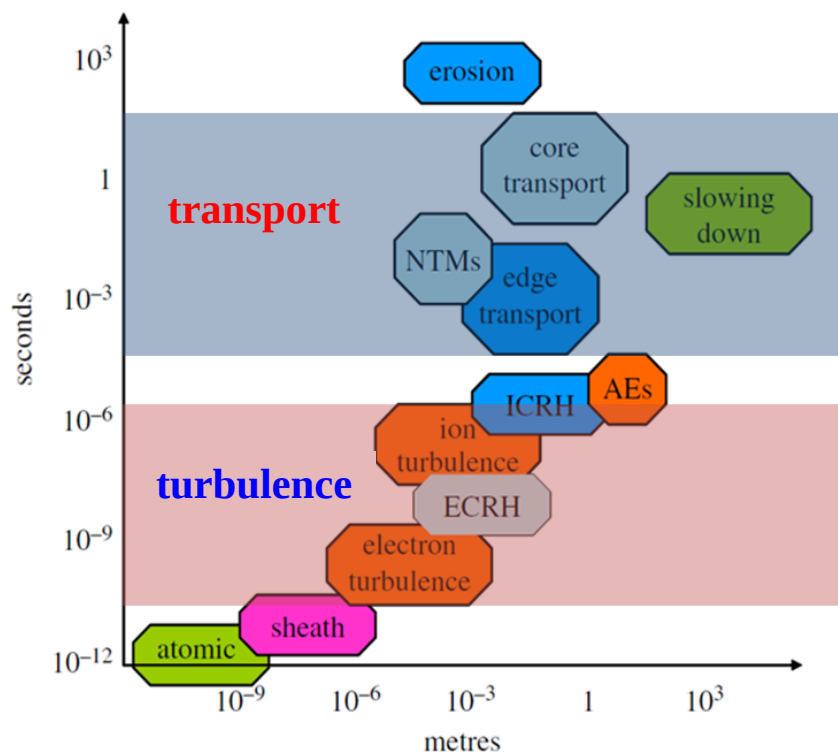


Q.Q. Yang et al., NF (2020)

G.S. Xu, et al., NF (2020)

Motivation

- To investigate the **physical mechanism**, **numerical simulation** is necessary
 - Also improve the ability of **predicting the edge plasma behavior** for future devices
- However, numerical simulation of **edge plasma evolution over multi-ELM cycles** is difficult due to **large gap between turbulence (10^{-7} s) and transport (10^{-2} s) time scales**



Transport codes	SOLPS-ITER 、EMC3-EIRENE、SOLEEDGE2D-EIRENE
Turbulence codes	BOUT++ 、JOEREK、GBS、SOLEEDGE3X、GRILLIX

Motivation

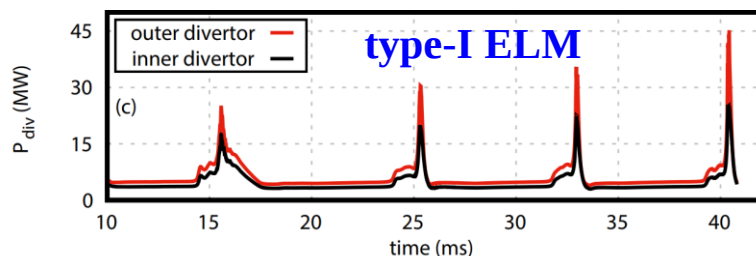
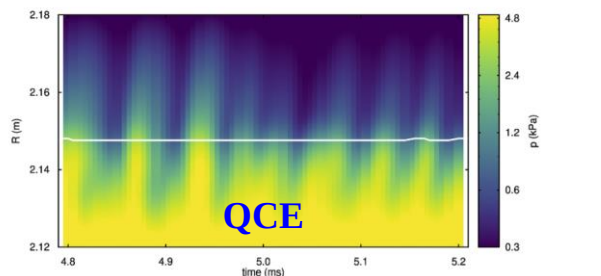


computational complexity

Turbulence simulation
in a long-time scale

Need artificial source

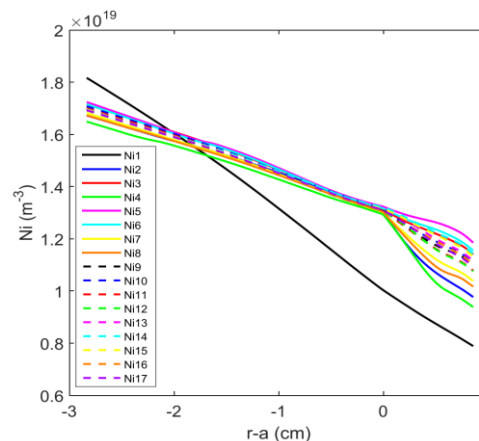
A Cathey, et al. PPCF (2022), NF (2020) JOREK



turbulence/transport
coupling simulation

Verified for steady-state simulation

T. D. Rognlien, et al., JNM (2005) BOUT-UEDGE
D. R. Zhang et al., NF (2020) BOUT++-SOLPS



Develop the multi-scale coupling
simulation framework

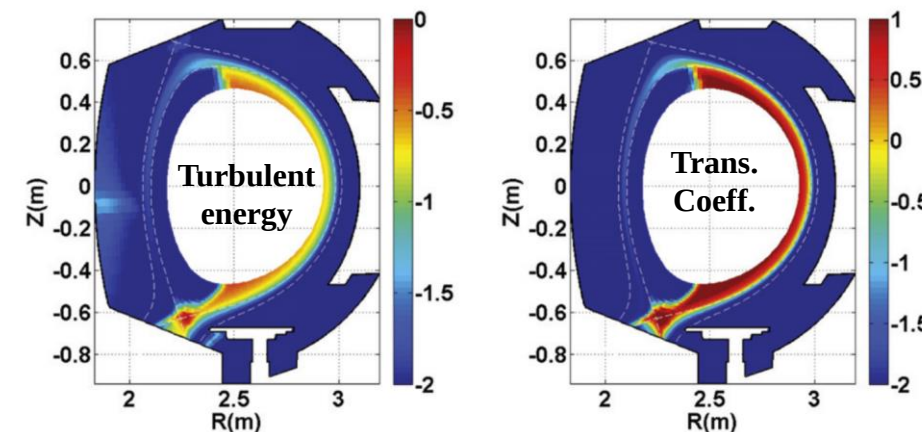
- ✓ Automatic
- ✓ High accuracy
- ✓ High efficiency

Include turbulent trans.
coeff. in transport code

Under development

S. Baschetti, et al., NF (2021) SolEdge2D-EIRENE
W. Dekeyser, et al., CPP (2022) SOLPS-ITER

Reynolds Averaged Navier–Stokes (RANS)



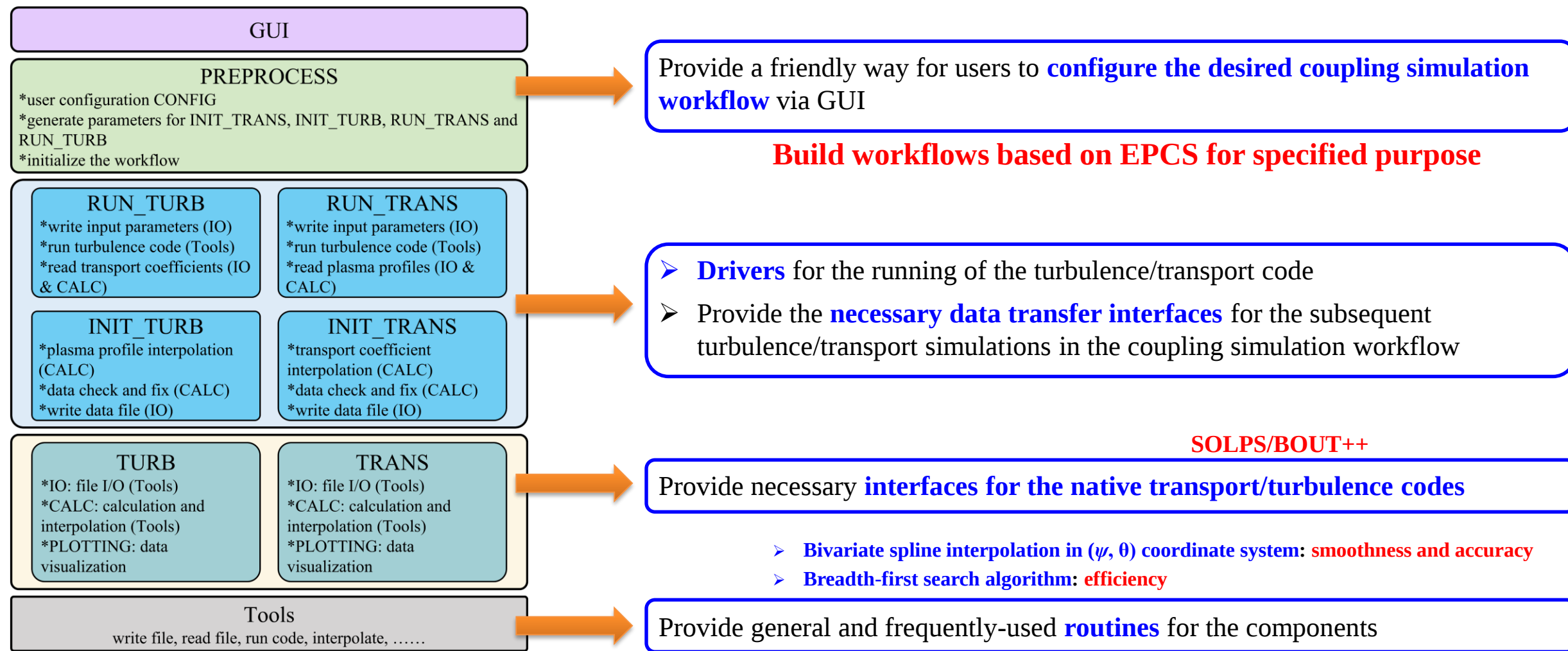
Time-dependent simulation
of edge plasma evolution
over multi-ELM cycles

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- Conclusion

■ Edge plasma coupling simulation framework is developed based on Python



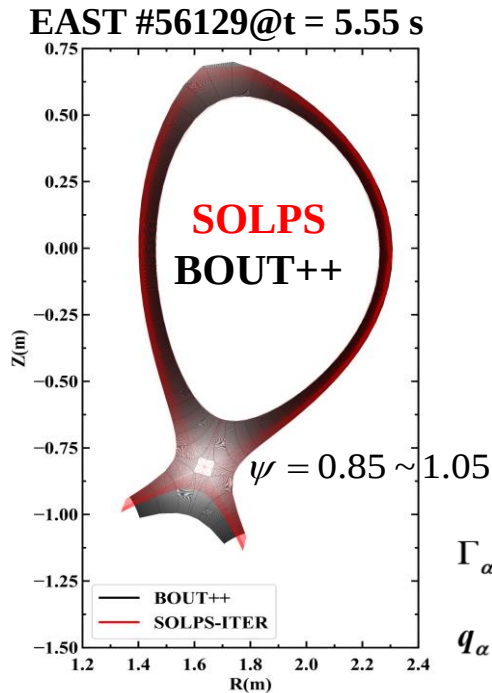
Steady-state coupling simulation workflow



- Initial profiles generated by SOLPS with assumed trans. coeff.
- Iteration between turbulence/transport codes until converges
- Test based on ELM-free stage during EAST H-mode discharge
- Speeding up the coupling simulation
 - Identify quasi-steady-state of turbulence simulation based on **coefficient of variation**

$$D_{i0} = 0.5 \text{ m}^2/\text{s}$$

$$\chi_{i0} = \chi_{e0} = 1.0 \text{ m}^2/\text{s}$$



SOLPS-ITER (36×64)

