

Spectrum Average Cross Sections (SACS) and its impact on evaluation of neutron standards



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Neutron Standards evaluation (2017)

TABLE II. Neutron Cross Section Standards.

Reaction	Standards Energy Range
H(n,n)	1 keV to 20 MeV
$^3\text{He}(n,p)$	0.0253 eV to 50 keV
$^6\text{Li}(n,t)$	0.0253 eV to 1.4 MeV
$^{10}\text{B}(n,\alpha)$	0.0253 eV to 1 MeV
$^{10}\text{B}(n,\alpha_1\gamma)$	0.0253 eV to 1 MeV
C(n,n)	10 eV to 1.8 MeV
Au(n, γ)	0.0253 eV, 0.2 to 2.5 MeV, 30 keV MACS
$^{235}\text{U}(n,f)$	0.0253 eV, 0.15 MeV to 200 MeV, 7.8-11 eV
$^{238}\text{U}(n,f)$	2 MeV to 200 MeV

reference XS: $^{239}\text{Pu}(n,f)$ 0.15 MeV to 200 MeV



Outline

- Introduction
- SACS: basic concepts and reference spectra
- STD evaluation issues
- Updated SACS-Cf experimental database
- Updated Manhart SACS evaluation
(based on measured SACS in Cf-252(sf) field)
- SACS-U5(nth,f) experimental database and
Manhart evaluation



Basic concepts: SACS in spectrum

SACS-Cf = SACS in Cf-252(sf) PFNS

$$SACS = \frac{\int \sigma(E) \varphi(E) dE}{\int \varphi(E) dE} \int_n \varphi(E) dE \equiv 1$$

$$SACS = \int \sigma(E) \varphi(E) dE \cong \sum_{k=0} \varphi(k) \sigma(k)$$

$$\frac{\partial(SACS)}{\partial \sigma(k)} = \varphi(k)$$

SACS sensitivity to $\sigma(k) =$
spectral weight $\varphi(k)$ @ \mathbf{E}_k

SACS are VERY CLEAN INTEGRAL DATA



IRDFF validation of Cf(sf) and U5(nth,f) neutron fields ~ 40+ reactions

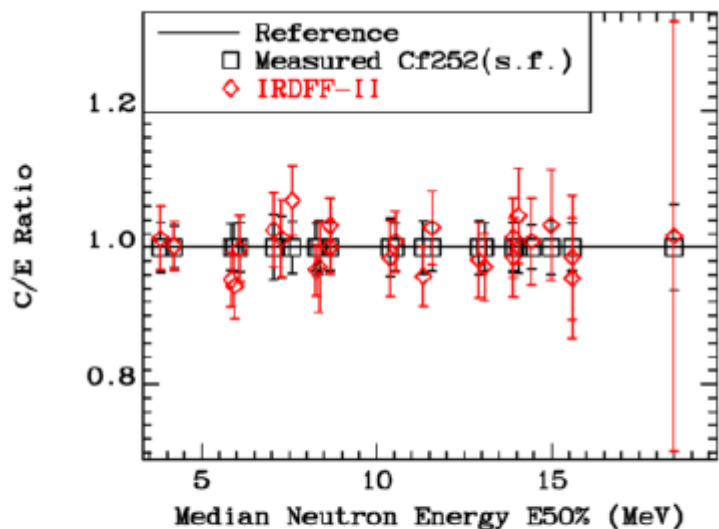


FIG. 123. (Color online) C/E relative to median energy $E_{50\%}$ for the IRDFF-II cross sections averaged in the $^{252}\text{Cf}(s.f.)$ neutron field measured at Řež near Prague. Plotted values are listed in Table 19.

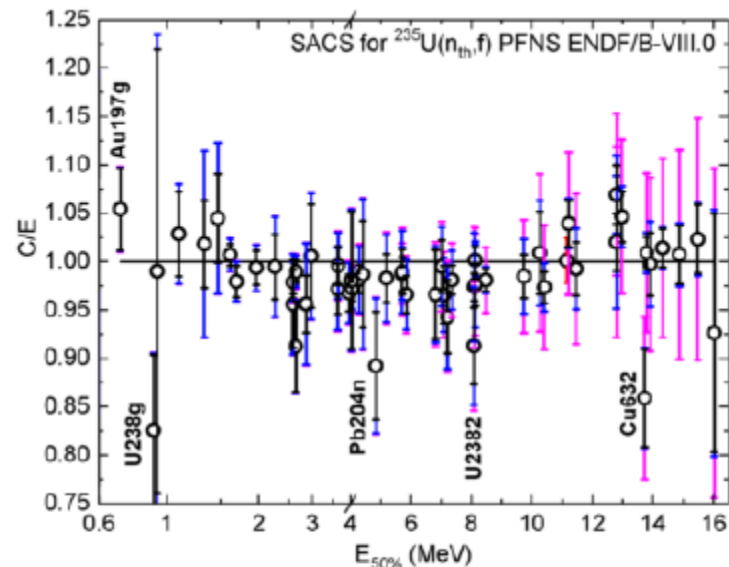
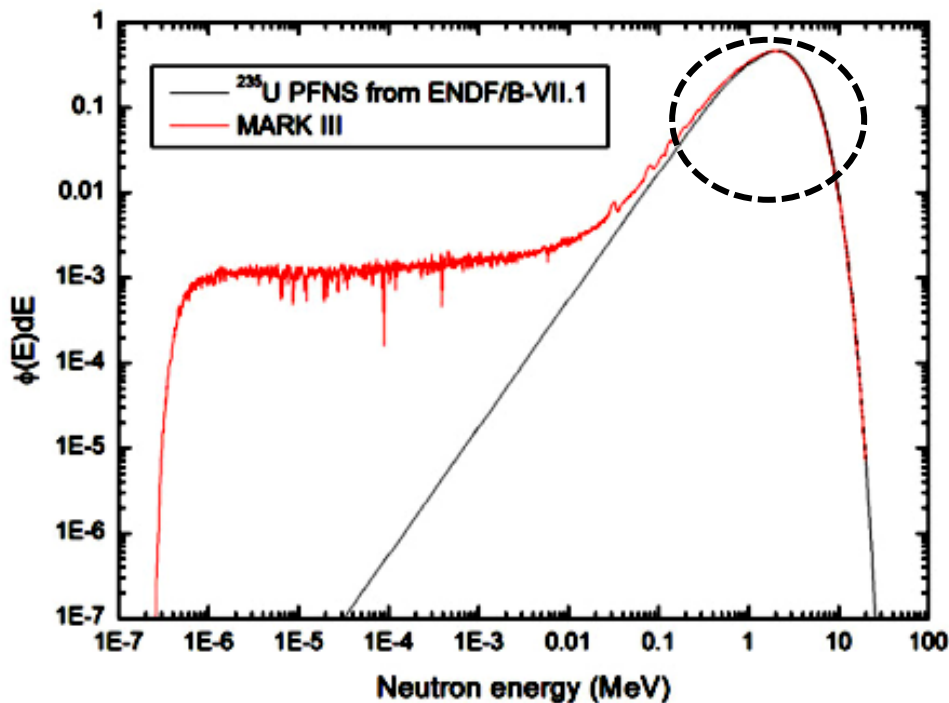
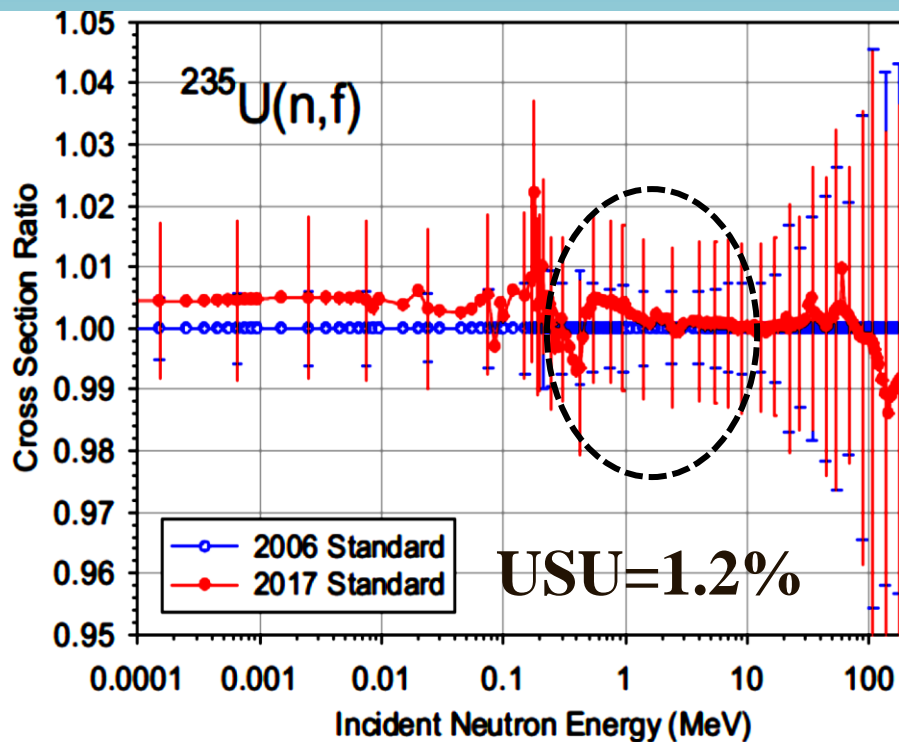


