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# The nuclear data evaluation pipeline of Uppsala University (NEPU)

- addressing model defects and data inconsistencies

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<sup>1</sup>with inspiration and previous work from: G. Schnabel, P. Helgesson and J. Hansson



#### Model Defects

A model that cannot reproduce the underlying truth, no matter its parameters, can have sever consequences

- Evaluation become biased towards the model.<sup>2,3</sup>
- Uncertainties will be underestimated often severely.<sup>2,3</sup>
- $\rightarrow$  Model defects must be addressed.



"All models are wrong, some are useful." – G.E. Box, 1976





- <sup>2</sup>P. Helgesson, Ph.D. thesis, Uppsala University (2018)
- <sup>3</sup>G. Schnabel, Ph.D. thesis, TU Wien (2015)

#### Background

The goal of this project is to develop a pipeline for nuclear data evaluation, that implements (and further develops) methodology to treat **model defects** and **inconsistent experimental data** that has originated in research activities at UU. In addition, the pipeline should

- automatize as much as possible the steps involved in an evaluation
- create fully reproducible ND evaluations
- provide an intuitive framework for ND evaluation

#### Nuclear Data Sheets 173 (2021) 239-284

Conception and Software Implementation of a Nuclear Data Evaluation Pipeline

G. Schnabel,<sup>1, \*</sup> H. Sjöstrand,<sup>2</sup> J. Hansson,<sup>2</sup> D. Rochman,<sup>3</sup> A. Koning,<sup>1</sup> and R. Capote<sup>1</sup>



### The ND Evaluation Pipeline

The pipeline is a bundle of software packages, along with a set of scripts that each perform a step in a nuclear data evaluation



Underlying assumption: knowledge about the cross-sections can be represented by a multi-variate normal distribution of TALYS parameters



# High Performance Computing

- Pipeline can run entirely on HPC cluster
- MPI wrapper for Talys – large scale parallelization
- Currently running on UPPMAX<sup>a</sup>

   Rackham cluster
- A full evaluation, including the generation of random files, can be performed in a few hours
- Greatly facilitates the testing and <u>validation</u> of ideas and methods





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#### Workflow in the Pipeline

is divided into a number of steps, each represented by an R-script.

- 1. Data is retrieved from EXFOR  $\rightarrow$  Mapped to TALYS predictions
- 2. Rule-based correction of uncertainties in data
- 3. Correction of uncertainties based on statistics
- 4. Talys parameter sensitivity evaluation
- 5. Setup of GP for energy dependence of parameters
- 6. Parameter optimization using the LM algorithm
- 7. Setup of GP in the observable domain
- 8. Re-optimization using the LM algorithm
- 9. Calculation of MVN approximation of the posterior pdf
- 10. Generation of random files



TALYS models the average cross-section, while experiments observe (unresolved) resonance structure. Therefore, the variance of the data around the mean cross-section is much larger than their reported random (statistical) variance.



Not treating this **model defect** can lead to biased results and strongly underestimated uncertainties of the fit.



- Estimate the distribution of data around a smooth energy-averaged cross-section.
- The smooth cross-section should be influenced by the model as little as possible.
- Assuming that the distribution is Normal, a Gaussian Process (GP) seems like a good candidate.
- A GP models data by estimating the correlation between close-lying points with a covariance function, e.g.

$$\operatorname{cov}(y(x_i), y(x_j)) = \sigma^2 \exp\left[-\frac{(x_i - x_j)^2}{2\lambda^2}\right] + \tau^2 \delta_{ij}$$

- The hyper-parameter  $\lambda$  controls the length-scale (smoothness)
- The random error in the data is modeled by the nugget parameter  $\tau$



To determine the distribution of data around a smooth mean function, we model it using a *heteroscedastic GP*  $^4$ .

$$\mathsf{cov}(y(x_i), y(x_j)) = \sigma^2 \exp\left[-rac{(x_i - x_j)^2}{2\lambda^2}
ight] + au^2 \delta_{ij}$$

• The *heteroscedastic GP* introduces latent variance variables, placed under a GP to allow a smoothly varying *nugget parameter* – variance of data around the mean

$$\tau^2 \delta_{ij} \rightarrow \delta(x_1), \delta(x_2), ..., \delta(x_n), \quad \delta(x) \sim GP$$



<sup>&</sup>lt;sup>4</sup>https://CRAN.R-project.org/package=hetGP

#### In practice...

- To separate random and systematic uncertainties, we apply the procedure experiment by experiment.
- Experiments for which to apply the procedure are selected based on the energy resolution in the experiment.
- The length scale is determined from a Marginal Likelihood Optimization on default TALYS predictions.
- Hyper-parameters for the heteroscedastic GP are optimized with the lengthscale  $\lambda$  fixed simultaneous inference of mean xs and the variance of the data





Example application on <sup>56</sup>Fe(n,tot) data<sup>5</sup>

Finally, the reported random uncertainties of the selected experiments are replaced by those estimated by the heteroscedastic GP before fitting TALYS parameters.

