

The Shape Method

Mathis Wiedeking

*NRF - iThemba LABS, Cape Town
University of the Witwatersrand, Johannesburg*

Supported by the National Research Foundation under grant number 118840.



science & innovation

Department:
Science and Innovation
REPUBLIC OF SOUTH AFRICA

WITS
UNIVERSITY



iThemba
LABS
Laboratory for Accelerator
Based Sciences

Shape Method



- D_0 is not known.
- No standard approach in absence of D_0 .
- Unambiguous identification of origin and destination of primaries.
- Functional form is retained between primaries from same excitation energy bin.
- Concepts from Average Resonance Capture, Ratio, and χ^2 methods.

PHYSICAL REVIEW C **104**, 014311 (2021)











PHYSICAL REVIEW C **107**, L011602 (2023)

Letter

Independent normalization for γ -ray strength functions: The shape method

M. Wiedeking ^{1,2,*} M. Guttormsen,³ A. C. Larsen,³ F. Zeiser,³ A. G3rgen ³ S. N. Liddick,^{4,5} D. M3ucher,^{6,7} S. Siem,³ and A. Spyrou^{4,8}

Extracting model-independent nuclear level densities away from stability

D. M3ucher ^{1,2,3,*} A. Spyrou,^{4,5,6,†} M. Wiedeking ^{7,8} M. Guttormsen ⁹ A. C. Larsen ⁹ F. Zeiser,⁹ C. Harris,^{10,5} A. L. Richard ^{10,6} M. K. Smith,¹⁰ A. G3rgen ⁹ S. N. Liddick,^{10,11} S. Siem,⁹ H. C. Berg ^{10,5} J. A. Clark,¹² P. A. DeYoung ¹³ A. C. Dombos,¹⁴ B. Greaves ¹ L. Hicks,^{10,5} R. Kelmar,¹⁴ S. Lyons,¹⁵ J. Owens-Fryar ^{10,5} A. Palmisano,^{10,5} D. Santiago-Gonzalez,¹² G. Savard,¹² and W. W. von Seeger¹³



science & innovation

Department:
Science and Innovation
REPUBLIC OF SOUTH AFRICA

WITS
UNIVERSITY



iThemba
LABS
Laboratory for Accelerator
Based Sciences

Shape Method Concepts

Identification of origin and destination of primaries.

Functional form is retained between primary transitions from a specific excitation energy.

Concepts from Average Resonance Capture, Ratio, and χ^2 methods



science & innovation

Department:
Science and Innovation
REPUBLIC OF SOUTH AFRICA

WITS
UNIVERSITY



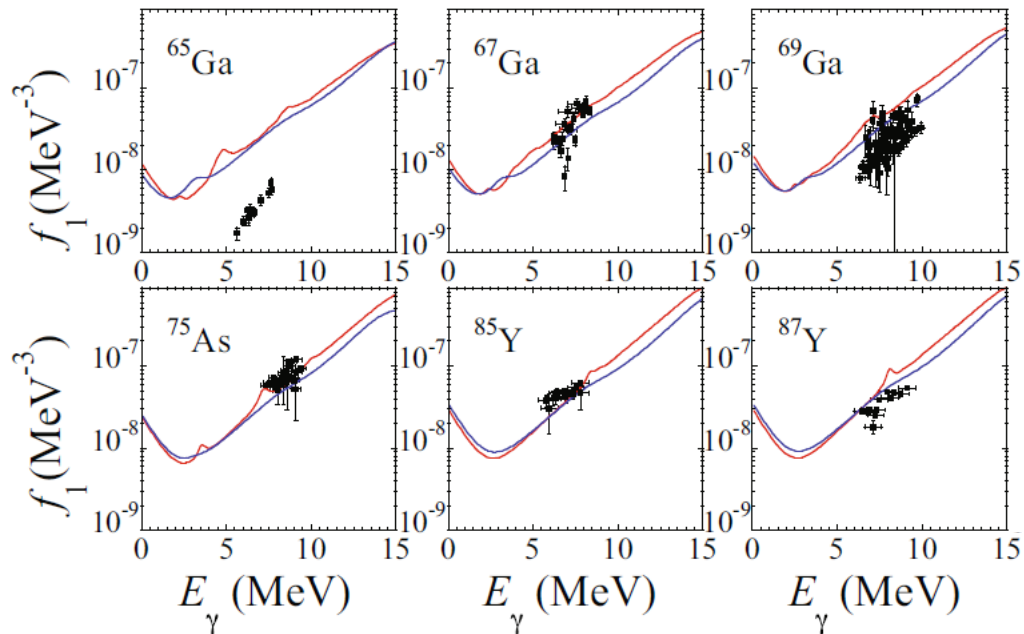
iThemba
LABS
Laboratory for Accelerator
Based Sciences

Shape Method Concepts

Identification of origin and destination of primaries.

Functional form is retained between primary transitions from a specific excitation energy.

