



Photon strength function modelling, status and perspectives.

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What is a Photon Strength Function ?

Photon Strength Function (PSF) = Gamma-ray Strength Function (GSF)



What is a Gamma-ray Strength Function ?





Global knowledge of nuclear excitations

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Electromagnetic excitations and shape oscillations

The multipole order *L* of the transition follows the selection rules: $|I_f - I_i| \le L \le I_f + I_i$



Electromagnetic excitations and shape oscillations

The multipole order *L* of the transition follows the selection rules: $|I_f - I_i| \le L \le I_f + I_i$



Electromagnetic excitations, Isospin scalar versus isospin vector

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Assumptions and systematic behaviour

Brink hypothesis (1955): The downward strength function on each excited state is equal to the photo-excitation strength function on the GS



Reaction theory relates the γ -ray transmission coefficient for excited states to the ground state photoabsorption assuming the giant resonance to be built on each excited state, although γ -decay strength functions are expected to depend on the temperature T_f of the final states, which is a function of the excitation energy of de-excited nucleus $E_f = E_i - \varepsilon_{\gamma}$



At first approximation, the gamma-ray strength function is mostly related to the dipole mode IVGDR (= γ absorption)

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Gamma-ray strengths : qualitative aspects from photoabsorption



Countesy of S. Hilaire

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Gamma-ray strengths : qualitative aspects from photoabsorption



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Gamma-ray strengths : qualitative aspects from photoabsorption



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2 Some Gamma-ray strength models

Focus on models able to provide systematics: input list of Talys code



Gamma-ray strength function = Talys input

Various options in Talys for various Gamma-ray strengths:

Phenomenological or analytic form

- strength = 1 : GLO model
- strength = 2 : SLO model
- strength = 3 : Skyrme-HFBCS + QRPA
- strength = 4 : Skyrme-HFB + QRPA
- strength = 5 : Hybrid model
- strength = 6 : *T*-dependent Skyrme-HFB + QRPA
- strength = 7 : *T*-dependent RMF-HFB + QRPA
- strength = 8 : Gogny-HFB + QRPA
- strength = 9 : SMLO
- strength =10 : T-dependent BSk27-HFB + QRPA





Standard Lorentzian (SLO)

Generalized Lorentzian (GLO)

Hybrid Model

[S. Goriely 1998]

Similar to GLO for GDR with an improved description of the low energy GDR tail following the fermi liquid model of Kadmenskii et al (1987).



For axially deformed nuclei, the GLO, SLO and Hybrid strength is split into 2 Lorentzians !

The Simplified M1 Lorentzian Model (SMLO) 2019

$$\overrightarrow{f_{M1}}(\varepsilon_{\gamma}) = \frac{1}{3\pi^{2}\hbar^{2}c^{2}}\sigma_{sc}\frac{\varepsilon_{\gamma} \Gamma_{sc}^{2}}{(\varepsilon_{\gamma}^{2} - E_{sc}^{2})^{2} + \varepsilon_{\gamma}^{2}\Gamma_{sc}^{2}} + \frac{1}{3\pi^{2}\hbar^{2}c^{2}}\sigma_{sf}\frac{\varepsilon_{\gamma} \Gamma_{sf}^{2}}{(\varepsilon_{\gamma}^{2} - E_{sf}^{2})^{2} + \varepsilon_{\gamma}^{2}\Gamma_{sf}^{2}}$$

Scissors mode for deformed nuclei

Spin-Flip mode

where the SMLO M1 properties are inspired from the D1M+QRPA predictions

$$\overleftarrow{f_{M1}}(\varepsilon_{\gamma}) = \overrightarrow{f_{M1}}(\varepsilon_{\gamma}) + C \exp(-\eta \varepsilon_{\gamma})$$

M1 upbend for de-excitation

...

where the upbend properties are inspired from the Shell Model predictions

 $C = 3.5 \ 10^{-8} \exp(-6\beta_2) \ \text{MeV}^{-3}$ n = 0.8 Schwengner et al. 2017 Sieja 2017 Midtbø et al. 2018 Presence and impact of possible low-energy M1 upbend: Violation of the Brink Hypothesis!

