A novel method to optimize omnigenity like quasisymmetry for stellarators

Caoxiang Zhu

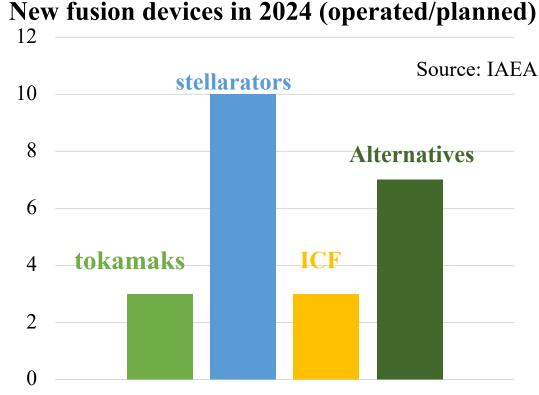
Piecewise omnigenous fields: a radically new family of optimized magnetic fields for stellarator reactors

José Luis Velasco

Introduction

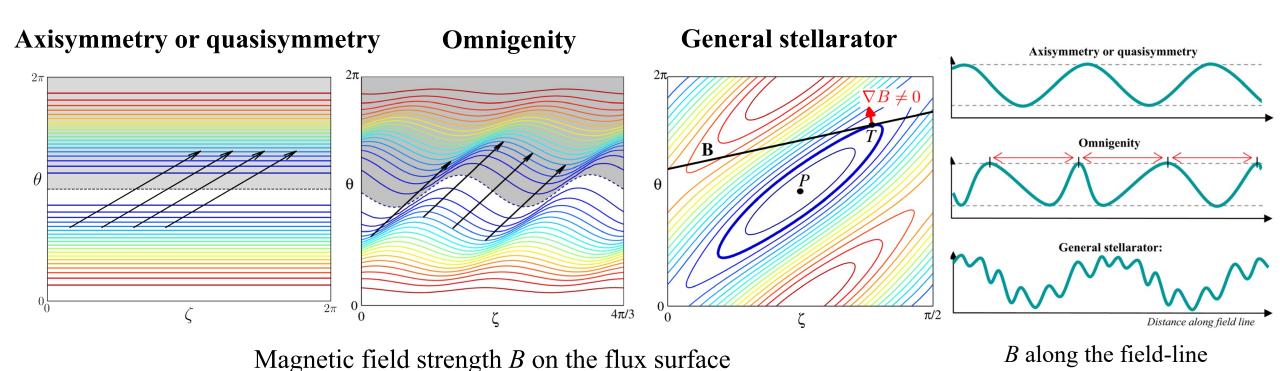
Stellarators have become the rapidest growing fusion concept

- ❖ A stellarator is a toroidal plasma confinement configuration that uses external coils to produce a non-axisymmetric magnetic field.
- Stellarators have many advantages.
 - Steady state operation
 - Low recirculating power
 - Stable to plasma currents inducing MHD instabilities
 - □ Free of disruptions
 - High density operation



❖ Conventional stellarators suffered bad neoclassical transport and it can be overcome by carefully optimized magnetic field [Beidler Nature 2021].

Omnigenity is a primary way to improve confinement



Omnigenity: time-averaged radial drift along each field line vanishes.

