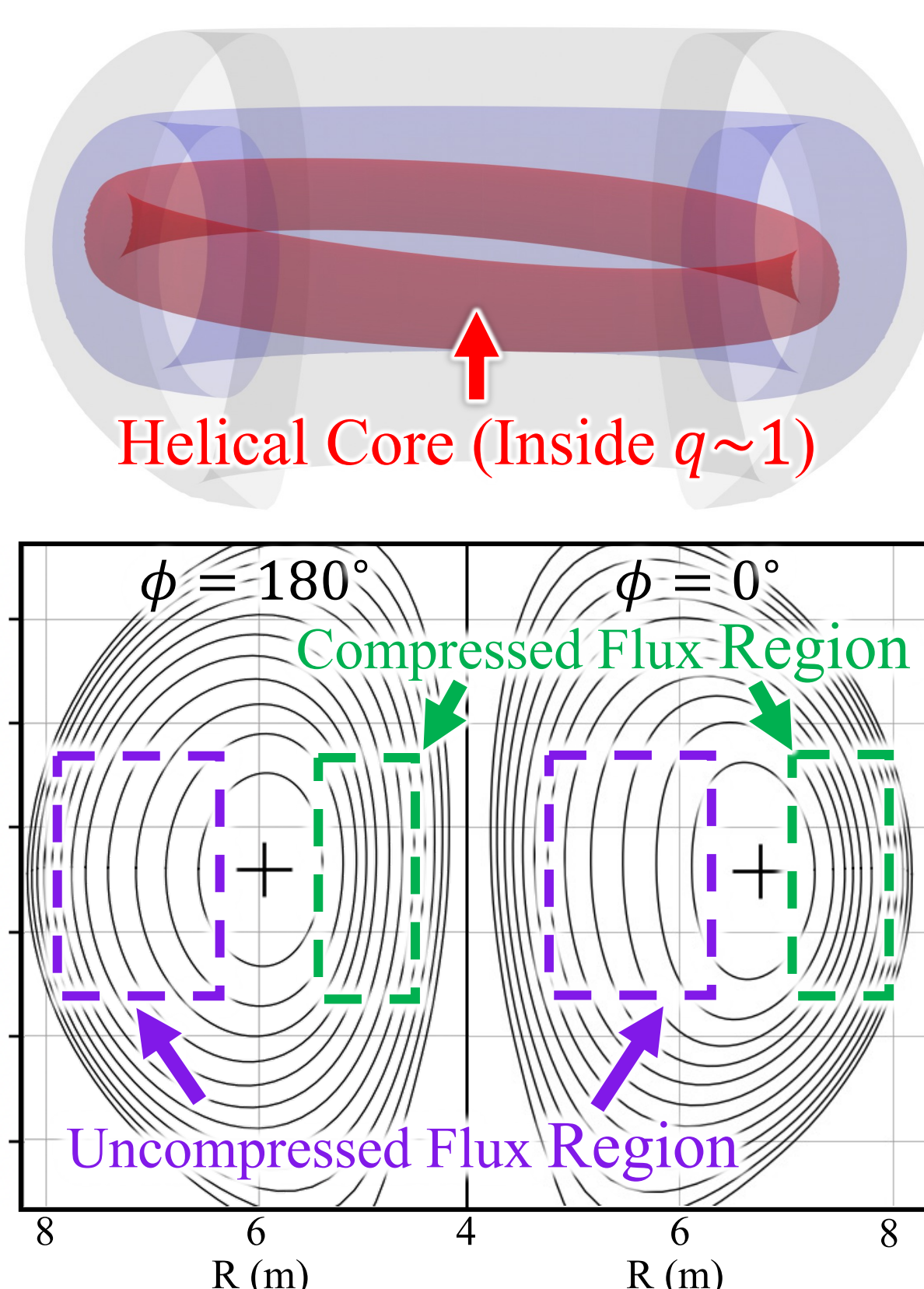


1. Background of Study & Research Objectives

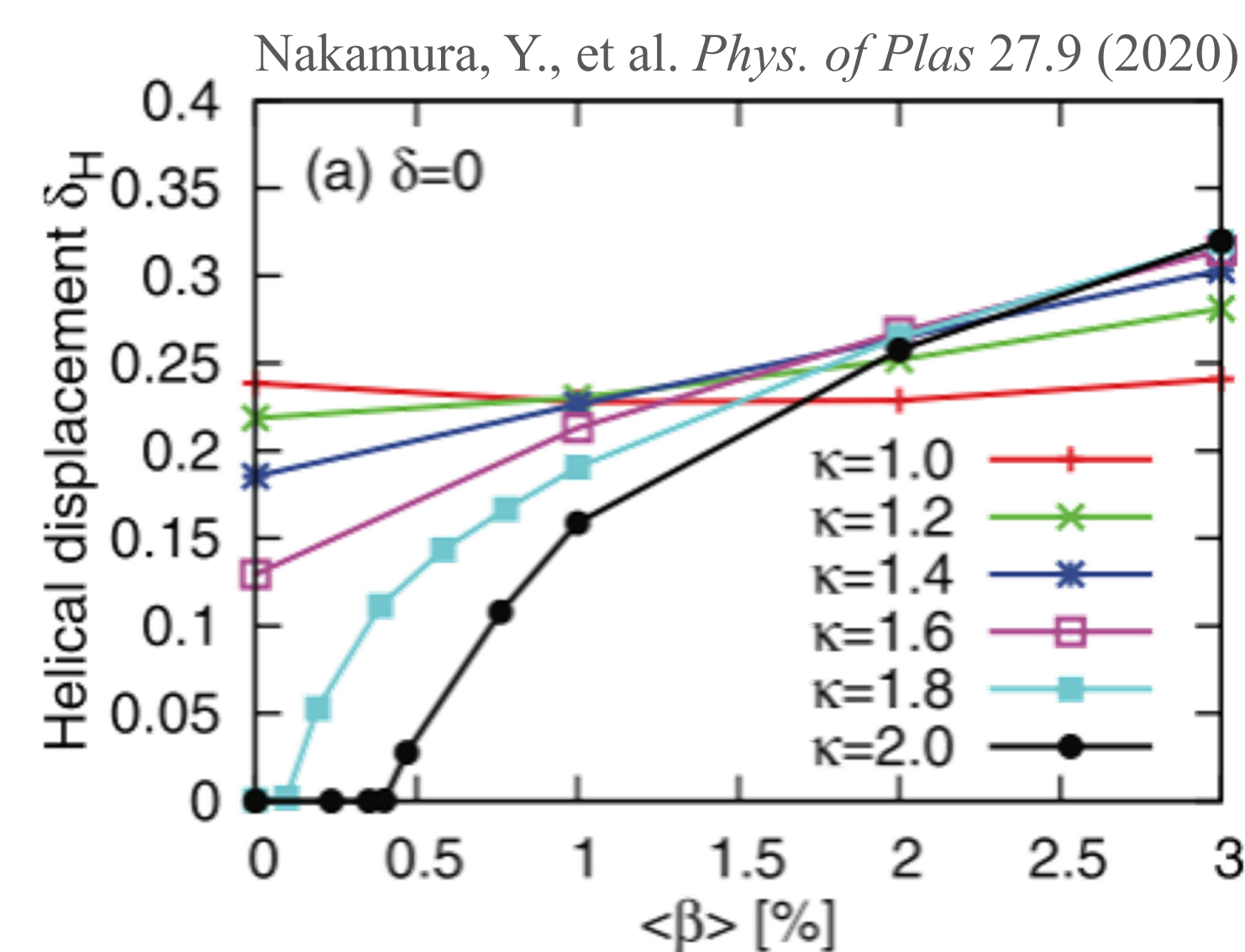
- In a **hybrid scenario** ($q \gtrsim 1$), a **kink/quasi-interchange** mode can **ideally** saturated, leading to a formation of a **HELICAL CORE (HC)**
 - Reported in MAST, DIII-D, and JT-60U
 - Chapman, I. T., et al. *Nuclear Fusion* 50.4 (2010): 045007
 - Cianciosia, Mark, et al. *Nuclear Fusion* 57.7 (2017): 076015
 - Bando, T., et al. *Plas. Phys. and Cntrl Fus.* 61.11 (2019): 115014
 - Spontaneous formation is predicted in ITER
 - Wingen A. et al. *Nuclear Fusion* 58.3 (2018)
- Have both “**Positive** ✓” and “**Negative** ✗” consequences on plasma performance.
 - ✓ **Poloidal Flux pumping** → Sawtooth-free
 - P. Piovesan et al 2017, I. Krebs et al, 2017
 - ✓ ✗ **Energetic Particle Profile broadening**
 - D. Pfefferle et al, 2014
 - ✗ **Plasma Rotation Flattening**
 - I.T. Chapman et al 2010, Y. Yuan et al 2020
- To control the **positive/negative** aspects of **HC**, **good predictability** is needed!