Concepts from Average Resonance Capture, Ratio, and X² methods



S. Goriely *et al.*, Eur. Phys. J. A 55, 172 (2019)



science & innovation

Department:
Science and Innovation
REPUBLIC OF SOUTH AFRICA

WITS
UNIVERSITY



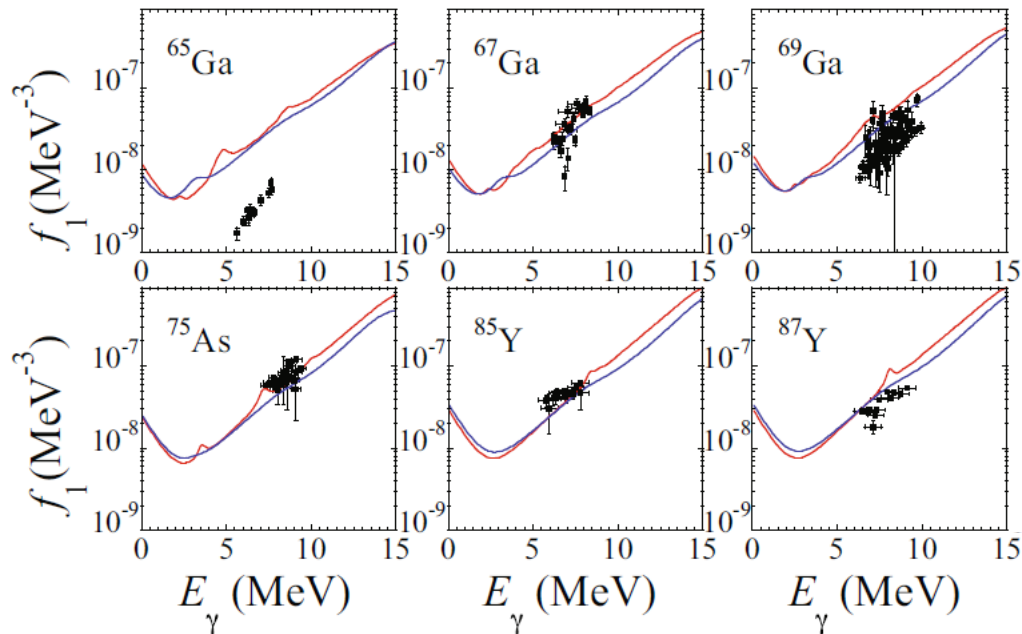
iThemba
LABS
Laboratory for Accelerator
Based Sciences

Shape Method Concepts

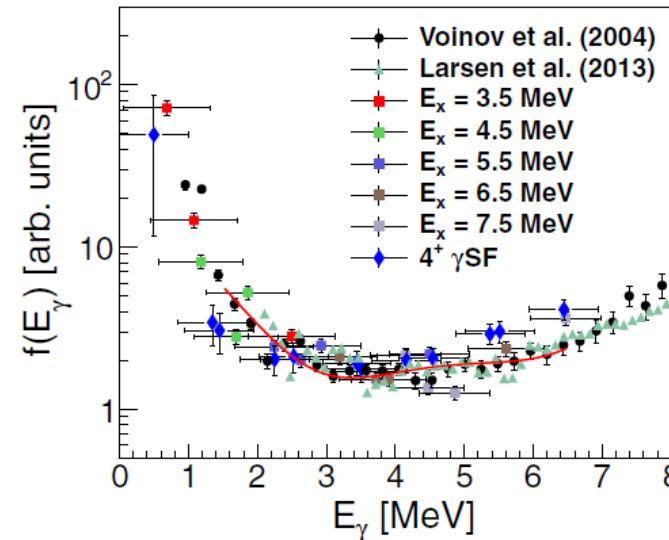
Identification of origin and destination of primaries.

Functional form is retained between primary transitions from a specific excitation energy.

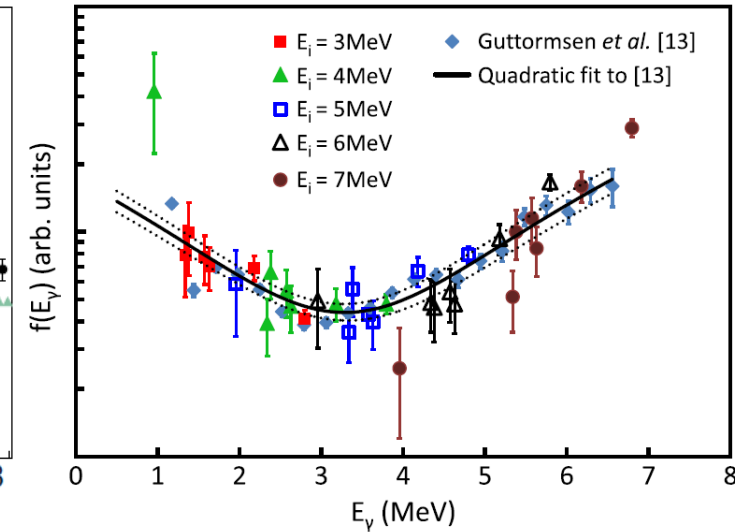
Concepts from Average Resonance Capture, Ratio, and X² methods



S. Goriely *et al.*, Eur. Phys. J. A 55, 172 (2019)



MD Jones *et al.*, PRC 97, 024327 (2018)



MW *et al.*, PRL 108, 0162503(2012).