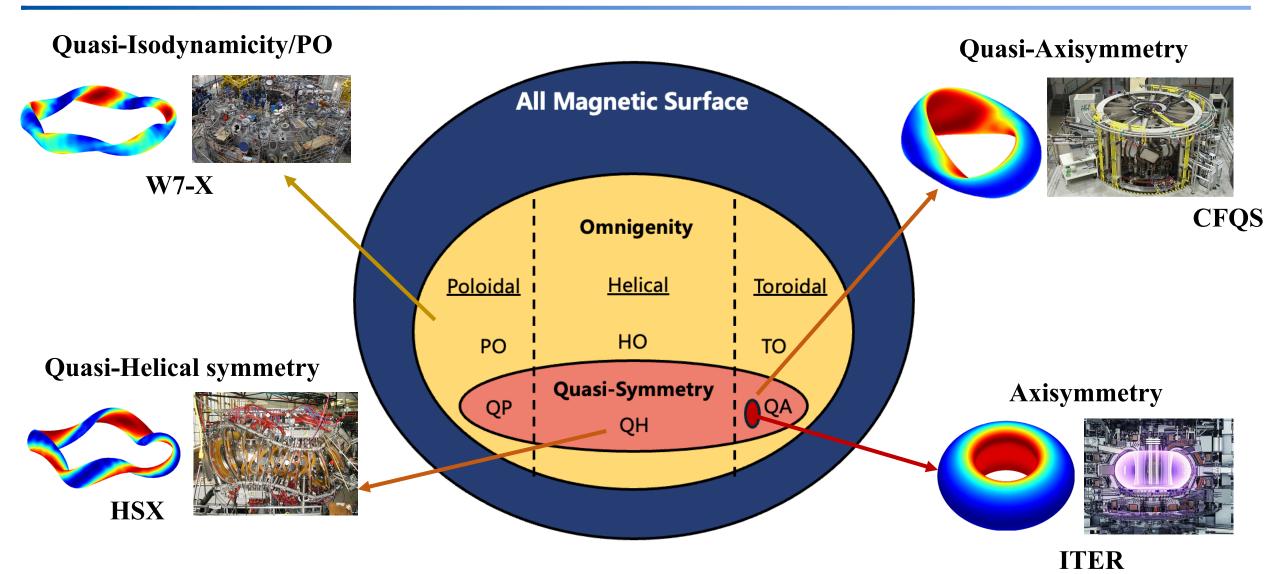
$$\langle \vec{v}_d \cdot \nabla \psi \rangle = 0 \iff \frac{\partial \mathcal{J}}{\partial \alpha} = 0 \qquad \mathcal{J} = m \int v_{\parallel} dl = \sqrt{2m(u - q\phi)} \oint \sqrt{1 - \frac{B}{B^*}} dl$$

➤ No closed *B* contours

[Landreman & Catto PoP 2012]

> Equal bounce distance

Quasisymmetry is a subset of omnigenity





A novel method to optimize omnigenity like quasisymmetry for stellarators

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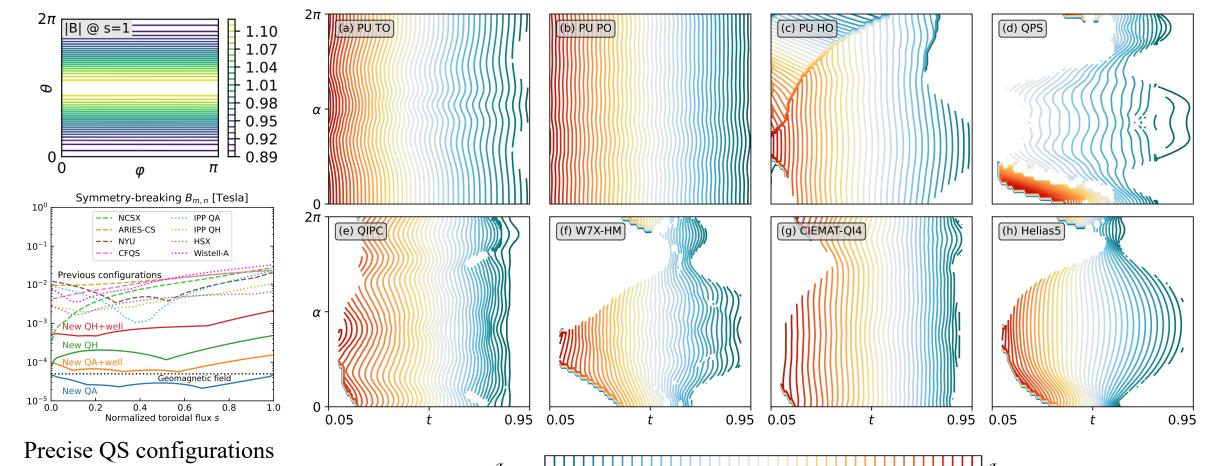
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Optimizing non-QS omnigenity is not easy



- > Quasisymmetry (QS) can be achieved at high accuracy by minimizing asymmetric modes.
- ➤ Non-QS omnigenity optimization is generally more difficult due to the lack of symmetry.