- Include currents and drifts
- CEI: $n_i = 2.2 \times 10^{19} \text{ m}^{-3}$, $T_i/T_e = 450/320 \text{ eV}$
- Evolving n_i , T_i , T_e , $J_{\parallel}$ and ϕ

BOUT++ (200×64×64)

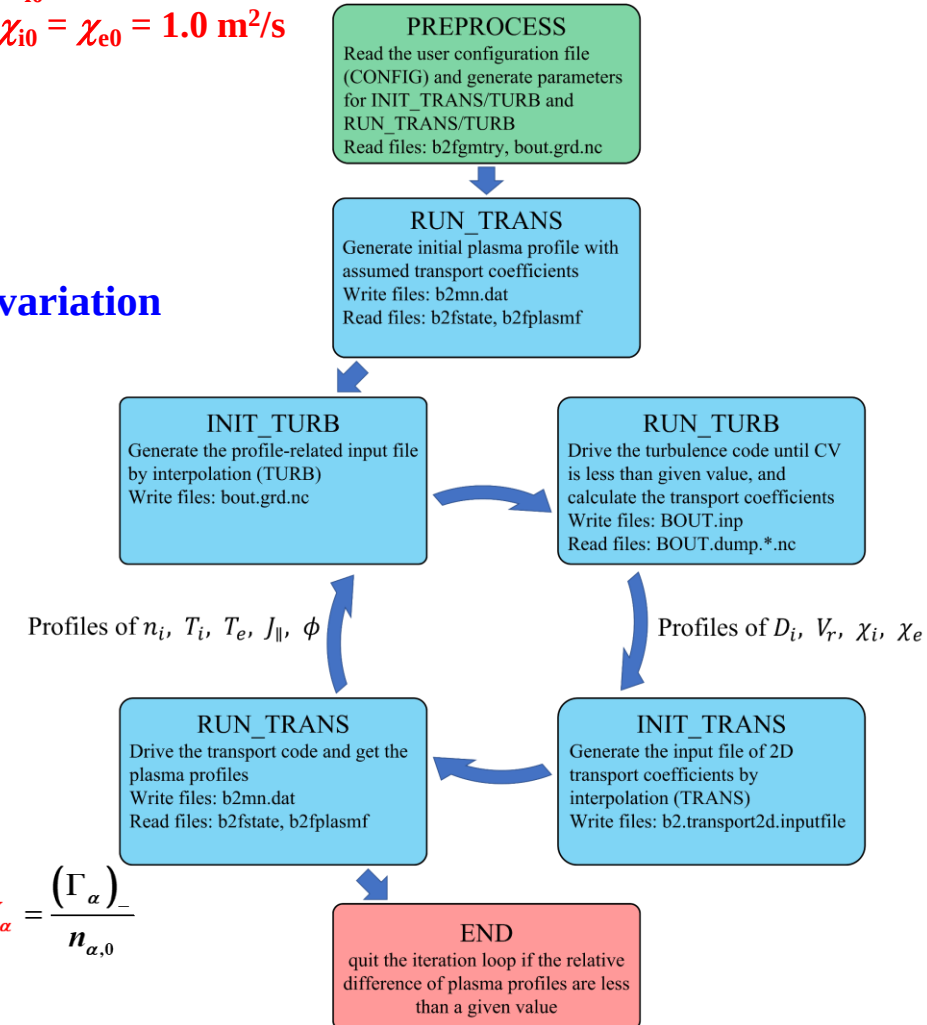
- Six-field two-fluid model
- $n = 0$ components fixed
- Provide transport coefficients D_i , V_i and χ_i/χ_e

$$\Gamma_{\alpha} = \langle n_{\alpha} V_{E,1} \rangle + \langle n_{\alpha} V_{\parallel, \alpha} b_1 \rangle$$

$$q_{\alpha} = \frac{5}{2} \langle n_{\alpha} T_{\alpha,1} V_{E,1} \rangle + \frac{5}{2} \langle n_{\alpha} V_{\parallel, \alpha} T_{\alpha,1} b_1 \rangle - \langle \kappa_{\parallel, \alpha} \nabla_{\parallel} T_{\alpha} b_1 \rangle$$

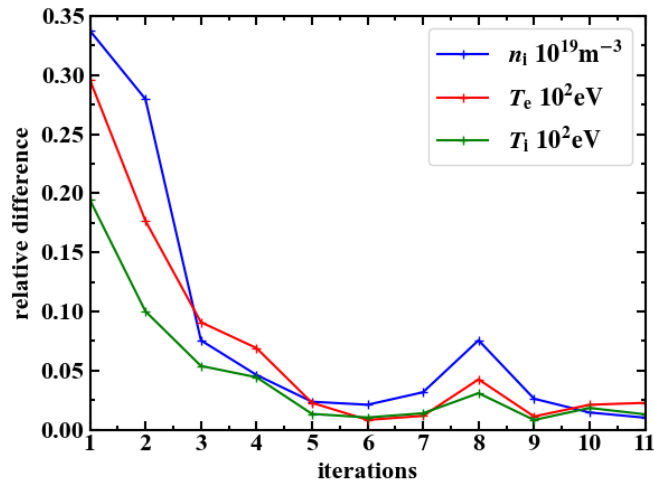
$$D_{\alpha} = -\frac{(\Gamma_{\alpha})_+}{\partial_r n_{\alpha,0}} \quad V_{\alpha} = \frac{(\Gamma_{\alpha})_-}{n_{\alpha,0}}$$

$$\chi_{\alpha} = -\frac{q_{\alpha}}{n_{\alpha,0} \partial_r T_{\alpha,0}}$$



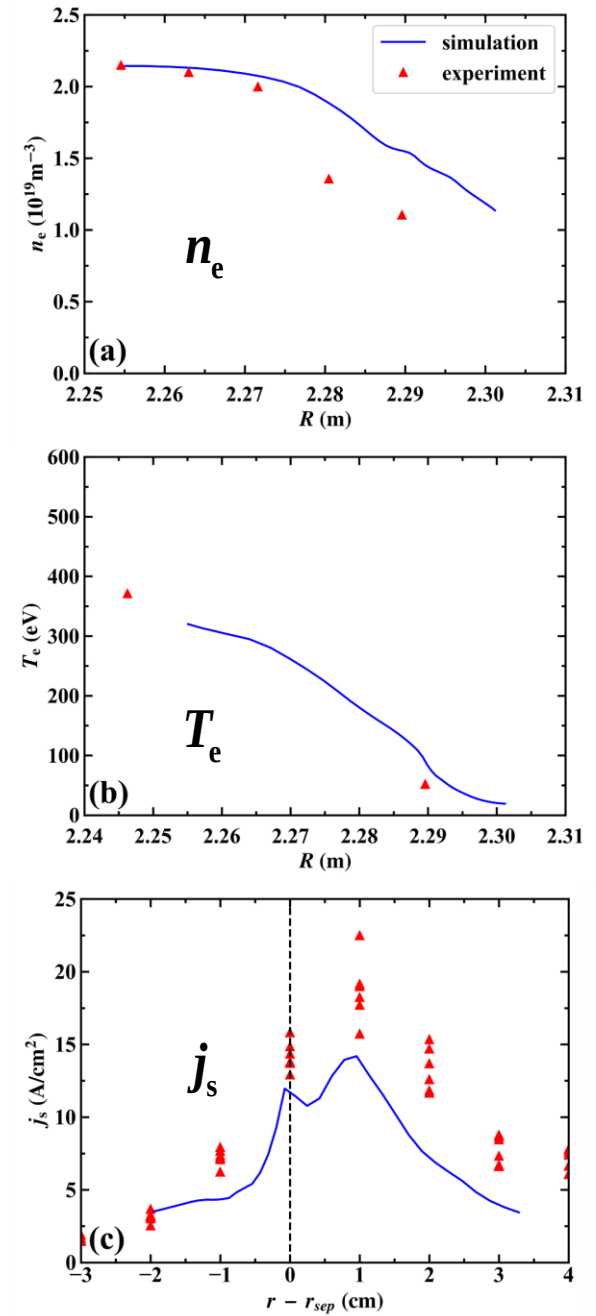
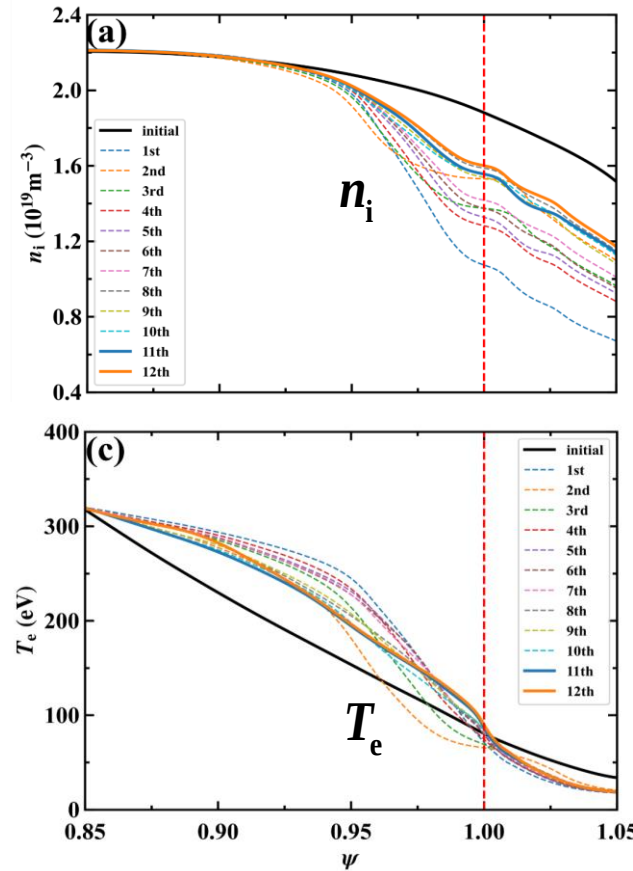
Steady-state coupling simulation workflow

- As expected, plasma profiles converge along with iterations
- Profiles at OMP and target in good agreement with experiment



Relative differences of plasma profiles
between m and $m-1$ iteration

$$\text{diff}(PP^m) \equiv \frac{\sum_{i=0}^{N_x-1} \sum_{j=0}^{N_y-1} |PP_{i,j}^m - PP_{i,j}^{m-1}|}{\sum_{i=0}^{N_x-1} \sum_{j=0}^{N_y-1} |PP_{i,j}^m|}$$



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Time-dependent coupling simulation workflow

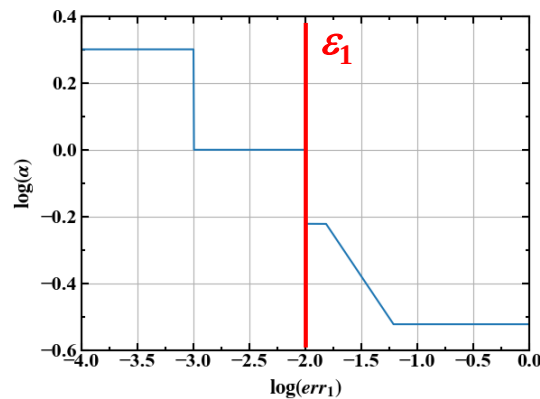
■ Loop1: inner iteration

- ✓ Ensure the **self-consistence** between the evolution of plasma profiles and the turbulence transport flux based on the **predictor-corrector method**

