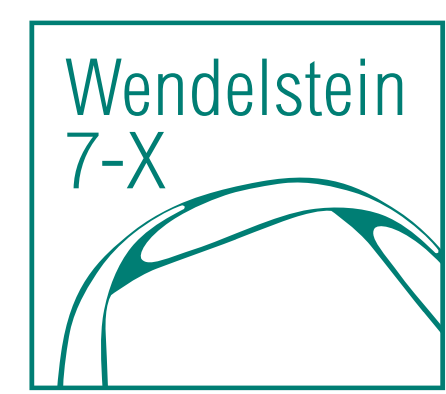


Correction of 1/1 and 2/2 error field in Wendelstein 7-X via divertor heat load symmetrization



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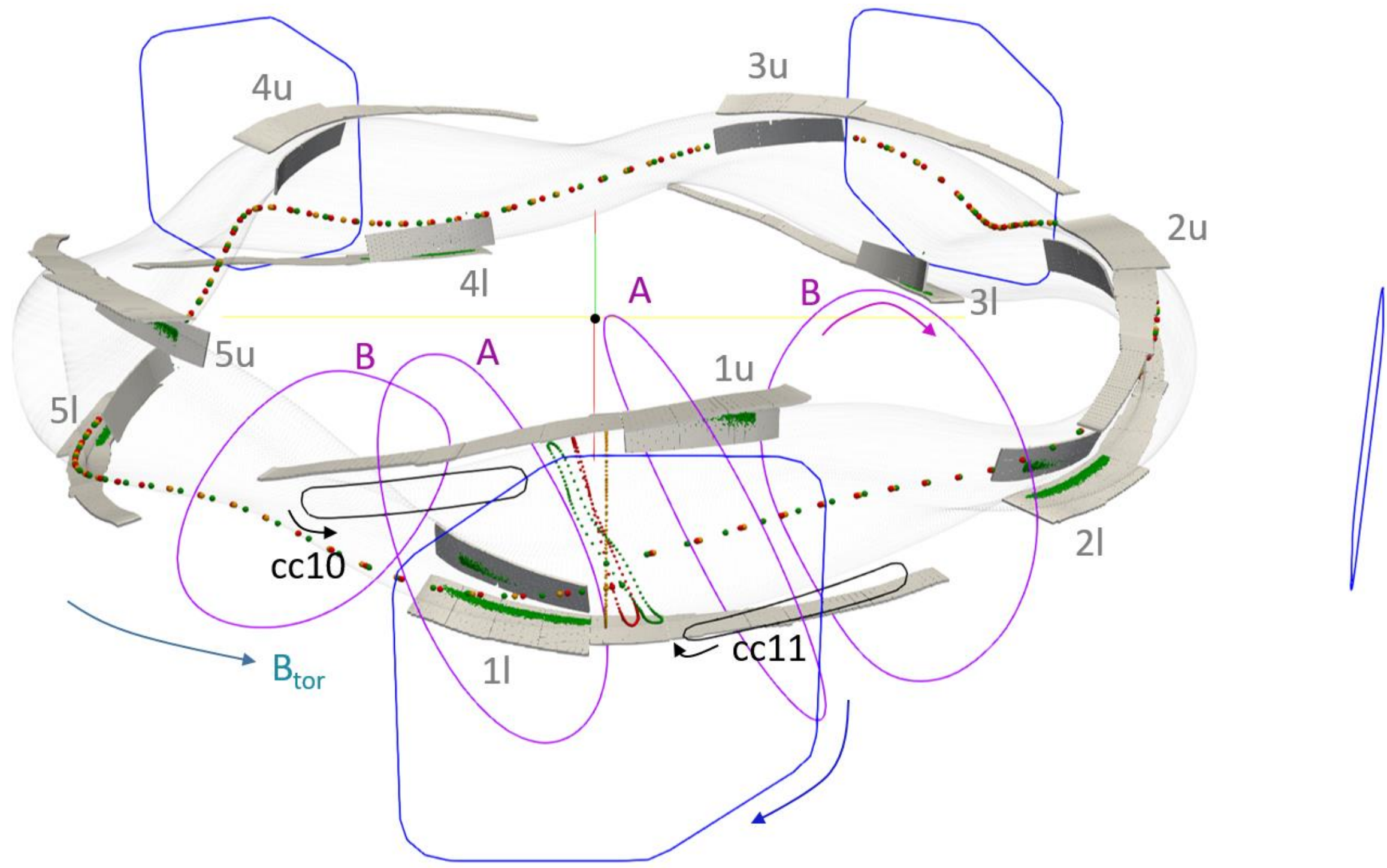
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ABSTRACT