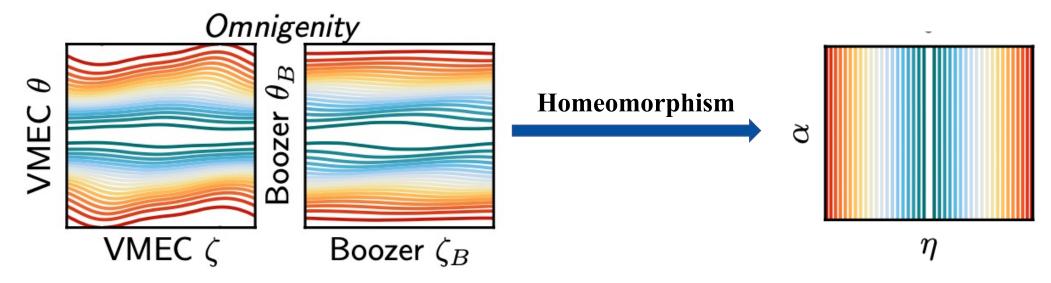
[Landreman & Paul PRL 2021]

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Homeomorphic coordinate mapping for omnigenity



- Omnigenous fields have no locally closed contours.
- There exists homeomorphic coordinates where B contours are straight.

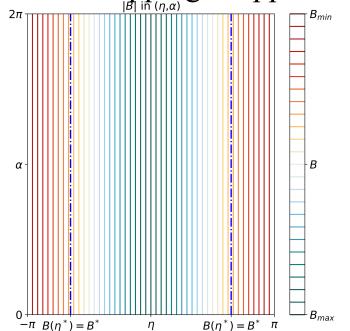


- For quasi-symmetry (QS), Boozer coordinates satisfy such conditions.
- For non-QS omnigenity, one have to find a new coordinate system that meets the requirements and **preserves omnigenity**.

Constructing omnigenous fields in Boozer coordinates is easier



- Several mappings (Cary & Shasharina PoP 1997, Landreman & Catto PoP 2012, Dudt JPP 2024) have been proposed to construct omnigeneous fields.
 - > Omnigenity is preserved
 - \triangleright Constant η is constant B
- A similar mapping is applied here.

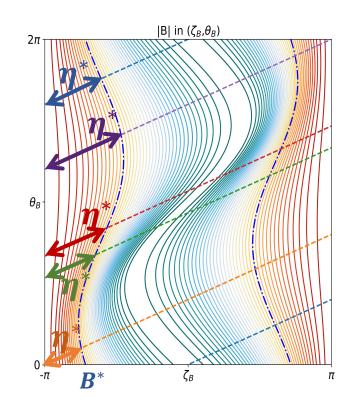


Preserve
$$\frac{\partial \tilde{\mathcal{J}}(B^*, \alpha)}{\partial \alpha} = 0$$

$$\tilde{\zeta}(\alpha, \eta) = \eta - D(\eta) \cdot S(\alpha, \eta)$$

$$\tilde{\theta} = \alpha$$

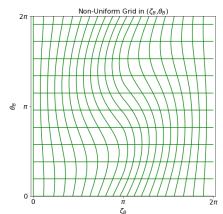
S controls the contour shape
D determines the bounce distance



Omnigenity OPtimization like quasiSymmetry (OOPS)



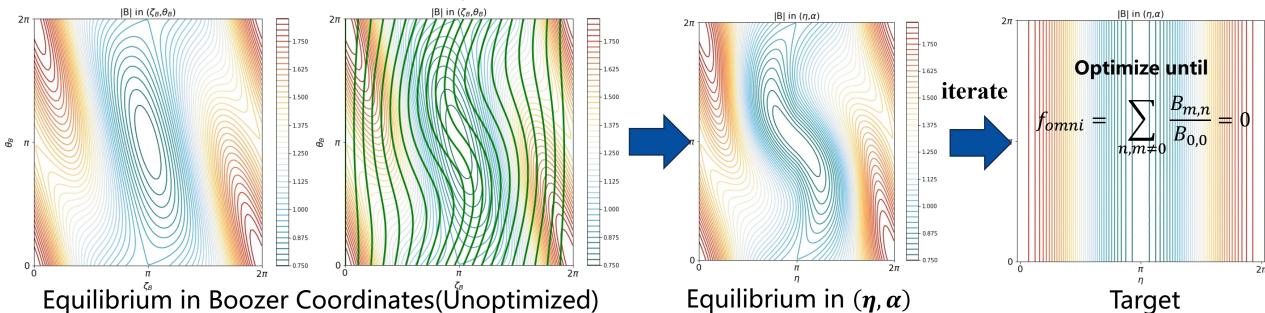
Pick up an **arbitrary** omnigenity mapping



For quasisymmetry, we can use $\eta = \zeta_B$, $\alpha = \theta_B$

The omnigenity mapping can be varied during the iteration of optimization.