science & innovation

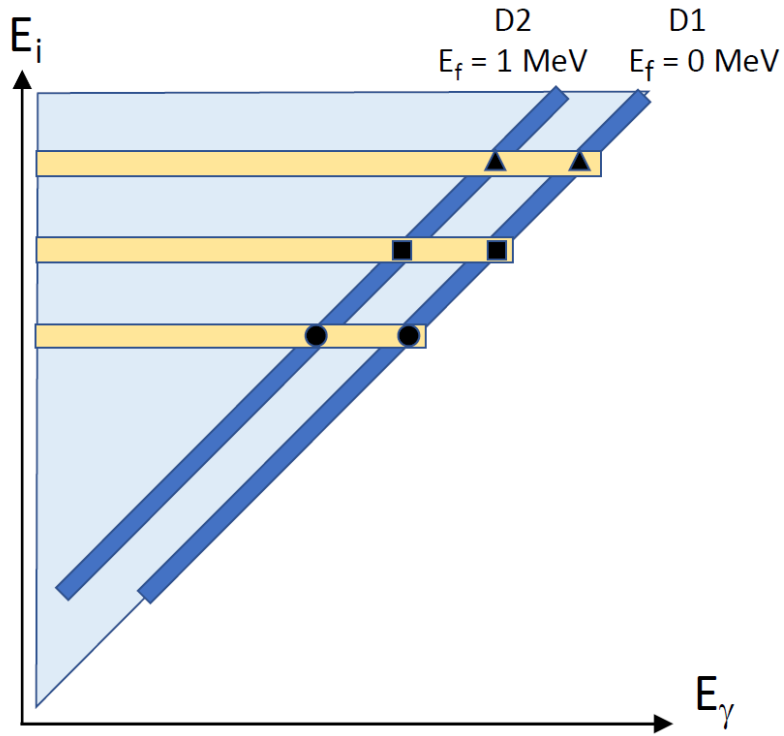
Department:
Science and Innovation
REPUBLIC OF SOUTH AFRICA

WITS
UNIVERSITY



iThemba
LABS
Laboratory for Accelerator
Based Sciences

Shape and Sewing Method



- Primary gamma-rays from intercepts of diagonals with E_x gate.



science & innovation

Department:
Science and Innovation
REPUBLIC OF SOUTH AFRICA

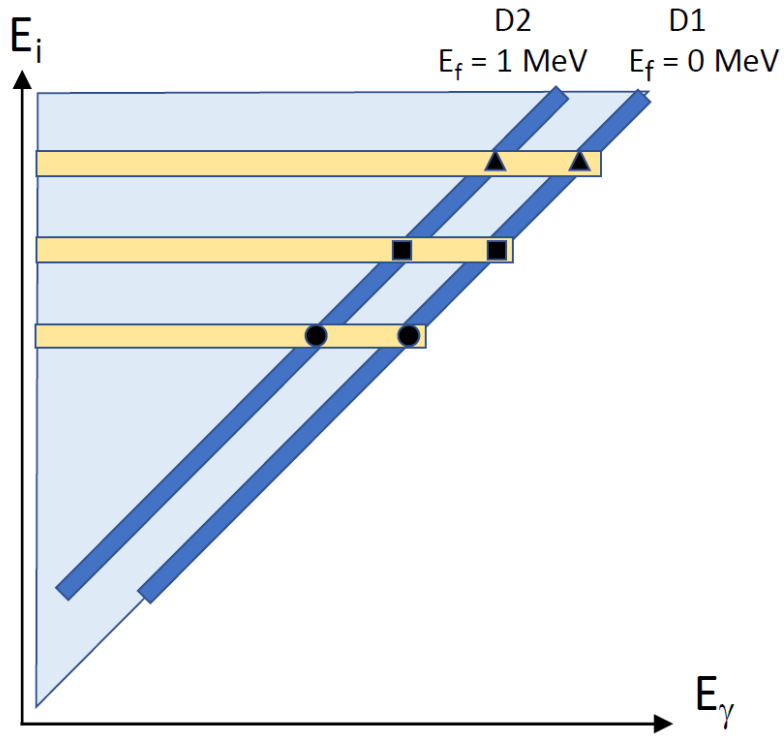
MW, Guttormsen, Larsen *et al.*, Phys Rev C 104, 014311 (2021).

WITS
UNIVERSITY

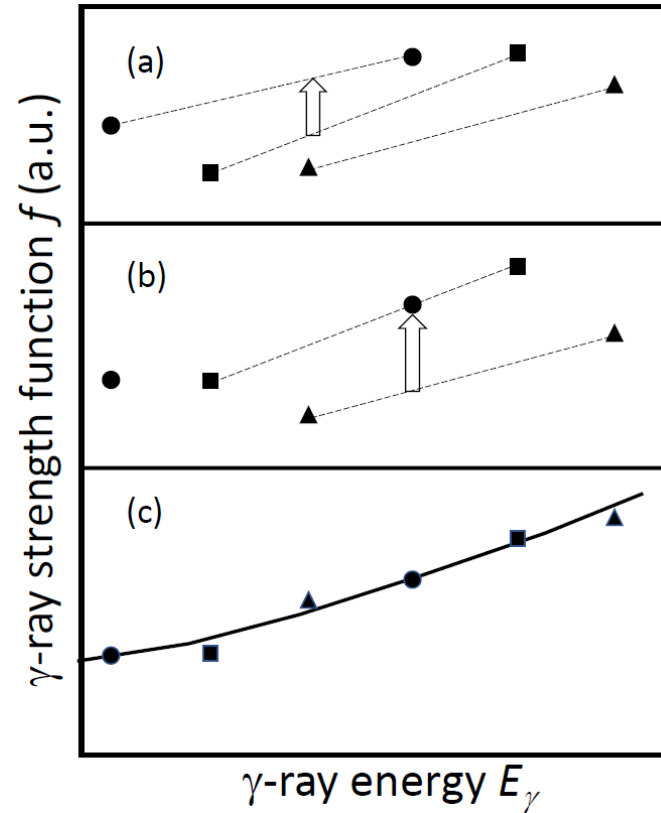


iThemba
LABS
Laboratory for Accelerator
Based Sciences

Shape and Sewing Method



- Primary gamma-rays from intercepts of diagonals with E_x gate.