$$\vec{f}_{E1}(\varepsilon_{\gamma}) \neq \vec{f}_{E1}(\varepsilon_{\gamma})$$
$$\vec{f}_{E1} = \vec{f}_{E1}(\varepsilon_{\gamma}, T_{f})$$







Gamma-ray strength function = Talys input

Various options in Talys for various Gamma-ray strengths:

Contains microscopic ingredients

- strength = 1 : GLO model (Kopecky & Uhl 1990)
- strength = 2 : SLO model
- strength = 3 : Skyrme-HFBCS + QRPA
- strength = 4 : Skyrme-HFB + QRPA
- strength = 5 : Hybrid model
- strength = 6 : T-dependent Skyrme-HFB + QRPA
- strength = 7 : T-dependent RMF-HFB + QRPA
- strength = 8 : Gogny-HFB + QRPA
- strength = 9 : SMLO 2019
- strength =10 : T-dependent BSk27-HFB + QRPA



What is the standard QRPA approach ?

The (Q)RPA methods describe nuclear excited states for all multipoles and both parities, whatever the intrinsic deformation of the ground state.

Quadrupole, octupole and higher multipolarities can be obtained even on top of spherical shapes.





What is the standard QRPA approach?

The (Q)RPA methods describe nuclear excited states for all multipoles and both parities whatever the intrinsic deformation of the ground state.

No rotational motion included even for deformed nuclei !

Linear response, i.e. harmonic potential approximation

Main approximation:



Generally, the discrete spectra is folded with a Lorentzian function $f_L(E, E_i, \gamma_i) = \frac{2}{\pi} \frac{\gamma_i E^2}{(E^2 - E_i^2)^2 + \gamma_i^2 E^2}$ Most of the "RPA" based gamma strength function models impose the spherical invariance. For deformed nuclei, phenomenological split of the IVGDR with SLO, GLO and hybrid recipe. $E_{\rm GDR}^1 + 2E_{\rm GDR}^2 = 3E_{\rm GDR}$ $E_{\rm GDR}^2 / E_{\rm GDR}^1 = 0.911\eta + 0.089$ n being ratio between symmetry and perpendicular radii cea

Microscopic systematic with "spherical" QRPA



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QRPA approach for intrinsic deformed nuclei Dynamic deformations versus intrinsic (static) ones

The axially-symmetric-deformed QRPA approach (ISAAC code) using matrix representation allows to provide excited state wave functions, excitation energies as well as transitions probabilities and densities from the GS to excited states and reverse.

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ISAAC describes excited states, transition probabilities for intrinsically deformed nuclei with axial symmetry. [S. Péru and M. Martini, Eur. Phys. J. A (2014) 50: 88] And the results are:



D1M HFB+QRPA in axial symmetry applied to E1 and M1 strength



Magnetic and electric modes on the same footing



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Gamma-ray strengths: D1M(0lim) versus analytical



S. Goriely et al, EPJA (2019) 55: 172



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Alternative resolution of QRPA equations



QFAM results

Luis Gonzalez-Miret Zaragoza, PhD Nov2024

RHB +QFAM, DD-PC1 using the program DIRQFAM v2. 0.0 [Bjelčić, A., & Nikšić, T. (2023), Computer Physics Communications, 287, 108689.]



"Ab-initio" interaction: Chiral QFAM results

PAN@CEA collaboration

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Luis Gonzalez-Miret Zaragoza, PhD Nov2024



Chiral interaction: Hüther, T., Vobig, K., Hebeler, K., Machleidt, R., & Roth, R. (2020). Family of chiral two-plus three-nucleon interactions for accurate nuclear structure studies. Physics Letters B, 808, 135651.4

3-body to 2-body reduction method: Frosini, M., Duguet, T., Bally, B., Beaujeault-Taudière, Y., Ebran, J. P., & Somà, V. (2021). In-medium k-body reduction of n-body operators: A flexible symmetry-conserving approach based on the sole one-body density matrix. *The European Physical Journal A*, *57*(4), 151.