(For simplicity, we keep it fixed.)



Precise, compact omnigenous configurations have been obtained



Toroidal Omnigenity (TO)

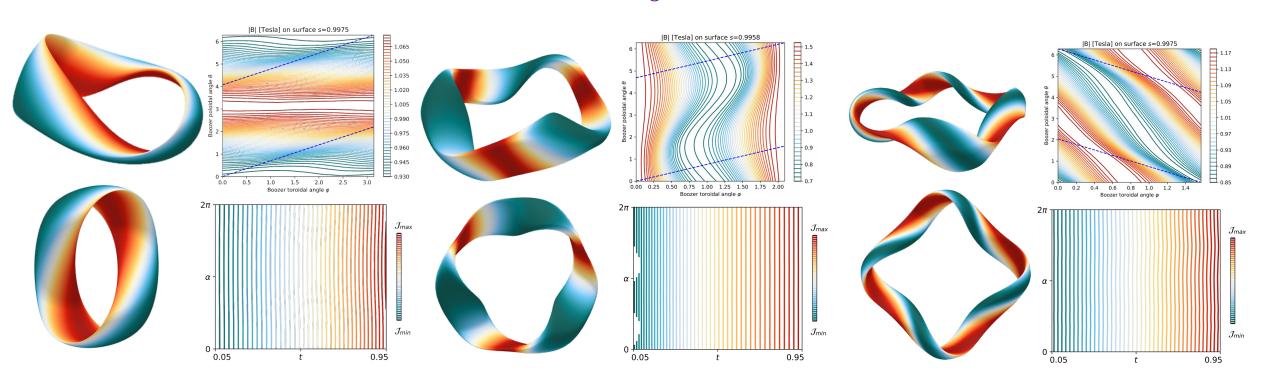
Nfp=2 Ap=6 $\iota_{edge}=0.711$

Poloidal Omnigenity (PO)

Nfp=3 Ap=6.5 $\iota_{edge} = 0.765$

Helical Omnigenity (HO)

Nfp=4 Ap=8 $\iota_{edge} = 1.326$



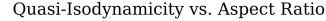
- > No warm starts needed. Initial guesses are circular torus.
- > Simplest mapping is used. (One single Fourier coefficient)
- \triangleright Alpha-particle losses at reactor size < 1%.

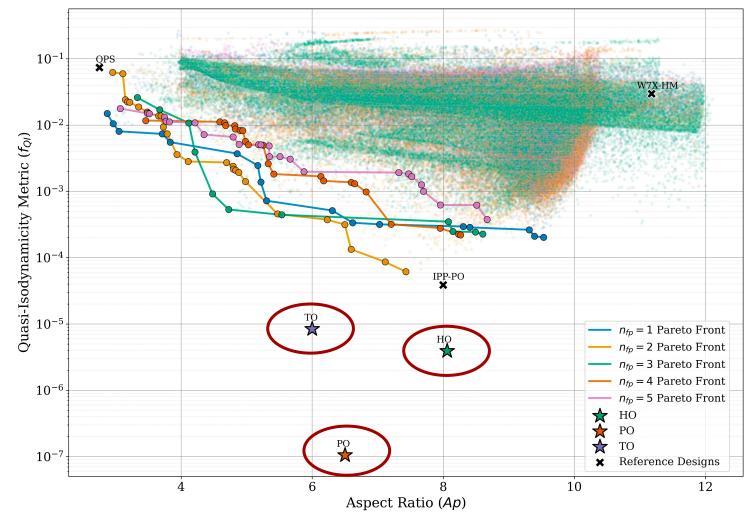
Beyond the Pareto fronts of the "Constellaration" database



- Proxima Fusion recently released the "Constellaration" database [Cadena arXiv 2025].
- ➤ 158, 000 QI configurations were optimized using existing approaches.
- Pareto fronts of the QIquality (f_{QI}) and aspect ratio (Ap) for each period are identified.

$$f_{QI} = \frac{1}{4\pi^2} \iint (B(\theta, \phi) - B^{QI}(\theta, \phi))^2 d\theta d\phi$$





Piecewise omnigenous fields: a radically new family of optimized magnetic fields for stellarator reactors