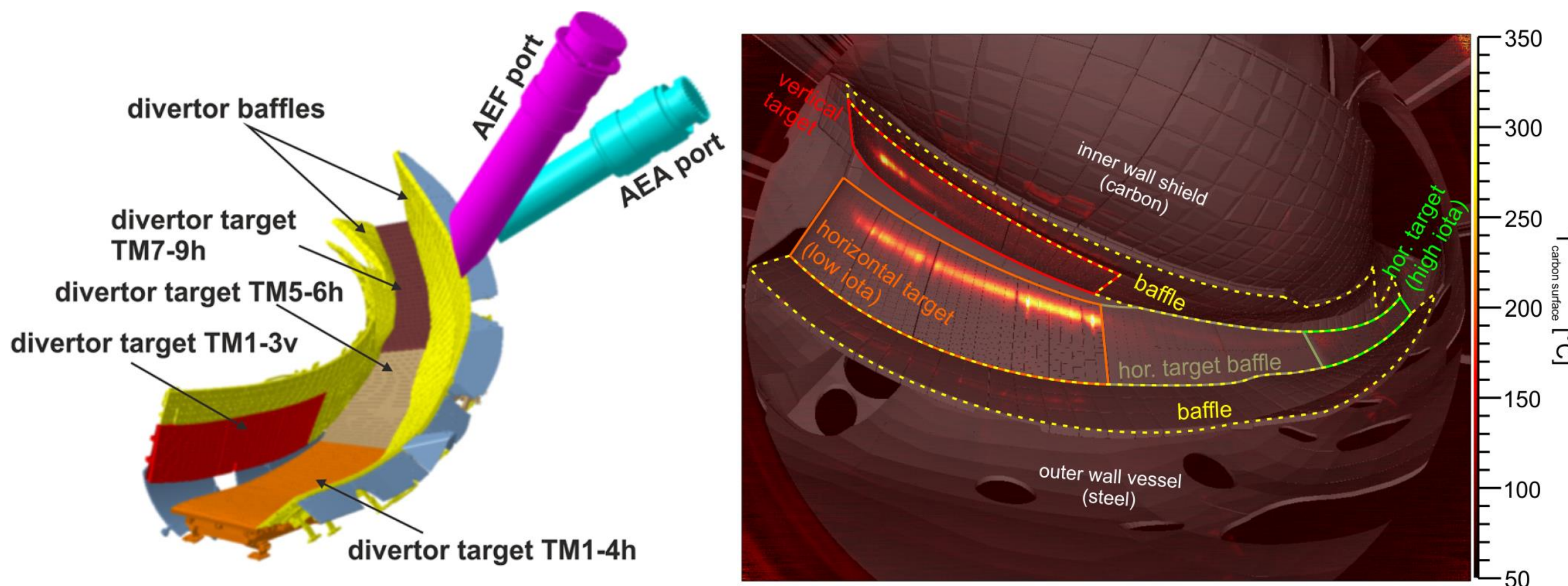
- Correction of the b_{11} error field in W7-X was achieved seven years ago using trim coils, supported by thermocouple measurements and flux surface mapping [1,2].
- With the installation of the new water-cooled divertor, an upgraded infrared diagnostic system [3,4], and the DELVER heat flux calculation code [5], error field correction has been revisited using divertor heat load symmetrization.
- For the first time, correction of the b_{22} error field is achieved through a phase-scan experiment of control coil currents, guided and validated from simulations.

