

New experimental techniques to inform
neutron-induced reaction cross sections on rare isotopes
with surrogate reactions

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Compound-Nuclear Reactions and Related Topics (CNR*24)

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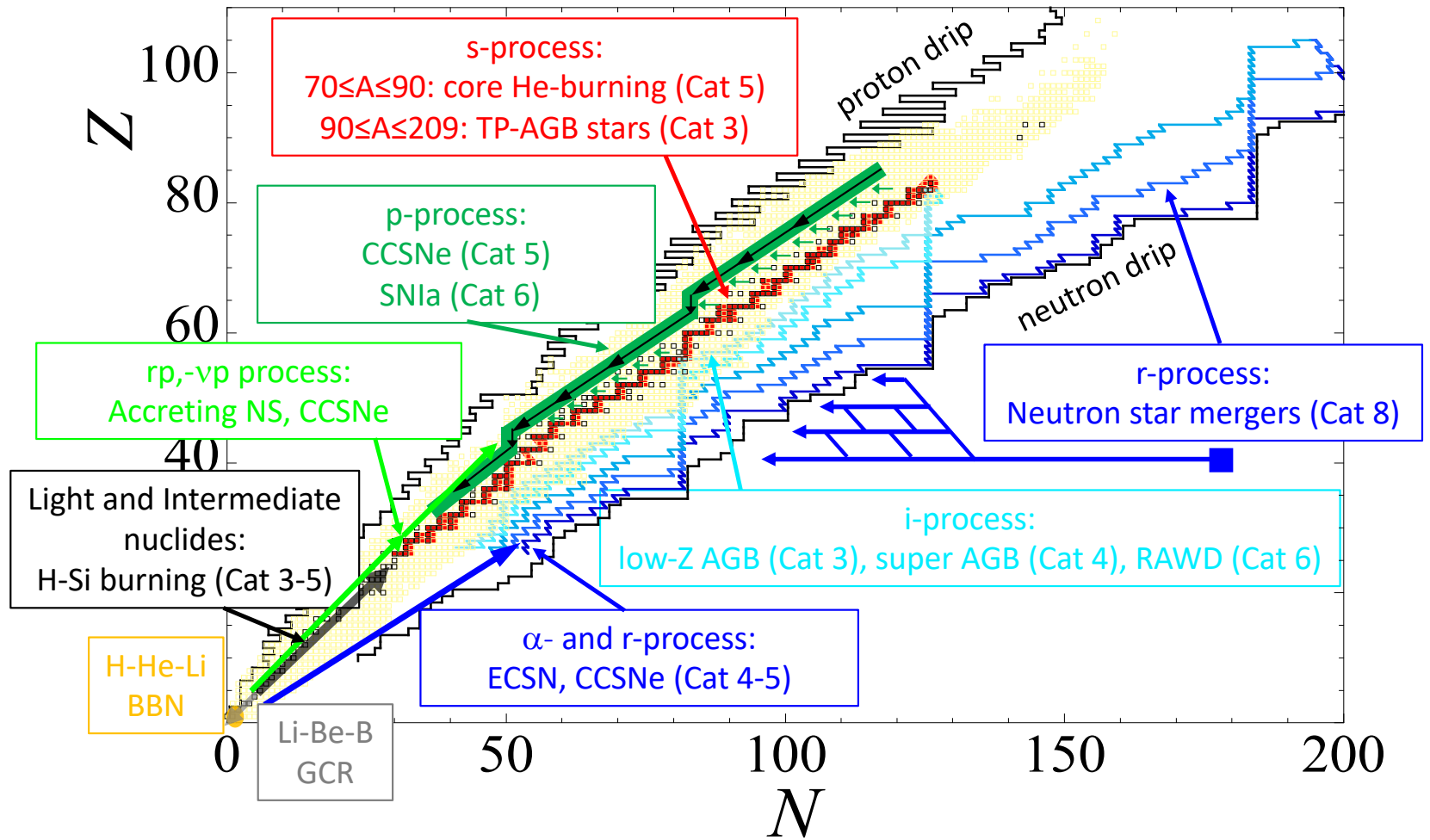
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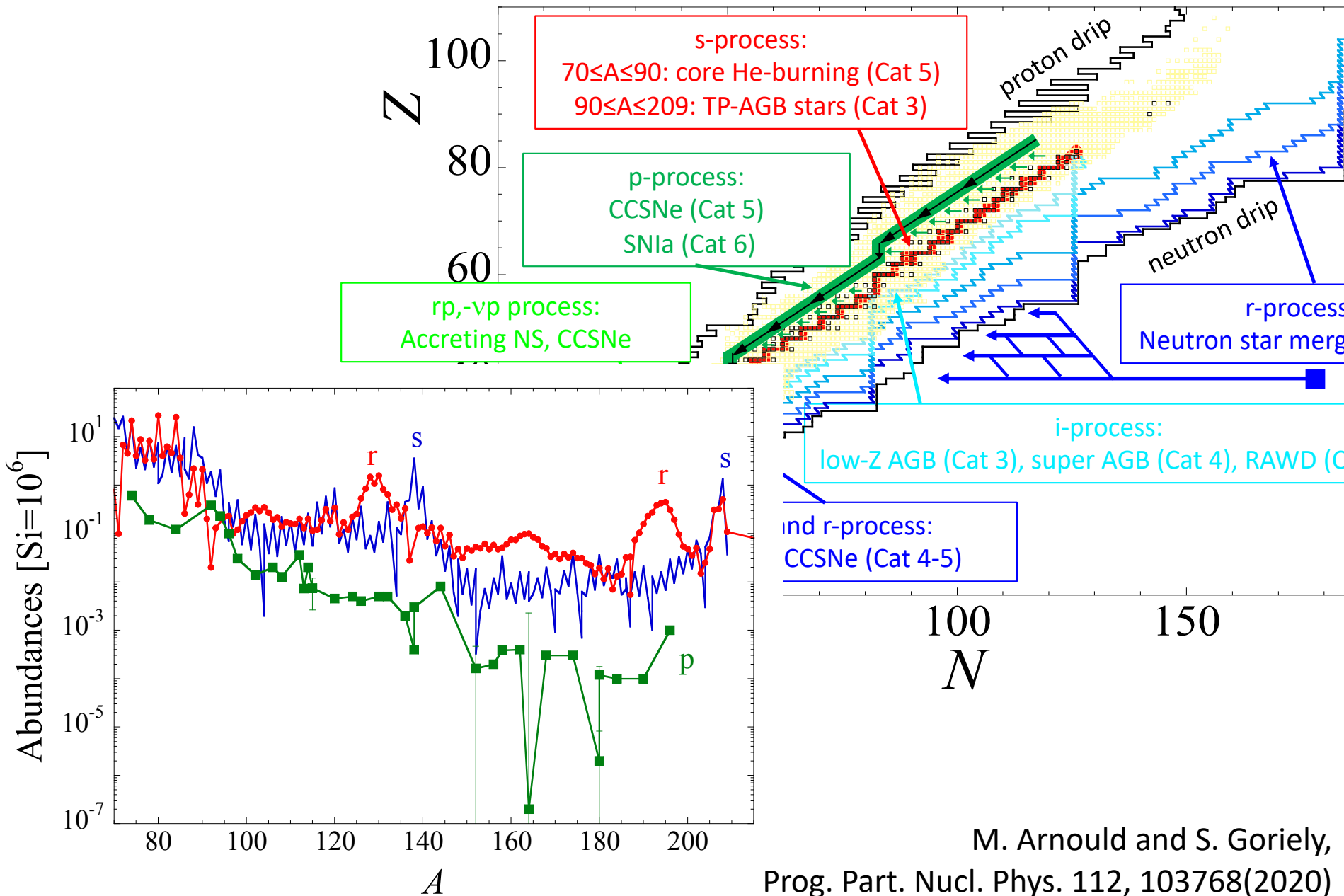
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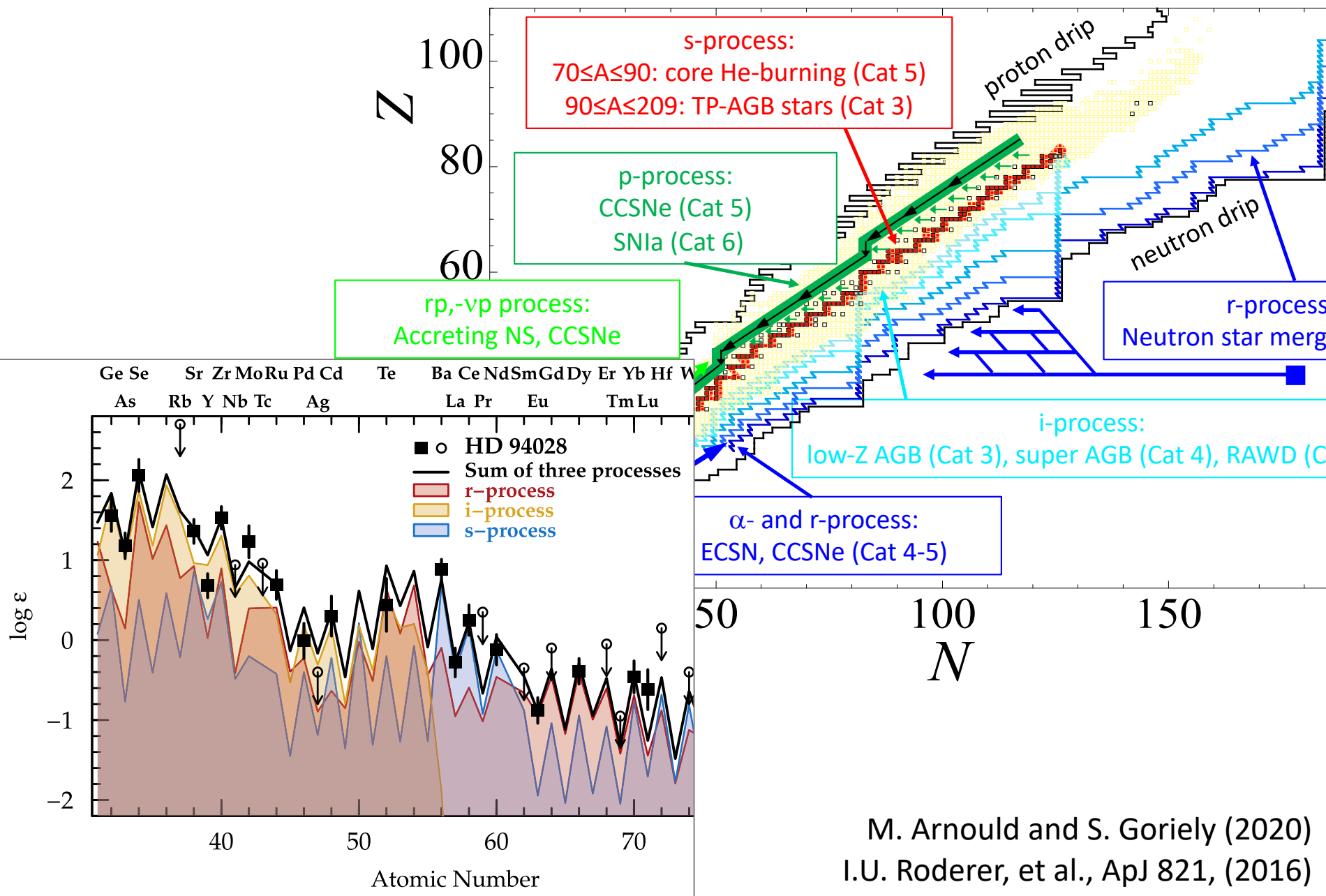


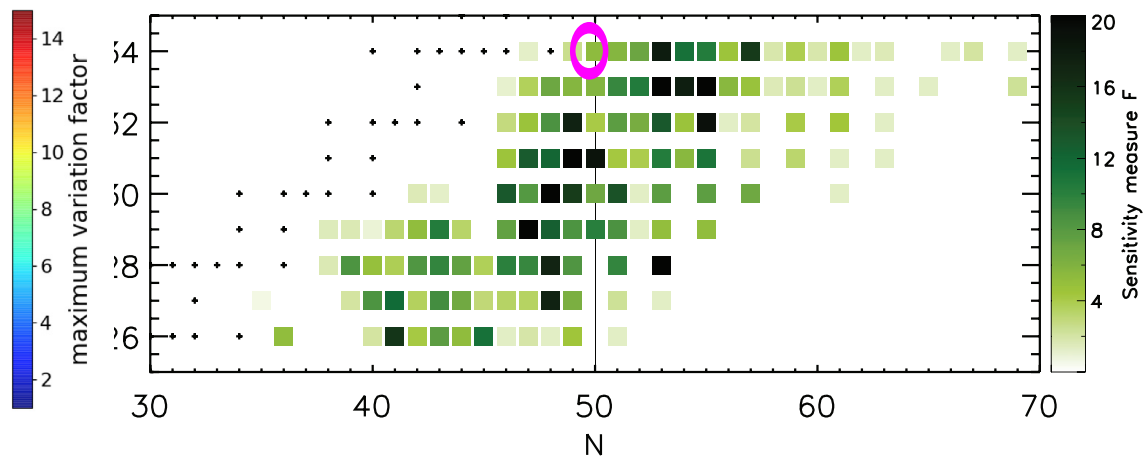
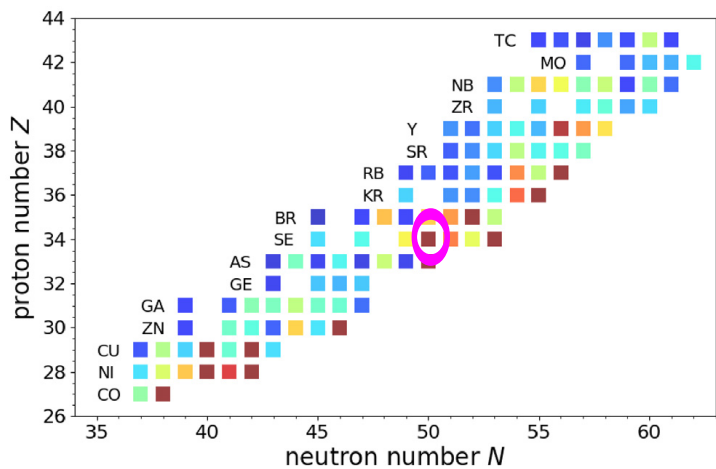
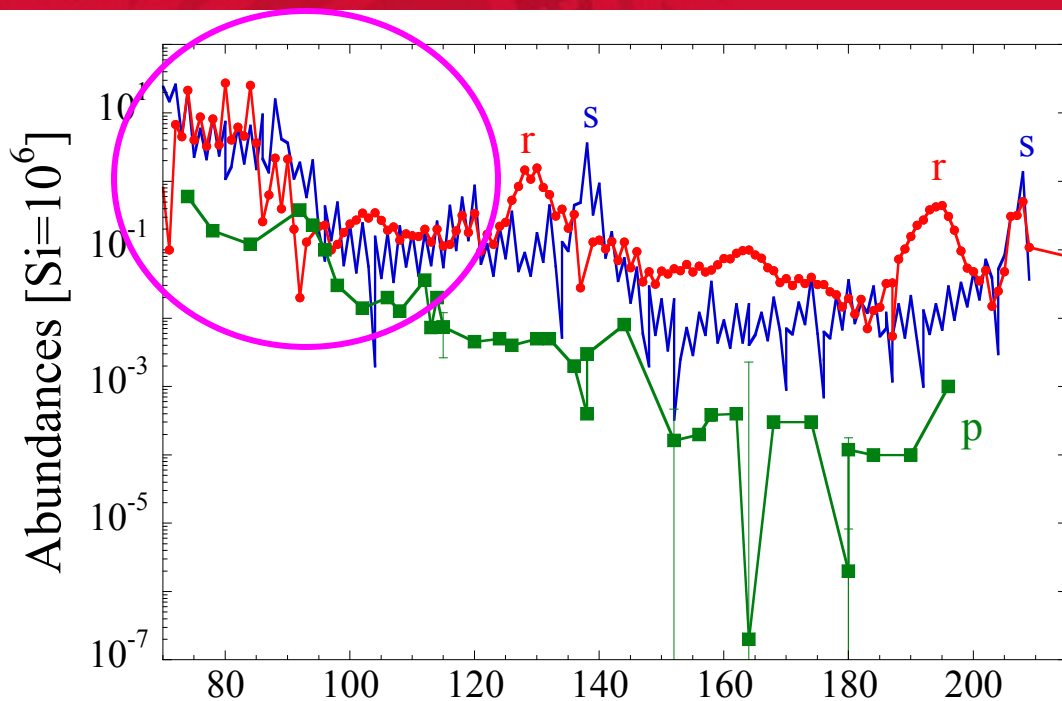
Work supported in part by U.S. Department of Energy and National Science Foundation