FIG. 124. (Color online) C/E as a function of median energy $E_{50\%}$ for the IRDFF-II cross sections averaged in the $^{235}\text{U}(nth,f)$ PFNS field are shown as circles. Uncertainty bars reflect a r.m.s. combination of uncertainty contributions from the measurement (black), IRDFF-II cross sections (blue) and spectra (pink). Plotted values are listed in Table 20. Only outlying C/E values are labelled with reaction IDs from Table 20.



Neutron Standard & Reference (n,f) XS



A.D. Carlson et al, Nucl. Data Sheets 148, 143 (2018)

J. Wagemans et al, EPJ Web of Conferences 106, 06003 (2016)

**SACS-Cf provide excellent normalization for many E_n energies:
0-10 MeV ~ 99% spectrum, lowest XS uncertainty**

**SACS-Cf provide better normalization than absol. fission XS/ratios
measurements in quasi-monoenergetic beams (USU=1.2% spread)**



SACS-Cf evaluation – updated Mannhart

```

cf dat.dat          Set 1
EXPERIMENT : Heaton + Grundl memo + Grundl-Gilliam + Schroeder + Davis/Knoll
10
1 1 0 1.216E+3 1.6200 U235F GRUNDL MEMO (Rev. Heaton 1976 ABSOL U-235f),indc(nds)-146, p.237
2 1 2 3.73 1.2000 U235F/U238F GRUNDL-GILLIAM indc(nds)-146, p.244, inverse = 0.2681
3 1 3 0.666 0.9000 U235F/PU239F GRUNDL-GILLIAM indc(nds)-146, p.244, inverse = 1.502 (0.9%)
4 3 1 1.500E+0 1.6000 PU239F/U235F Heaton 1976 ANL-76-90 60% ratio correl derived from common ratio uncert.
5 2 1 0.2644 1.3200 U238F/U235F Heaton 1976 ANL-76-90 60% ratio correl derived from common ratio uncert.
6 2 1 0.269E+0 1.2000 U238F/U235F Schroeder JANS 50(1985)154
7 3 1 1.500E+0 0.8000 PU239F/U235F Schroeder JANS 50(1985)154
8 1 0 1.234E+3 1.4500 U235F Schroeder JANS 50(1985)154
9 1 0 1.215E+3 1.7900 U235F Davis/Knoll ANE 5 (1978) 583
10 3 0 1.790E+3 2.2600 PU239F Davis/Knoll ANE 5 (1978) 583

100
23 100
-9 36 100
0 0 0 100
0 0 0 60 100
0 0 0 0 0 100
0 0 0 0 0 77 100
0 0 0 0 0 0 0 100
0 0 0 0 0 0 0 0 100
0 0 0 0 0 0 0 0 59 100

Set 2
EXPERIMENT : ADAMOV
2
1 2 1 2.741E-1 1.6600 U238F/U235F *1.0 ADAMOV
2 3 1 1.475E+0 1.5000 PU239F/U235F *1.0

100
29 100

Set 3
EXPERIMENT : NBS-VNC + SPIEGEL
1
1 2 1 2.491E-1 5.2200 U238F/U235F *2.0

100
    
```

EVAL <SIGMA> in CF-252 (PRIOR VALUES)

3			
1	1.205E+3	50.0000	U-235 (N, F)
2	3.180E+2	50.0000	U-238 (N, F)
3	1.807E+3	50.0000	PU-239 (N, F)
100			
	0	100	
	0	0	100

**SACS exp. data
13 sets**

PRIOR (uninf.)

EVAL <SIGMA> - CF-252

3			
1	1.221E+3	0.9065	U-235 (N, F)
2	3.264E+2	1.0577	U-238 (N, F)
3	1.825E+3	1.0122	PU-239 (N, F)
100			
	81	100	
	88	87	100

**with new data
(13 datasets)**

Pu9(n,f)/U5(n,f) SACS ratio	1.495 (1.8%) Pu9f & U5f ind.
U8(n,f)/U5(n,f) SACS ratio	0.267 (2.0%) U8f & U5f ind.

EVALUATION



SACS–Cf eval. – Mannhart updated

Quantity	Mannhart updated SACS (b)	STD 2017 SACS (b)
U5(n,f) SACS	1.221 (0.9%)	1.2267 (1.21%)
Pu9(n,f) SACS	1.825 (1.0%)	1.7978 (1.25%)
U8(n,f) SACS	0.326 (1.1%)	0.3215 (1.3%)
Pu9(n,f)/U5(n,f) SACS ratio	1.495 (0.7%) no corr:1.8%	1.466 (C/E=0.98)
U8(n,f)/U5(n,f) SACS ratio	0.267 (1.0%) no corr:2.0%	0.262 (C/E=0.98)

EXPERIMENT	
Pu9(n,f)/U5(n,f) Schroeder 1985	1.50 (1) (0.8%)
Pu9(n,f)/U5(n,f) Heaton 1976	1.50 (2) (1.6%)
Pu9(n,f)/U5(n,f) Grundl-Gilliam	1.50 (1) (0.9%)
U8(n,f)/U5(n,f) Grundl-Gilliam	0.268 (3) (1.2%)
U8(n,f)/U5(n,f) Schroeder	0.269 (3) (1.2%)
U8(n,f)/U5(n,f) Heaton 1976	0.264 (3) (1.3%)

```

EVAL <SIGMA> - CF-252
3
1 1.221E+3 0.9065 U-235 (N, F)
2 3.264E+2 1.0577 U-238 (N, F)
3 1.825E+3 1.0122 PU-239 (N, F)
    
```

100		
81	100	
88	87	100

**with new data
(13 datasets)**

Pu9(n,f)/U5(n,f) SACS ratio	1.495 (1.8%) Pu9f & U5f ind.
U8(n,f)/U5(n,f) SACS ratio	0.267 (2.0%) U8f & U5f ind.