ERROR FIELD AND TARGET HEAT LOADS

- W7-X is designed with a five-fold toroidal modular and an up-down flip symmetry.
- Error field from finite imperfections in coil manufacturing, installation misalignments, electromagnetic deformations, and ferromagnetic materials, can break the symmetry of heat loads on the ten divertor units.
- Five trim coil and ten control coils can be used to correct b_{11} and b_{22} error fields, respectively.



- Water-cooled high heat flux divertor units have been in operation since 2023.
- Safe operation is ensured by real-time monitoring of all ten divertor units with wide-angle infrared thermography.
- Heat flux analysis is performed with DELVER (Divertor Energy Load Versatile Estimator), a 3D implicit anisotropic heat diffusion solver that accounts for multi-layer heat transport, water-cooling conditions, and surface layer effects.



COIL CURRENTS FOR ERROR FIELD CORRECTION

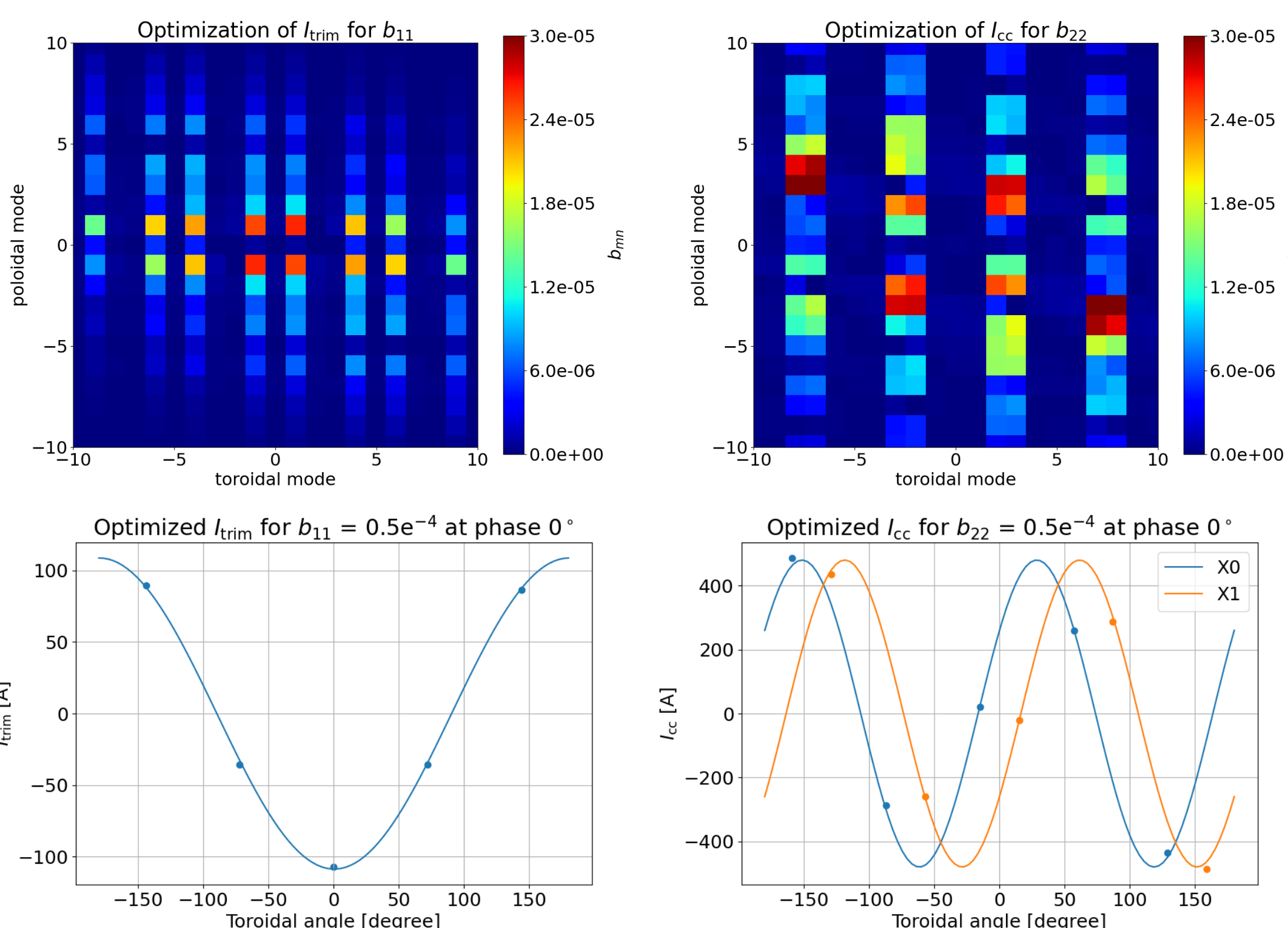
- Constructing flux coordinates for the last closed flux surface (LCFS):