- Pair of data points internally normalized and proportional to PSF.
- Average γ energy of the extremes of 2 neighboring pairs.
- 2nd pair scaled by a factor to match 1st pair.
- Logarithmic interpolation.
- Results in functional form of PSF.



science & innovation

Department:
Science and Innovation
REPUBLIC OF SOUTH AFRICA

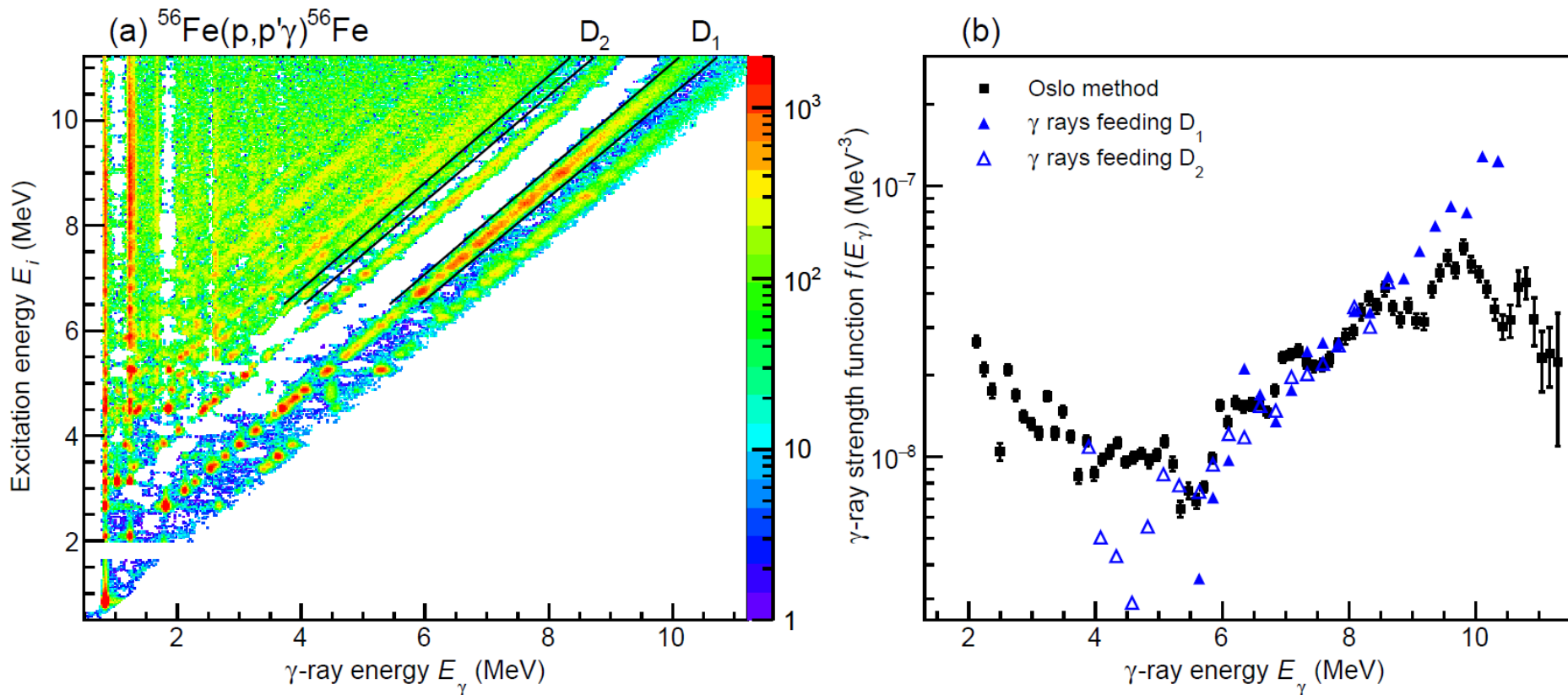
MW, Guttormsen, Larsen *et al.*, Phys Rev C 104, 014311 (2021).