- ❑ We used 7 data of U5 & Pu9 SACS-Cf (no ratios !) in STD 2017 evaluation (GMA)
- ❑ Mannhart used activation + 7 SACS fission data
- ❑ Updated GMA-py + 13 data incl. precise ratios -> EVAL

```

EXPERIMENT : Heaton + Grundl memo + Grundl-Gilliam + Schroeder + Davis/Knoll
10
1 1 0 1.216E+3 1.6200 U235F GRUNDL MEMO (Rev. Heaton 1976 ABSOL U-235f),indc(nds)-146, p.237
2 1 2 3.73 1.2000 U235F/U238F GRUNDL-GILLIAM indc(nds)-146, p.244, inverse = 0.2681
3 1 3 0.666 0.9000 U235F/PU239F GRUNDL-GILLIAM indc(nds)-146, p.244, inverse = 1.502 (0.9%)
4 3 1 1.500E+0 1.6000 PU239F/U235F Heaton 1976 ANL-76-90 60% ratio correl derived from common ratio uncert.
5 2 1 0.2644 1.3200 U238F/U235F Heaton 1976 ANL-76-90 60% ratio correl derived from common ratio uncert.
6 2 1 0.269E+0 1.2000 U238F/U235F Schroeder JANS 50(1985)154
7 3 1 1.500E+0 0.8000 PU239F/U235F Schroeder JANS 50(1985)154
8 1 0 1.234E+3 1.4500 U235F Schroeder JANS 50(1985)154
9 1 0 1.215E+3 1.7900 U235F Davis/Knoll ANE 5 (1978) 583
10 3 0 1.790E+3 2.2600 PU239F Davis/Knoll ANE 5 (1978) 583

```

3 abs. U5f, 10 ratios

```

Set 2
EXPERIMENT : ADAMOV
2
1 2 1 2.741E-1 1.6600 U238F/U235F *1.0 ADAMOV
2 3 1 1.475E+0 1.5000 PU239F/U235F *1.0
100
29 100

Set 3
EXPERIMENT: NBS-VNC + SPIEGEL
1
1 2 1 2.491E-1 5.2200 U238F/U235F *2.0
100

```



- ❑ No U5(nth,f) SACS used in STD 2017 evaluation (GMA)
- ❑ Mannhart compiled 3 datasets

```

EXPERIMENT : NBS Smolenice 1983 + Fabry(1978) EXFOR 20947 set_3.dat
3
1 1 0 1.216E+3 1.6100 U-235 (n,f) NBS
2 2 1 1.504E+0 1.6200 Pu-239 (n,f) /U-235 (n,f) Fabry
3 5 1 2.540E-1 2.6900 U-238 (n,f) /U-235 (n,f)
100
0 100
0 0 100
set_2.dat
EXPERIMENT : Fabry(1975) EXFOR 20946
4
1 1 5 3.940E+0 2.0000 U-235 (n,f) /U-238 (n,f) Fabry
2 2 5 5.930E+0 2.1900 Pu-239 (n,f) /U-238 (n,f)
100
0 100
set_8.dat
EXPERIMENT : Grundl(1968) EXFOR 12193 + Leachman(1957) EXFOR 12448
7
1 5 0 3.109E+2 1.6300 U-238 (n,f) Leachman 1957 nu=2.4320
2 1 5 3.850E+0 6.0000 U-235 (n,f) /U-238 (n,f) Grundl 1968
100
0 100

```

SACS in $^{235}\text{U}(n_{th},f)$

**2 abs. U5f,U8f
5 ratios**



SACS-U5(nth,f) eval. – Mannhart

Quantity	Mannhart 2008 eval SACS (b)	STD 2017 SACS (b)
U5(n,f) SACS	1.217 (1.1%)	1.2253 (1.21%)
Pu9(n,f) SACS	1.831 (1.7%)	1.7933 (1.25%)
U8(n,f) SACS	0.3094 (1.1%)	0.3062 (1.2%)
Pu9(n,f)/U5(n,f) SACS ratio	1.504 (~2.0%)	1.463 (C/E=0.973)
U8(n,f)/U5(n,f) SACS ratio	0.254 (~1.6%)	0.250 (C/E=0.98)

EXPERIMENT	
Pu9(n,f)/U5(n,f) Fabry 1978	1.504 (1.6%)
U8(n,f)/U5(n,f) Fabry 1978	0.254 (2.7%)
U8(n,f)/U5(n,f) Fabry 1975	0.254 (2.0%)
Pu9(n,f)/U8(n,f) Fabry 1975	5.93 (2.2%)

```
Chi**2 = 0.914 Data = 3 Iteration = 2

EVAL <sigma> - U-235
 1 1.217E+3 1.1226 U-235 (n,f)
 2 1.831E+3 1.6541 Pu-239 (n,f)
 5 3.094E+2 1.1325 U-238 (n,f)

| 100
 59 100
 63 52 100
```

Mannhart SACS evaluation 2008



SACS-Cf & SACS-U5(nth,f)

EXPERIMENT

Quantity	Mannhart 2008 eval [b] in U5(nth,f)	Mannhart updated SACS [b]
U5(n,f) SACS	1.217(1.1%) (U/Cf=1)	1.221 (0.9%)
Pu9(n,f) SACS	1.831(1.7%) (U/Cf=0.99)	1.825 (1.0%)
U8(n,f) SACS	0.3094(1.1%) (U/Cf=0.99)	0.326 (1.1%)
Pu9(n,f)/U5(n,f) SACS ratio	1.504(~1%) (U/Cf=1.006)	1.495 (0.7%)
U8(n,f)/U5(n,f) SACS ratio	0.254 (U/Cf=0.95)	0.267 (1.0%)

Cf

U5

Pu9(n,f)/U5(n,f) Schroeder 1985	1.50 (1) (0.8%)
Pu9(n,f)/U5(n,f) Heaton 1976	1.50 (2) (1.6%)
Pu9(n,f)/U5(n,f) Grundl-Gilliam	1.50 (1) (0.9%)
U8(n,f)/U5(n,f) Grundl-Gilliam	0.268 (3) (1.2%)
U8(n,f)/U5(n,f) Schroeder	0.269 (3) (1.2%)
U8(n,f)/U5(n,f) Heaton 1976	0.264 (3) (1.3%)

Pu9(n,f)/U5(n,f) Fabry 1978	1.504 (1.6%)
U8(n,f)/U5(n,f) Fabry 1978	0.254 (2.7%)
U8(n,f)/U5(n,f) Fabry 1975	0.254 (2.0%)
Pu9(n,f)/U8(n,f) Fabry 1975	5.93 (2.2%)

SACS-Cf and SACS-U5(nth,f) can be used for the STD fit



SACS-Cf & SACS-U5(nth,f)