■ Loop2: adaptive change of time step

- ✓ **ELM burst**: decrease time step size to ensure accuracy
- ✓ **Recovery**: increase time step size to improve efficiency

change ratio of the time step size



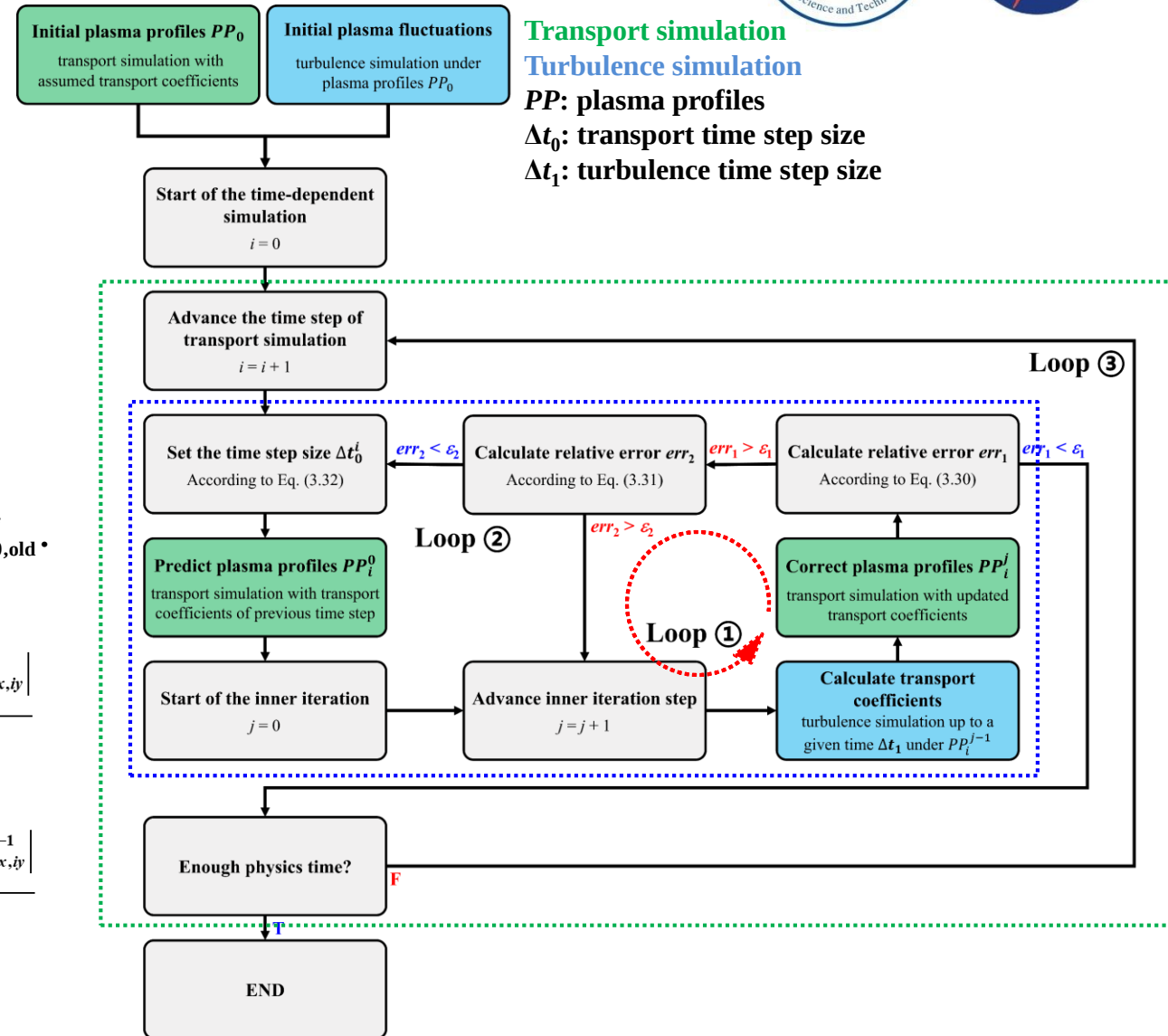
$$\Delta t_{0,\text{new}}^i = \left(\frac{\varepsilon_1}{err_1} \right)^{\frac{1}{k+1}} \Delta t_{0,\text{old}}^i = \alpha(err_1) \Delta t_{0,\text{old}}^i.$$

Relative error

$$err_1(PP_i^j) = \frac{\sum_{ix=0}^{nx-1} \sum_{iy=0}^{ny-1} |PP_{i,ix,iy}^j - PP_{i,ix,iy}^0|}{\sum_{ix=0}^{nx-1} \sum_{iy=0}^{ny-1} PP_{i,ix,iy}^j}$$

$$err_2(PP_i^j) = \frac{\sum_{ix=0}^{nx-1} \sum_{iy=0}^{ny-1} |PP_{i,ix,iy}^j - PP_{i,ix,iy}^{j-1}|}{\sum_{ix=0}^{nx-1} \sum_{iy=0}^{ny-1} PP_{i,ix,iy}^j}$$

■ Loop3: advance physics time step



Simulation setup



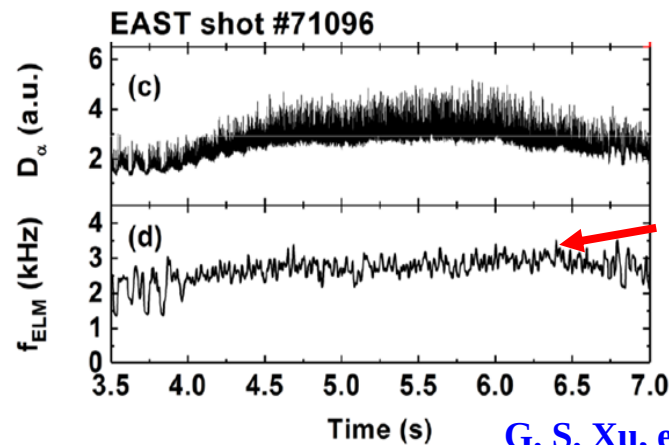
■ Based on EAST grassy ELM experiment (#71096)

● SOLPS-ITER (36×64)

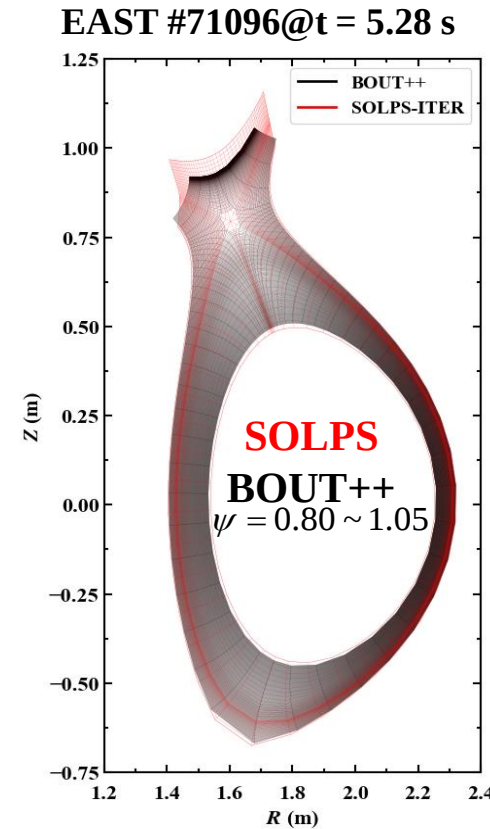
- CEI: $n_i = 1.5 \times 10^{19} \text{ m}^{-3}$, $P_{\text{SOL}} = 1.6 \text{ MW}$
- Include currents and drifts, time-dependent
- Δt_0 : adaptive ($\Delta t_{\text{SOLPS}} = 1 \times 10^{-6} \text{ s}$)
- Evolving n_i , T_i , T_e , $J_{\parallel}$ and ϕ

● BOUT++ (200×64×64)

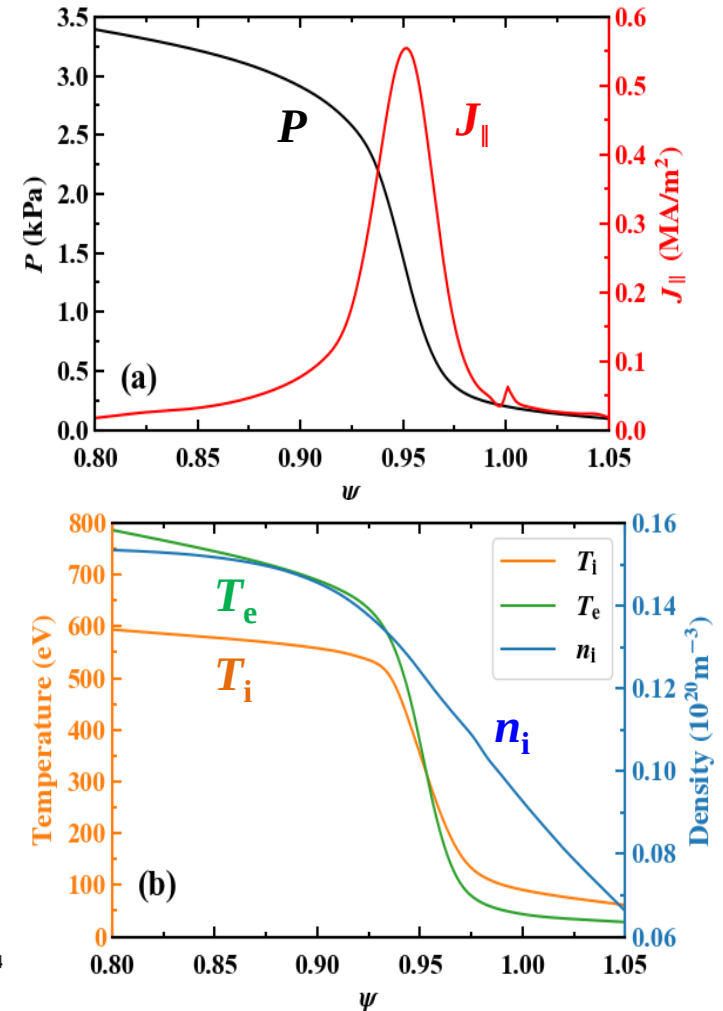
- Six-field two-fluid model, $n = 0$ components fixed
- $\Delta t_1 = 20 \tau_A$ ($\Delta t_{\text{BOUT++}} = 1 \tau_A$)
- Provide transport coefficients D_i , V_i and χ_i/χ_e