WITS
UNIVERSITY



iThemba
LABS
Laboratory for Accelerator
Based Sciences

Shape Method in practice: ^{56}Fe



$$D_1 = 2^+ \text{ 847 keV}$$

$$D_2 = 2^+ \text{ 2658 keV}$$



science & innovation

Department:
Science and Innovation
REPUBLIC OF SOUTH AFRICA

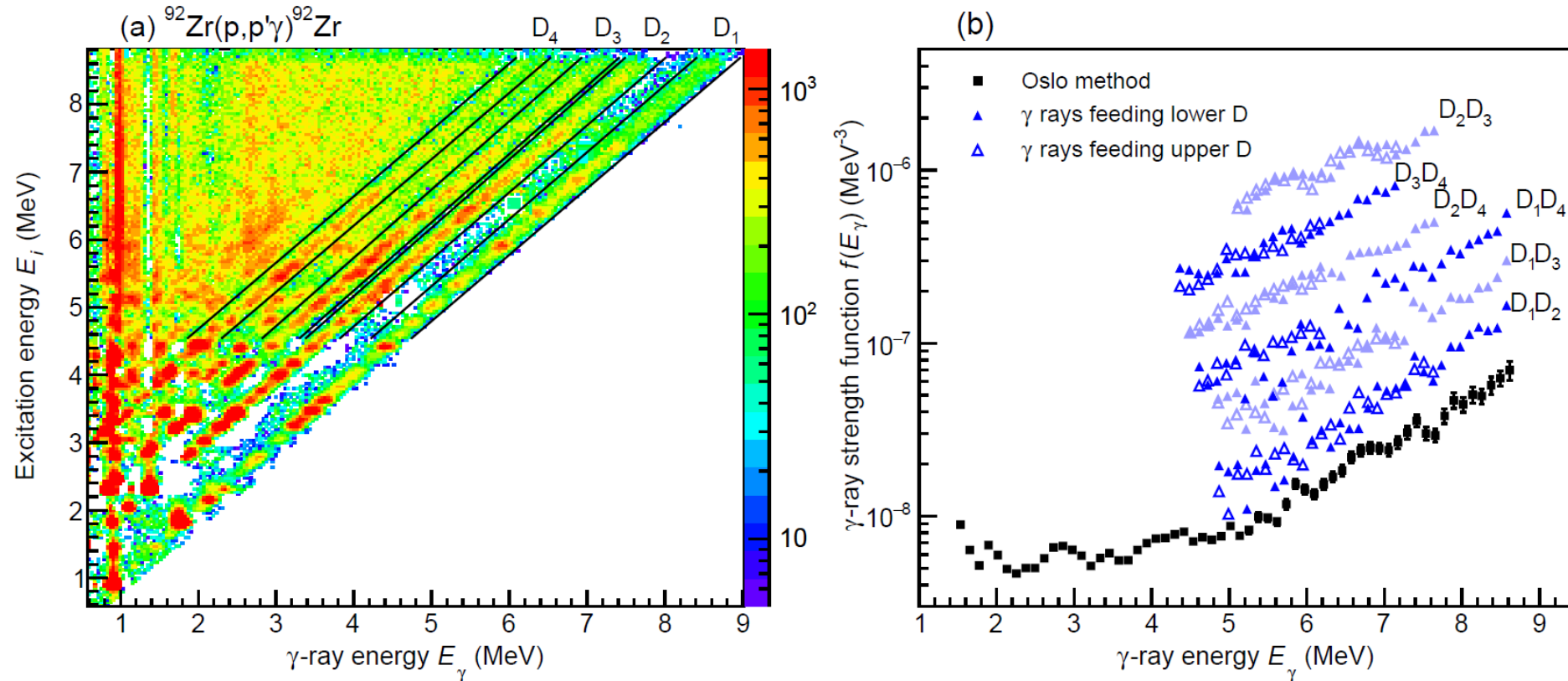
MW, Guttormsen, Larsen *et al.*, Phys Rev C 104, 014311 (2021).

WITS
UNIVERSITY



iThemba
LABS
Laboratory for Accelerator
Based Sciences

Shape Method in practice: ^{92}Zr



$$D_1 = 0^+ 0 \text{ keV}$$

$$D_3 = 0^+ 1383 \text{ \& } 4^+ 1495 \text{ keV}$$

$$D_2 = 2^+ 934 \text{ keV}$$

$$D_4 = 3^- 2340 \text{ \& } 4^+ 2398 \text{ \& } 5^- 2486 \text{ keV}$$



science & innovation

Department:
Science and Innovation
REPUBLIC OF SOUTH AFRICA

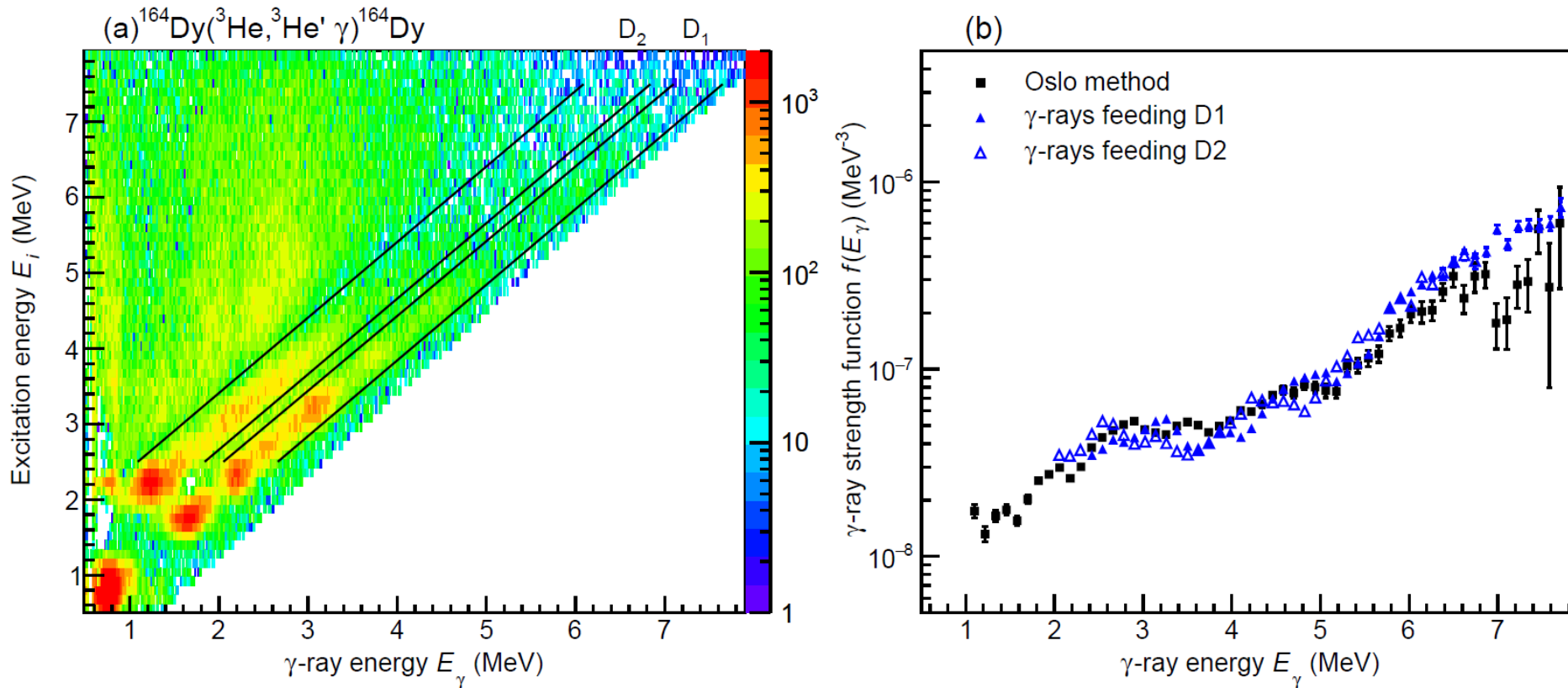
MW, Guttormsen, Larsen *et al.*, Phys Rev C 104, 014311 (2021).