Synthesis of $A \approx 80$: many (n, γ) processes

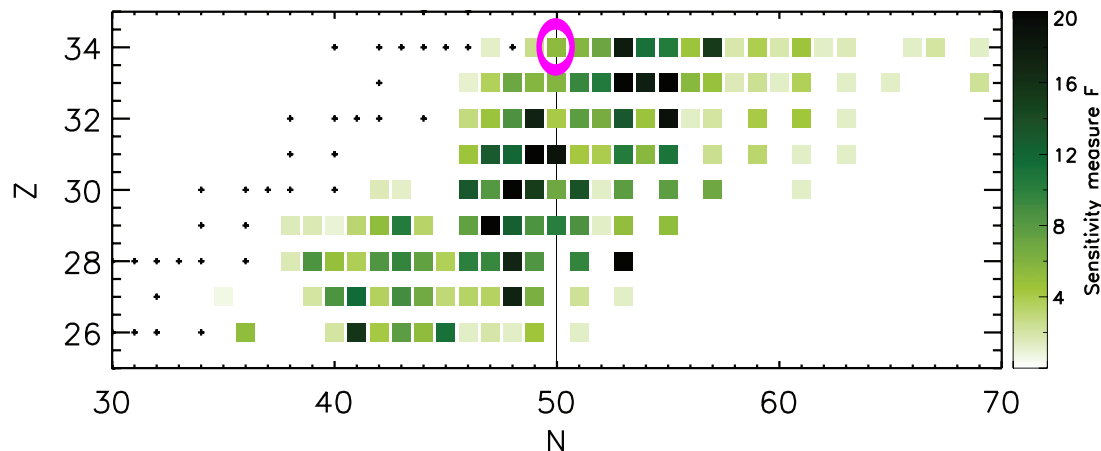
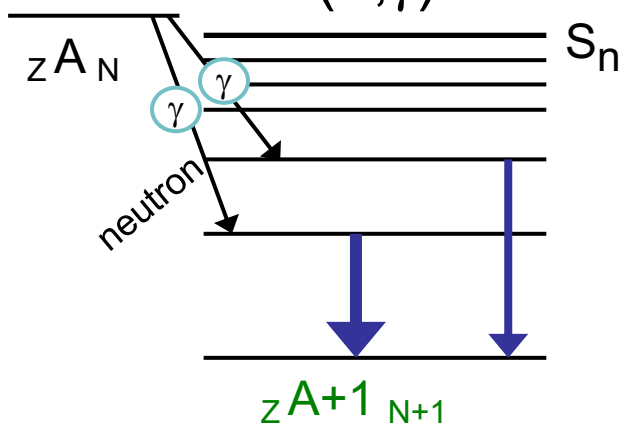






Focus: $N=50$ ^{84}Se

Direct-semi-direct
Near N shell closures
(n, γ)



Near closed shells

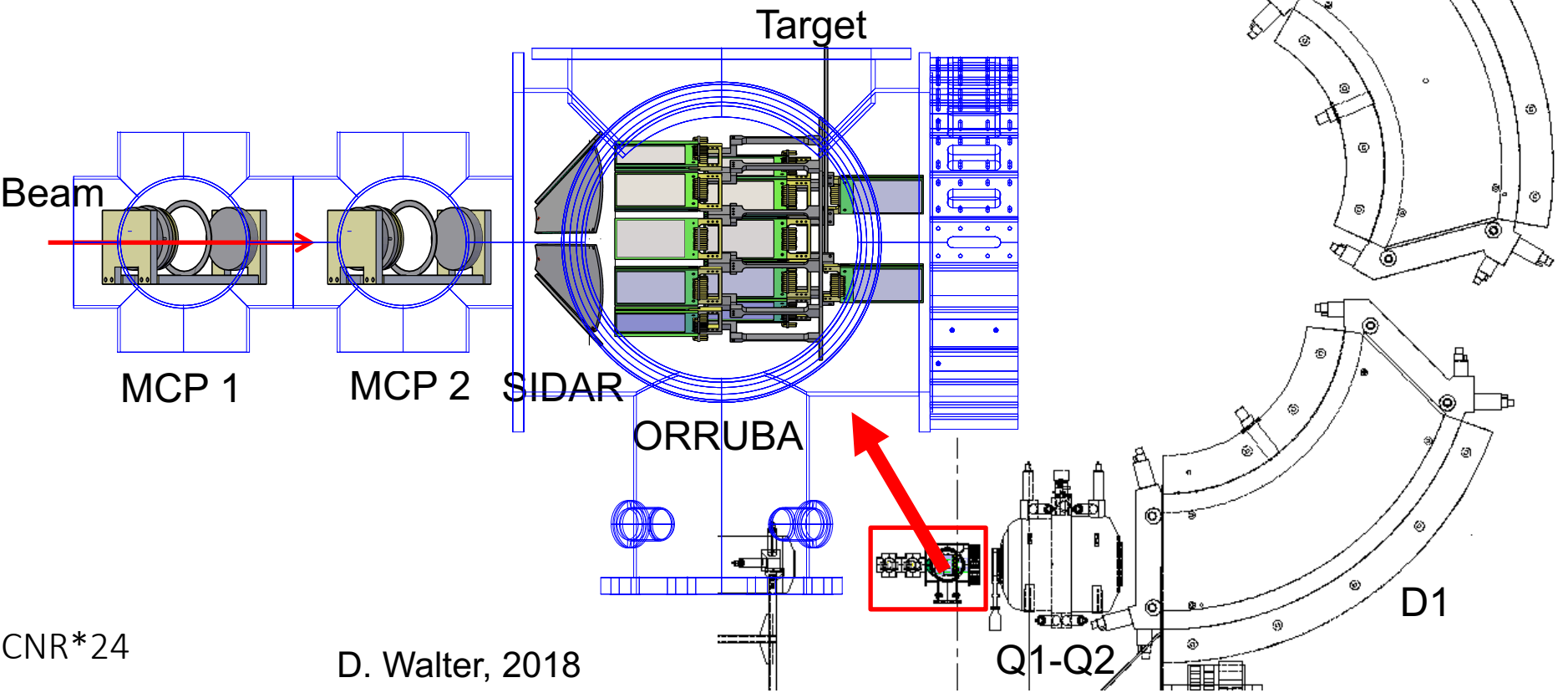
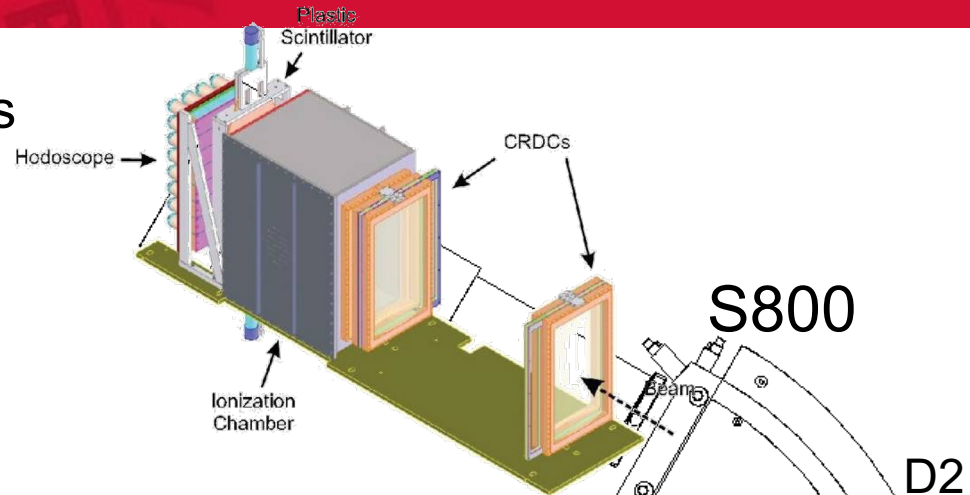
- Level density low near S_n
- Direct neutron capture important
- Depends on
 - E_x of low- ℓ single particle states
 - Spectroscopic factor S

$$S = \left(\frac{d\sigma}{d\Omega} \right)_{exp} / \left(\frac{d\sigma}{d\Omega} \right)_{thy}$$

R. Surman et al., (weak-r process)
AIP Advances **4**, 041008 (2014)

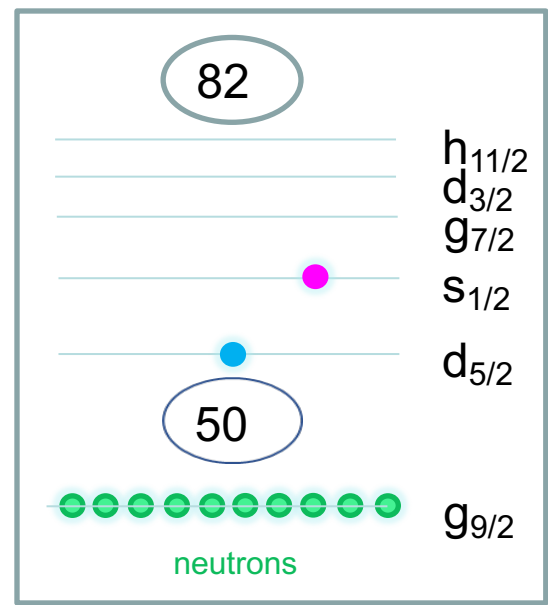
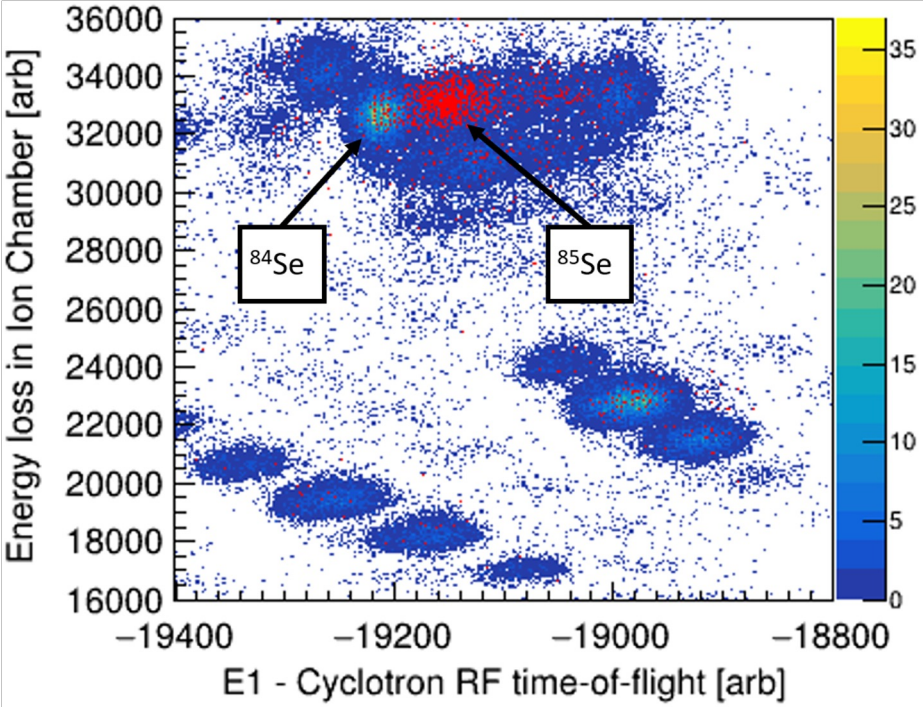
(d,p) with ^{84}Se 45 MeV/u NSCL beams

- CD_2 targets
- Upstream beam tracking
- ORRUBA (Oak Ridge Rutgers University Barrel Array) + SIDAR
- Heavy recoils S800 focal plane



45 MeV/u at NSCL

$$S = \left(\frac{d\sigma}{d\Omega} \right)_{exp} / \left(\frac{d\sigma}{d\Omega} \right)_{thy}$$