$$\sum_{mn} \{R_{mn}, z_{mn}\} e^{i(m\theta + sn)\varphi}, \varphi_g = \varphi + \sum_{mn} \varphi_{mn} e^{i(m\theta + sn)\varphi}$$

- Calculating Fourier spectra for the perturbation fields produced by individual coils:

$$b_{mn} = \frac{1}{r R_0 B_0} \cdot \left(\vec{B}_{pert} \cdot \left[\frac{\partial \vec{r}}{\partial \theta} \times \frac{\partial \vec{r}}{\partial \varphi} \right] \right)_{mn}$$

- Employing an optimization algorithm to determine current combinations that achieve target modes while suppressing unwanted harmonics.



- Target mode:

$$b_{mn} = A \cdot e^{i\varphi_g}$$

$$A = 0.5 \cdot 10^{-4}$$

$$\varphi_g = 0^\circ$$

- Sidebands exist, but not resonant with $\epsilon = 1$. Thus, minor effects on 5/5 islands.

- Optimal coil currents can be fitted by $\cos\varphi$ for trim or $\cos 2\varphi$ for cc coils, with unique correlation to the b_{mn} phase.

CONCLUSION AND REFERENCE

- Divertor heat loads from all ten divertor units are used for error field correction.
- Simulation establishes a direct link between coil current waveform and perturbation fields, guiding the design of phase-scan experiment.
- Divertor load distributions can be expressed as superpositions of cosine functions, reflecting combined effects of b_{11} and b_{22} fields.
- Experiments achieve the highest level of heat load symmetrization when both b_{11} and b_{22} error fields are corrected, with qualitative agreement from simulations.
- Results confirm earlier b_{11} correction [2] (seven years ago) despite different diagnostics and divertor components, and validate simulation predictions for the b_{22} field performed previously based on flux surface mapping results [1].
- Findings indicate long-term stability and mechanical integrity of the W7-X magnetic coil system.

[1] S. Bozhrenkov et al. NF 60 026004 (2019)

[3] M. Jakubowski et al. RS/89 10E116 (2018)

[5] S. Thiede Master's thesis, Uni. Greifswald (2023)

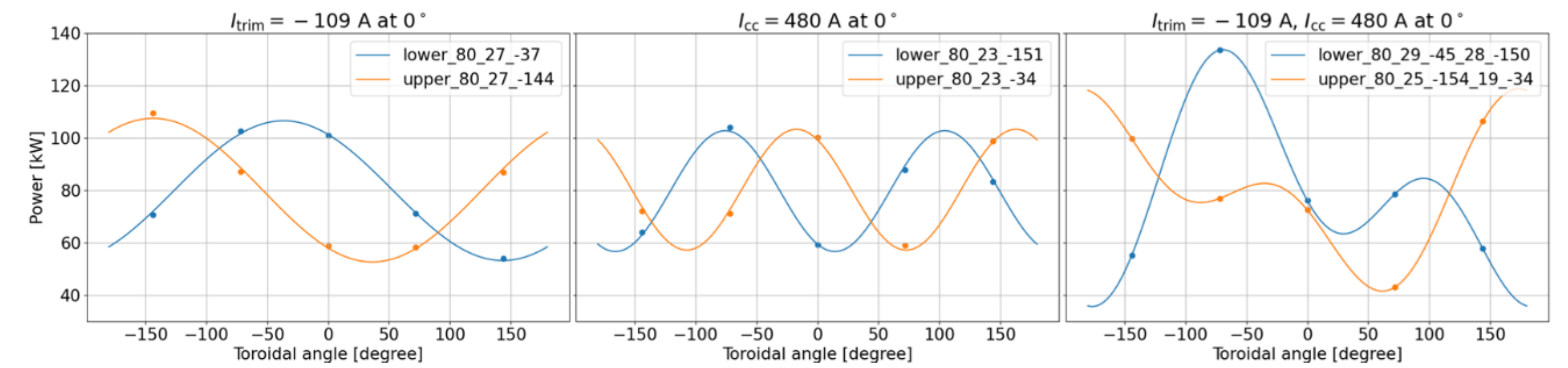
[2] S.A. Lazerson et al. PPCF 60 124002 (2018)