- Prior studies using **VMEC/ANIMEC**, reveal the dependence of **HC** on:
 1. Plasma Shape
 2. Plasma Pressure
 3. Safety Factor

Hirshman S.P., et al. *Phys. of Fld* 26.12 (1983)
Nakamura, Y., et al. *Phys. of Plas.* 27.9 (2020)
Kawagoe, S., et al. *Plas. Phys. Cntrl. Fus* 64.10 (2022)
Cooper, W. A., et al. *Plas. Phys. Cntrl. Fus* 53.2 (2011)

- In **ITER**, significant population of **fusion-born alphas** are expected in the core.
 - Alphas** can affect the stability of the **m/n=1/1** mode, thus affecting **HC**



Raise a Key Question : What is the interplay between **Helical Core** equilibrium and **alphas** dynamics?

2. Simulation Models

MEGA MHD-PIC Sim. Todo, Y. et al. *Phys. of Plas.* 5.5 (1998)

- Nonlinear Resistive MHD (bulk) + PIC (Alpha)**

$$\frac{\partial \rho}{\partial t} = -\nabla \cdot (\rho \vec{v}) + \nu_n \nabla^2 (\rho)$$

$$\rho \frac{\partial \vec{v}}{\partial t} = -\rho (\vec{v} \cdot \nabla) \vec{v} + \left(\frac{\nabla \times \vec{B}}{\mu_0} - \vec{j}_\alpha \right) \times \vec{B} - \nabla P - \nabla \times (\nu_p \nabla \times \vec{v}) + \frac{4}{3} \nabla (\nu_p \nabla \cdot \vec{v})$$

$$\frac{\partial P}{\partial t} = -\nabla \cdot (P \vec{v}) - (\gamma - 1) [P \nabla \cdot \vec{v} - \nu_p \nabla (\nabla \times \vec{v})^2 - \frac{4}{3} \nu_p P (\nabla \cdot \vec{v})^2 - \eta \vec{j} \cdot \delta \vec{j}] + \chi_{\parallel} \nabla_{\parallel}^2 P + \chi_{\perp} \nabla_{\perp}^2 P$$

$$\frac{\partial \vec{B}}{\partial t} = -\nabla \times \vec{E} \quad \mu_0 \vec{j} = \nabla \times \vec{B} \quad \vec{E} = -\vec{v} \times \vec{B} + \eta \delta \vec{j}$$

- Initial Value Problem (Quasi-steady state solution)
 - + Alpha kinetic effects
 - + Multiple Saturation Mechanism:
 - Field line bending
 - Radial mixing
 - Particle trapping
 - ✗ **Numerically Expensive**

VMEC 3D Ideal Equilibrium Solver Hirshman, S.P., et al. *Phys. of Fld.* 26.12 (1983)