Excitations in ⁸⁵Se

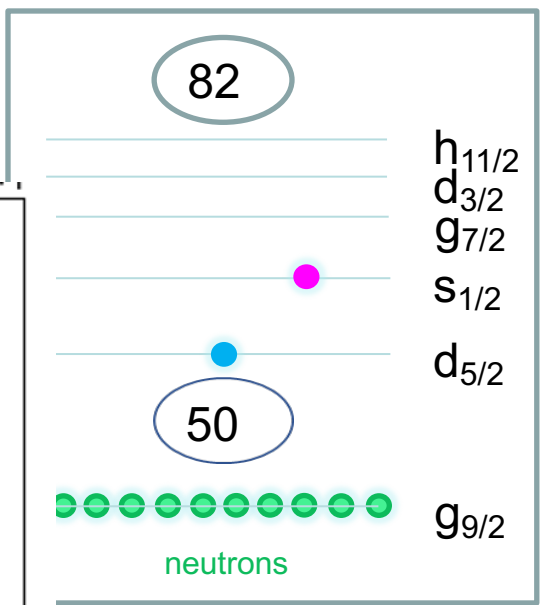
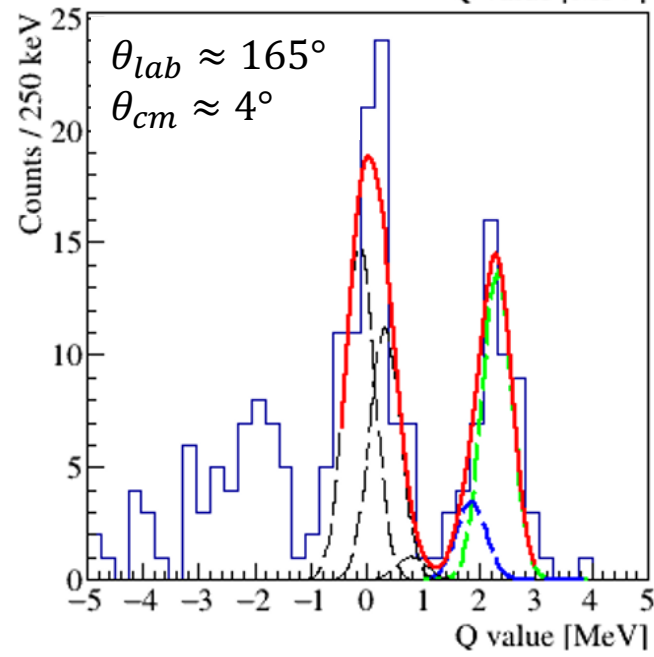
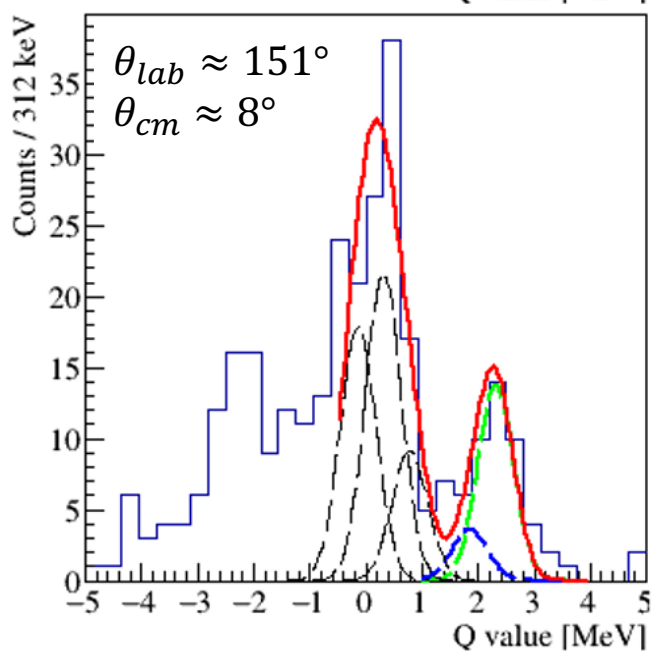
S800 FP particle ID

- (red) gate on ORRUBA
- Gate on ⁸⁵Se
- Q-value spectra
- $\left(\frac{d\sigma}{d\Omega} \right)$

H.E. Sims Phd Dissertation (2020)
 H.E. Sims, D Walter et al.,
 in preparation for PRC (2023)

45 MeV/u at NSCL

$$S = \left(\frac{d\sigma}{d\Omega} \right)_{exp} / \left(\frac{d\sigma}{d\Omega} \right)_{thy}$$



Excitations in ⁸⁵Se

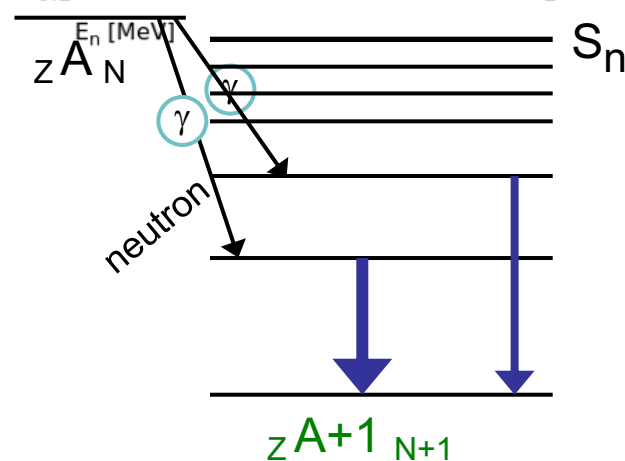
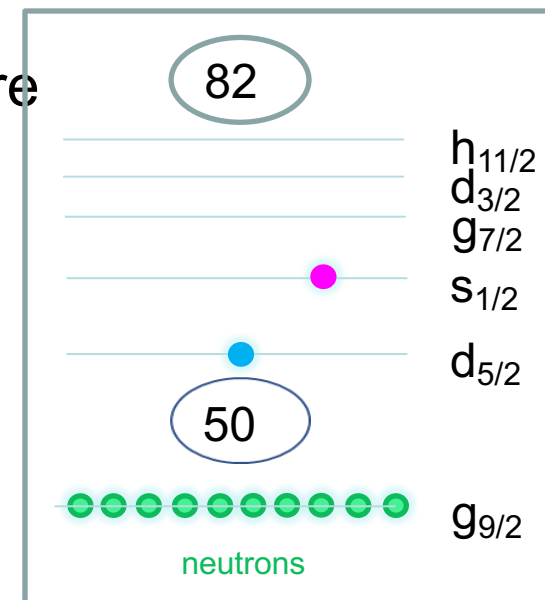
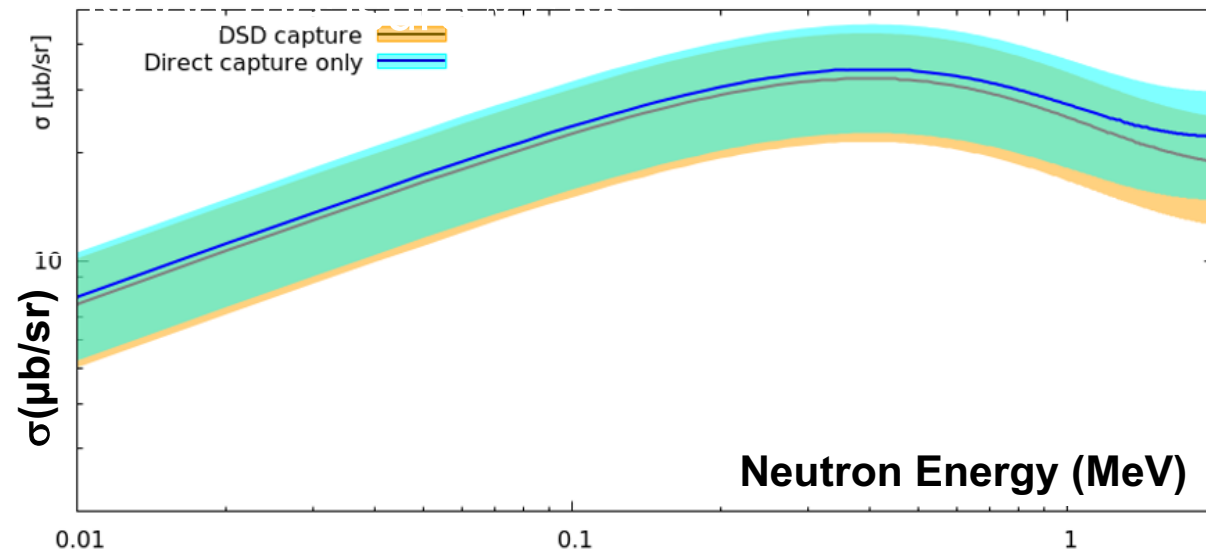
FR-ADWA w/ KD OPM

5/2 ⁺ E _x = 0	S = 0.28 (4)
1/2 ⁺ E _x = 0.462 MeV	S = 0.26 (6)

H.E. Sims Phd Dissertation (2020)
 H.E. Sims, D Walter et al.,
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Direct-semi-direct (DSD) capture

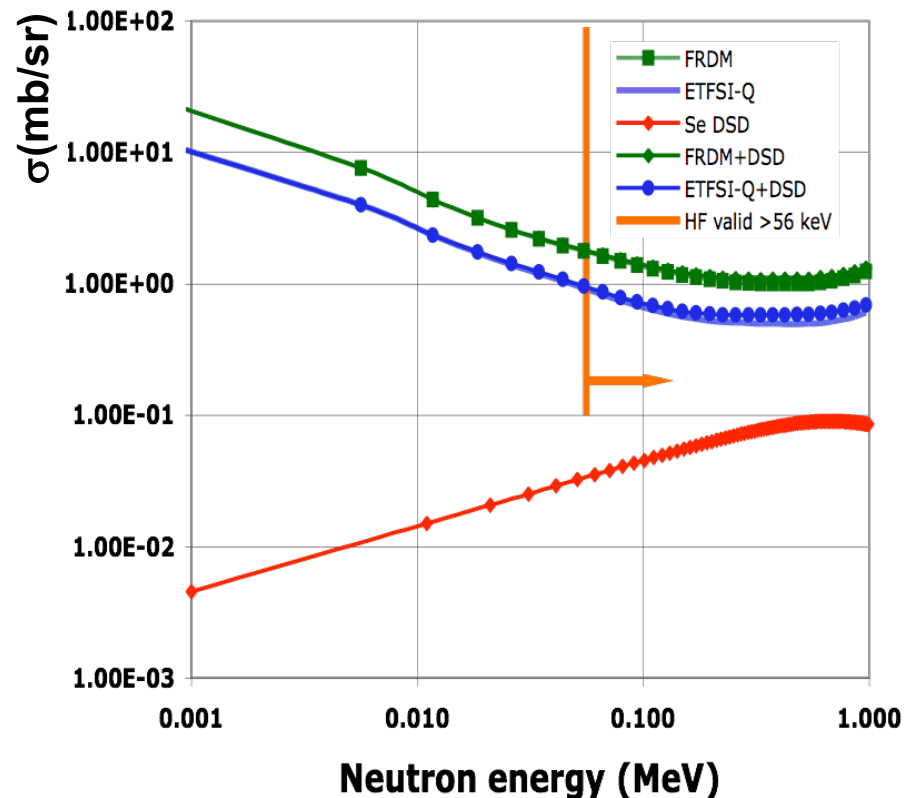
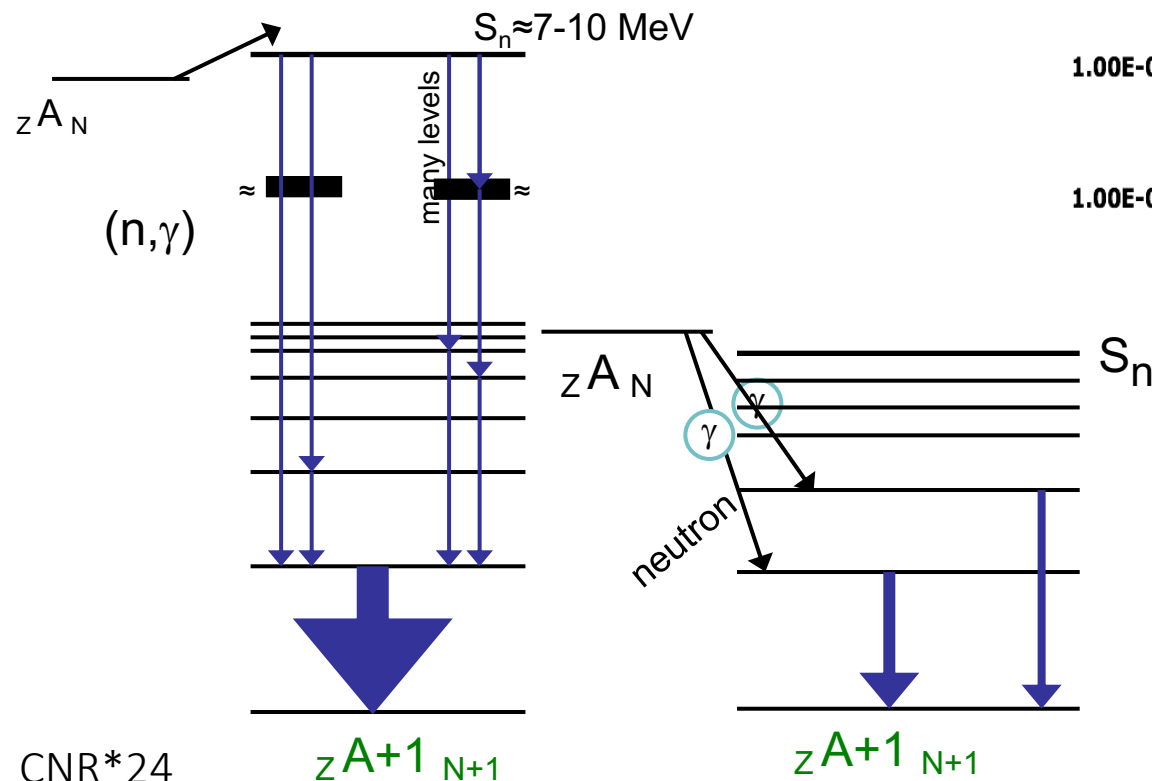
- Cross sections small $\approx 20 \mu\text{b/sr}$; p -wave capture
- Statistical capture? σ much larger?