[4] J. Fellinger et al. FED 203 114413 (2024)

[6] Y. Feng PPCF 64 125012 (2022)

PERTURBATION FIELD EFFECT ON HEAT LOADS

- EMC3-Lite [6] is used with parallel electron heat conduction and perpendicular heat diffusion terms: $\nabla \cdot (-\kappa_e \nabla_{\parallel} T - \chi n \nabla_{\perp} T) = 0$, with Bohm sheath boundary condition.
- $T = T_i = T_e = 100$ eV, $n = n_i = n_e = 1 \cdot 10^{19} \text{ m}^{-3}$, $\chi = \chi_i + \chi_e = 1 \text{ m}^2/\text{s}$, $P = 800$



- b_{11} perturbation leads to a target heat load waveforms in $a_0 + a_1 \cos\varphi$.
- b_{22} perturbation leads to a target heat load waveforms in $a_0 + a_2 \cos 2\varphi$.
- Apply both b_{11} and b_{22} , the heat load waveforms are mostly superimposed.
- Fitting will fail with stronger $b_{mn} > 1 \cdot 10^{-4}$, or strongly reduced $\chi < 0.1 \text{ m}^2/\text{s}$. Both increasing asymmetry level such that certain targets receiving almost no loads.

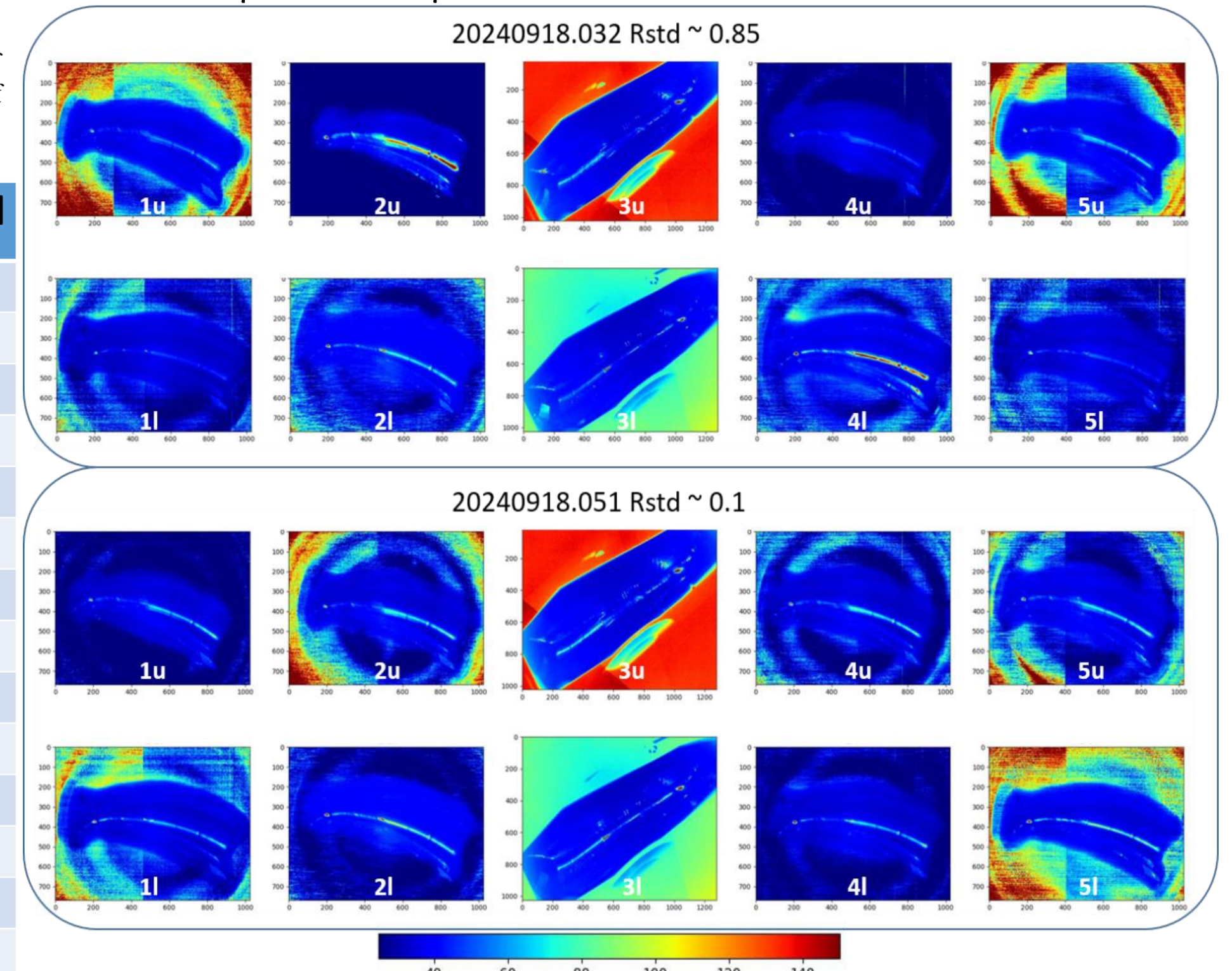
PHASE-SCAN EXPERIMENT

- Discharges all run with 1.8 MW heating power, and line-integrated electron density of $2 \cdot 10^{19} \text{ m}^{-2}$, with each probing a specific phase of perturbation field, while the amplitude for both b_{11} and b_{22} is fixed at $0.5 \cdot 10^{-4}$, from previous studies [1,2].