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<sup>&</sup>lt;sup>5</sup>E.Cornelis,L.Mewissen,F.Poortmans – EXFOR entry 22316001

#### Inconsistent data

What to do when the difference between the datasets is too large to be explained by the reported uncertainties?





#### Correction of Systematic Uncertainties

The presence of unrecognized uncertainties can be identified if data-sets are inconsistent with each other.

- A linear spline with a MVN prior on the values at the knot-points induces a Gaussian process
- We use a prior on the second derivative at the knot-points



- The prior is based on the default TALYS calculation
  - $\mu$  default TALYS prediction
  - $\Sigma \operatorname{diag}(\mu)$



#### Correction of Systematic Uncertainties

The presence of unrecognized uncertainties can be identified if data-sets are inconsistent with each other.

• The resulting distribution of linear splines is used in a marginal likelihood optimization of normalization uncertainties in the experiments.

$$\det \left( \boldsymbol{\Sigma} \right)^{-1/2} \exp \left[ -\frac{1}{2} (\vec{x} - \vec{\mu})^T \boldsymbol{\Sigma} (\vec{x} - \vec{\mu}) \right]$$

 $\vec{x} = \text{experimental cross sections}$  $\vec{\mu} = \text{linear spline}$  $\mathbf{\Sigma} = \mathbf{\Sigma}_{\text{exp}} + \mathbf{\Sigma}_{\text{spline}} + \mathbf{\Sigma}_{\text{extra}}$ 

Added normalization uncertainty of each experiment is contained in  $\pmb{\Sigma}_{\mathsf{extra}}$ 



#### Correction of Systematic Uncertainties

Outliers are assigned inflated normalization uncertainty.

section (mbarn) inflated 150 total unc. 100 posterior mean of linear spline 50 cross 0 10 15 20 energy (MeV)

Cr-52(n,p)





## Treatment of Model Defects

#### - GP in the parameter domain<sup>6</sup>

- Incident energy-dependent variation of parameters around global value
- The variation is modeled with a Gaussian process (GP)

$$\sigma(E_j) = f(E_j; \vec{p} + \vec{\delta}(E_j)) + \varepsilon, \qquad \vec{\delta}(E) \sim \mathsf{GP}$$

- Smooth variation of parameter values with energy
- Consistent physics description at each energy
- TALYS conserves the sum-rules
- In the presence of model defects, parameter uncertainty is mainly constrained were there is data



<sup>&</sup>lt;sup>6</sup>P. Helgesson & H. Sjöstrand, Ann. Nucl. Energy 120 (2018) 35-47

# EXAMPLE OF RESULTS

#### APPLICATION OF THE PIPELINE ON <sup>52</sup>CR CROSS-SECTIONS



#### Exclusive particle production xs



- posterior mean (black)
- - prior mean (red)





#### Channels affected by resonance structure



- posterior mean (black)
- - prior mean (red)
- Low  $\chi^2$  for the (n,tot)-channel could indicate an overestimated random uncertainty by the heteroscedastic GP



#### Cross-validation

number of degrees of freedom is not well defined for non-linear models with priors

- 5-fold cross-validation
  - Experimental data is randomly divided into 5 subsets
  - each time 20% is left out
- The pipeline is executed in full on each data-set
- $\chi^2$  for the data left out from the fit

$$\begin{split} \chi^2 &= r^T \mathbf{\Sigma}^{-1} r \\ \mathbf{\Sigma} &= \mathbf{\Sigma}_{\text{exp}} + \mathbf{\Sigma}_{\text{res}} + \mathbf{\Sigma}_{\text{extra}} + \mathbf{\Sigma}_{\text{GP}} \end{split}$$



#### Cross-validation - results

- Overall good performance.
- Indicates that the automated procedures perform well.
- A slight tendency to overestimate uncertainties is noted.



DATASET	ndf	$\chi^2$	$\chi^2/ndf$
1	1731	1735.56	1.00
2	1731	1732.94	1.00
3	1729	1755.52	1.02
4	1730	1498.83	0.87
5	1730	1659.85	0.96
sum	8651	8378.70	$0.97{\pm}0.02$





#### Outlook: Low-energy structure

Energy-dependent Talys parameters cannot reproduce rapid variation in low energy region (1-5 MeV).