WITS
UNIVERSITY



iThemba
LABS
Laboratory for Accelerator
Based Sciences

Shape Method in practice: ^{164}Dy



$D_1 = 0^+, 2^+, 4^+, 6^+, 0 - 0.5$ MeV
 $D_2 = 14$ levels $0.76 - 1.39$ MeV



science & innovation

Department:
Science and Innovation
REPUBLIC OF SOUTH AFRICA

MW, Guttormsen, Larsen *et al.*, Phys Rev C 104, 014311 (2021).

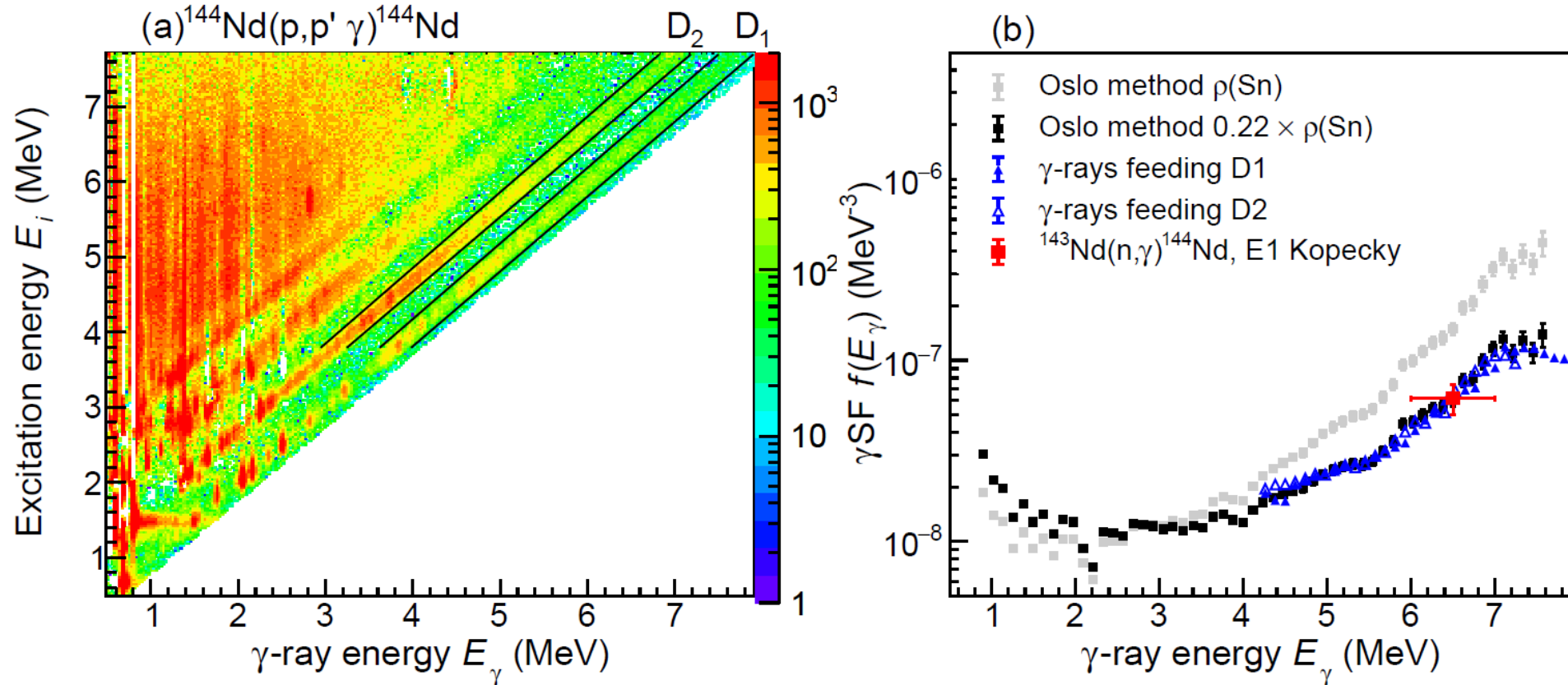
WITS
UNIVERSITY



iThemba
LABS
Laboratory for Accelerator
Based Sciences

Shape Method in practice: ^{144}Nd

Guttormsen, Ay, Ozgur et al., Phys. Rev. C 106, 034314 (2022).
Comprehensive study on PSF evolution for 9 Nd isotopes.