G. S. Xu, et al., PRL (2019)

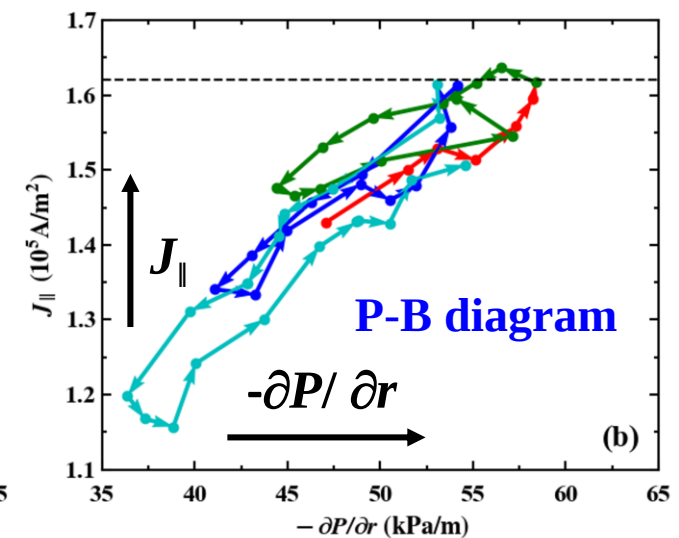
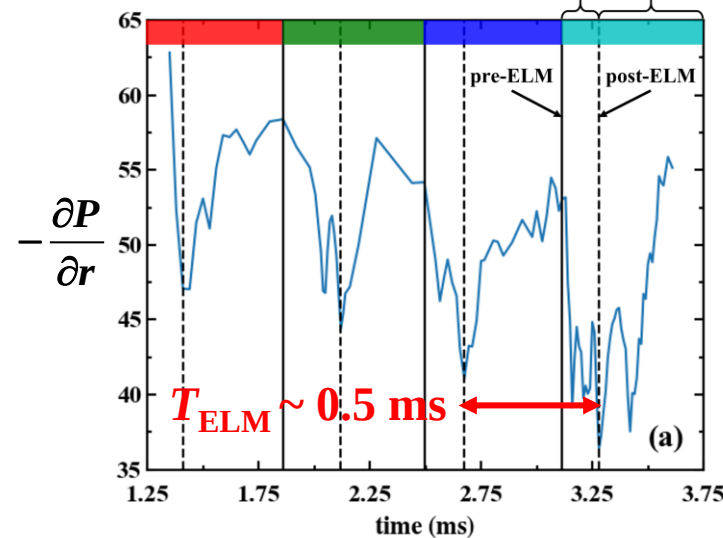
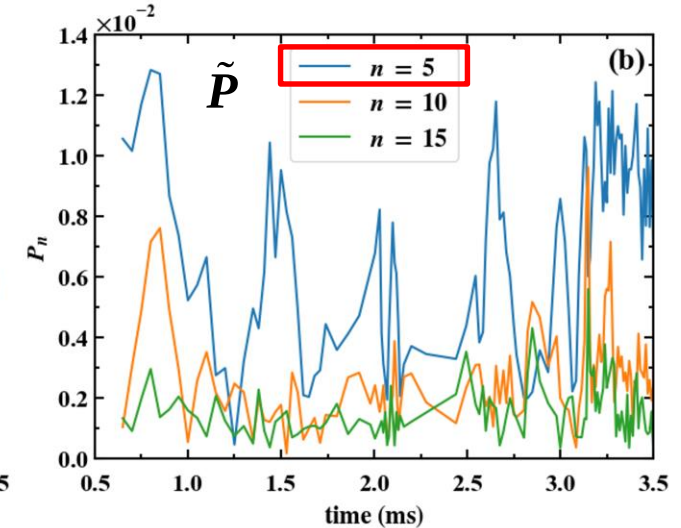
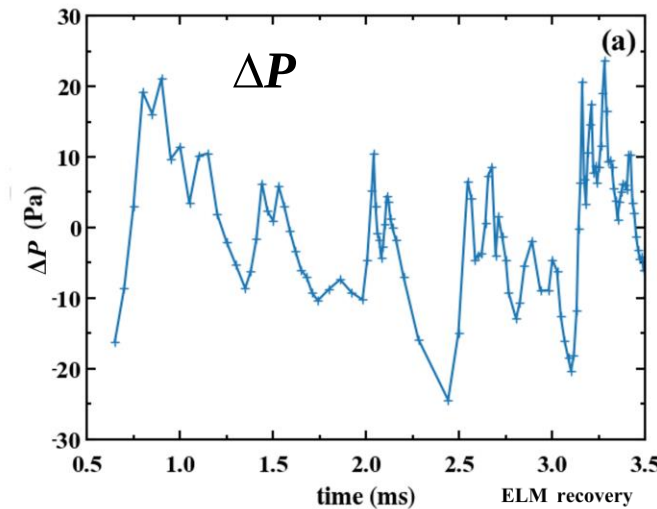
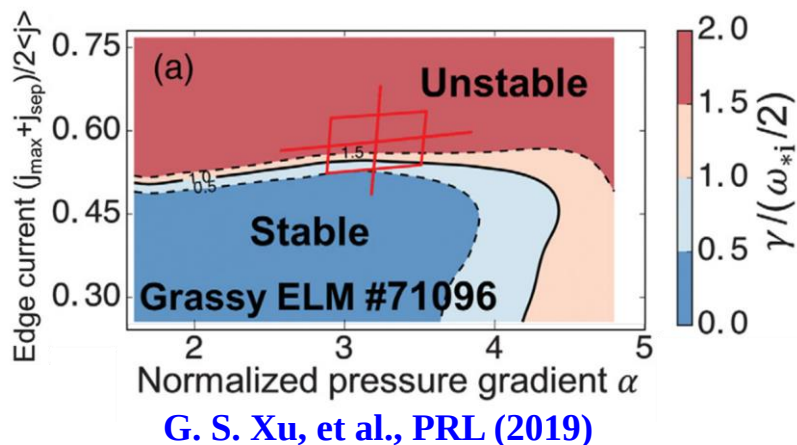


Initial profiles



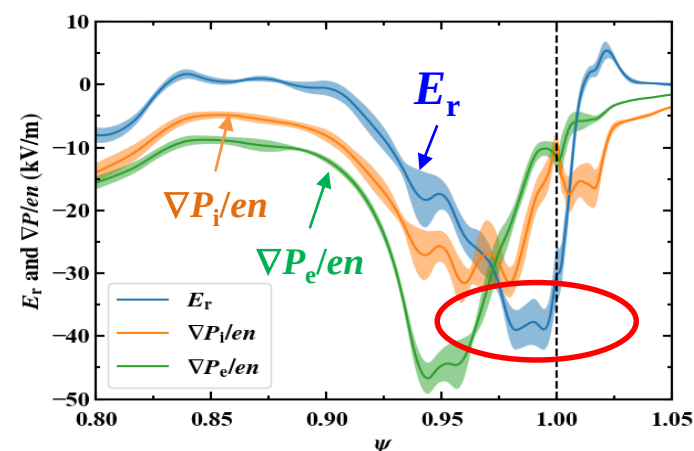
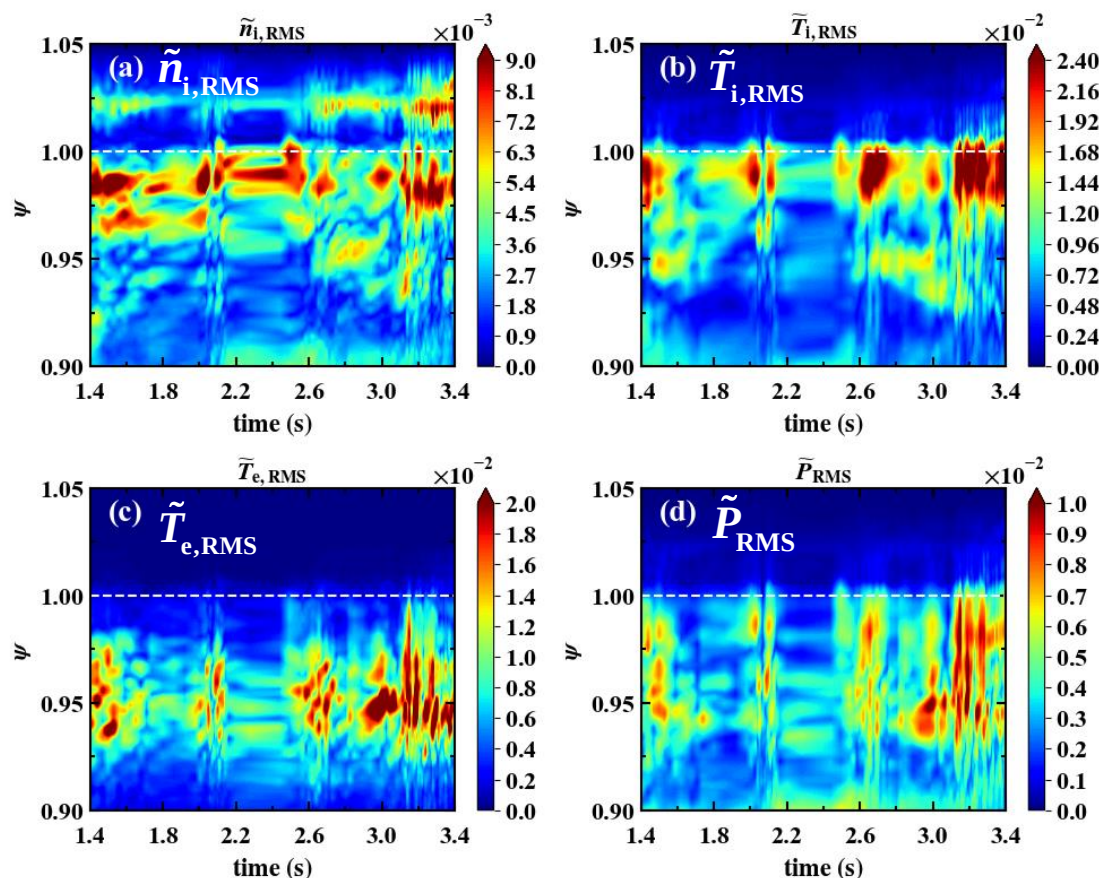
ELM cycles

- Quasi-periodical rise and fall of pressure appears at **pedestal foot** ($\psi \approx 0.98 \sim 1.00$)
- **ELM frequency** ~ 2 kHz – consistent with experiment
- **Counter-clockwise trajectory** on the P-B diagram
 - Cross the **peeling boundary**
 - In agreement with the **linear simulation**

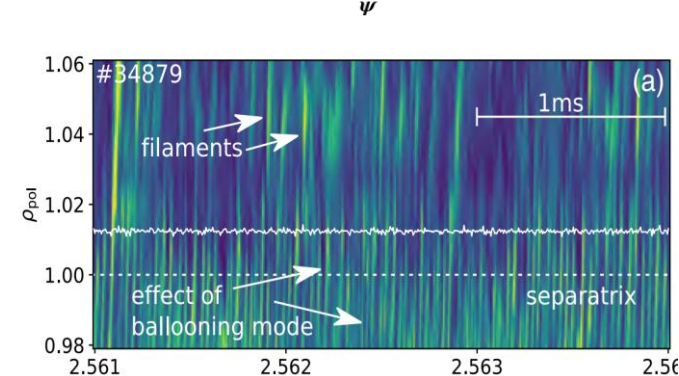


Radial distribution of fluctuations

- Density and ion temperature fluctuations locate at **pedestal foot** ($\psi \approx 0.99$)
- Electron temperature fluctuations locates at **gradient region** ($\psi \approx 0.95$)