- Relative standard deviation (Rstd) of integral divertor is used to quantify the

$$\text{symmetry level: } \mu = \frac{1}{5} \sum_{t=1}^5 P_t, R = \frac{\sigma}{\mu} = \frac{\sqrt{\sum_{t=1}^5 (P_t - \mu)^2}}{5\mu}, Rstd = \frac{1}{2} (R_{up} + R_{low})$$

TABLE 1. Phase scan experiment performed on 20240918. Table includes program ID, amplitude of the coil current waveform, and the relevant phase of the produced b_{11} and b_{22} perturbation fields.

PID	I_{trim} [A]	Φ_{b11} [°]	I_{cc} [A]	Φ_{b22} [°]
31	-109	-162	0	0
32	-109	-162	0	0
33	-109	-126	0	0
34	-109	-90	0	0
35	-109	-54	0	0
36	-109	-18	0	0
41	-109	18	0	0
42	-109	54	0	0
50	-109	-18	480	126
51	-109	-18	480	54
54	-109	-18	480	126
57	-109	-18	480	-90
58	-109	-18	480	-18
59	-109	-18	480	90



- Rstd valley provides confidence, indicating intrinsic b_{11} at $\varphi_g = -18^\circ + 180^\circ = 162^\circ$, b_{22} at $\varphi_g = 54^\circ - 180^\circ = -126^\circ$ (φ_g opposite to the correction field).
- With b_{22} correction, Rstd reduces to ~ 0.1 from ~ 0.3 obtained with b_{11} correction.
- Simulation can reproduce experimental waveform with known error fields.