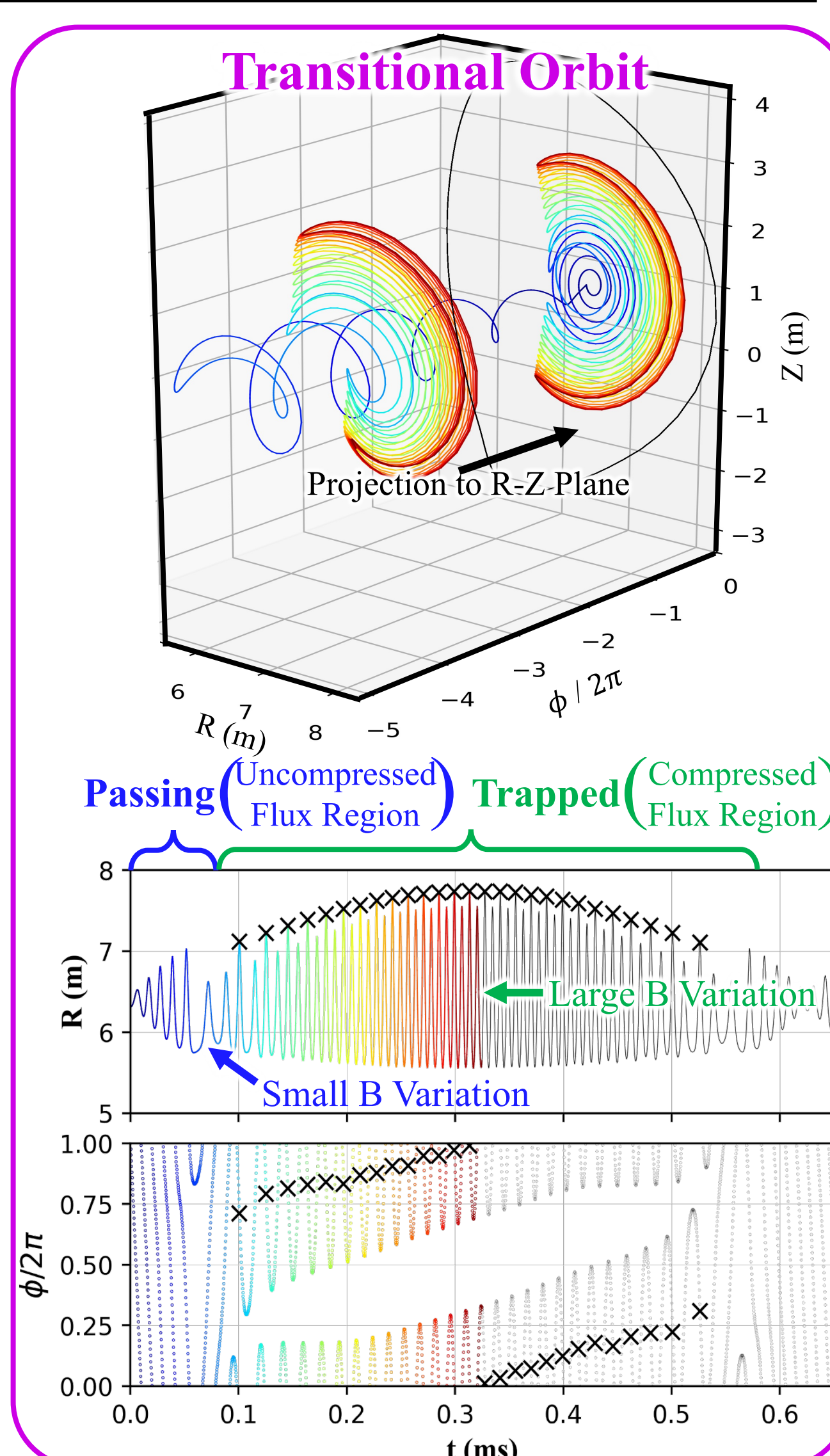
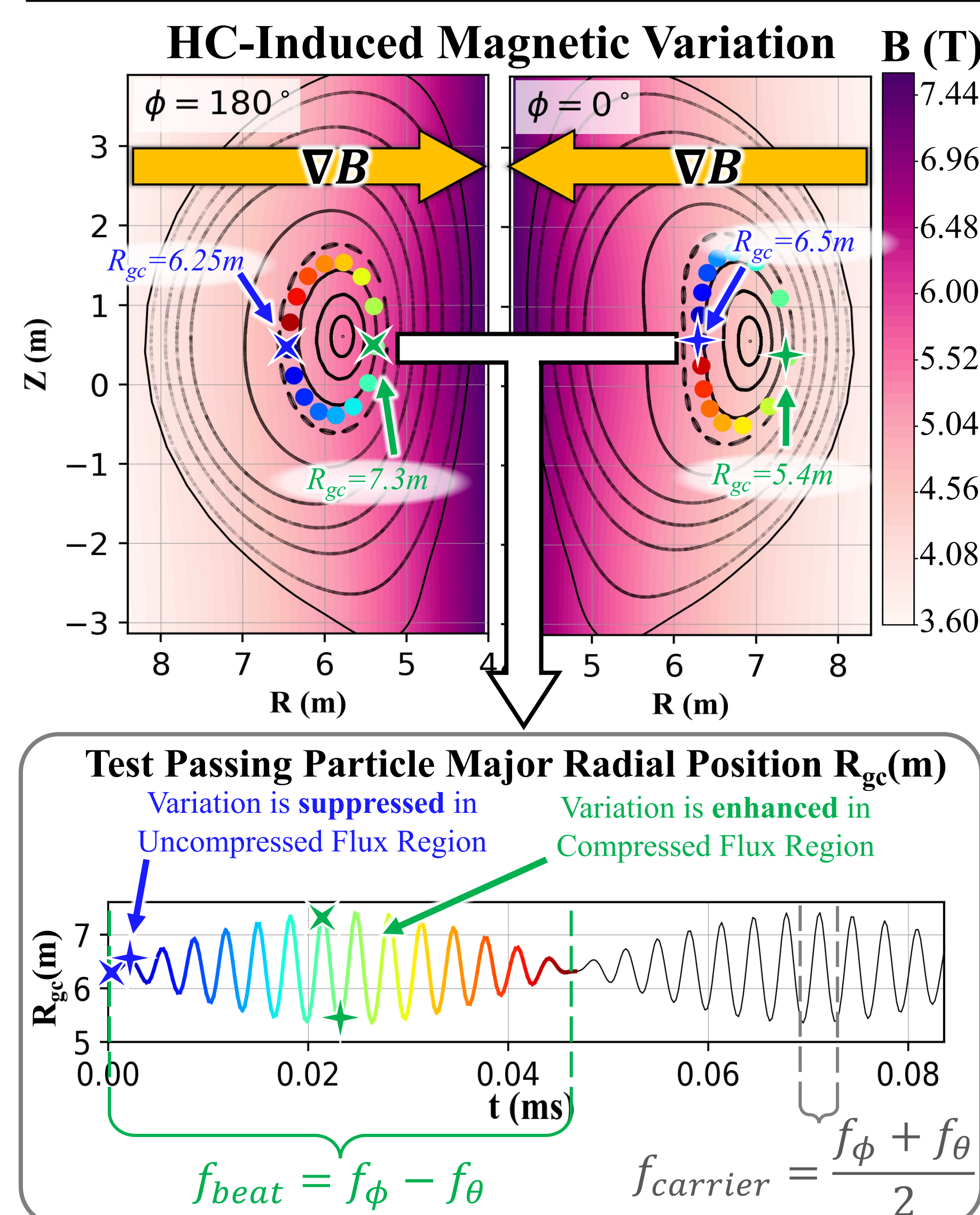
- Minimized Ideal MHD Energy Functional**