Similar simulated E_r profile reported on FEC2025



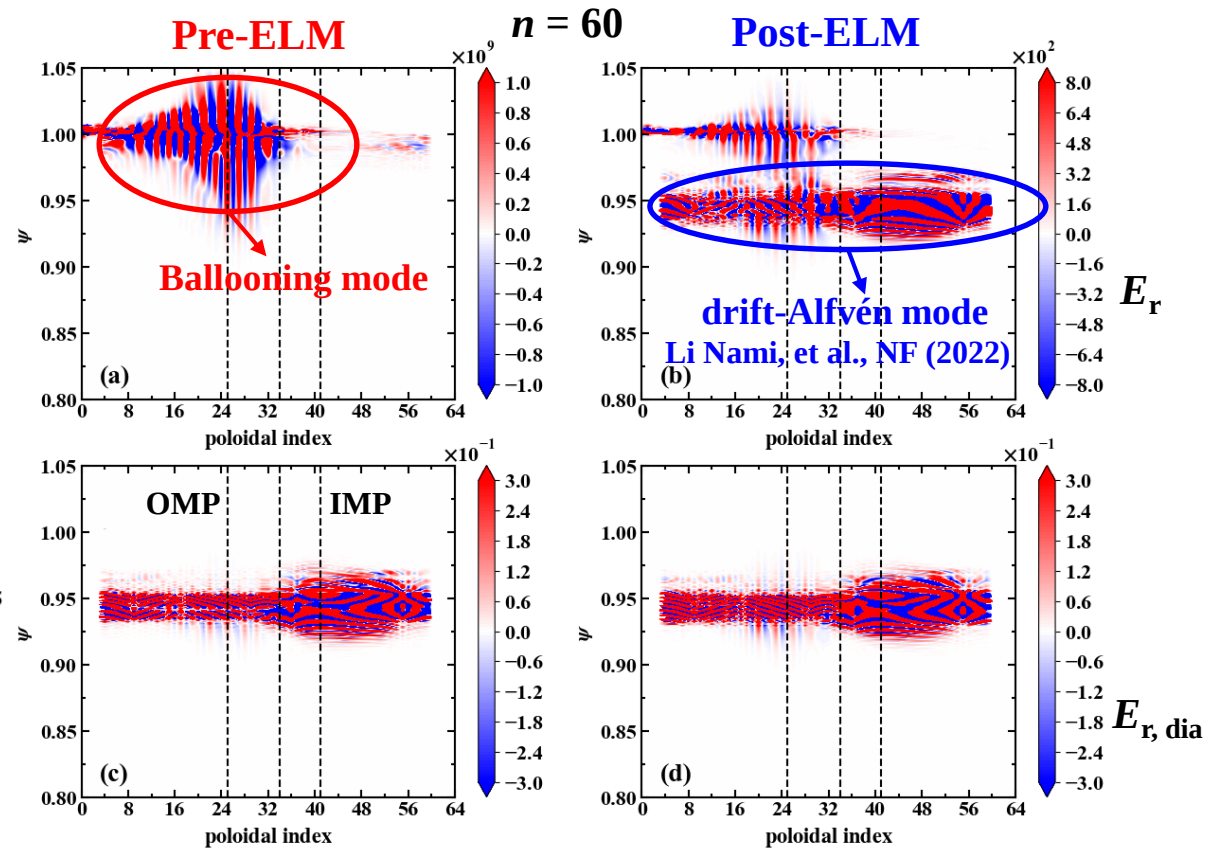
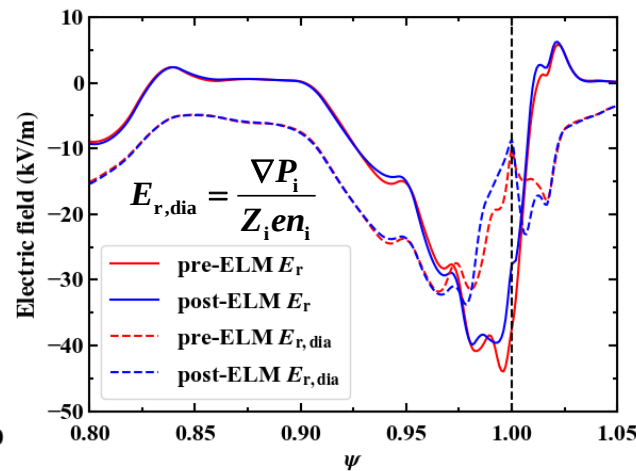
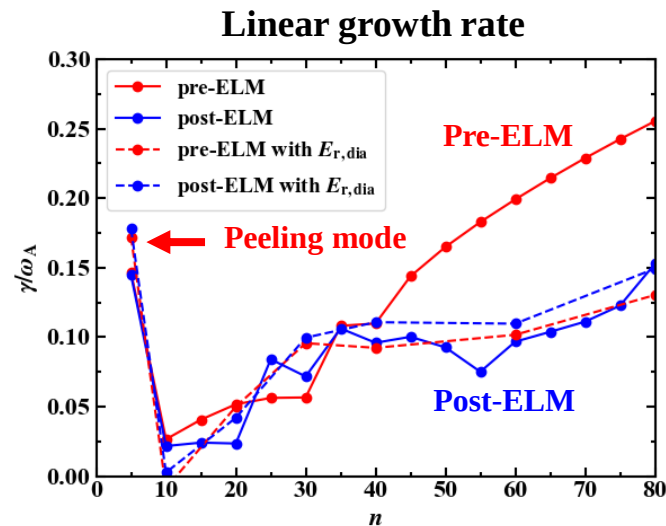
G. F. Harrer, et al., PRL (2022)

↑
QCE on AUG

Ballooning mode

Physical mechanism: linear growth rate

- Comparing linear growth rate under profiles **pre-** and **post-ELM**
 - **$n = 5$ peeling mode** most unstable (agree with the analysis in G. S. Xu, et al., PRL (2019))
 - Periodical change for **high n ballooning modes (50-80)** with **simulated E_r**



Physical mechanism: nonlinear interaction

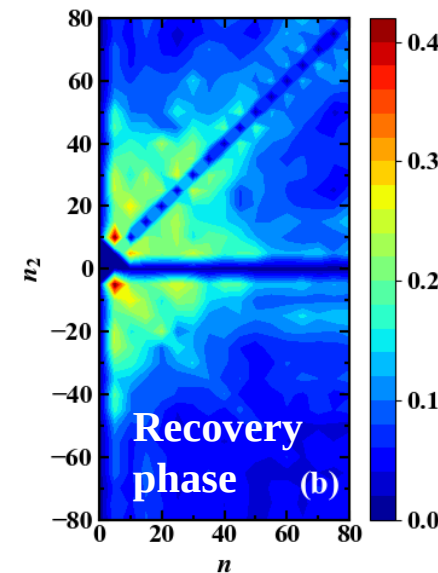
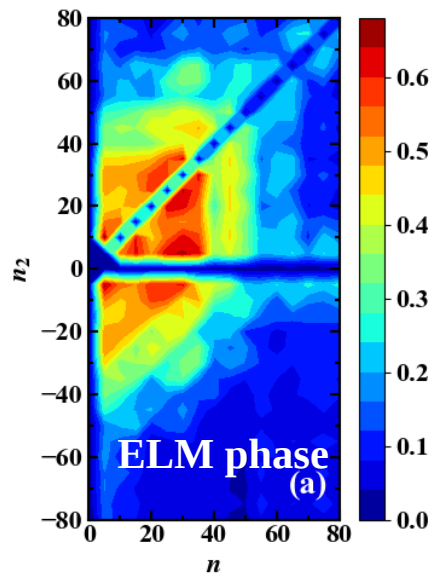
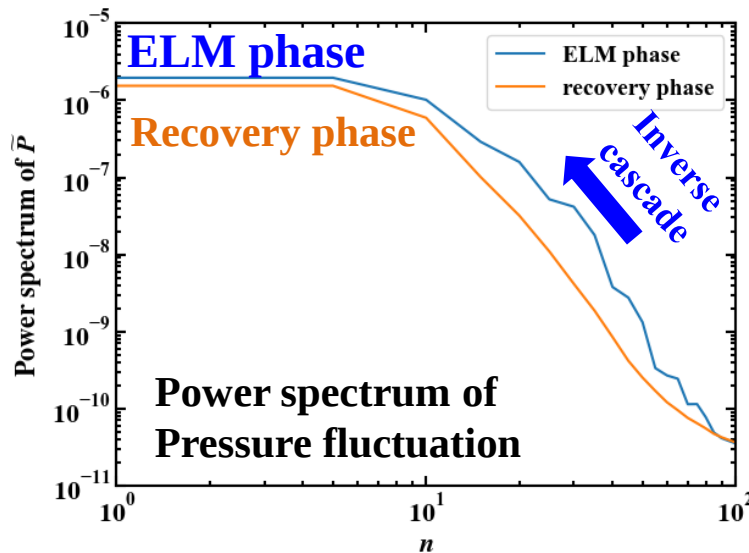
- However, while the linear growth rate almost unaffected, strength of **$n = 5$ mode periodically evolves**
- The strength of **nonlinear interaction between low and high n modes**:
 - Amplitude of low n mode increases in ELM phase
 - Strong interaction during ELM phase



Low n mode driven by nonlinear interaction: inverse cascade

$$\frac{\partial}{\partial t} P_n(t) = \underbrace{\gamma_n P_n(t)}_{\text{Linear growth}} + \sum_{\substack{n_1 \geq n_2, \\ n_1 + n_2 = n}} \underbrace{\Lambda_n(n_1, n_2) P_{n_1}(t) P_{n_2}(t)}_{\text{Nonlinear interaction}} + \text{dissipation},$$

Ch. Ritz, et al., Phys. Fluids (1989)
S. Chai, Y. Xu*, et al., PoP (2017)



bispectrum

$$\hat{b}_{XYZ}^2(n_1, n_2) = \frac{|\hat{B}_{XYZ}(n_1, n_2)|^2}{|X(n_1)Y(n_2)|^2 |Z(n_1 + n_2)|^2}$$