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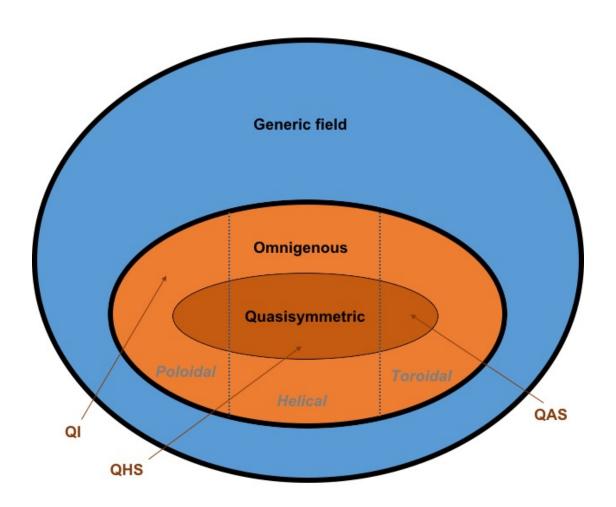
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IAEA-FEC 2025





Are there any other $B(\theta,\zeta)$ that confine orbits perfectly?

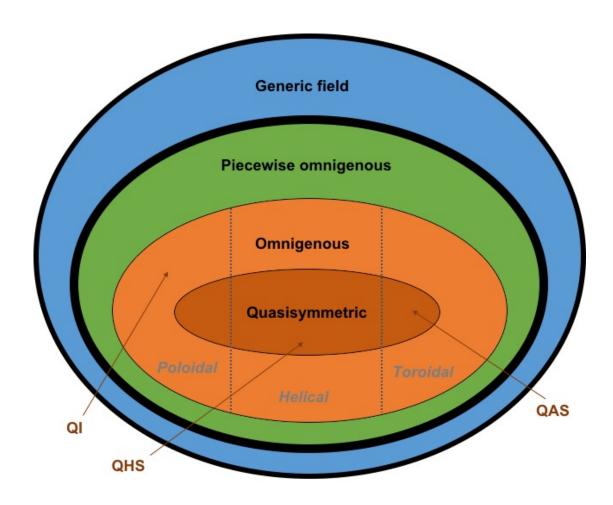


Piecewise omnigenity generalizes omnigenity:

- Motivation: fulfilling constraints of omnigenity may lead to complicated plasma shapes and coils, and to fields sensitive to design errors.
- Goal: remove constraint that all contours of constant *B* close in the toroidal, poloidal or helical direction while keeping collisionless confinement of orbits.

If no global direction of symmetry, **broader** region of configuration space.

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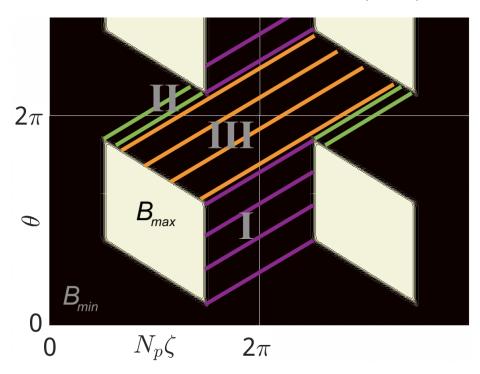
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Piecewise omnigenity: example of model field [Velasco (2024) PRL]

Example of piecewise omnigenous (pwO) field:

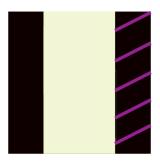


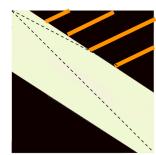
- lacksquare $B(\theta,\zeta)=B_{\max}$ inside a parallelogram.
- lacksquare $B(heta,\zeta)=B_{\min}$ outside.
- \blacksquare ι such that corners are connected by field lines.

■ Several regions / classes of orbits:

- Purple orbits locally see an omnigenous field.
- ▶ Orange (and green) see a different omnigenous field.

B-contours not necessarily aligned with $M\theta - N_p N\zeta$.

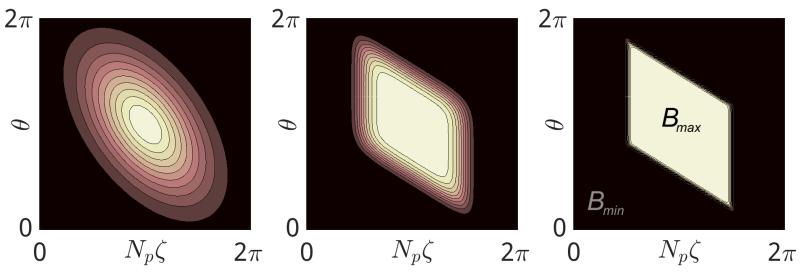




- $\overline{\mathbf{v}_{\mathsf{M}}\cdot\nabla s}=0$ for all classes of orbits.
- Junctures between regions I, II and III do not cause $1/\nu$ transport.