$$W = \int \left(\frac{B^2}{2\mu_0} + \frac{P}{\gamma - 1} \right) J d\psi d\theta^* d\phi$$

$$P_{tot} = P_{mhd}(\psi) + P_{\alpha}(\psi)$$

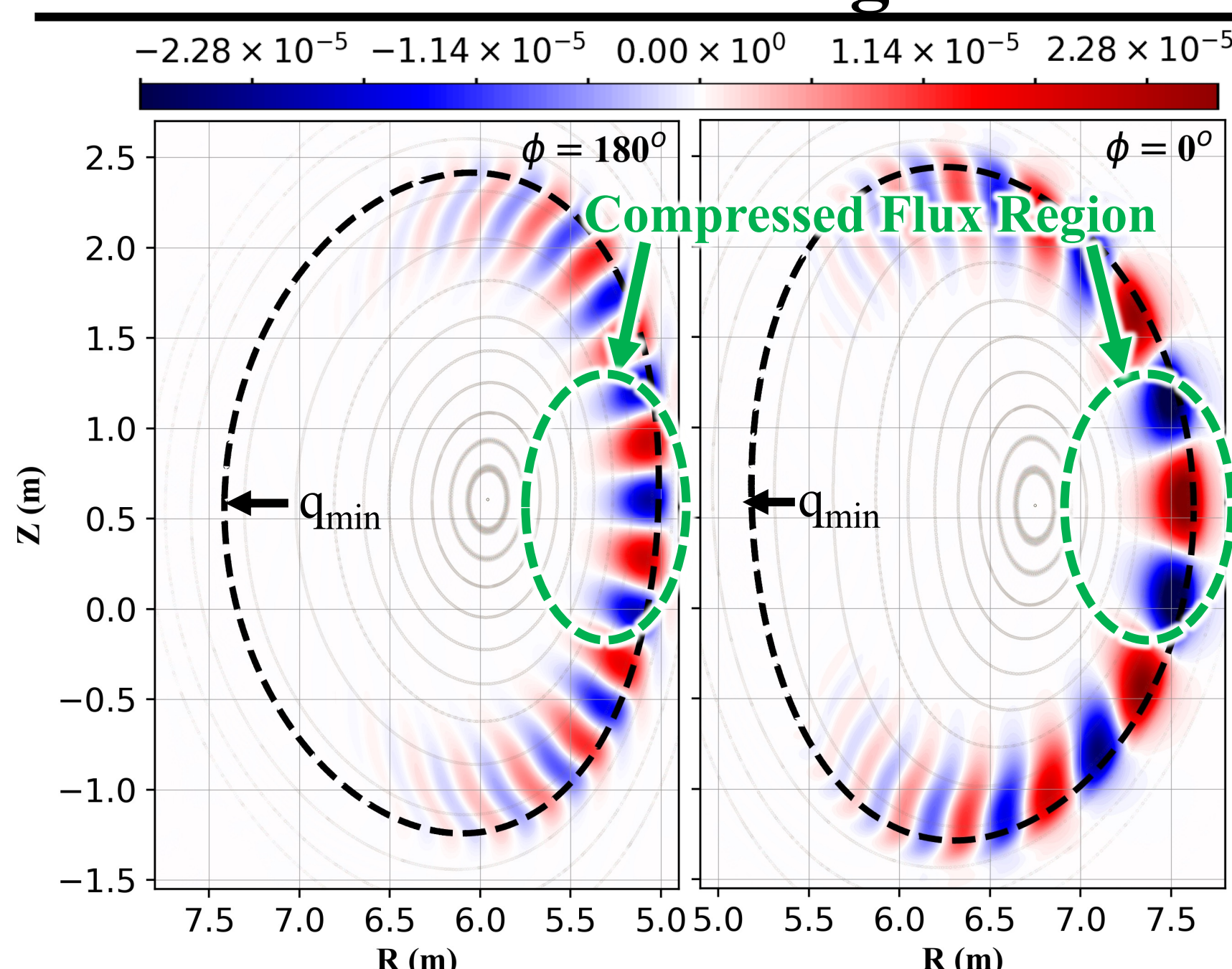
- Boundary Value Problem (Steady state solution)
 - + Numerically **Inexpensive**
 - ✗ No kinetic effect
 - ✗ Stability is excluded