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Time-Dependent Density Functional Theory

see the poster of Paul Stevenson







5 minutes in the nuclear structure world



L. Gaudefroy, S. Péru, et al, PRC97, 064317 (2018)



What is the nature of these J=4 isomers?



No calculated half-live reproduces the experimental one.

A very small K=1 component in the wave function would explain the observations.

There are 3 main mechanisms for K admixture :
F. G. Kondev, G.D. Dracoulis and T. Kibedi, ADNDT 103, 50 (2015)
High level density
Triaxial shape
Mixing with Coriolis interaction



T ½ ns	¹⁶⁰ Nd	¹⁶² Sm	¹⁶⁴ Gd	¹⁶⁶ Dy	¹⁶⁸ Er	¹⁷⁰ Yb	¹⁷² Hf
Exp.	1670(210)	1780(70)	605(30)	?	109(7)	370(15)	~1
QRPA	6970	11105	3980	285	365	260	1,5
QRPA/Exp.	4,17	6,24	6,57	?	3,35	0,703	1,5

L. Gaudefroy, S. Péru, et al, PRC97, 064317 (2018)

More transition probabilities are now available

Low energy spectroscopy in spherical nuclei : $2^+_2 \rightarrow 2^+_1$ and $4^+_1 \rightarrow 2^+_1$ transition probabilities





Theoretical description of « up-bend » : increase of γ -ray strength function at low energy





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3 Some perspectives for γ-ray strength functions

Going back to the photon strength function definition !



Absorption versus decay



E1

≻Eγ

 $F(E_{\gamma}, E_{exc}1)$

M1

 $F(E_{\gamma}, E_{exc}1)$

The γ-ray strength function depends on the excitation energy and on the level density















Absorption versus gamma decay, again...















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Rotational bands in deformed nuclei

 $E_J = E_K + E_{rot}$ with $E_{rot} = \frac{J(J+1) - K^2}{2I_x(Z,N)}$

Gamma emission in deformed nuclei

Intra band transition probability calculations

Inter band transition probability calculations

Gamma emission in deformed nuclei

Intra band transition probability calculations

Inter band transition probability calculations

Gamma emission in deformed nuclei

Intra band transition probability calculations

Inter band transition probability calculations

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E1 Folding procedure

De-excitation PSF at an initial energy U_i

 $f_{XL}(E_{\gamma}U_i) = \sum_{J_{i,\pi i}} f_{\text{conv}} < B(XL) > (E_{\gamma}U_{ij}J_{ij},\pi_i) \rho(U_{ij}J_{ij},\pi_i)$

Reciprocity theorem $\overrightarrow{f_{XL}}(E_{\gamma}) = \overleftarrow{f_{XL}}(U_i, E_{\gamma})$

De-excitation PSF at $U_i = E_{\gamma}$ after folding should correspond to the smooth (after folding) photo-absorption PSF at E_{γ} f_{E1} de-excitation PSF before folding

Courtesy of S.Goriely

E1 Folding procedure

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Comparison with Oslo data

A little recap

- Microscopic ingredients improve the gamma-ray strength function models
- >Many photo-absorption based on QRPA are obtained for various interactions.
- >Beyond standard QRPA approaches are promising for future systematics (QPM, ab inito);

Shell Model can be competitive for light systems;

- TDDFT cam provides photo absorption for many system up to heaviest and deformed ones.
- >K mixing for isomer description: probabilities of transitions between QRPA excited states are needed.
- >Intra-band and inter-band transition probabilities beyond standard QRPA are now accessible.
- > work still in progress to improve γ -strength functions with microscopic inputs.

 $F(E\gamma) \rightarrow F(E\gamma, Ex) \rightarrow F(E\gamma, Ex, \delta Ex, J, \pi)$

Thanks for your attention