EXPERIMENT

Quantity	Mannhart 2008 SACS eval [b]	STD 2017 SACS (b)
U5(n,f) SACS	1.217 (1.1%)	1.2253 (1.26%) 0.36% sp 1.1% reac
Pu9(n,f) SACS	1.831 (1.7%)	1.7933 (1.30%) 0.37% sp 1.2% reac
U8(n,f) SACS	0.3094 (1.1%)	0.3062 (1.4%) 0.75% sp 1.2% reac

U5

Pu9(n,f)/U5(n,f) Fabry 1978	1.504 (1.6%)
U8(n,f)/U5(n,f) Fabry 1978	0.254 (2.7%)
U8(n,f)/U5(n,f) Fabry 1975	0.254 (2.0%)
Pu9(n,f)/U8(n,f) Fabry 1975	5.93 (2.2%)

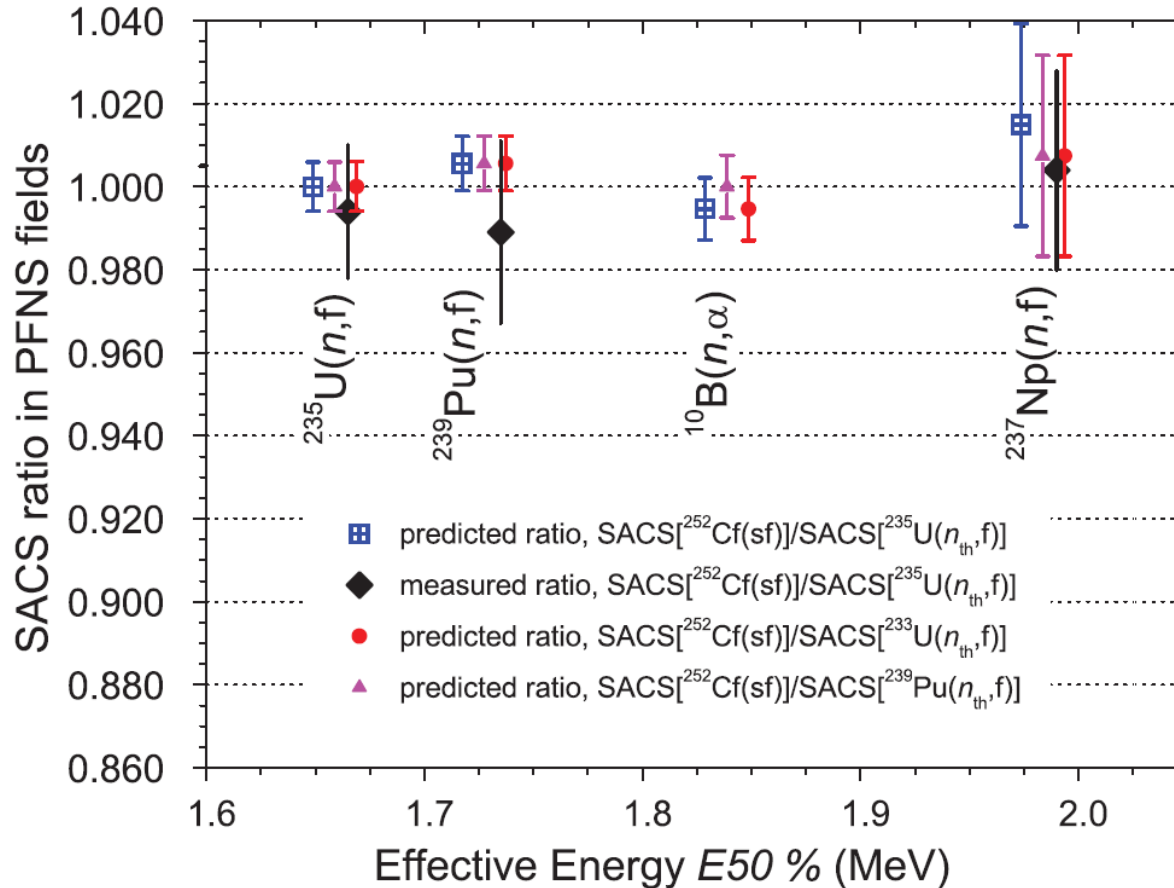
Capote, R. and Trkov, A., "Predicting Spectrum Averaged Cross Sections in Prompt Fission Neutron Fields," *Reactor Dosimetry: 16th International Symposium, ASTM STP1608*, M. H. Sparks, K. R. DePriest, and D. W. Vehar, Eds., ASTM International, West Conshohocken, PA, 2018, pp. 117-123, <http://dx.doi.org/10.1520/STP160820170114>²