4. Effects of Asymmetry on Particle Orbit



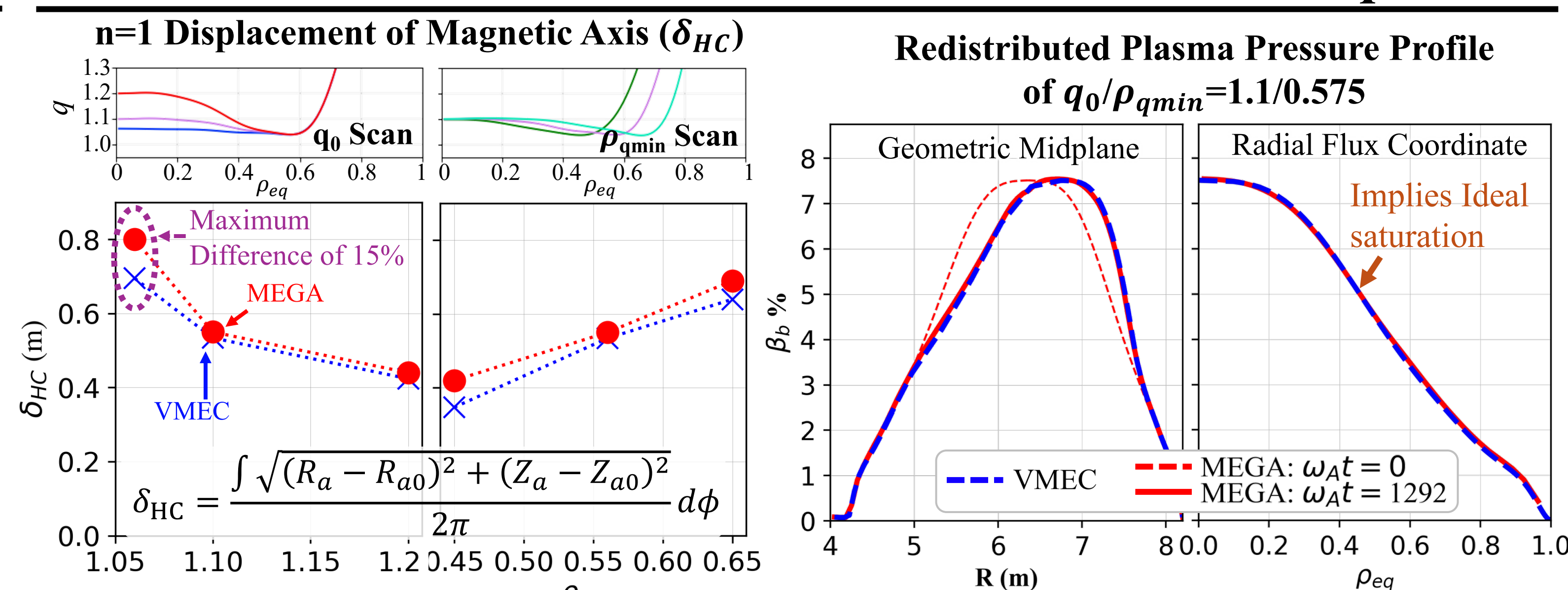
- B-field strength appears mostly axisymmetric in the lab frame, $B \propto \frac{1}{R}$; however, $R_{gc}(m)$ is **modulated** by **HC**, leading to **B-field variation** in the **particle frame**
 - Beat-like pulsation in R_{gc} because $f_\phi \sim f_\theta$ (due to $q \sim 1$)
 - Causing a **transitional** orbit for particle located near the passing-trapped boundary
 - Passing orbit in the **Uncompressed** flux region (**Small B-variation**)
 - Trapped orbit in the **Compressed** flux region (**High B-variation**)