H.E. Sims Phd Dissertation (2020)
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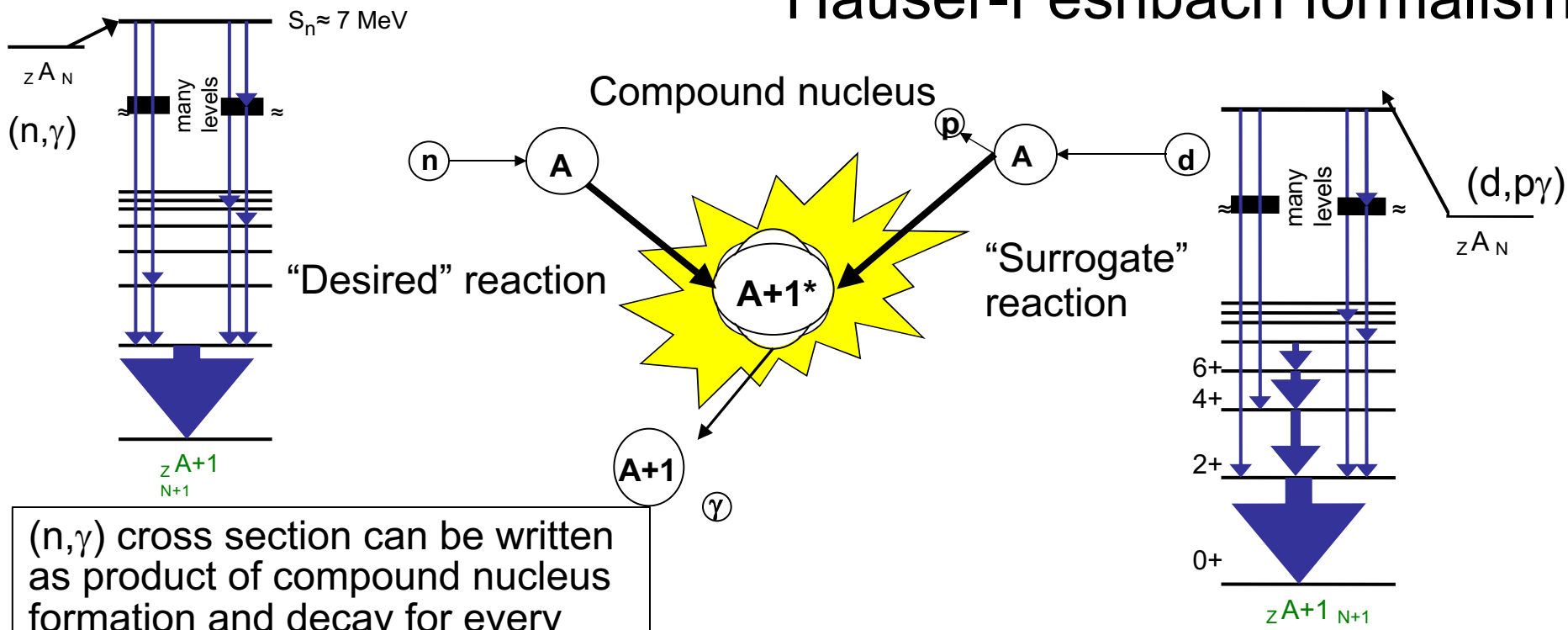
Direct-semi-direct capture

- Cross sections small $\approx 20 \mu\text{b/sr}$ for p -wave capture
- Statistical capture? σ much larger?
- Need valid (n,γ) surrogate reaction



H.E. Sims Phd Dissertation (2020)
 H.E. Sims, D Walter et al.,
 in preparation for PRC (2023)
 J.A. Cizewski et al,
 AIP CP **1090**, 463 (2009)

Surrogate reaction concept & Hauser-Feshbach formalism



(n, γ) cross section can be written as product of compound nucleus formation and decay for every spin and parity:

$$\sigma_{n\gamma}(E_n) = \sum_{J, \pi} \sigma_n^{CN}(E_x, J, \pi) G_\gamma^{CN}(E_x, J, \pi)$$

Surrogate particle-gamma coincidence can be written as product of compound nucleus formation and decay for every spin and parity:

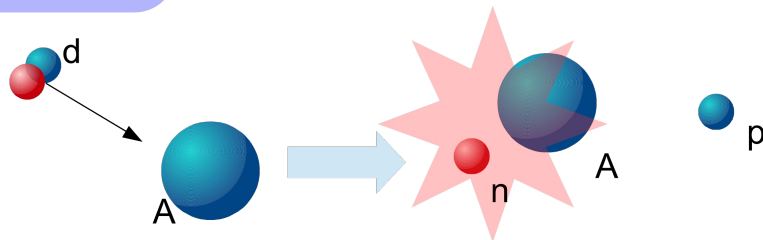
$$P_{p\gamma}(E_x, \theta) = \sum_{J, \pi} F_{dp}^{CN}(E_x, J, \pi, \theta) G_\gamma^{CN}(E_x, J, \pi)$$

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Neutron transfer (d,p) to unbound states, non-elastic breakup and surrogate for (n, γ)

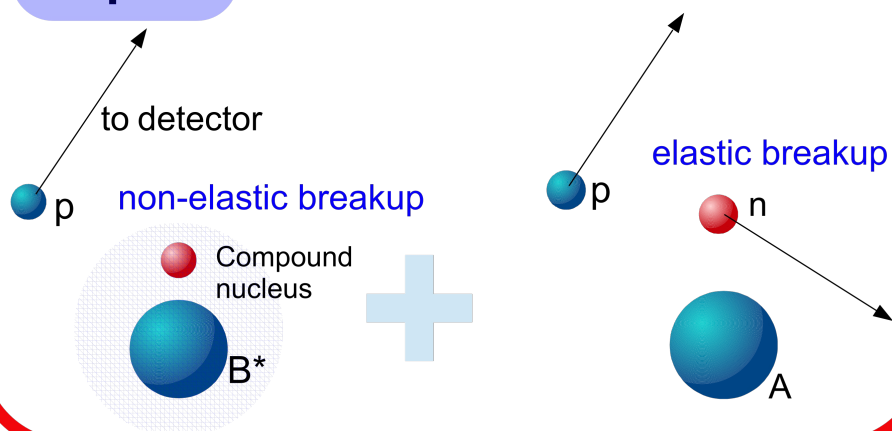
step 1

separation of the proton



step 2

propagation of n in the field of B^*



Two-step process

- d breakup; B.E. = 2.2 MeV
- n propagation
 - Elastic breakup
 - Non-elastic breakup \Rightarrow CN and surrogate (n, γ)
 - Predicts J^π transfer

Gregory Potel et al. PRC 92, 034611(2015) \Rightarrow path to CN formation

(d,p) reaction to forms compound nucleus

- ❖ Need to measure $P(d,p\gamma)$
- ❖ Need theory to calculate formation of CN: F^{CN}
- ❖ Need to deduce decay of CN: G^{CN}

$$P_{p\gamma}(E_x, \theta) = \sum_{J, \pi} F_{dp}^{CN}(E_x, J, \pi, \theta) G_{\gamma}^{CN}(E_x, J, \pi)$$

Validate with $^{95}\text{Mo}(d,p\gamma)$ reaction & ^{96}Mo gammas
 $\ell = 0$ capture on $5/2^+ \Rightarrow 2^+, 3^+$

$\sigma(n,\gamma)$ was measured and informed

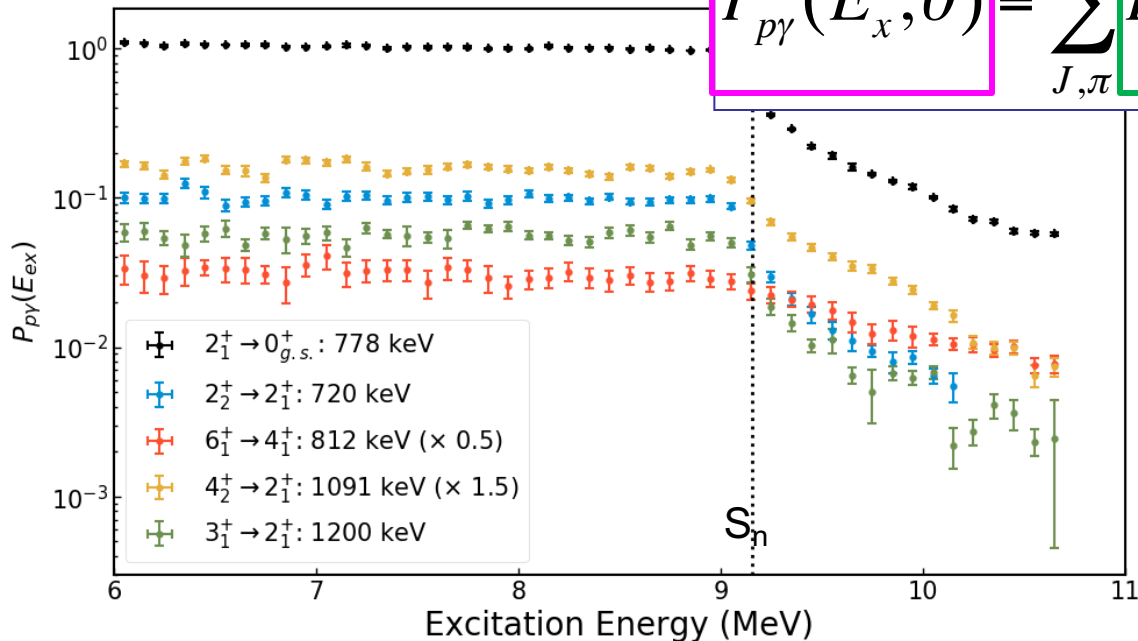
$$P_{pY}(E_x) = \frac{\text{Number of CN decays via channel } Y}{\text{Number of times the CN is formed}}$$

- Channel Y: individual discrete γ transitions to low-lying states
 - Intensity (=counts/efficiency) of specific transitions
- Number of times CN is formed
 - Intensity of single protons as a function of E_x

$$P_{pY}(E_x) = \frac{N_{pY}(E_x)}{\varepsilon_Y} / N_p(E_x)$$

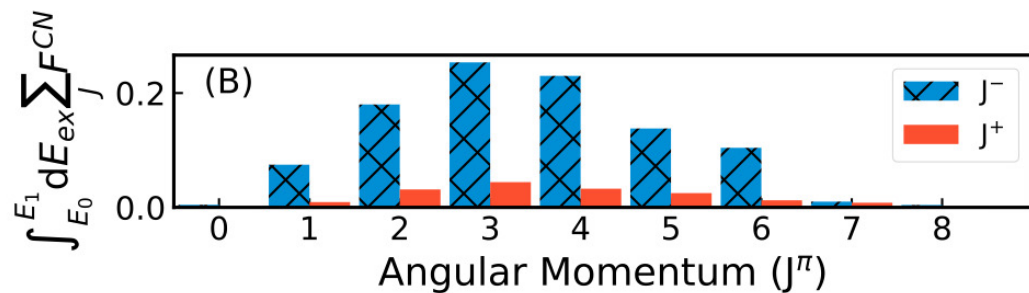
- Normal kinematics "easy"
 - Stable heavy target; light stable beam
 - Silicon detectors predominantly at forward angles
 - Don't need heavy recoil detection

$$P_{p\gamma}(E_x, \theta) = \sum_{J, \pi} F_{dp}^{CN}(E_x, J, \pi, \theta) G_\gamma^{CN}(E_x, J, \pi)$$



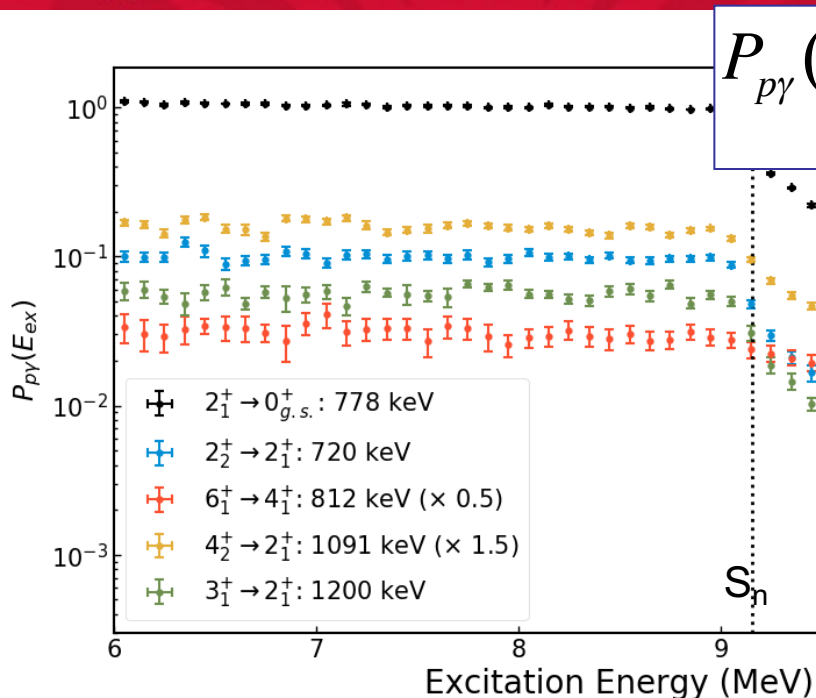
Surrogate (d,p γ) data

Potel: ^{96}Mo J^π population



A. Ratkiewicz et al., PRL **122**, 052502 (2019)

G. Potel et al, PRC 92, 034611(2015)



$$P_{p\gamma}(E_x, \theta) = \sum_{J, \pi} F_{dp}^{\text{CN}}(E_x, J, \pi, \theta) G_{\gamma}^{\text{CN}}(E_x, J, \pi)$$

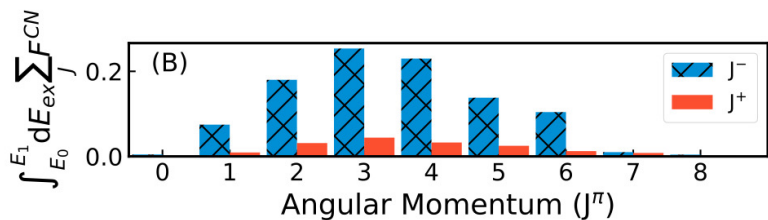
Surrogate (d,p γ) data

HF calculations (Jutta Escher)

- F^{CN} from Gregory Potel
- Bayesian fit to observed $P(d,p\gamma)$
 - Level density: Gilbert & Cameron
 - No norm to D_0
 - Lorentzian γ strength function;
 - No $\langle \Gamma(\gamma) \rangle$