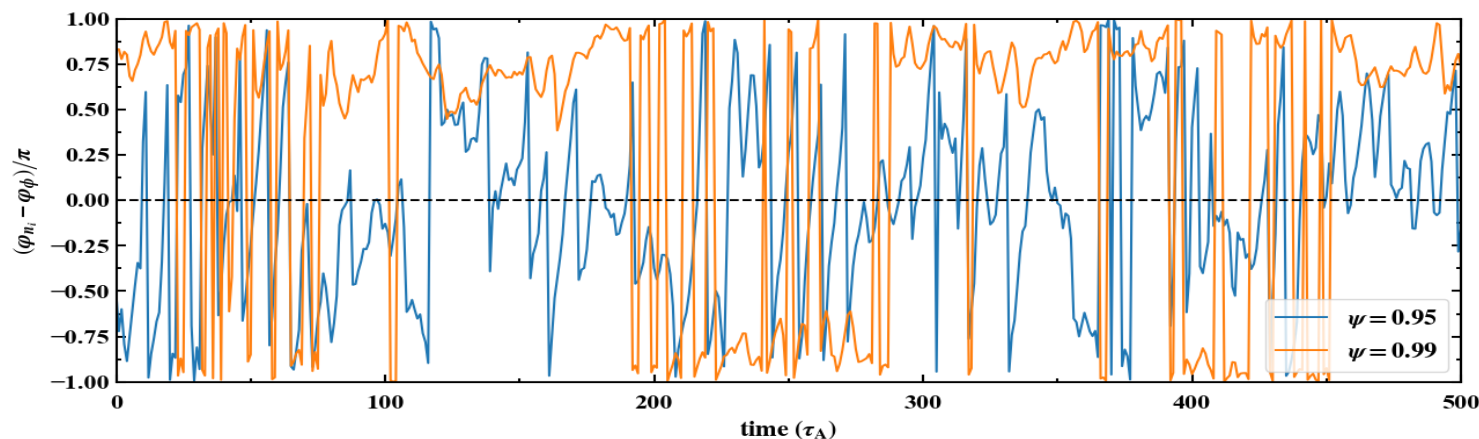
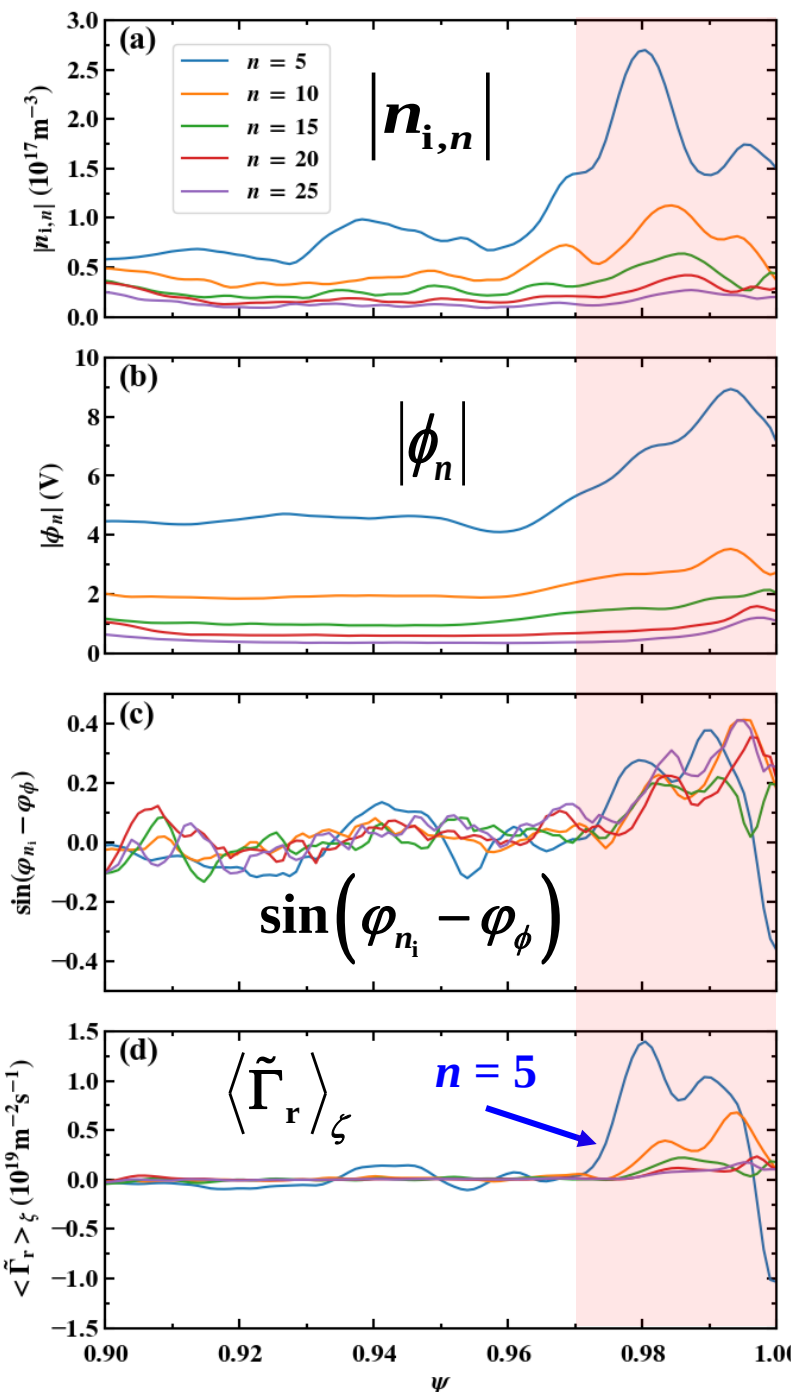
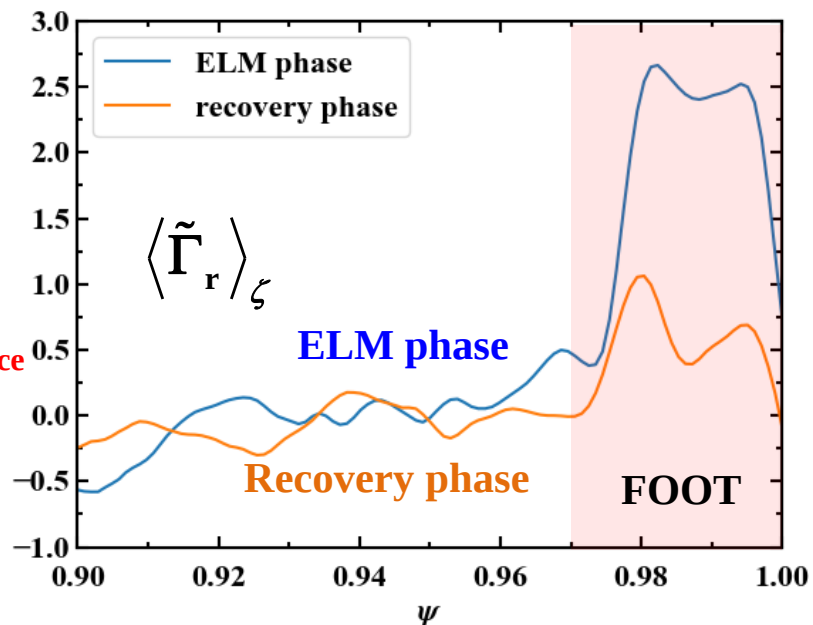
$$\hat{B}_{XYZ}(n_1, n_2) = X(n_1)Y(n_2)Z^*(n_1 + n_2)$$

Radial particle transport

- **Dominated by $n = 5$ mode**
- **Strong particle transport at pedestal foot: important for maintaining low density gradient**

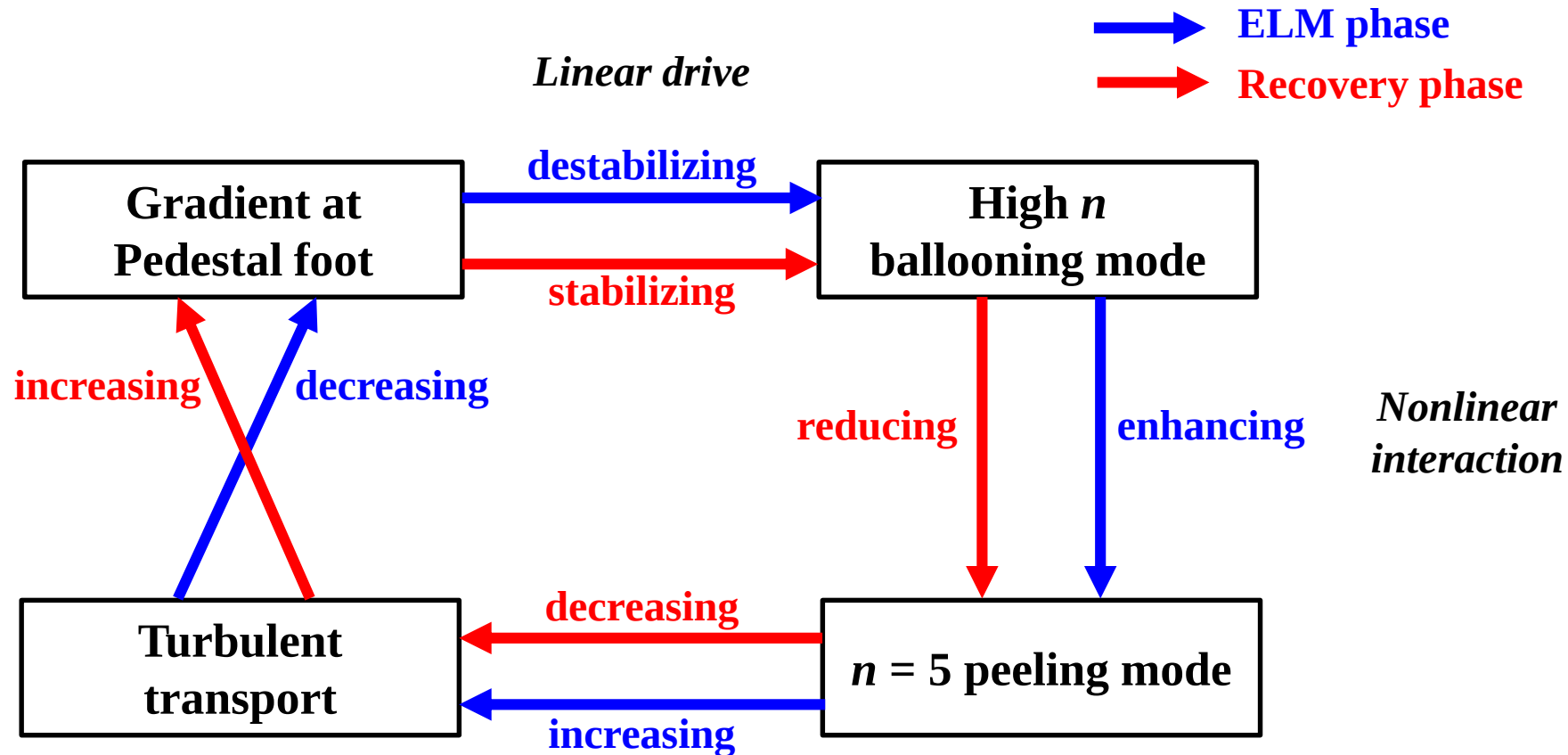
Radial particle flux density fluc. Potential fluc. Phase difference

$$\langle \tilde{\Gamma}_r \rangle_\zeta \approx \frac{2}{RB_p} \sum_{n>0} n |n_{i,n}| |\phi_n| \sin(\varphi_{n_i} - \varphi_\phi)$$



Weak $E \times B$ shear at pedestal foot facilitates turbulence transport

Physical mechanism: grassy ELM cycle



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Simulation setup



- Simultaneous **detachment** and **ELM mitigation** achieved in EAST experiment with **Ne injection**
- To **qualitatively** simulate the edge plasma profile evolution after impurity seeding

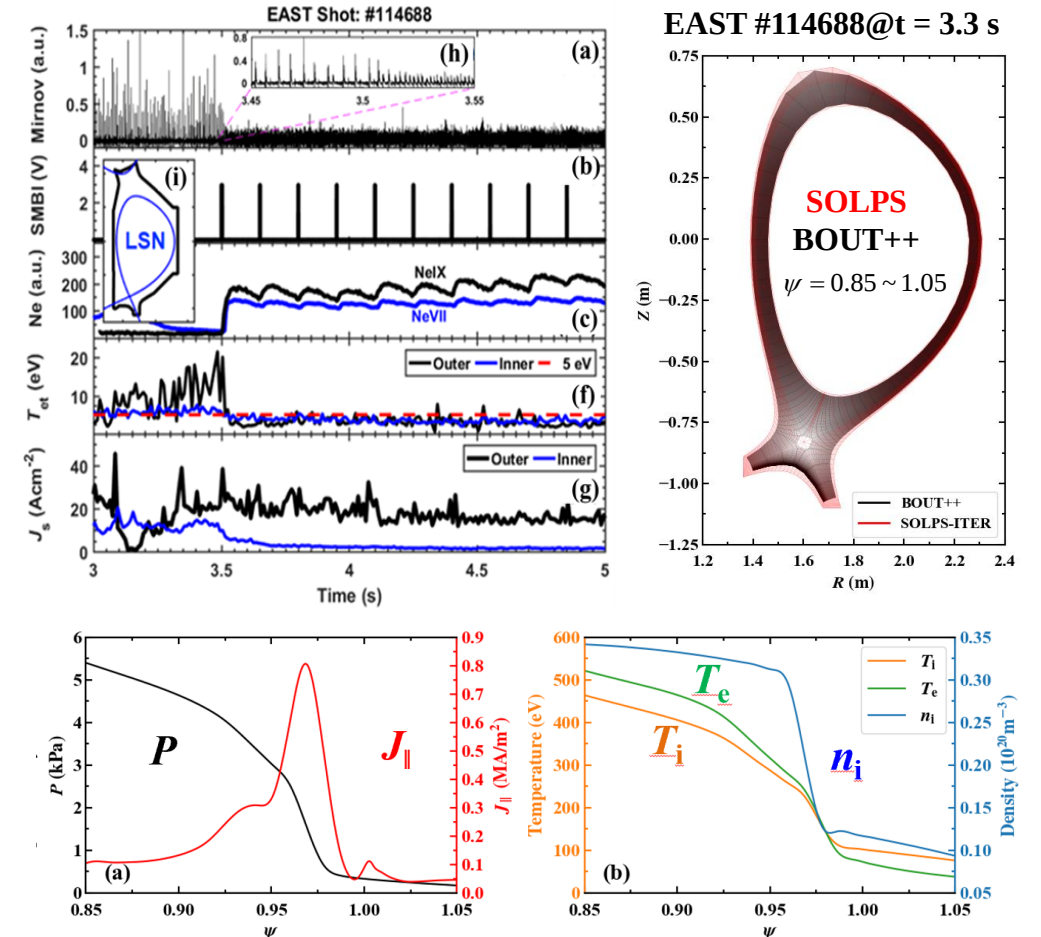
- **SOLPS-ITER (36×64)**

- CEI: $n_i = 3.4 \times 10^{19} \text{ m}^{-3}$, $P_{\text{SOL}} = 3 \text{ MW}$
- Include currents and drifts, time-dependent
- **Impurity seeding with fixed Ne^{8+} density at CEI**
- **Evolving n_i , T_i , T_e , $J_{\parallel}$ and ϕ**