SACS-Cf and SACS-U5(nth,f) can be used for the STD fit

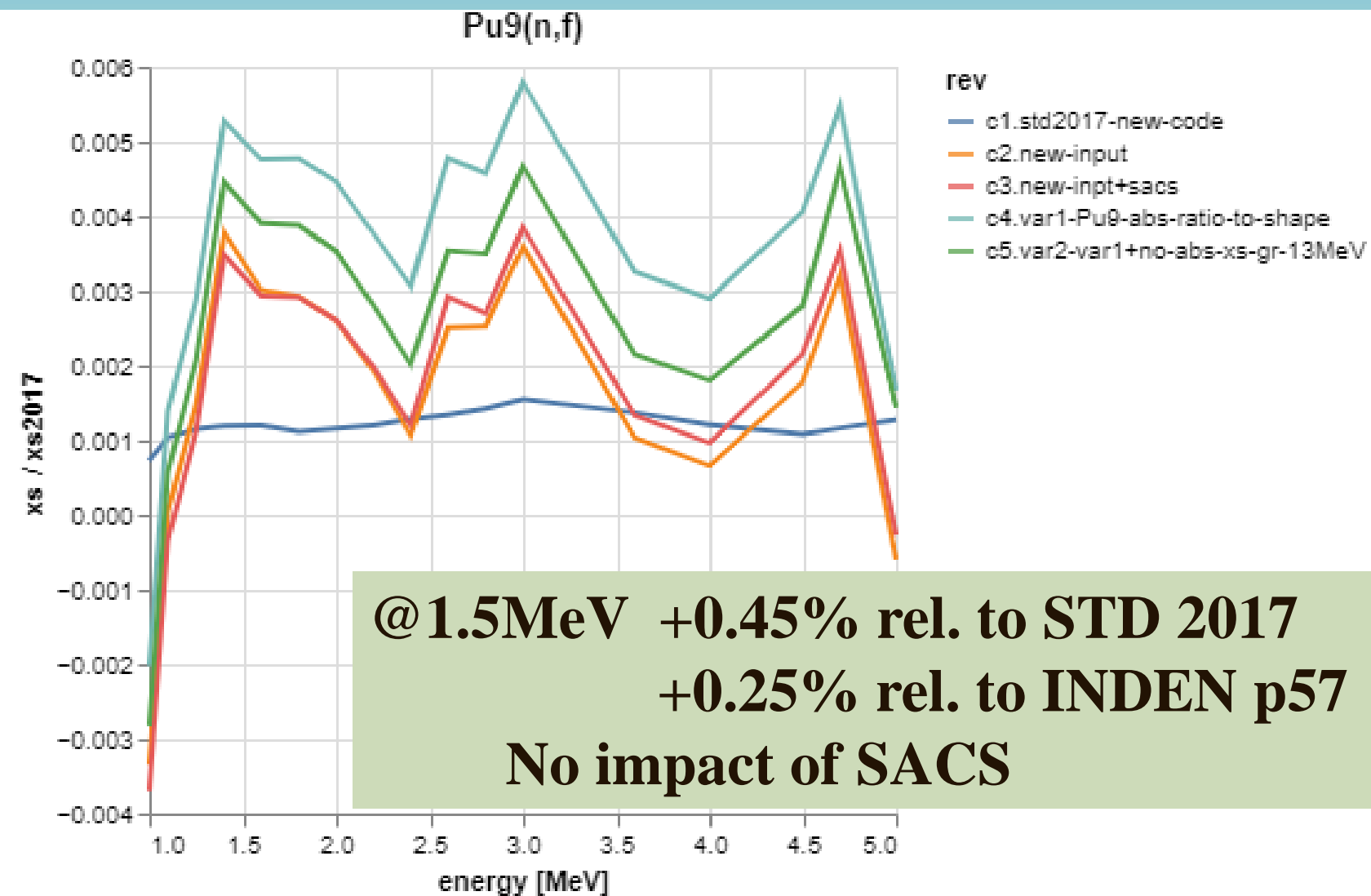


SACS(nf) independent of the PFNS

Capote, R. and Trkov, A., "Predicting Spectrum Averaged Cross Sections in Prompt Fission Neutron Fields," *Reactor Dosimetry: 16th International Symposium, ASTM STP1608*, M. H. Sparks, K. R. DePriest, and D. W. Vehar, Eds., ASTM International, West Conshohocken, PA, 2018, pp. 117-123, <http://dx.doi.org/10.1520/STP160820170114>²



Pu9f reference: 2017 vs current – GMA-py



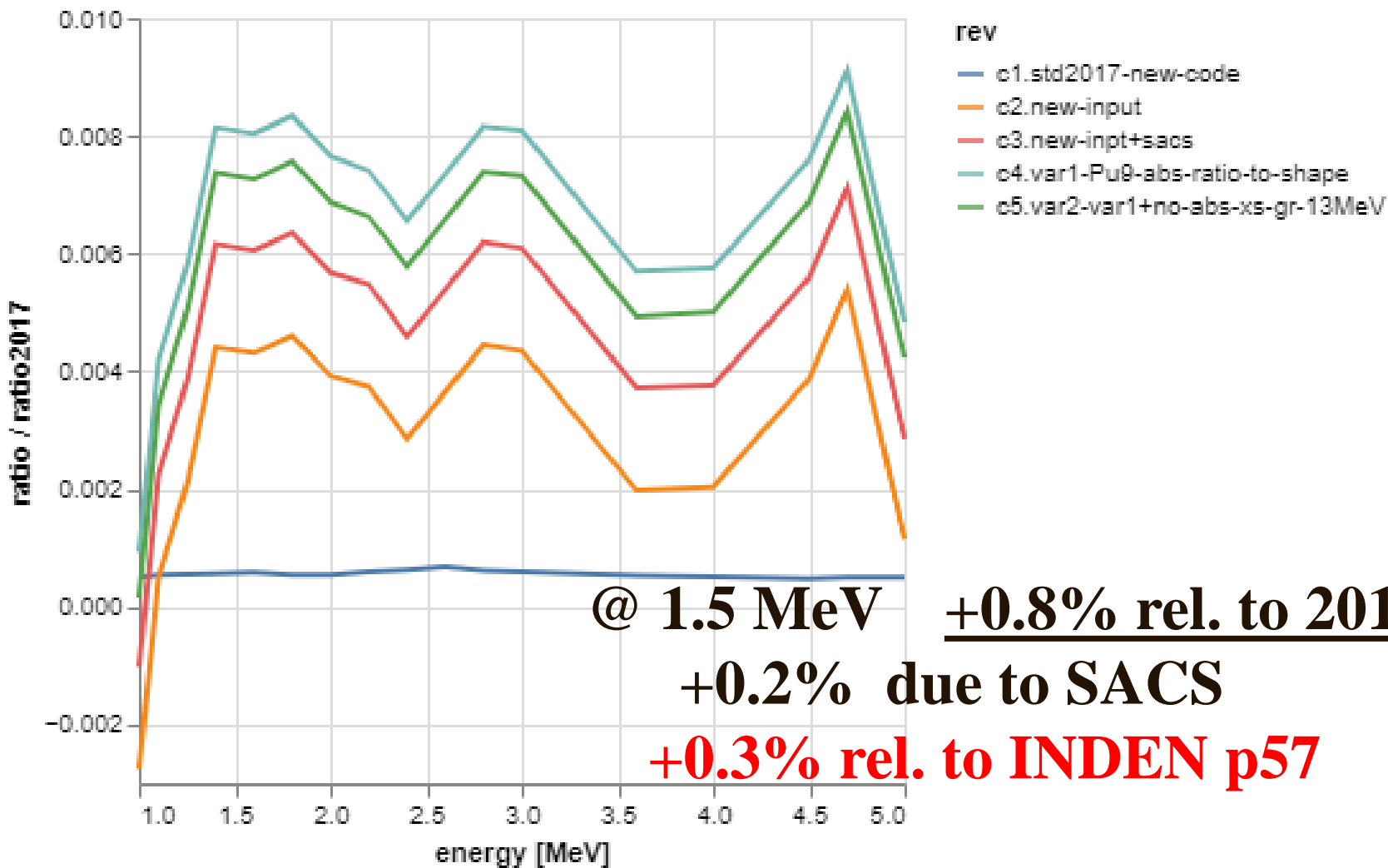
Summary and conclusions

- ✓ SACS in ref. spectra -a key for STD (n,f) normalization
- ✓ STD 2017 show similar problems in both refer. spectra
- ✓ 13 SACS-Cf datasets identified and used
- ✓ Mannhart identified 7 SACS-U5(nth,f) data
- ✓ Use of SACS-U5 data planned
- ✓ Impact of the spectrum uncertainty on SACS(nf) very small