➤ $G^{\text{CN}}(E_x, J, \pi)$

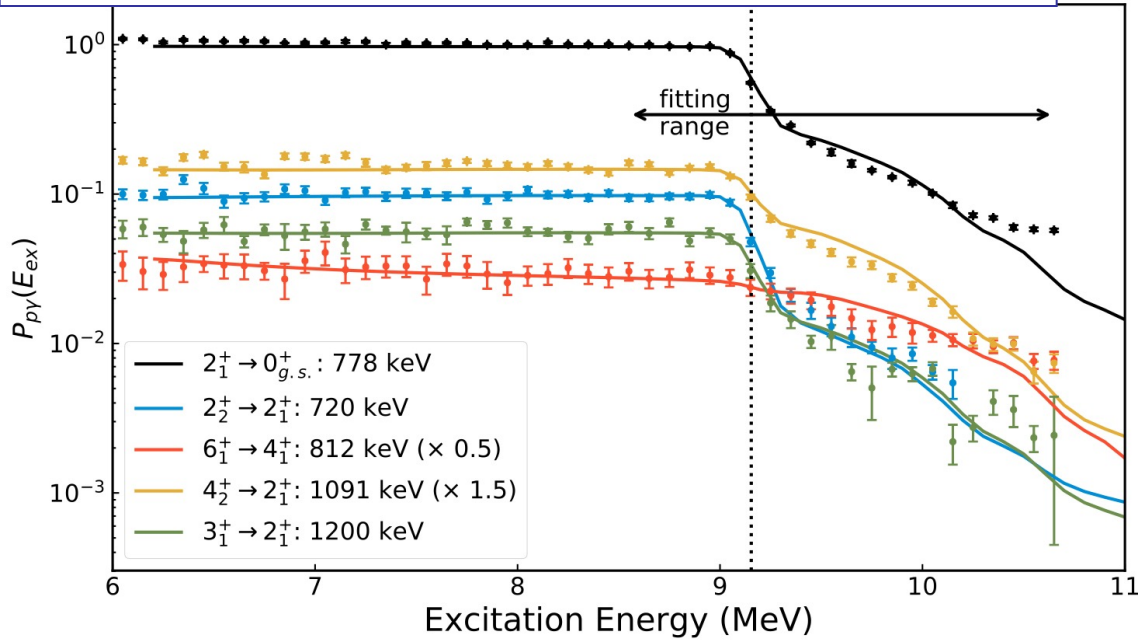
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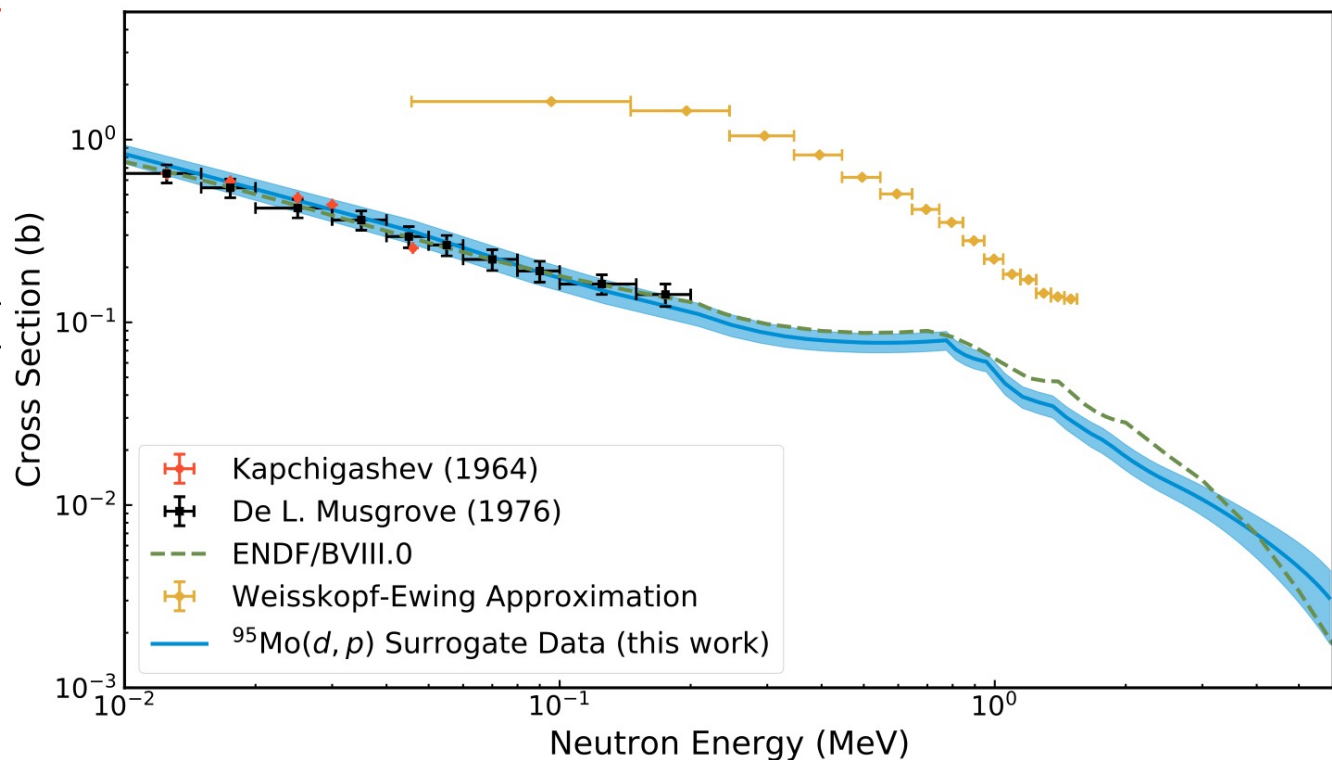
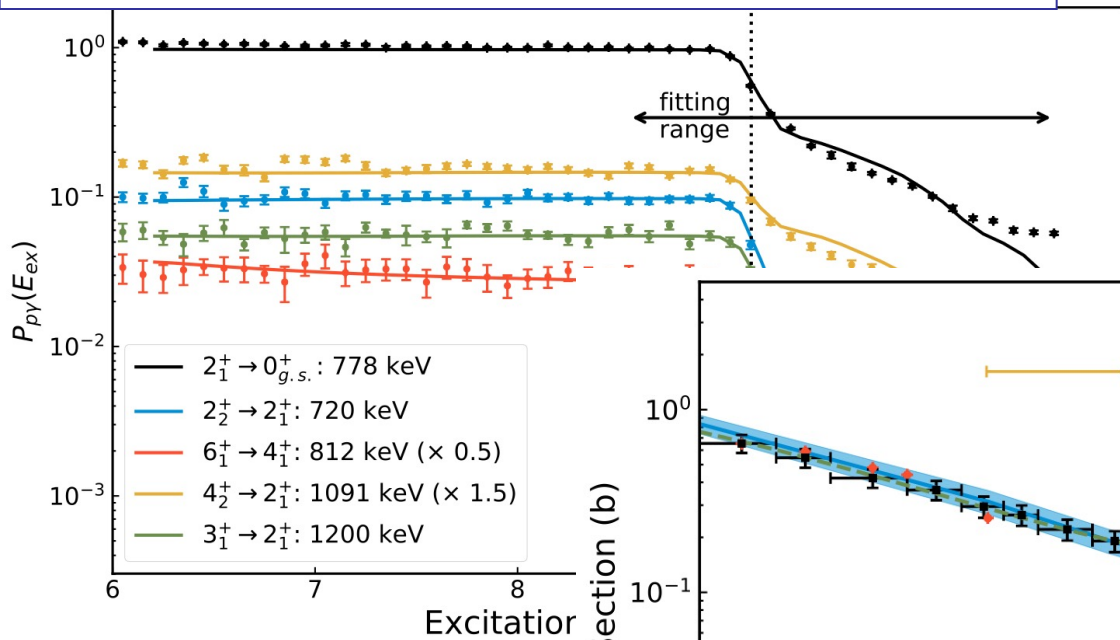
$$P_{p\gamma}(E_x, \theta) = \sum_{J, \pi} F_{dp}^{CN}(E_x, J, \pi, \theta) G_{\gamma}^{CN}(E_x, J, \pi)$$



A. Ratkiewicz et al., PRL **122**, 052502 (2019)

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$$P_{p\gamma}(E_x, \theta) = \sum_{J, \pi} F_{dp}^{CN}(E_x, J, \pi, \theta) G_{\gamma}^{CN}(E_x, J, \pi)$$



A. Ratkiewicz et al., PRL **122**, 052502 (2019)

CNR*24

$$\sigma_{n\gamma}(E_n) = \sum_{J, \pi} \sigma_n^{CN}(E_x, J, \pi) G_{\gamma}^{CN}(E_x, J, \pi)$$

- Heavy beam on light (CD_2) target = inverse kinematics
- Proton detection: good energy and angle resolution: ORRUBA
- Challenge: detecting discrete gammas
 - Relatively low gamma efficiency, especially discrete γ
 - Away from even-even closed shells
 - High level density even at low E_x
 - Especially final odd-odd nuclei
- Want Y – the gamma decay channel:
 - Not dependent on specific gammas

$$P_{pY}(E_x) = \frac{\text{Number of CN decays via channel } Y}{\text{Number of times the CN is formed}}$$

$$P_{pY}(E_x) = \frac{\text{[Diagram: A blue and red nucleus decaying into a blue and red nucleus with a wavy line representing a gamma ray]}{\text{[Diagram: A blue and red nucleus]}}$$

- $^{84}\text{Se}(d,p)$ populates $^{85}\text{Se}^*$ CN
- CN at $E_x < S_n$: only decays by gamma emission \Rightarrow ^{85}Se
- CN at $E_x > S_n$: if decays by gamma emission \Rightarrow ^{85}Se = channel Y
- CN at $E_x > S_n$: if decays by neutron emission \Rightarrow ^{84}Se

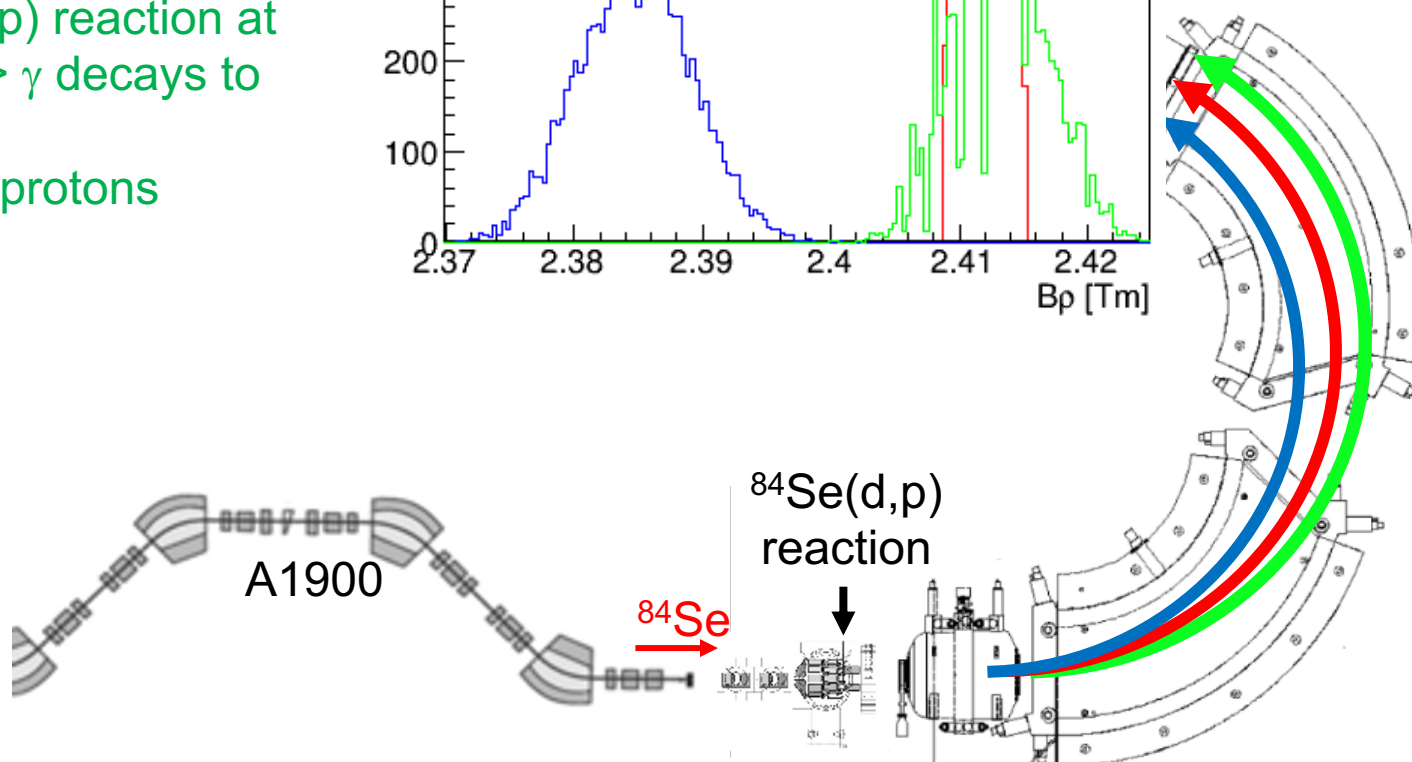
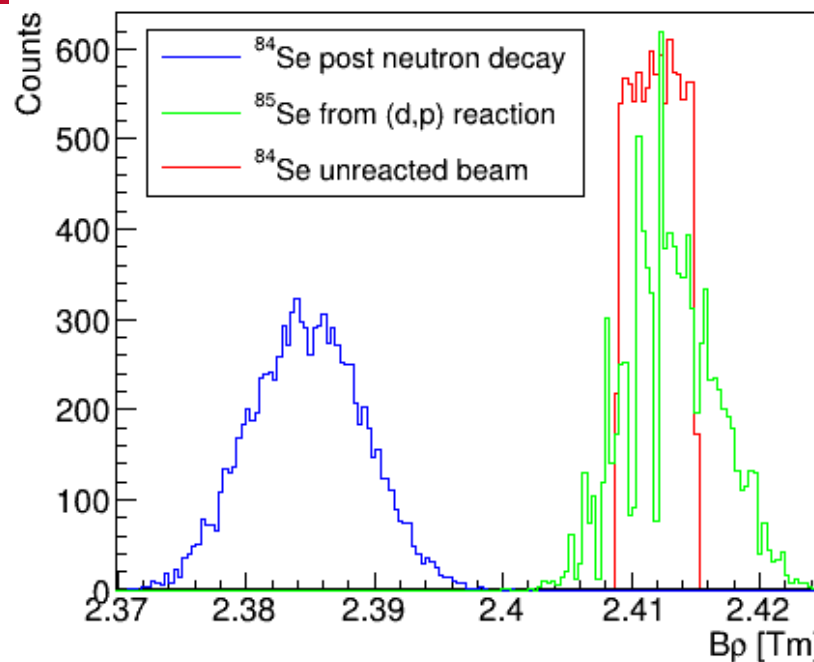
$$P_{pY}(E_x) = \frac{\text{Number of CN decays via channel Y}}{\text{Number of times the CN is formed}}$$

$$P_{pY}(E_x) = \frac{N_{p-^{85}\text{Se}}(E_x)}{\varepsilon} / N_p(E_x)$$

- Detection efficiency of heavy recoils $>$ gammas
- No dependence on details of γ -decay
- Need excellent separation of ^{85}Se and ^{84}Se

Three scenarios:

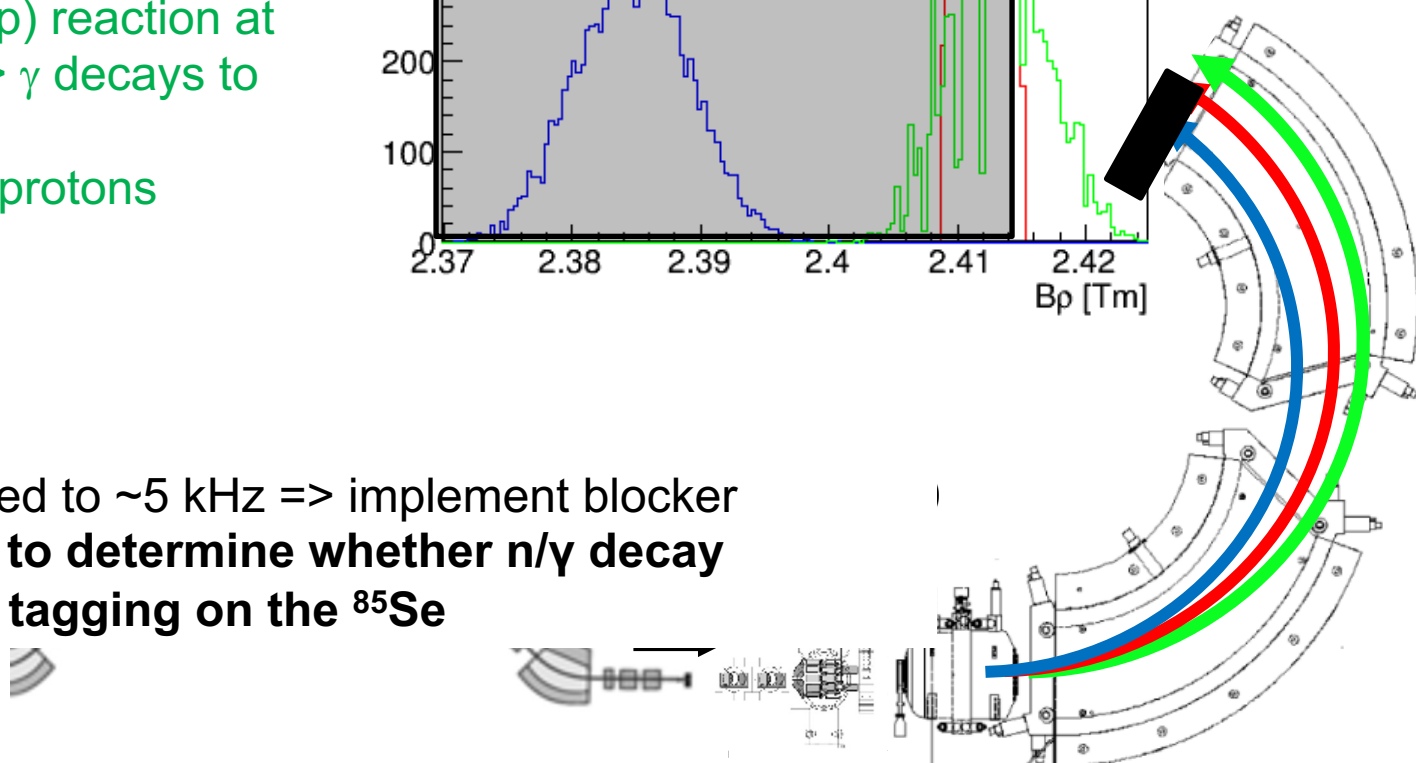
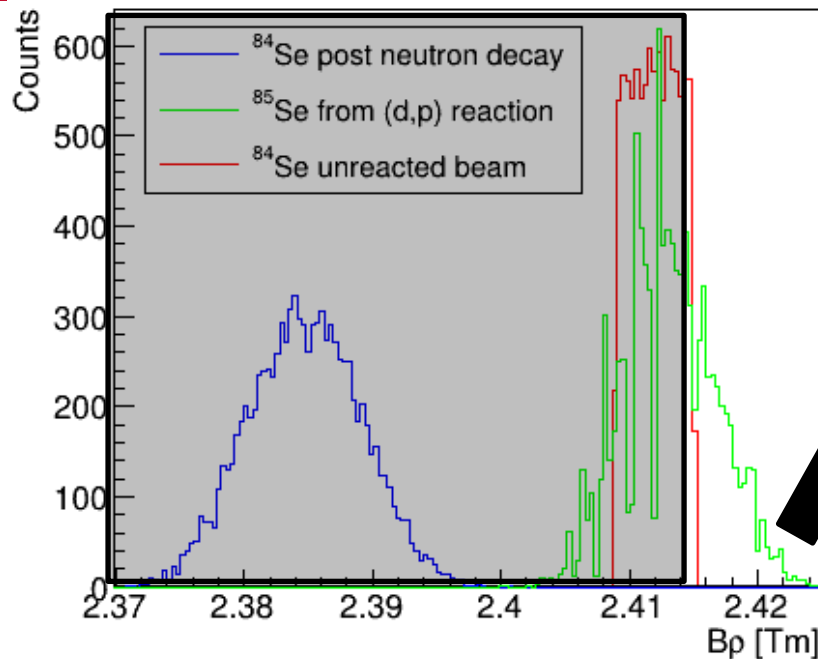
1. ^{84}Se does not react with CD_2 target, continues with same momentum distribution as determined by slits in A1900
2. ^{84}Se undergoes (d,p) reaction at $\text{CD}_2 \Rightarrow \text{CN } ^{85}\text{Se} \Rightarrow \gamma$ decays to ^{85}Se g.s.
 - Know E_x from protons



1. Same as point 2, except CN ^{85}Se emits neutron $\Rightarrow ^{84}\text{Se}$

Three scenarios:

1. ^{84}Se does not react with CD_2 target, continues with same momentum distribution as determined by slits in A1900
2. ^{84}Se undergoes (d,p) reaction at $\text{CD}_2 \Rightarrow \text{CN } ^{85}\text{Se} \Rightarrow \gamma$ decays to ^{85}Se g.s.
 - Know E_x from protons



- S800 is rate-limited to ~ 5 kHz \Rightarrow implement blocker
- **Use the recoils to determine whether n/ γ decay ($^{84}\text{Se}/^{85}\text{Se}$) – by tagging on the ^{85}Se**

3. Same as point 2, except CN ^{85}Se emits neutron \Rightarrow ^{84}Se

Advantages:

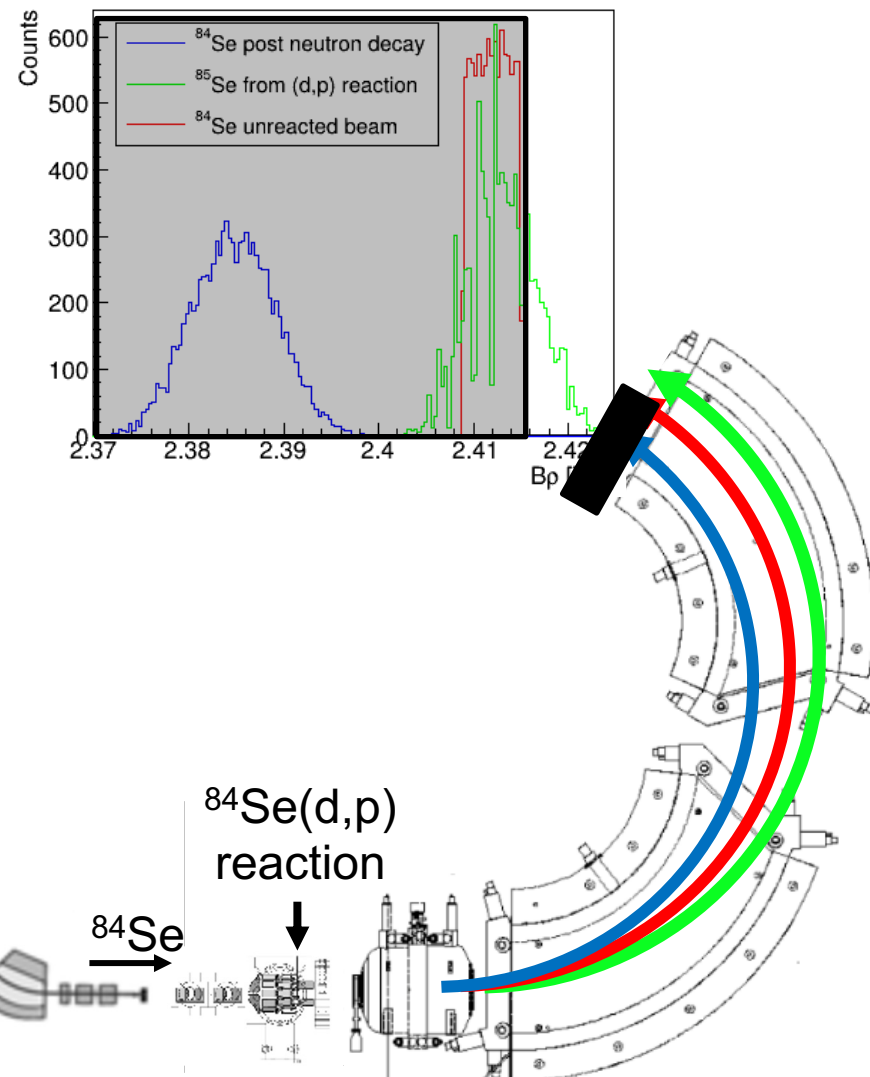
- With (low intensity RIBs) all statistics in single observable
- ~25-30% detection efficiency (much better than γ efficiency $\approx 13\%$)
 - Can measure by looking at bound states
 - Not reliant on simulations
 - If can tighten up momentum acceptance, less beam-recoil overlap
- No need for complicated cascade info – get emission probability without knowledge of how gamma decay occurs

Difference:

- No details or constraint on specific gamma branches or cascade

Challenges:

- Need significant characterization of background from Carbon in target



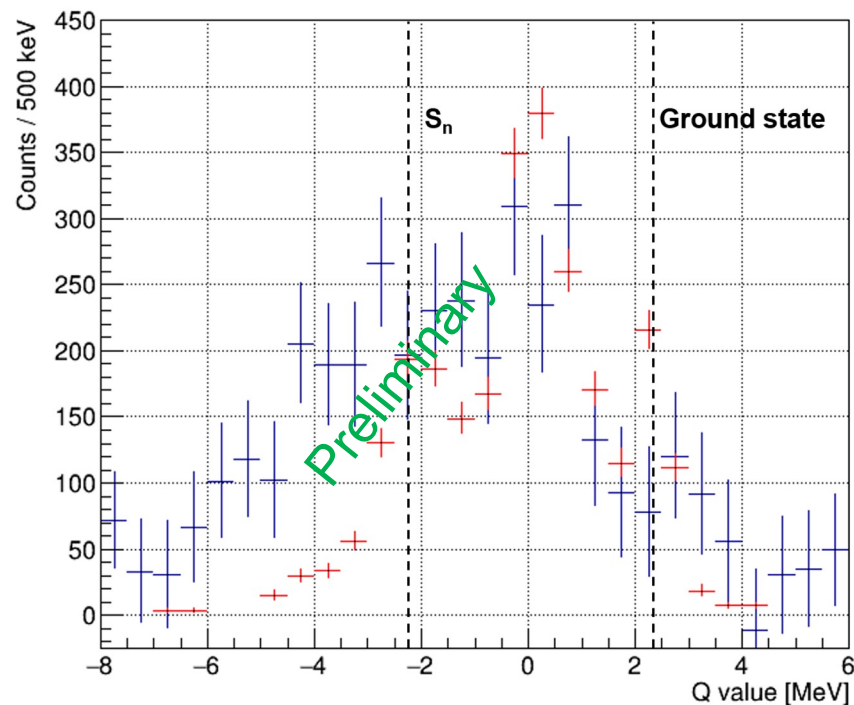
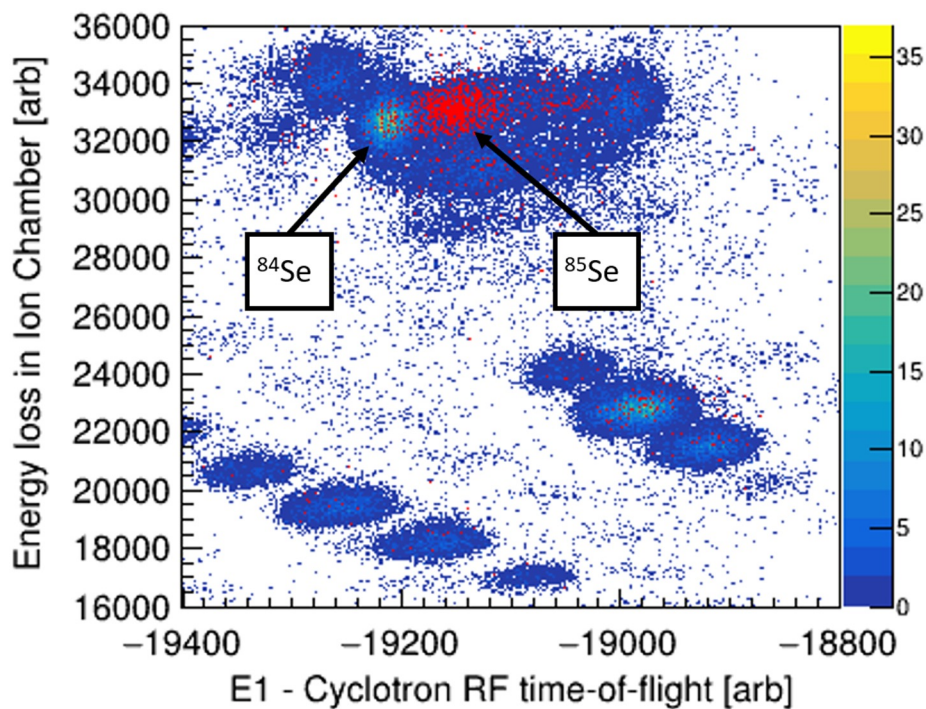
P_γ from S800 coincidences

$$P_\gamma(E_x) = \frac{N_{p-^{85}\text{Se}}(E_x) / \epsilon(^{85}\text{Se})}{N_{p\text{-singles}}(E_x)}$$

Proton-S800 coincidences

S800 acceptance

Proton singles (background subtracted)



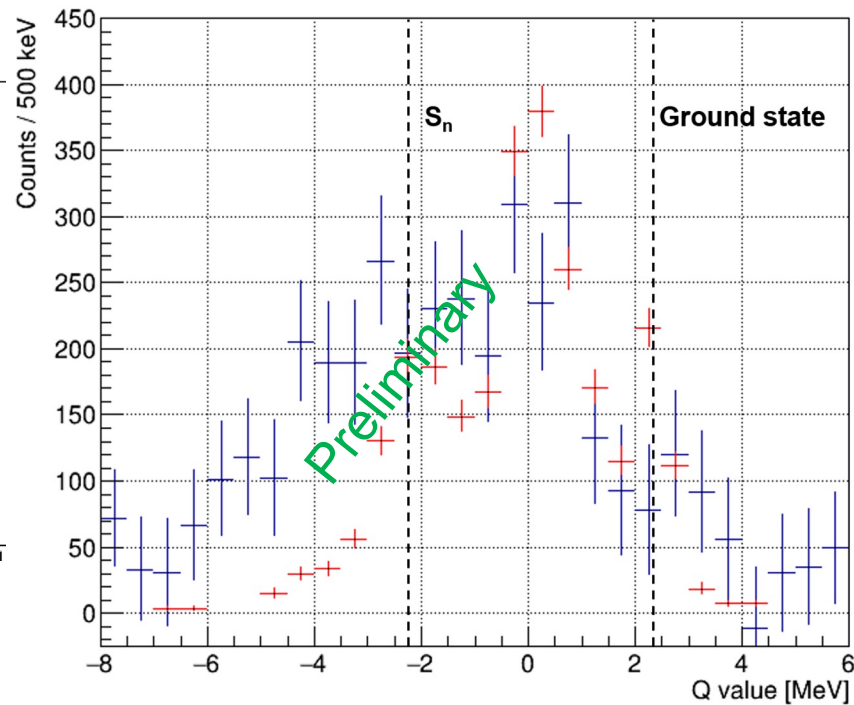
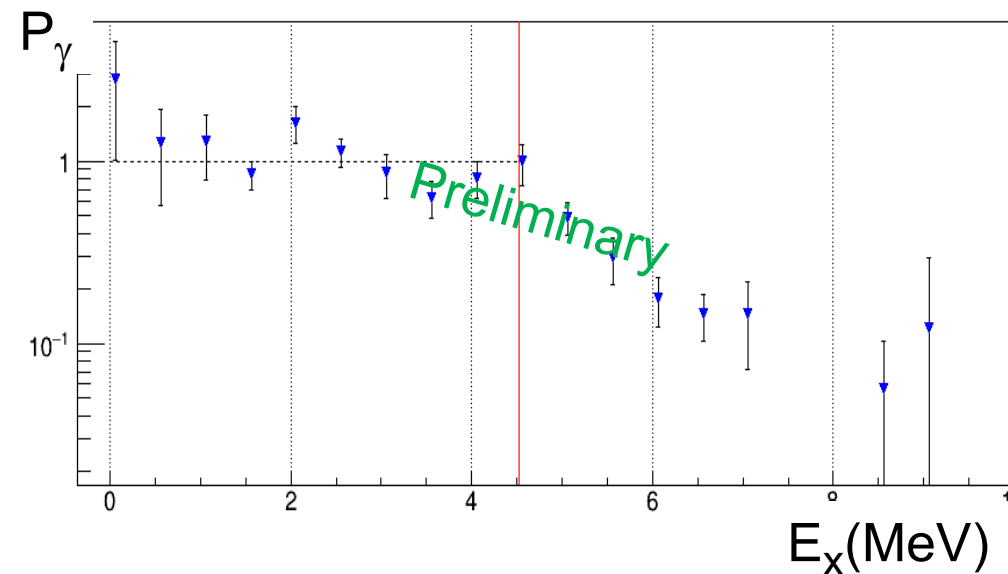
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Proton-S800 coincidences