- **BOUT++ (200×64×64)**

- Six-field two-fluid model, $n = 0$ components fixed
- **Including impurity effect via vorticity (only Ne^{8+})**
- **Transport coefficients D_i , V_i and χ_i/χ_e (same for impurities)**

$$\varpi = \frac{n_i m_i}{B_0} \left(\nabla_{\perp}^2 \phi + \frac{1}{Z_i e n_i} \nabla_{\perp}^2 P_i + \frac{1}{n_i} \nabla_{\perp} n_i \cdot \nabla_{\perp} \phi \right) + \frac{n_{\text{imp}} m_{\text{imp}}}{B_0} \left(\nabla_{\perp}^2 \phi + \frac{1}{Z_{\text{imp}} e n_{\text{imp}}} \nabla_{\perp}^2 P_{\text{imp}} + \frac{1}{n_{\text{imp}}} \nabla_{\perp} n_{\text{imp}} \cdot \nabla_{\perp} \phi \right)$$



Simulation results



■ Phase A: Large ELMs / attached

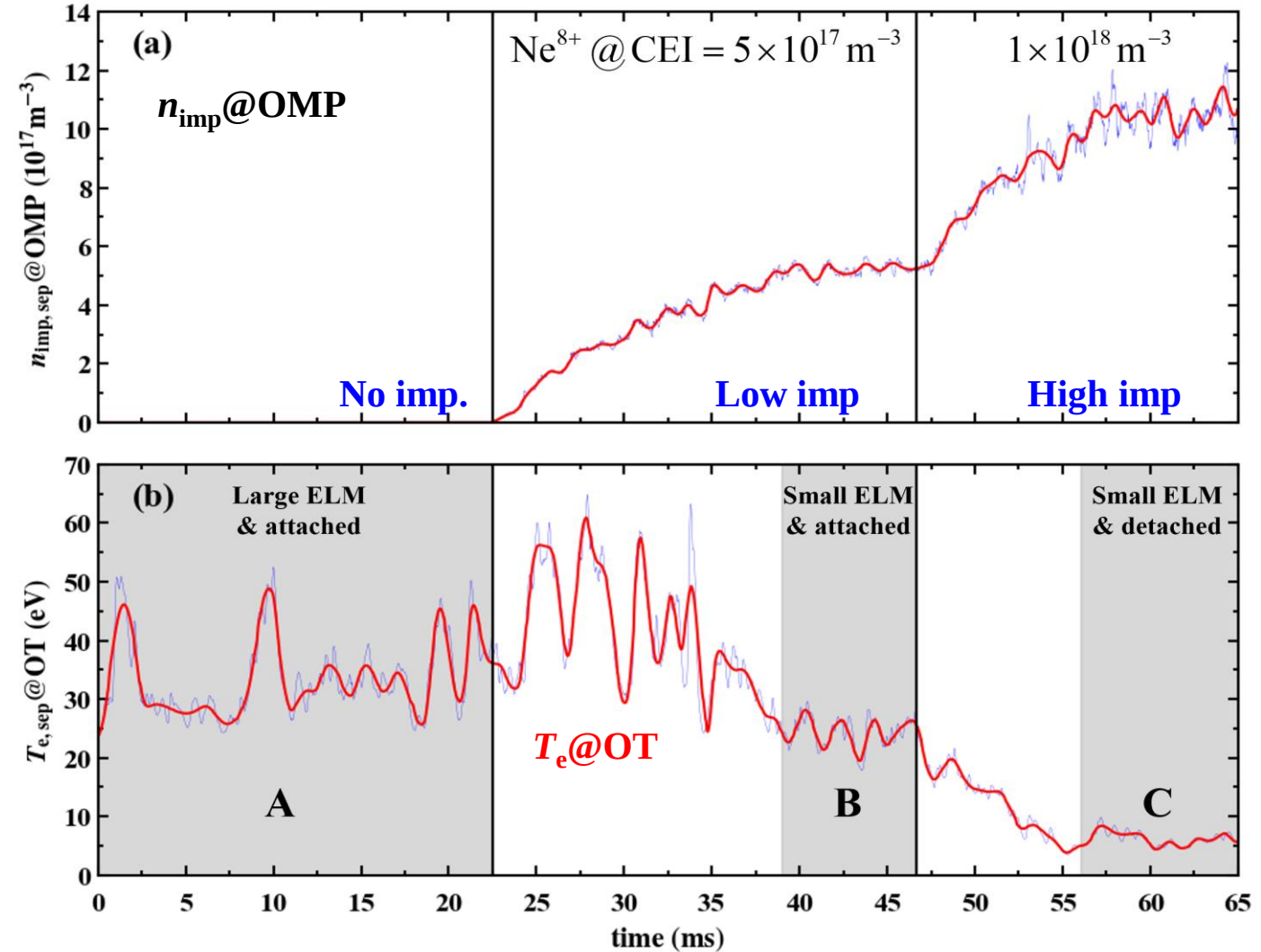
- No impurity
- Rapid increase of $T_{e,OT}$ due to large ELM
- Maximum T_e at SP on OT ≈ 50 eV

■ Phase B: small ELMs / attached

- Ne^{8+} density at CEI: $5 \times 10^{17} m^{-3}$
- Dramatic decrease of T_e fluctuation
- Average T_e at SP on OT ≈ 25 eV

■ Phase C: small ELMs / detached

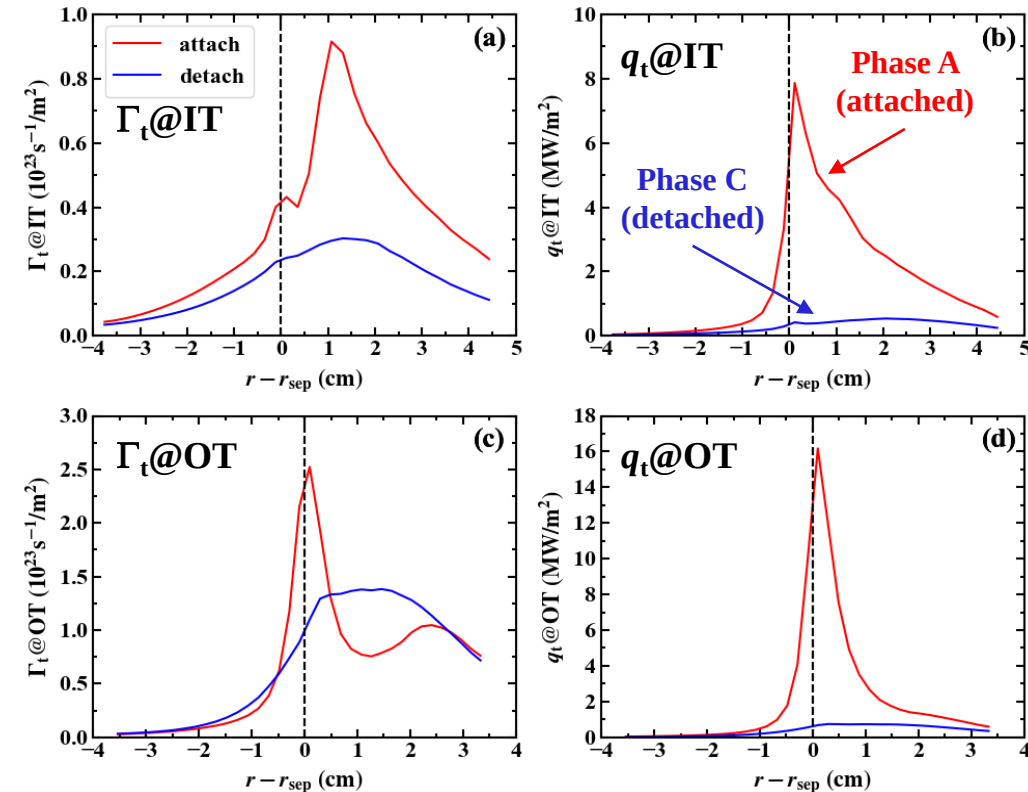
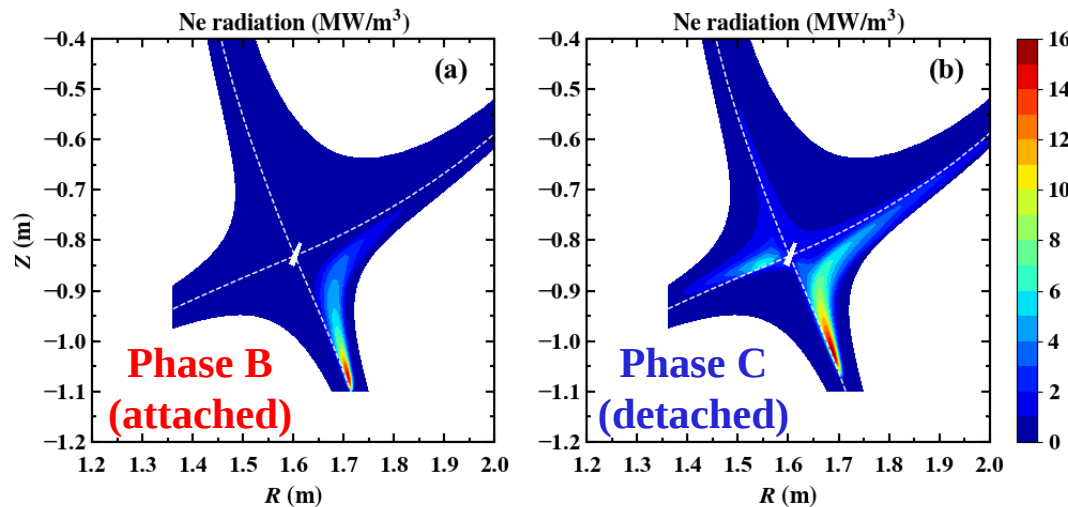
- Ne^{8+} density at CEI: $1 \times 10^{18} m^{-3}$
- T_e fluctuation almost vanishes
- Average T_e at SP on OT ≈ 5 eV



Divertor plasma: attached $\rightarrow$ detached

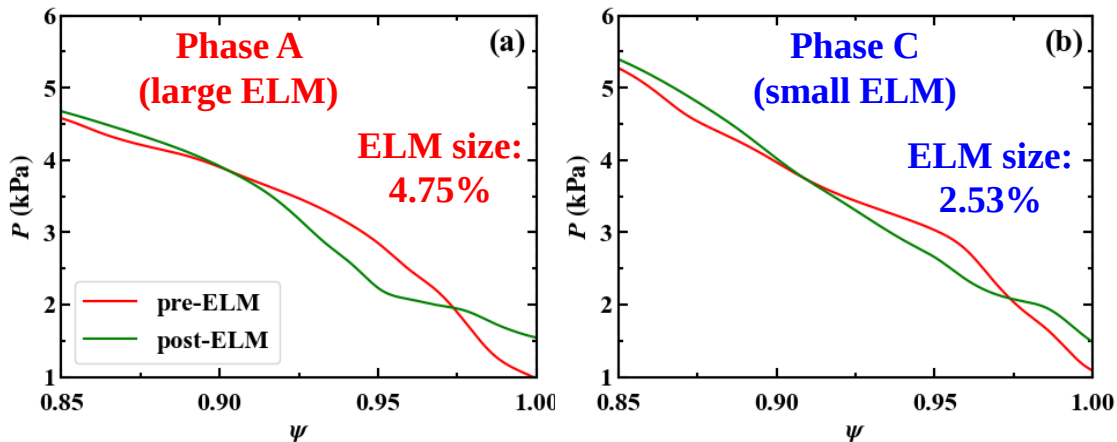
- Both inner and outer divertor achieve **energy detachment**, higher particle detachment level for inner target
 - **Qualitatively consistent with experiment**
- When approaching detachment, radiation region moves from outer target toward X point
- Total radiation power 2.39 MW (**80% P_{SOL}**), 0.68 MW from core region (**28% radiation fraction**)