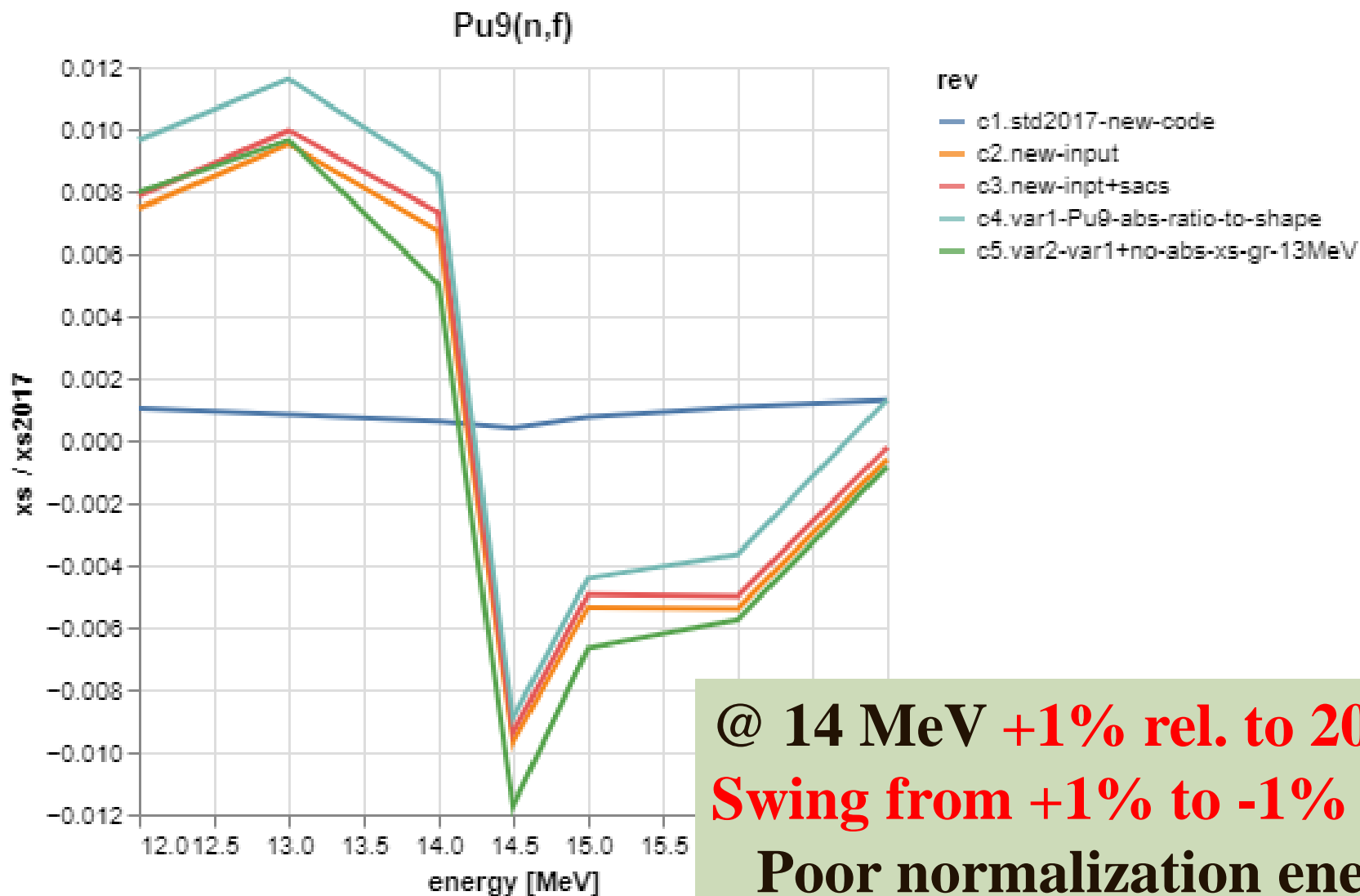


Pu9f/U5f: 2017 vs current – GMA-py

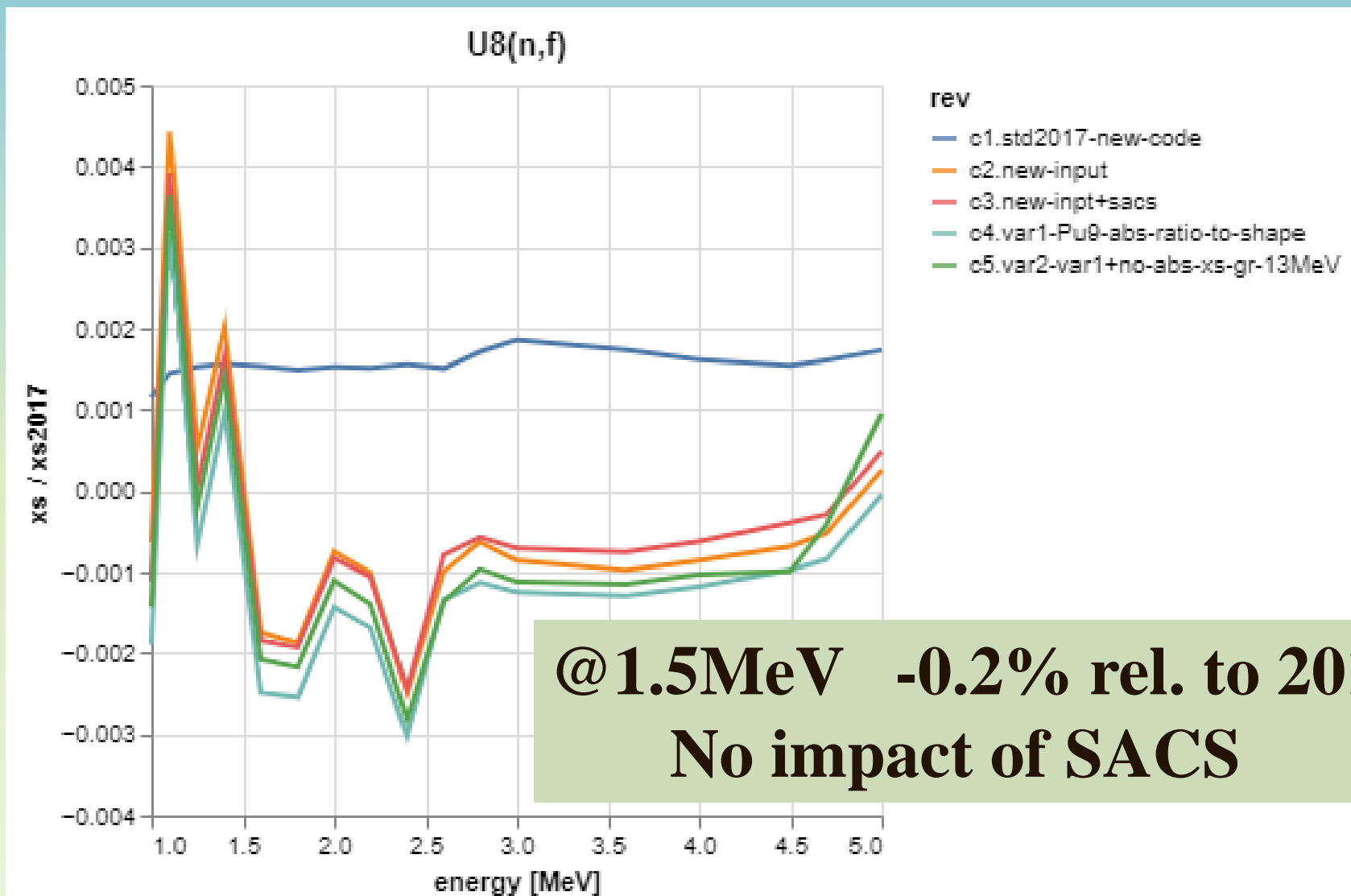
Pu9(n,f) / U5(n,f)