science & innovation

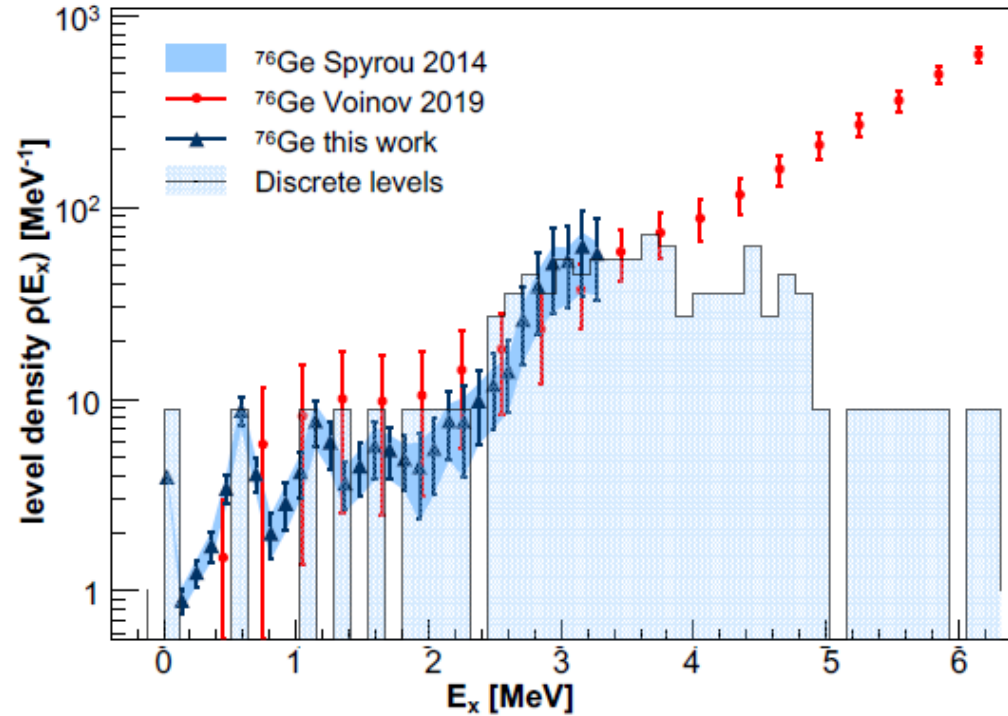
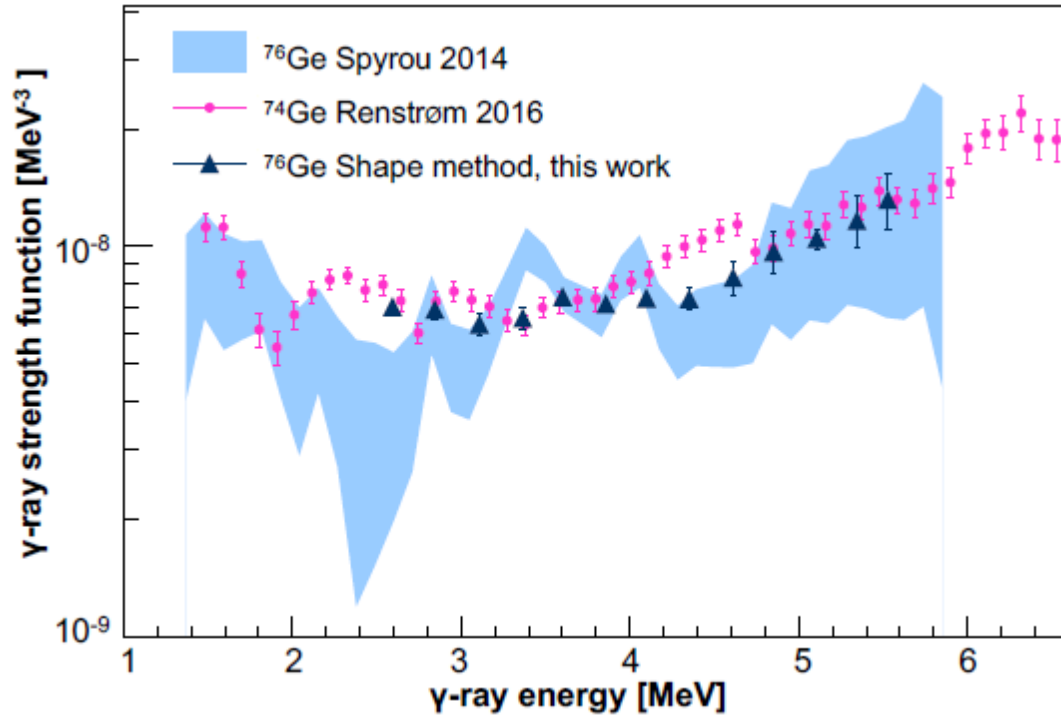
Department:
Science and Innovation
REPUBLIC OF SOUTH AFRICA

WITS
UNIVERSITY



iThemba
LABS
Laboratory for Accelerator
Based Sciences

Shape Method and NLD on stable isotope



Mücher, Spyrou, MW et al., Phys. Rev. C 107, L011602 (2023).