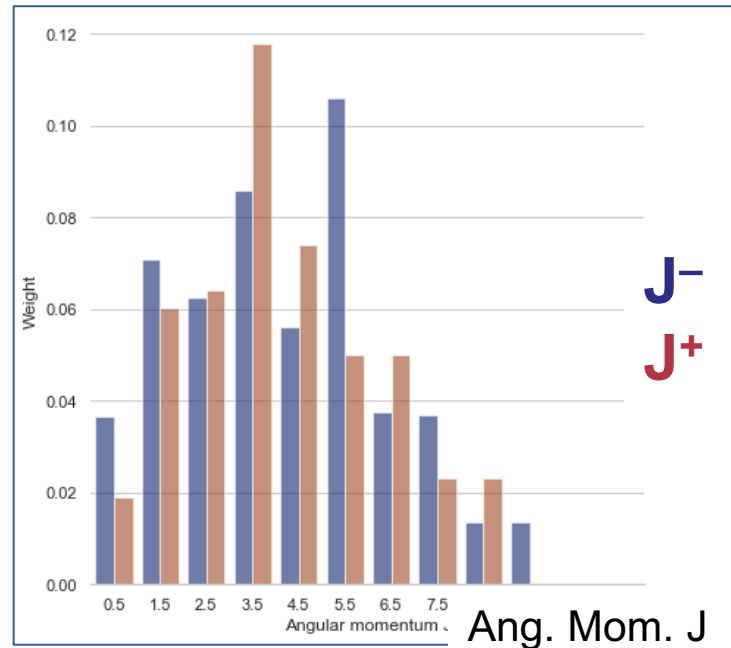
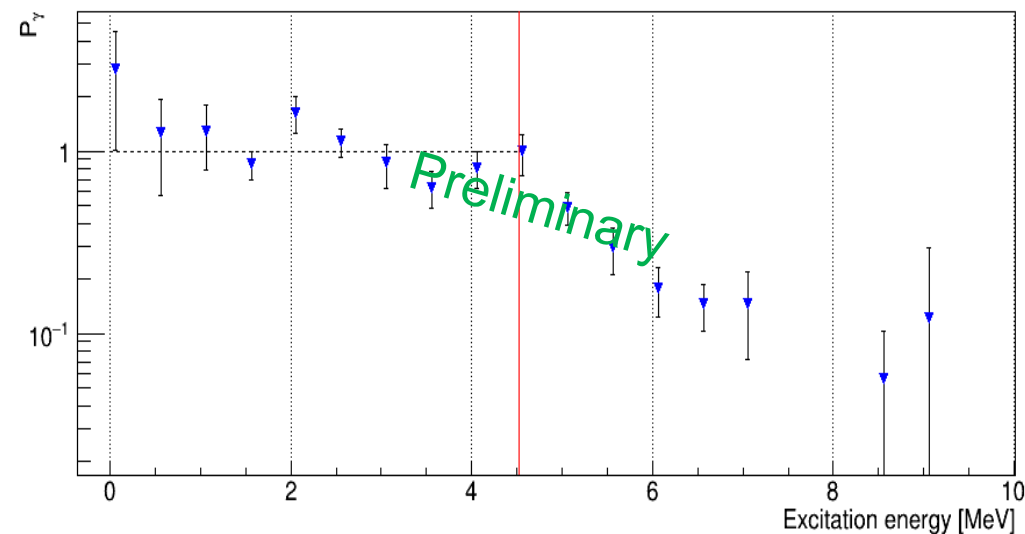
S800 acceptance

Proton singles (background subtracted)



$$P_\gamma(E_x) = \sum_{J, \pi} F_{dp}^{CN}(E_x, J, \pi, \theta) G_\gamma^{CN}(E_x, J, \pi)$$

$$\sigma_{n\gamma}(E_n) = \sum_{J, \pi} \sigma_n^{CN}(E_x, J, \pi) G_\gamma^{CN}(E_x, J, \pi)$$



45 MeV/u $^{84}\text{Se}(d,p) F_{dp}^{CN}$ at S_n

Theory: Escher, Potel, Gorton
 (prelim, 6/2024)

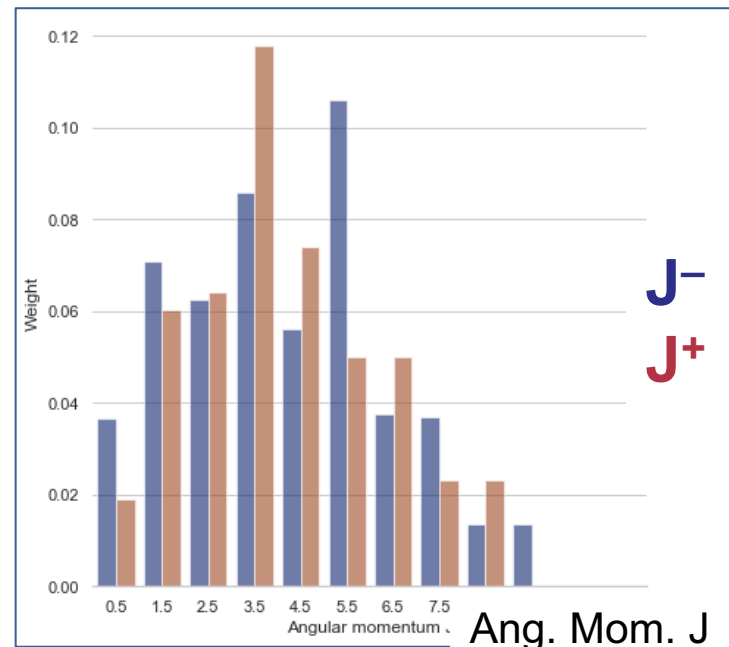
$\Rightarrow \sigma(n, \gamma)$ from surrogate reaction data

$$P_\gamma(E_x) = \sum_{J, \pi} F_{dp}^{CN}(E_x, J, \pi, \theta) G_\gamma^{CN}(E_x, J, \pi)$$

$$\sigma_{n\gamma}(E_n) = \sum_{J, \pi} \sigma_n^{CN}(E_x, J, \pi) G_\gamma^{CN}(E_x, J, \pi)$$

Theory:

1. Reaction mechanism for (d,p) J^π population vs E_x
2. Hauser-Feshbach code (YAHFC) and J^π
 - Decay of the CN ^{85}Se $G_\gamma^{CN}(E_x, J, \pi)$
3. Markov-Chain Monte-Carlo to fit HF decay parameters from surrogate observables
4. Calculate desired $\sigma^{84}\text{Se}(n, \gamma)$ by sampling posterior parameter distribution



45 MeV/u $^{84}\text{Se}(d, p) F_{dp}^{CN}$ at S_n

Theory: Escher, Potel, Gorton
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P_γ from S800 coincidences & theory

$\Rightarrow \sigma(n, \gamma)$ from surrogate reaction data

$$P_\gamma(E_x) = \sum_{J, \pi} F_{dp}^{CN}(E_x, J, \pi, \theta) G_\gamma^{CN}(E_x, J, \pi)$$

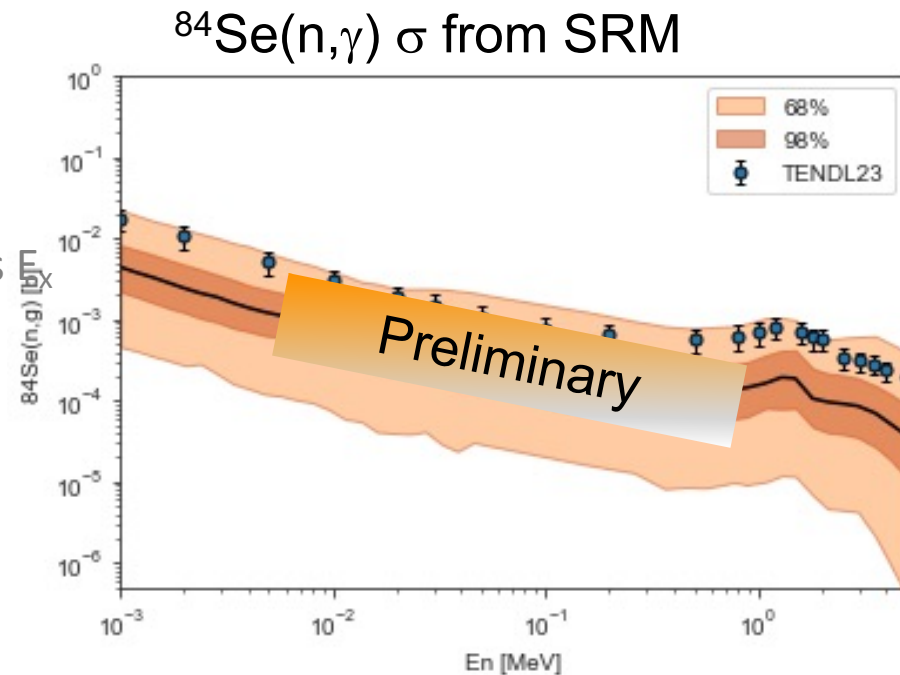
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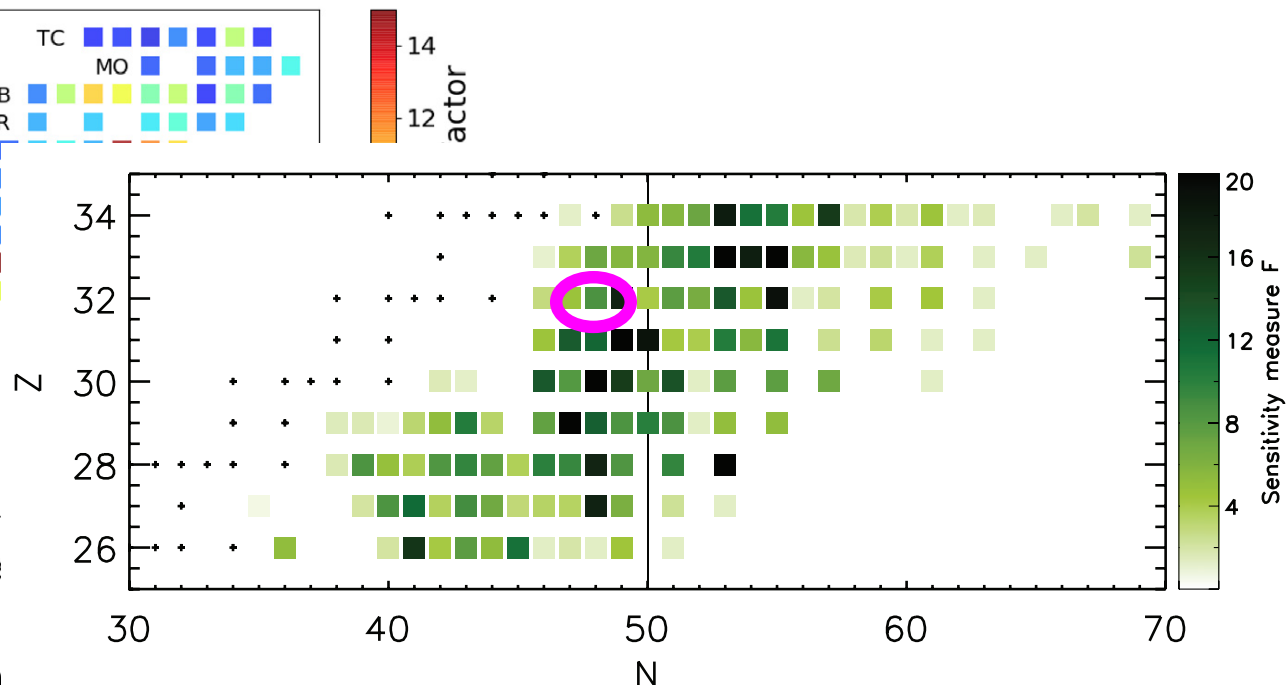
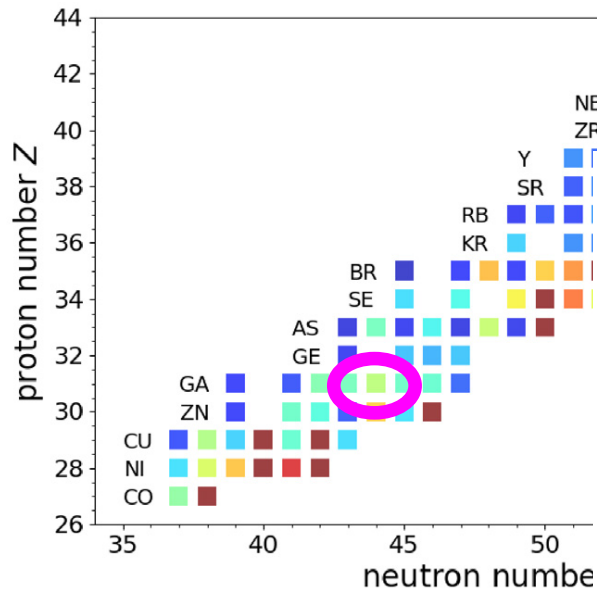
Results

1. $\sigma(n, \gamma)$ constrained by data, no D_0 or $\langle \Gamma_\gamma \rangle$
2. Not sensitive to details of γSF
3. Similar results w/ different parameter vectors