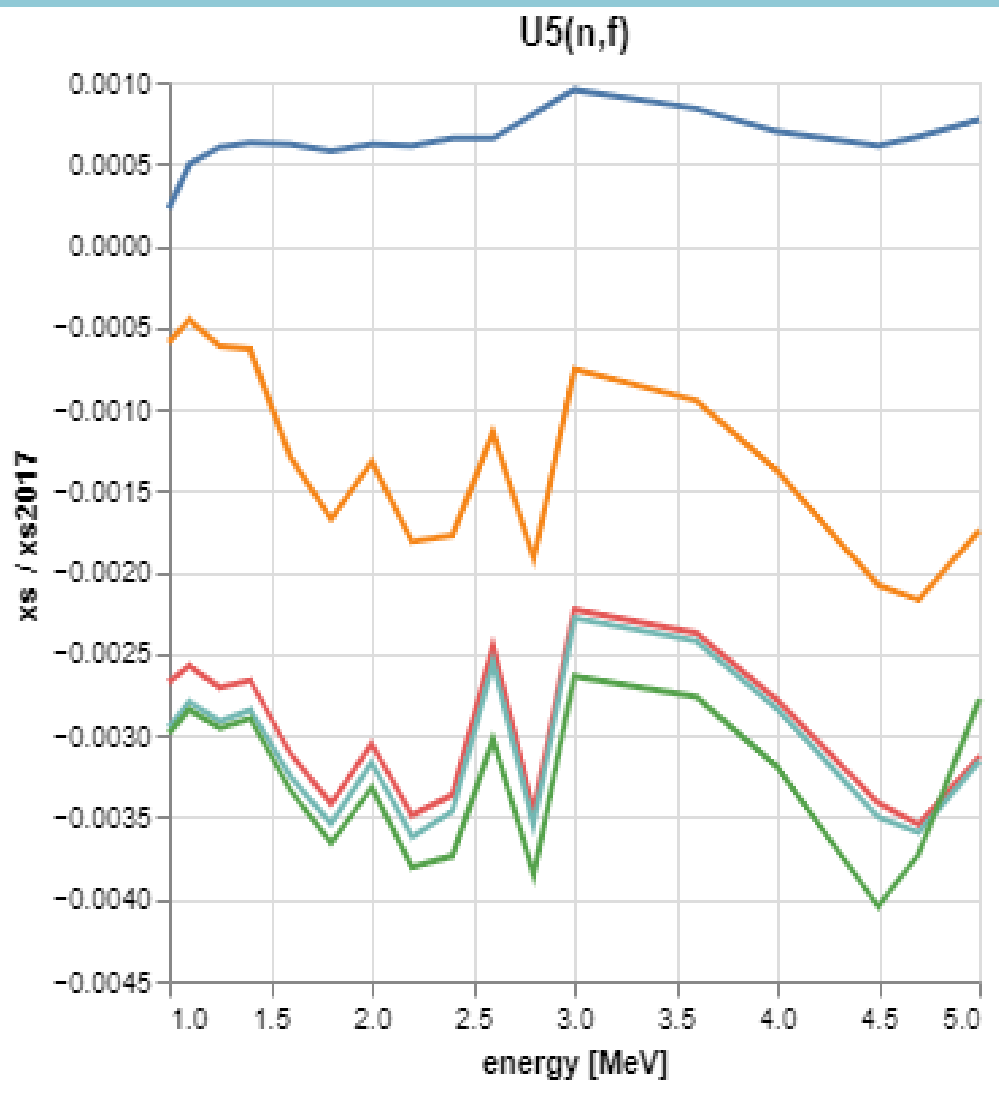
Pu9f/U5f: 2017 vs current – GMA-py



U8f standard: 2017 vs current – GMA-py



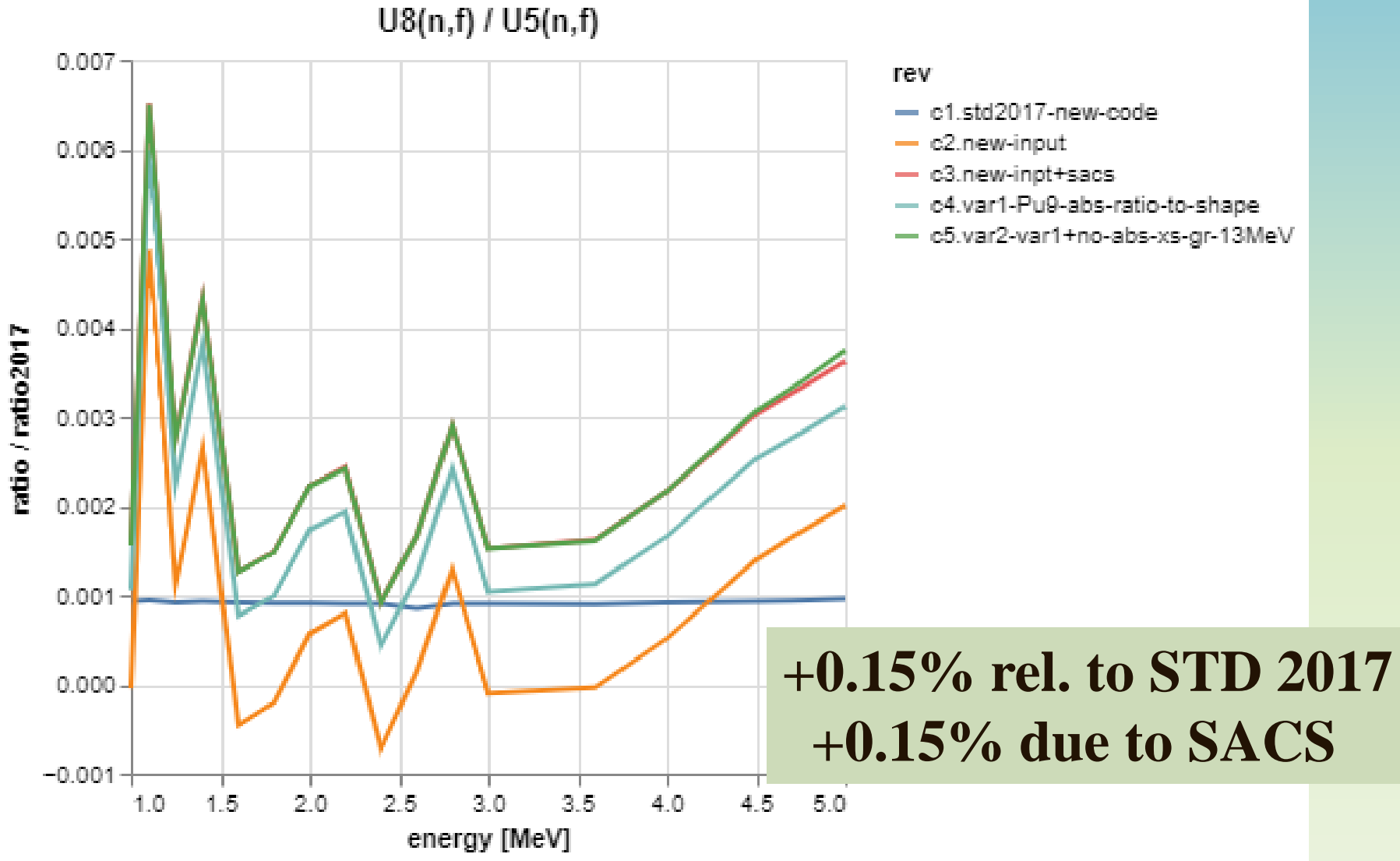
U5f standard: 2017 vs current – GMA-py



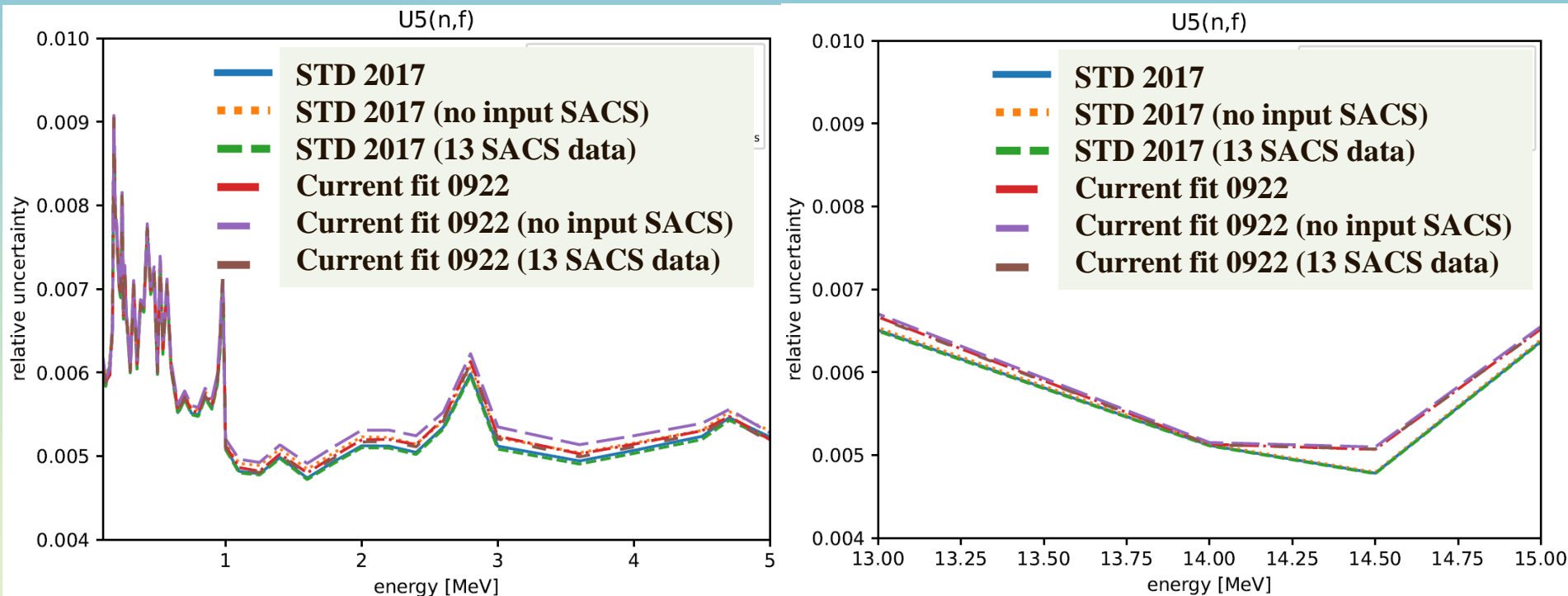
-0.3% rel. to STD 2017
-0.15% reduction
due to new SACS



U8f/U5f: 2017 vs current – GMA-py



U5f uncert.: 2017 vs current – GMA-py