science & innovation

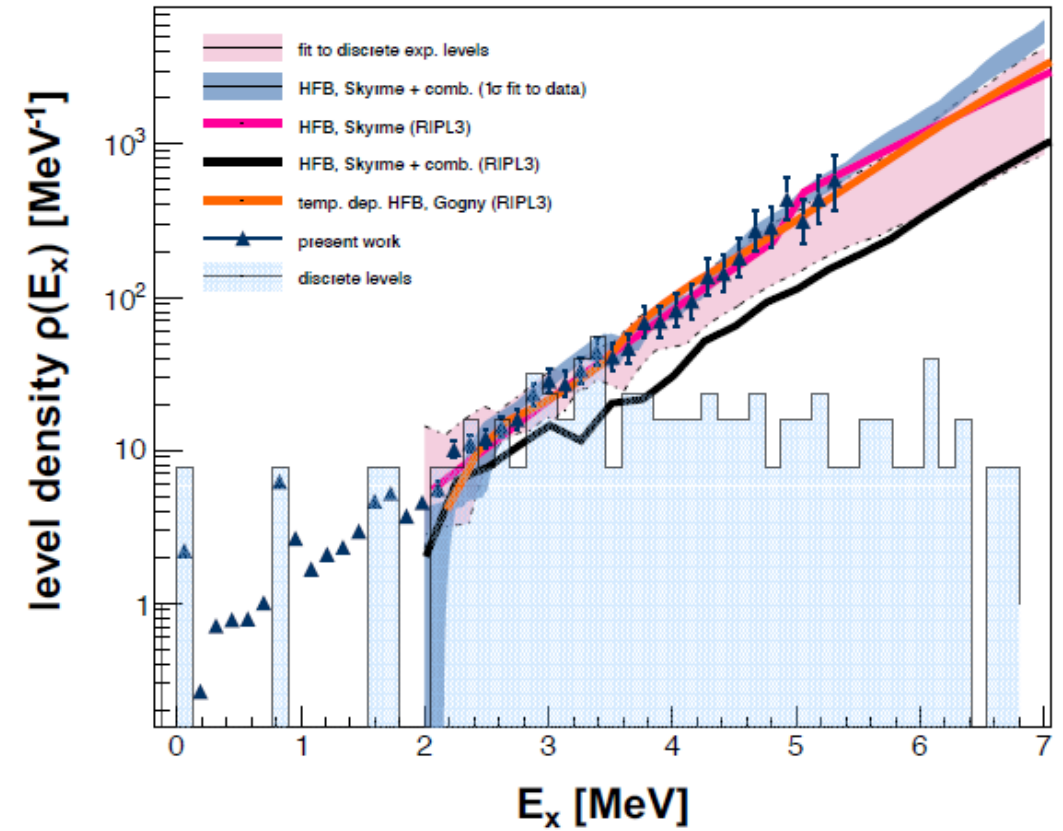
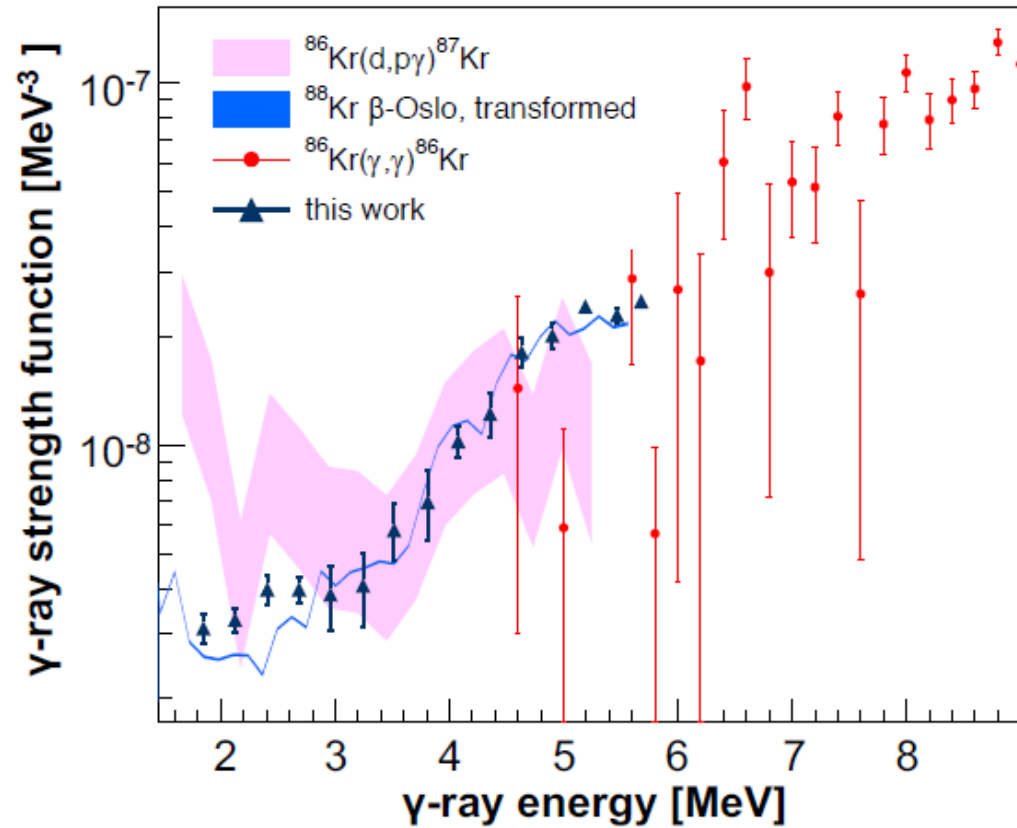
Department:
Science and Innovation
REPUBLIC OF SOUTH AFRICA

WITS
UNIVERSITY



iThemba
LABS
Laboratory for Accelerator
Based Sciences

Shape Method and NLD on radioactive isotope



Mücher, Spyrou, MW et al., Phys. Rev. C 107, L011602 (2023).



science & innovation

Department:
Science and Innovation
REPUBLIC OF SOUTH AFRICA

WITS
UNIVERSITY



iThemba
LABS
Laboratory for Accelerator
Based Sciences