6. Short-wavelength Instability in HC Equilibrium



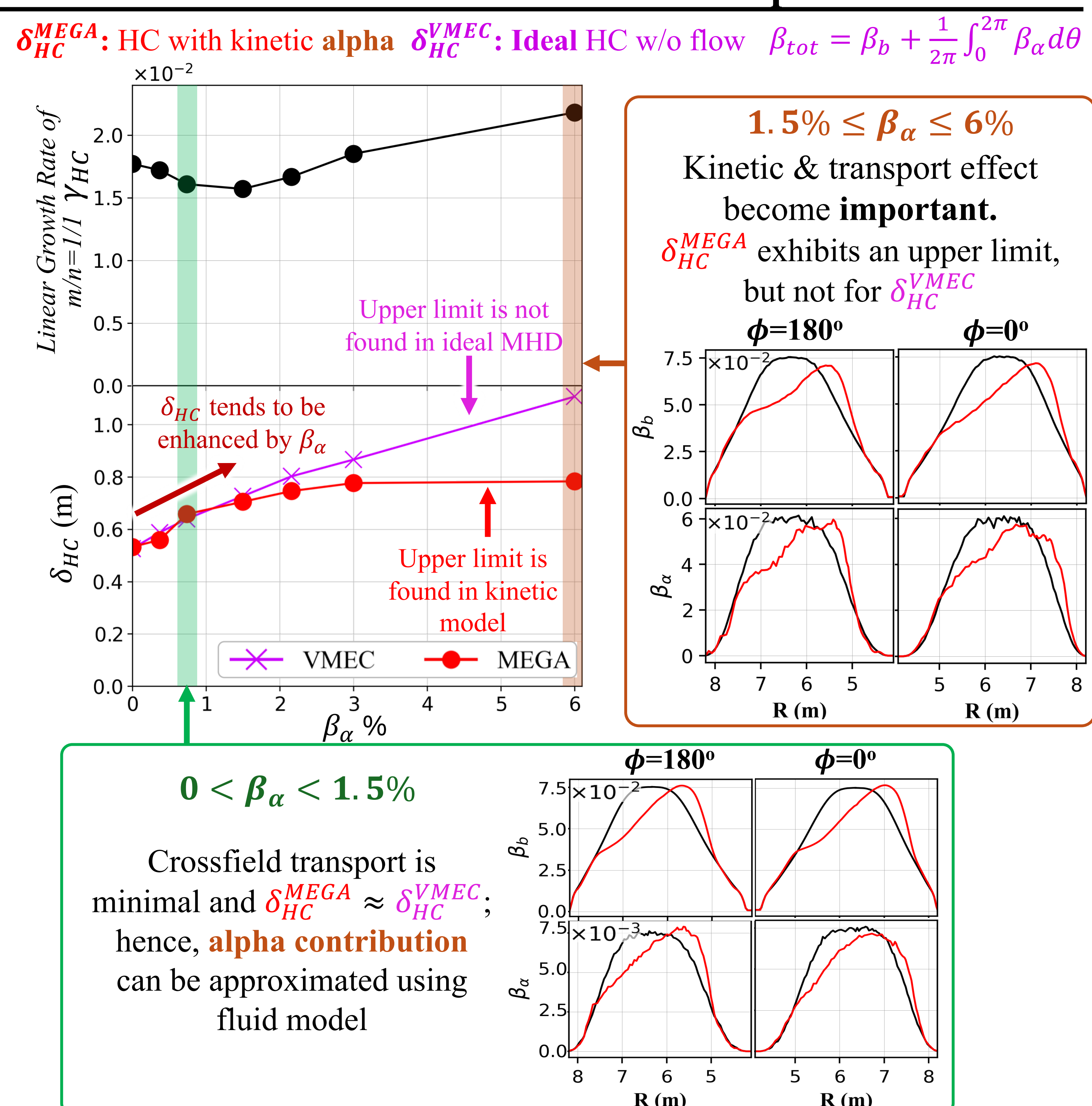
- Short-wavelength mode** is destabilized after HC formation in some equilibria
- Fluctuation is **localized** along the **compressed flux region** of HC
 - At q_{min} radial position
- They can cause **magnetic chaos**
 - Facilitate radial mixing of bulk plasma and alphas
- * This mode is suppressed in other sections, using a n=1 toroidal low-pass filter.
- ** Short-wavelength spectrum of this mode may require EM turbulence models

3. MEGA & VMEC Benchmark without Kinetic Alphas



- Since **VMEC** has been **validated** against **experimental data**, benchmarking **MEGA** against **VMEC** helps ensure that **MEGA** provides a reliable **HC Solution**
- MEGA** yields a good agreement with **VMEC** in the case without **kinetic alphas**

5. HC Formation with Kinetic Alphas



7. Conclusion

- We investigated the interplay between **alphas** and **Helical Core** in ITER-scale (~13 MA) plasma
 1. We found that **HC displacement (δ_{HC})** tends to be **enhanced** by **alphas**
 - HC steady state** is determined mainly from the **quasi-steady state β_b & β_α**
 - $\beta_\alpha \leq 1.5\%$: $\delta_{HC}^{MEGA} \approx \delta_{HC}^{VMEC}$ (Ideal MHD is sufficient because transport is small)
 - $\beta_\alpha \geq 1.5\%$: $\delta_{HC}^{MEGA} < \delta_{HC}^{VMEC}$ (Transport is significant)
 2. **HC** induces a **B-field** variation in the particle frame by modulating R_{gc}
 - Connecting passing and trapped domains**, leading to a **transitional orbit**

Preprint is available: <https://arxiv.org/abs/2509.11749>
“Helical Core Formation and MHD Stability in ITER-Scale Plasmas with Fusion-born Alpha Particles”