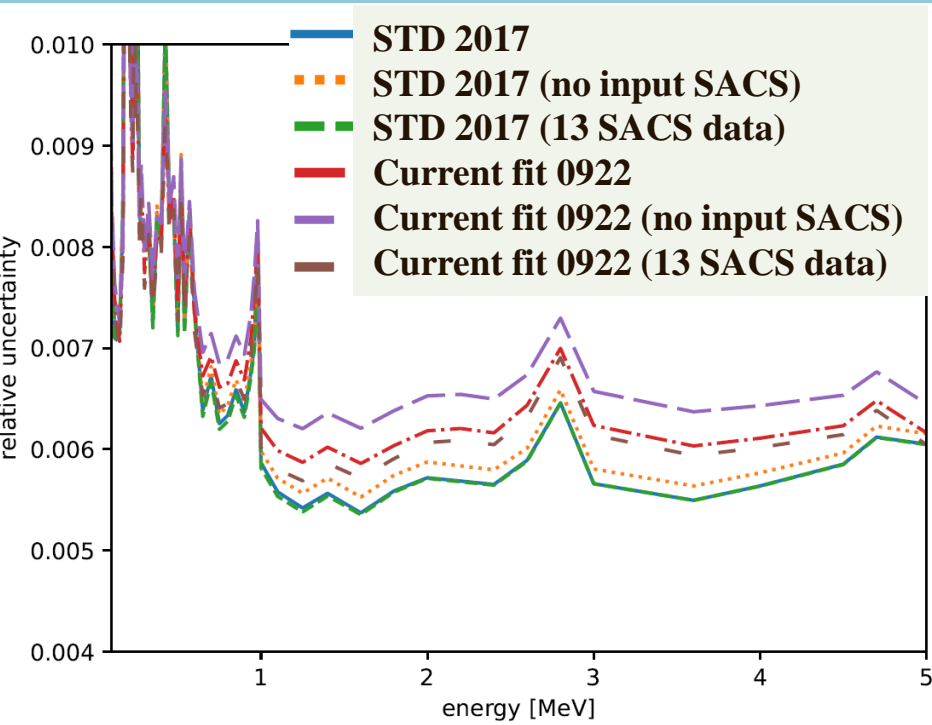


Last unc. 0.5-5 MeV ~0.5%-0.55% Last unc. 13-15MeV ~0.5%-0.65%

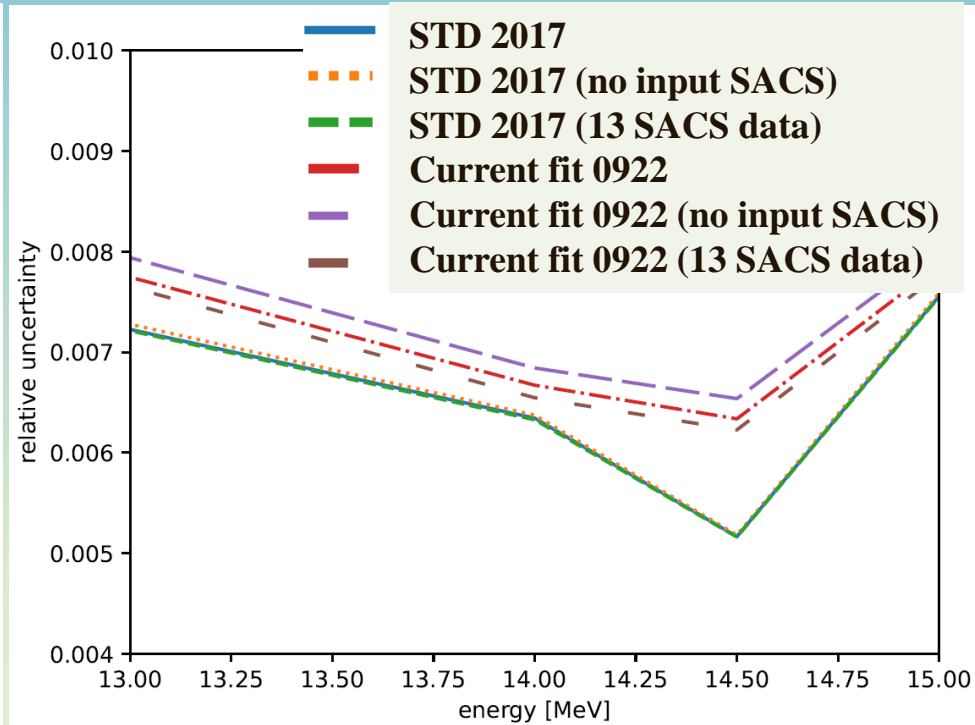
U5f uncert. at ~1.5 and ~14 MeV very similar



Pu9f uncert.: 2017 vs current – GMA-py



Last unc. 0.5-5 MeV ~0.6%-0.7%



Last unc. 13-15MeV ~0.7%-0.8%

Pu9f uncert. at ~1.5 slightly lower than at 14 MeV