A. Leonard, PPCF 2018

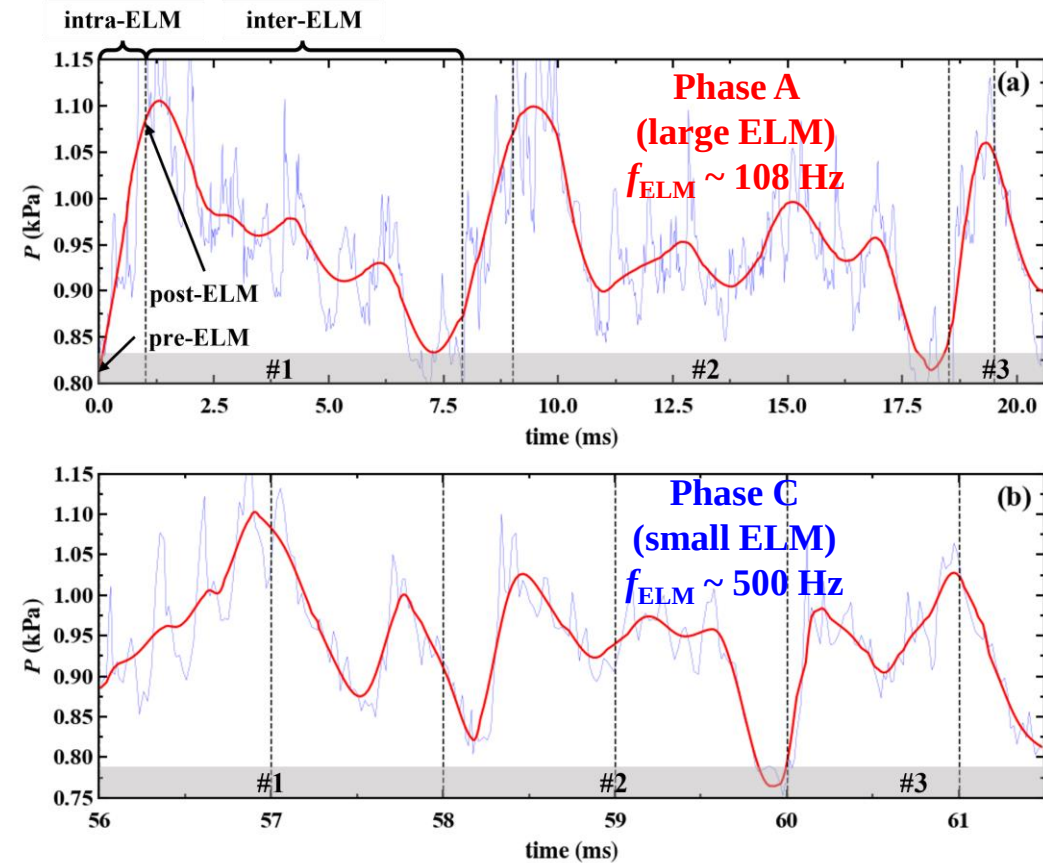


ELM size: large $\rightarrow$ small

- Distinct recovery phase following ELM burst for **large ELM (phase A)**: $f_{\text{ELM}} \sim 108 \text{ Hz}$ (Exp. $\sim 200 \text{ Hz}$)
- Quasi-continuous exhaust feature for **small ELM (phase C)**: $f_{\text{ELM}} \sim 500 \text{ Hz}$ (consistent with Exp.)
- ELM size of **small ELM (2.53%)** is about **half** of that for **large ELM (4.75%)**



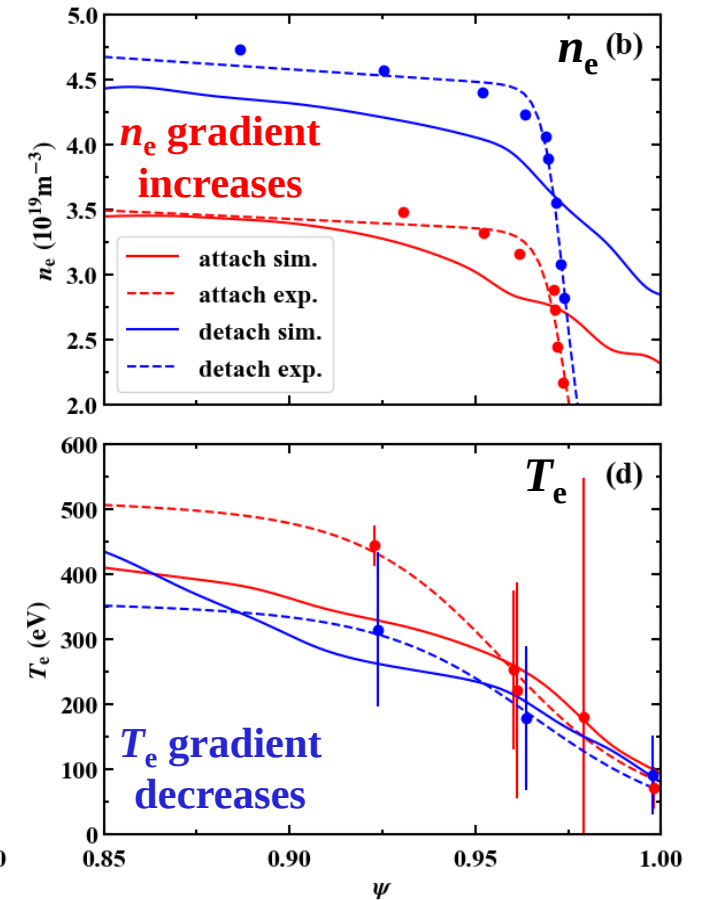
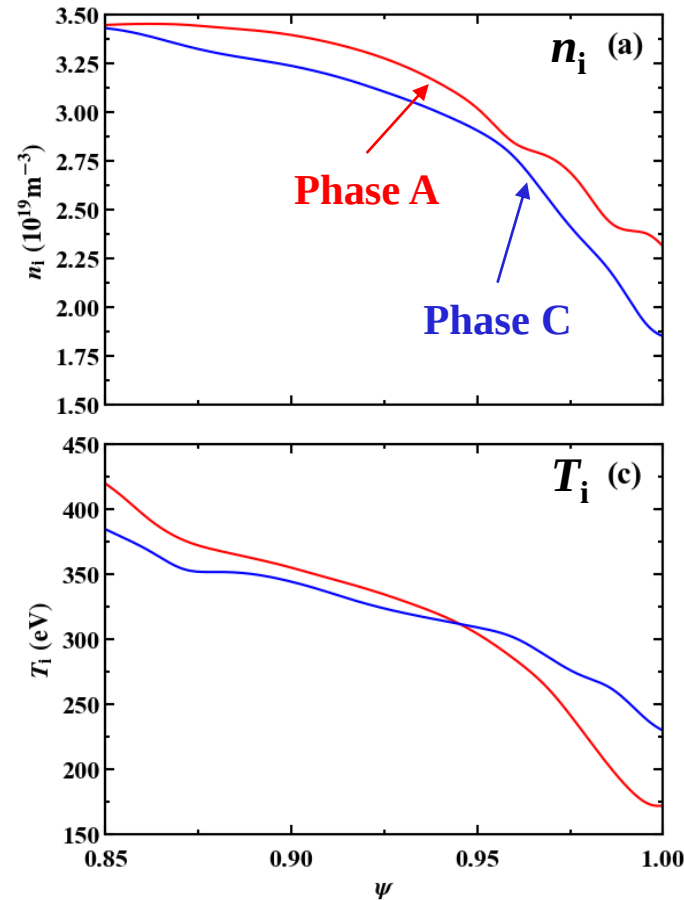
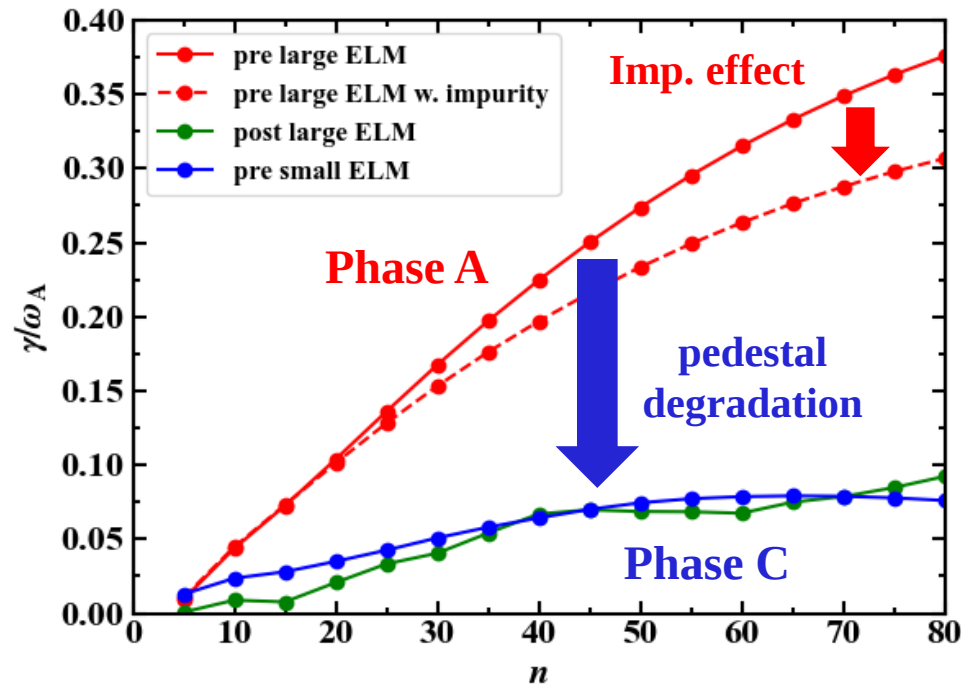
$$\text{ELM size} = \frac{\Delta W_{\text{ped}}}{W_{\text{ped}}} = \frac{\int_{\psi_{\text{in}}}^{\psi_{\text{out}}} d\psi \oint \sqrt{gd\theta d\zeta} (P_{\text{pre-ELM}} - P_{\text{post-ELM}})}{\int_{\psi_{\text{in}}}^{\psi_{\text{out}}} d\psi \oint \sqrt{gd\theta d\zeta} P_{\text{pre-ELM}}} \times 100\%$$



ELM mitigation: degradation of pedestal profiles



- Degradation of pedestal profile after impurity seeding: **suppress pedestal instabilities**
- Impurity itself also has **stabilization effect**  **S.F. Mao, Poster in this meeting #17**



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Conclusion



- **EPCS framework** is developed for **research** of physics mechanism behind ELM/detachment control and **prediction** of edge plasma behavior in future device
- Simulations are performed based on EAST experiments
 - **Grassy ELM:**
 - ELM frequency ~ 2 kHz and counter-clockwise trajectory in P-B diagram: consistent with experiment
 - At pedestal foot: high n ballooning mode $\rightarrow$ nonlinearly enhancing peeling mode $\rightarrow$ ELM burst
 - Strong turbulent particle transport at pedestal foot: facilitates maintaining of low density gradient
 - **Simultaneous detachment and ELM mitigation by neon impurity injection:**
 - After impurity seeding, large ELM $\rightarrow$ small ELM and attachment $\rightarrow$ energy detachment
 - ELM mitigation mainly due to the degradation of pedestal profile after impurity seeding
- Next step:
 - Validation (and investigation) for more experiments and devices. Welcome collaboration!
 - Development with more physics model (e.g. micro-turbulence)
 - Simulation for reactor level devices (prediction)

yemy@ustc.edu.cn
sfmao@ustc.edu.cn



Thanks for your attention!