Tokamak-like neoclassical transport ($\varepsilon_{eff} = 0$).

Piecewise omnigenity as a target for a stellarator reactor design

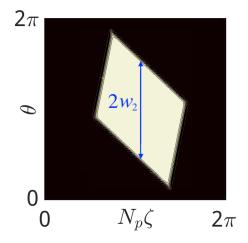


Neoclassical transport compatible with a reactor requires only approximate piecewise omnigenity.

 $(B(\theta,\zeta))$ from left to right: from less to more piecewise omnigenous model fields).

A stellarator reactor requires a divertor:

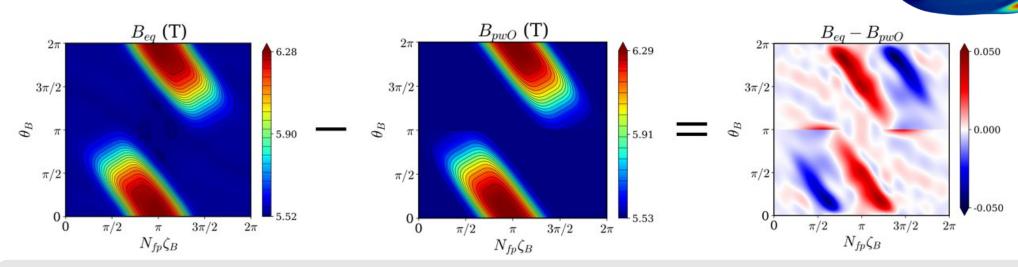
- The most mature concept, the island divertor, was thought to be compatible only with QI fields.
- A subset of pwO fields ($w_2 = \pi$) have reduced bootstrap current, a requirement of an island divertor [Calvo (2025) PRE].



How close to piecewise omnigenity can a magnetic configuration be?

Master Thesis of Víctor Fernández-Pacheco, paper in preparation.

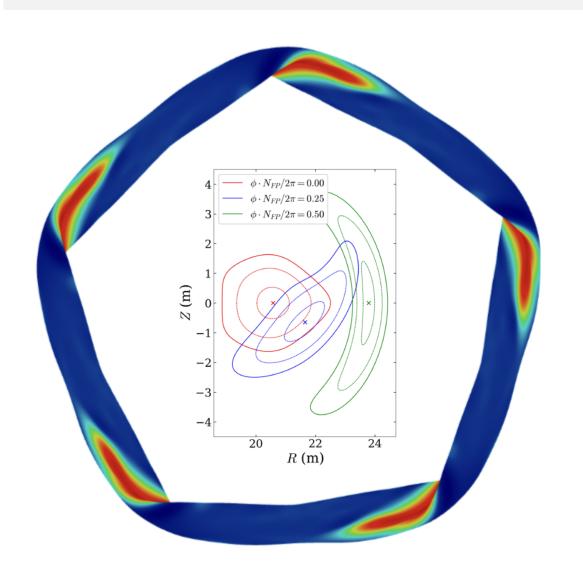
- Optimization w.r.t. piecewise omnigenity implemented in DESC.
- Goal of the work: push the boundaries of the concept of pwO.
 - 1. Select family of B_{pwO} as far as possible from omnigenity.
 - 2. Make B approach B_{pwO} on a flux-surface as much as possible.
 - \diamond In a reactor candidate, we can (and we will) relax 1 and 2.
 - 3. Check that MHD equilibria exist with reasonable shapes and basic properties.

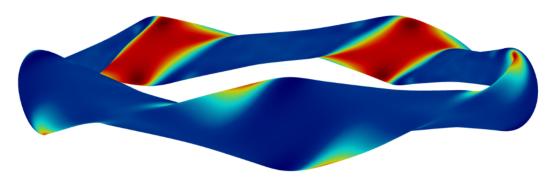


Equilibria with $|B - B_{pwO}|/B_{pwO} < 1\%$ (and likely smaller) can be found.