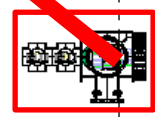
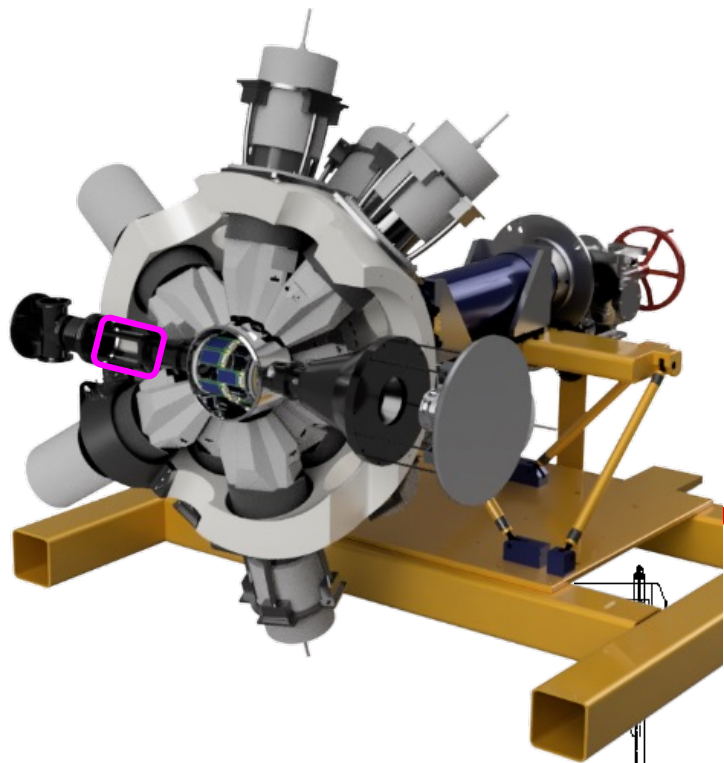
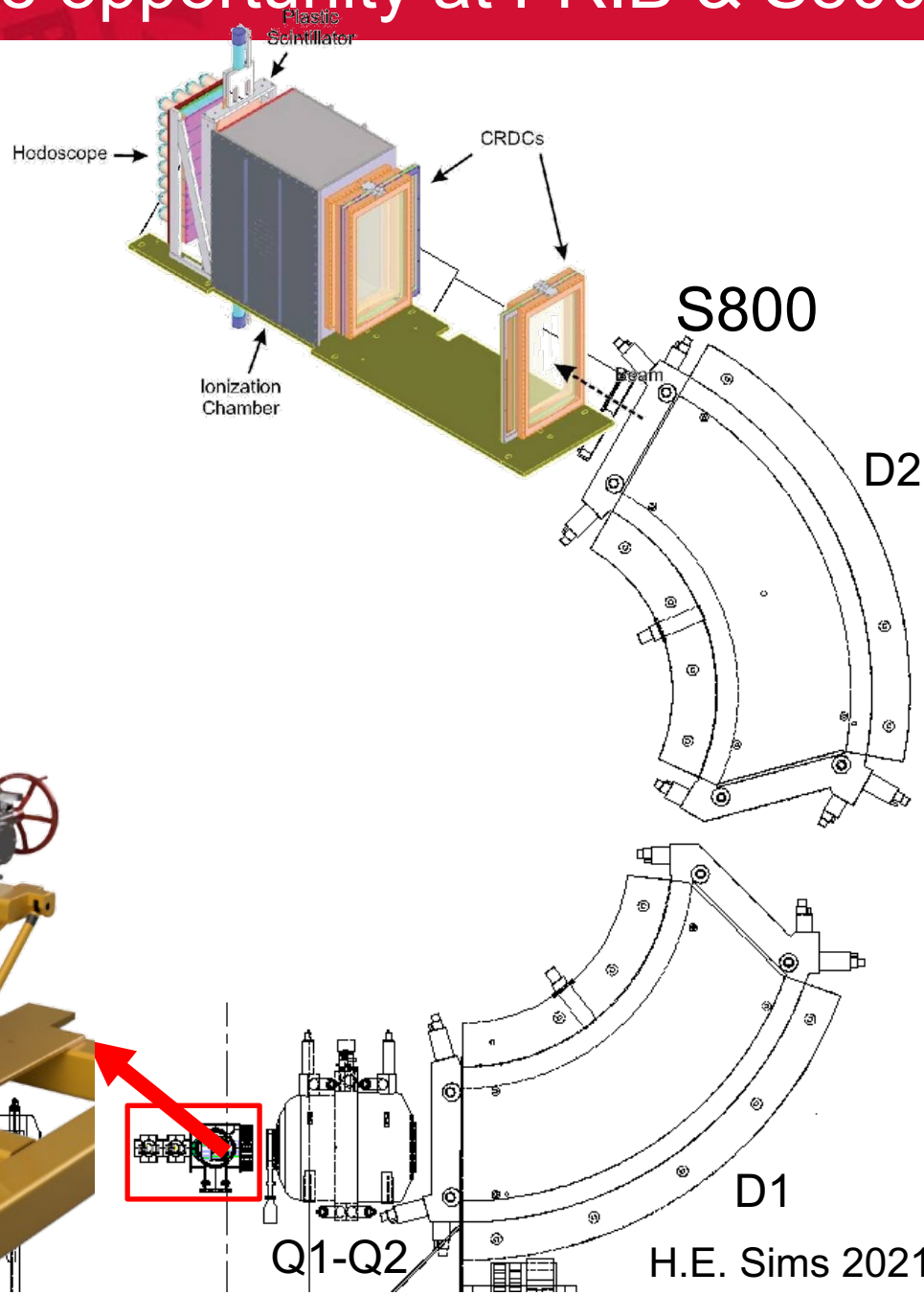


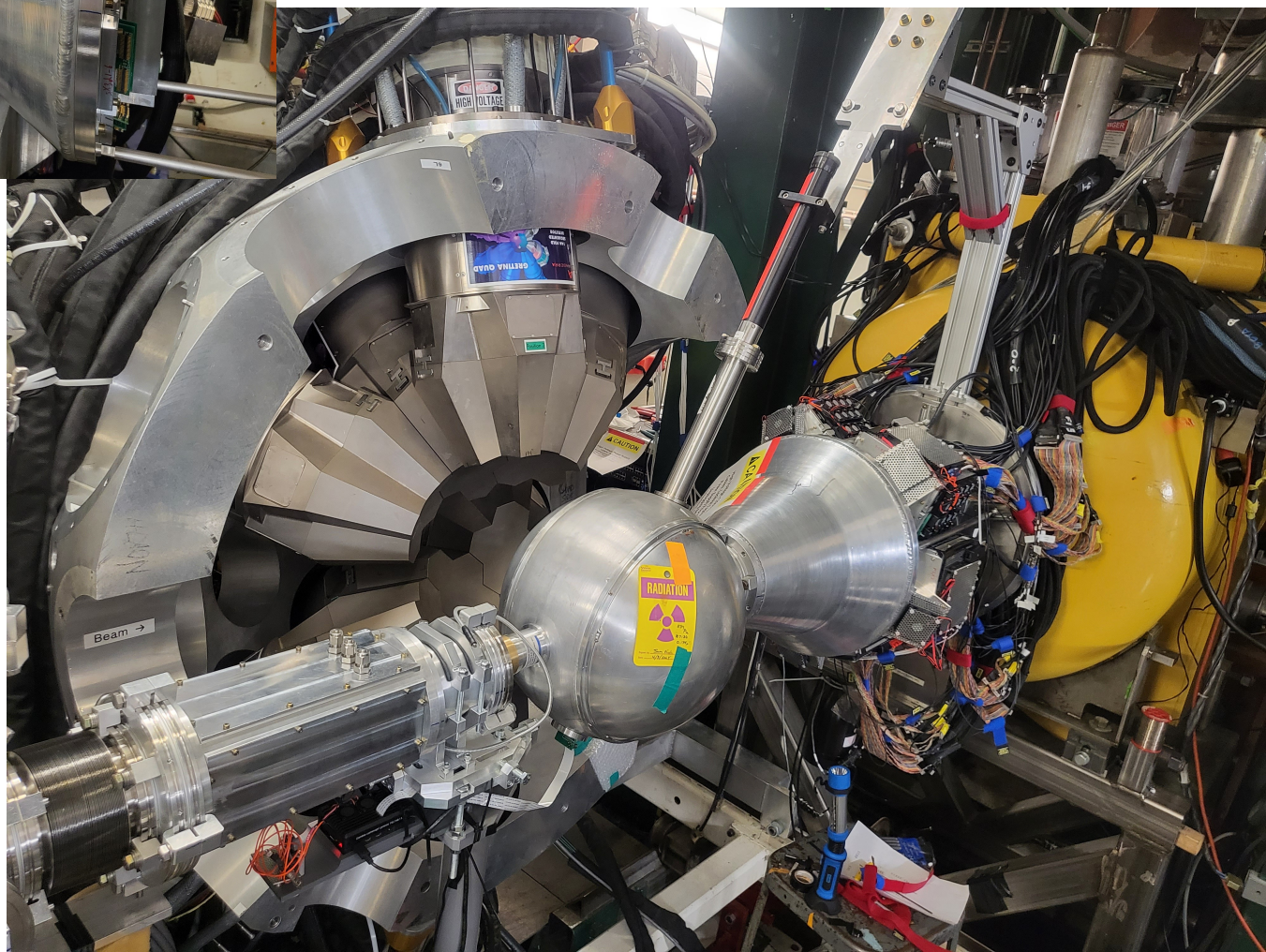
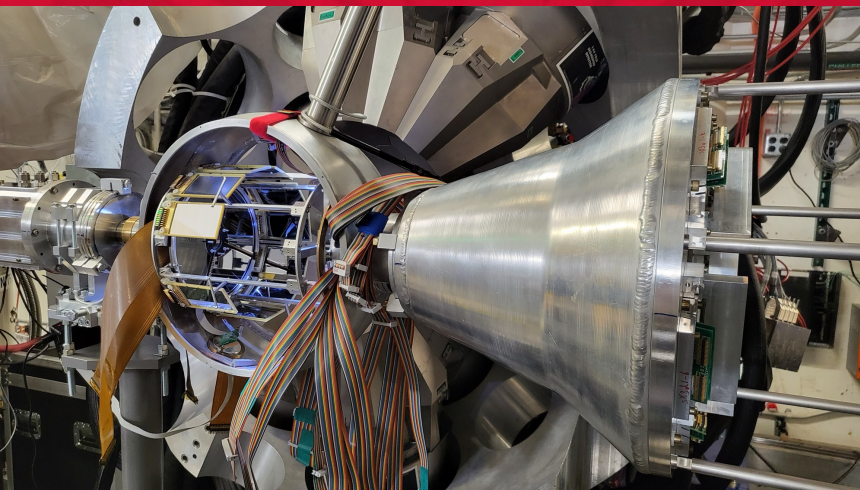
Theory: Escher, Potel, Gorton
(prelim, 6/2024)

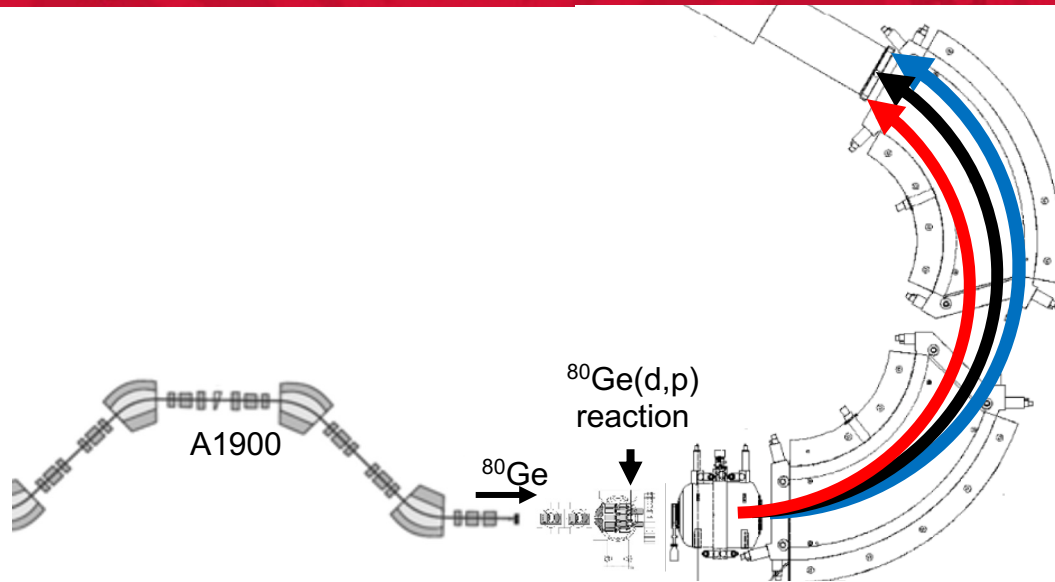
- Measure: $(d, p\gamma)$ with ≈ 45 MeV/u ^{80}Ge (N=48) and ^{75}Ga beams + ORRUBA + GRETINA + S800
- Inform $\sigma(n, \gamma)$
 - No gamma surrogate reaction method
 - Discrete gamma SRM; Gamma rays would confirm isotopics
- Inform i- and weak r-process nucleosynthesis



- ORRUBA + GRETINA at S800
 - beam tracking (gas) detectors
- S800 excellent PID
 - Can separate isotopes
 - Beam blocker
- Requires CD_2 and CH_2 data







GODDESS at FRIB Spring 2024

- Upstream beam tracking chamber
- ORRUBA – charged particles
- GRETINA – gamma rays
- S800 – heavy recoils
 - Blocked $^{80}\text{Ge}(32^+)$ and $^{80}\text{Ge}(31^+)$ beams
- ORRUBA-GRETINA-S800 coincidences

- Can cleanly identify ^{81}Ge channel from (d,p) on $^{80}\text{Ge}(32^+)$
 - Need full analysis
 - Maximize proton energy resolution: Beam tracking
 - Isolate (d,p) protons: Subtraction of CH_2 protons from CD_2 data
 - Maximize ID of ^{81}Ge recoils: use full suite of S800 FP detectors and TOF
 - Prospects for surrogate (n, γ) analysis promising
- Unexpected preliminary results
 - See $^{80}\text{Ge}(31^+)(\text{d,p})^{81}\text{Ge} + \text{n}$: prospects for surrogate (n,n')?
 - See $^{80}\text{Ge}(31^+)(\text{d,p})^{81}\text{Ge} + 2\text{n}$: prospects for surrogate (n,2n)?
- Also, $^{75}\text{Ga}(\text{d,p}\gamma)^{76}\text{Ga}^*$ for surrogate (n, γ) for i-process nucleosynthesis

- (d,p) and (d,p γ) reactions inform i- and weak r- process A \approx 80 nucleosynthesis
- Direct-semi-direct capture near neutron closed shells
 - Measure spectroscopic factors with (d,p)
 - Deduce DSD (n, γ)
- (d,p γ) validated surrogate reaction method (SRM) for (n, γ)
 - Measure discrete gammas
 - Inform LD and γ SF $\Rightarrow G_{\gamma}^{CN}(E_x, J, \pi) \Rightarrow$ inform $\sigma(n,\gamma)$
- Prospects for No Gamma Surrogate (NGS) reaction method
 - Measure total population A+1 nucleus
 - Details of gamma decay not needed
 - $G_{\gamma}^{CN}(E_x, J, \pi) \Rightarrow$ inform $\sigma(n,\gamma)$ with new SRM framework
- Recent measurements ^{80}Ge , $^{75}\text{Ga}(d,p\gamma)$ at FRIB
ORRUBA+GRETINA+S800
 - Preliminary (and unexpected) results

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