The evaluation must respect the sum-rules.





#### Construction of a Defect model

Sum-rules are defined in accordance with TALYS notation

$$\sigma_{ ext{tot}} = \sigma_{ ext{el}} + \sigma_{ ext{non-el}}$$
 $\sigma_{ ext{non-el}} = \sum_{n} \sum_{p} \sum_{d} \sum_{t} \sum_{h} \sum_{\alpha} \sigma^{ ext{ex}}(n, p, d, t, h, lpha)$ 

- An energy grid is chosen, on which the evaluation is to be performed.
  - Intermediate energies are linearly interpolated.
  - At each energy one 'parameter' per **open** exclusive cross-section is introduced.
- From the parameters other cross-sections can be calculated, for example

$$\sigma_{(n,xn)} = \sum_{n} \sum_{p} \sum_{d} \sum_{t} \sum_{h} \sum_{\alpha} n \sigma^{ex}(n, p, d, t, h, \alpha)$$



#### Using the Defect model

The sum-rules constitutes a linear model, whose output is fully represented by

 $\varepsilon_m = \mathbf{J}\beta$ 

where  $\beta$  is the vector of exclusive cross-sections on the chosen energy grid.

This simple construction is intended to be used to model the residual of the TALYS fit, i.e. the data vector is modeled

$$\mathbf{D} = \mathbf{f}(\mathbf{x}; \mathbf{p}) + \varepsilon + \varepsilon_m,$$

where **f** is the TALYS output,

- $\varepsilon$  is the experimental uncertainty and
- $\varepsilon_m$  is the defect model



#### Gaussian Process on the Defect model

The vector  $\boldsymbol{\beta}$  is then placed under a Multi-variate normal prior.

 $\beta \sim \mathcal{N}(0, \mathbf{K}) \quad \{\mathbf{K}\}_{i,j} = \nu K_l(E_i, E_j)$ 

- Exclusive cross-sections are considered uncorrelated.
- Within each exclusive channel, prior correlation is parameterized based on the energy distance by a covariance function  $K_l(E_i, E_j)$ .



In other words: Energy dependence of the exclusive cross-sections is modeled using a Gaussian Process.



### A first test... on $^{56}\mathrm{Fe}$



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### Summary

- We are developing a pipeline for evaluation of the fast energy range
  - based around the TALYS code system
  - implements automated procedures for
    - treatment of inconsistent experimental data
    - treatment of model defects
    - new treatment of resonance structure based on heteroscedastic GP
  - designed for fully reproducible ND evaluations
  - capability to take advantage of large-scale parallel computing
- Application of the pipeline on <sup>52</sup>Cr has been presented
  - cross-validation shows that the model, the automated correction procedures, and the treatment of model defects work well





#### Thank's for the attention!



#### Gaussian Process on the Defect model

The covariance matrix that represents the MVN prior on the model parameters is block diagonal, with one block per open exclusive channel

$$\mathsf{K} = \left[ egin{array}{ccc} \mathsf{K}_1 & & & \ & \ddots & & \ & & & \mathsf{K}_k \end{array} 
ight]$$

The model parameters and experimental data are then joint normally distributed. The full covariance matrix consists of four blocks

$$\boldsymbol{\Sigma} = \left[ \begin{array}{cc} \boldsymbol{\Sigma}_{11} & \boldsymbol{\Sigma}_{12} \\ \boldsymbol{\Sigma}_{21} & \boldsymbol{\Sigma}_{22} \end{array} \right] = \left[ \begin{array}{cc} \boldsymbol{\mathsf{K}} & \boldsymbol{\mathsf{K}} \boldsymbol{\mathsf{J}}^{\mathcal{T}} \\ \boldsymbol{\mathsf{J}} \boldsymbol{\mathsf{K}} & \boldsymbol{\mathsf{J}} \boldsymbol{\mathsf{K}} \boldsymbol{\mathsf{J}}^{\mathcal{T}} + \boldsymbol{\Sigma}_{\mathsf{exp}} \end{array} \right]$$

By conditioning on the observed residual  $\mathbf{r}$  we can find the conditional mean and covariance of the parameter vector.

$$\overline{\beta} = \mathbf{\Sigma}_{12} \, \mathbf{\Sigma}_{22}^{-1} \, \mathbf{r}, \quad \overline{\mathbf{\Sigma}}_{11} = \mathbf{\Sigma}_{11} - \mathbf{\Sigma}_{12} \mathbf{\Sigma}_{22}^{-1} \mathbf{\Sigma}_{21}$$