CIEMAT-pw1: reactor-relevant physics properties [Fernández-Pacheco]





- $N_p = 5, A = 12.7, \kappa = 6.7$
- Mercier MHD stability.
- $4/5 < \iota < 5/5 \Rightarrow$ no low order rationals, compatible with island divertor.
- Reduced neoclassical transport ($\varepsilon_{eff} < 0.005$).
- Reduced bootstrap current ($\Delta \iota_{LCFS} < 1\%$).
- Good fast ion confinement at reactor β (> 95% alpha-heating efficiency, most losses for t > 0.01 s).

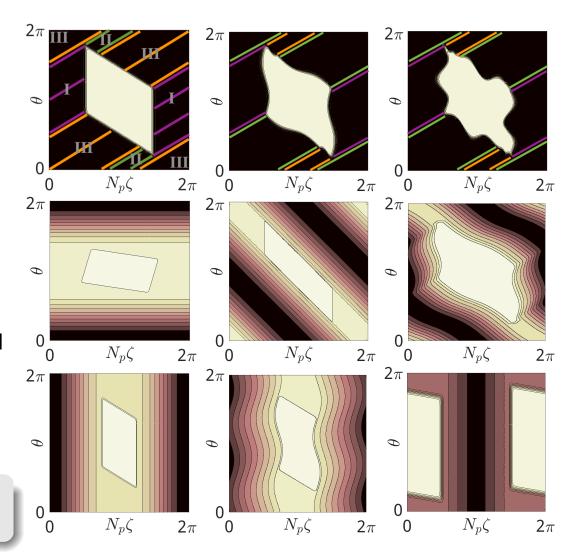
Physics properties compatible with a reactor.

Piecewise omnigenity: vast region of stellarator conf. space [Velasco (2025) NF]

Different types of model fields proposed:

- Fields completely away from omnigenity (as in [Velasco (2024) PRL]).
 - Reactor-relevant configurations exist.
- Fields that combine omnigenity with piecewise omnigenity.
 - ▶ Deeply and barely trapped particles would behave differently.
- Special relevance: fields with (small) deviations from QI that cause negligible neoclassical radial and parallel transport [Calvo (2025) PRE, Velasco, in preparation].
 - ▶ $B \approx B_{min}$ -contours: closed poloidally
 - $ightharpoonup B pprox B_{max}$ -contours: parallelogram shape.

The best reactor candidate could lie somewhere in between.

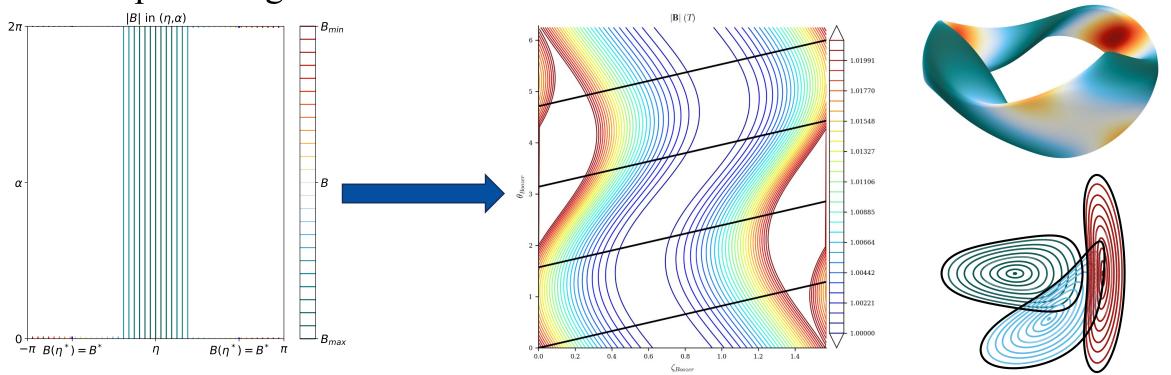


Configurations Combining Omnigenity and Piecewise Omnigenity

Optimizing pwO using OOPS

pwO configurations have locally closed contours, however:

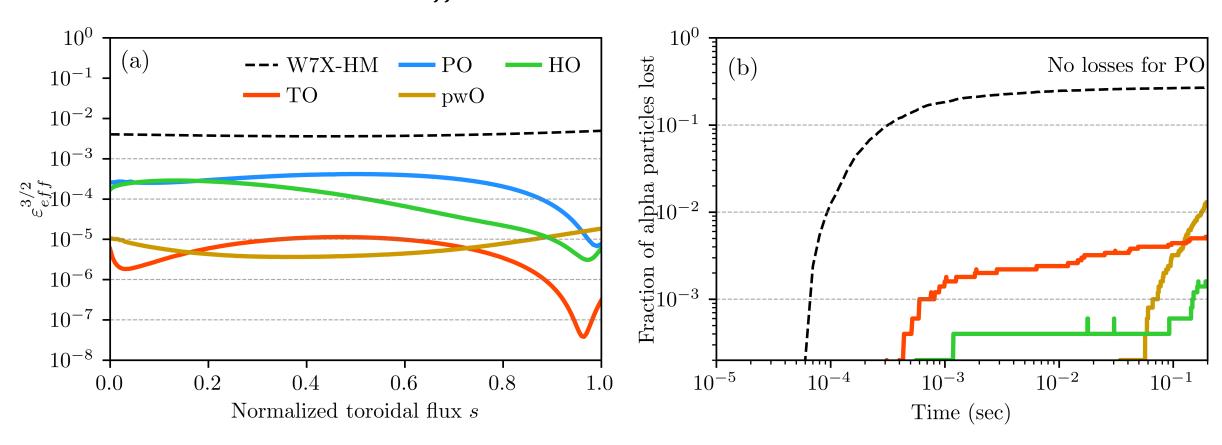
- \triangleright OOPS can still work if we **bound** η and focus out of the Bmax region.
- \triangleright B contours have to be **strongly shaped** such that B_{max} regions can close and form "parallelograms".



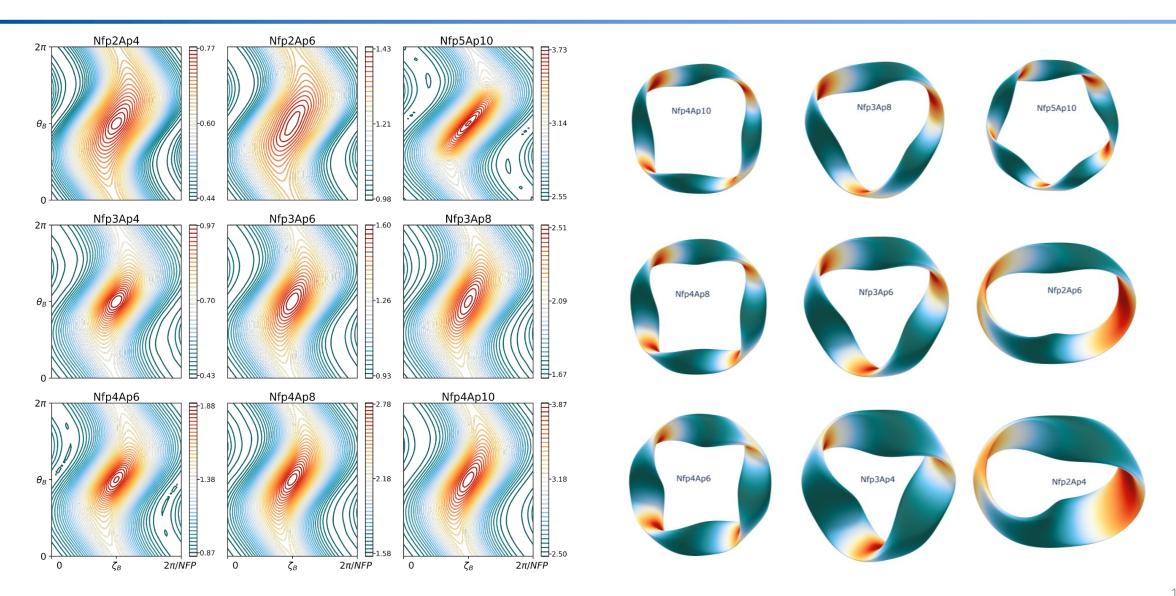
Good confinement properties have been achieved

Efficative Ripple $\epsilon_{eff}^{3/2}$

Loss Fraction of Collisionless 3.5 MeV α -Particles



More pwO + QI configurations are available



Summary

- A new method, OOPS, has been proposed to optimize omnigenity. Precise, compact omnigenous configurations have been obtained.
- ➤ Piecewise omnigenity radically broaden the parameter space of optimized stellarators.
- ➤ Various configurations that combine omnigenity and piecewise omnigenity have been obtained using OOPS, with the potential to achieve more compact configurations and/or to use simpler coils while keeping good confinement.

Thanks for your attention! Both posters available on Saturday morning