

DE LA RECHERCHE À L'INDUSTRIE



The NEVFAR project:

New Evaluation of  $\nu$  Fluxes At Reactors

# Revisiting the summation calculation of reactor antineutrino spectra

**Lorenzo Périssé<sup>(a)</sup>**

Xavier Mougeot, Anthony Onillon<sup>(b)</sup>, Matthieu Vivier

CEA/IRFU/DPHP – CEA/List/LNE-LNHB

CEA-Saclay, 91191 Gif-sur-Yvette, FRANCE

[www.cea.fr](http://www.cea.fr)

**IAEA TM on Nuclear Data Needs for Antineutrino Spectra Applications**

18 January 2023

<sup>(a)</sup>Now at ILANCE (CNRS/UTokyo), Japan

<sup>(b)</sup>Now at TUM, Germany

## 1. Introduction & motivations

- a. Reactors as antineutrino sources
- b. Experimental anomalies
- c. Different modeling methods

## 2. Revised summation method

- a.  $\beta^-$  spectrum calculation
- b. Nuclear data content
- c. Uncertainty budget

## 3. Preliminary comparisons

- a. Integral measurements
- b. Spectrum shape

## 4. Conclusion & perspectives

## 1. Introduction & motivations

- a. Reactors as antineutrino sources
- b. Experimental anomalies
- c. Different modeling methods

## 2. Revised summation method

- a.  $\beta^-$  spectrum calculation
- b. Nuclear data content
- c. Uncertainty budget

## 3. Preliminary comparisons

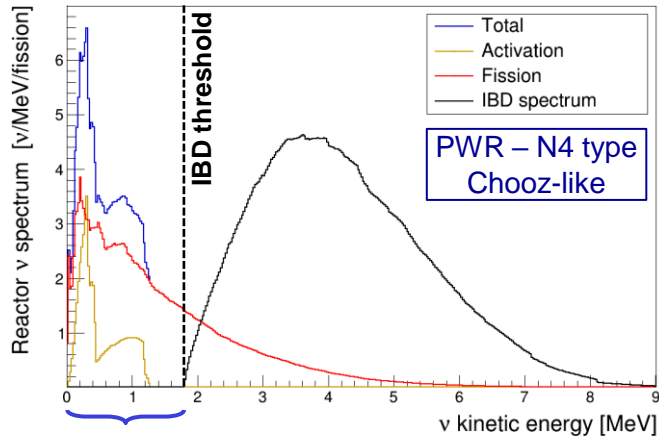
- a. Integral measurements
- b. Spectrum shape

## 4. Conclusion & perspectives

### PRESSURIZED WATER REACTOR (PWR)

- Fuel: lowly enriched uranium,  $^{238}\text{U}$  + 3-5%  $^{235}\text{U}$
- High power:  $\sim 3 - 4 \text{ GW}_{\text{th}}$
- Similar reactor design & fuel contents for all PWR

⇒ Similar  $\bar{\nu}_e$  spectra



~75%  $\bar{\nu}_e$ : 76% fission + 24% capture

#### Typical fission fraction

$^{235}\text{U}$	0.559	} ~83% $\Phi_{\bar{\nu}_e}$
$^{239}\text{Pu}$	0.291	
$^{238}\text{U}$	0.088	
$^{241}\text{Pu}$	0.062	

#### Activation [ $\bar{\nu}_e$ /fission]

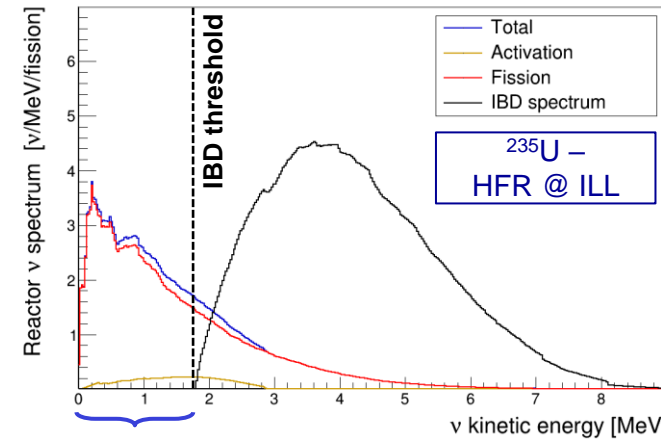
$^{239}\text{U}$	0.6	} ~17% $\Phi_{\bar{\nu}_e}$
$^{239}\text{Np}$	0.6	

Average event/fission for a Chooz type reactor ( $\sim 4\% ^{235}\text{U}$ ) over a 12-month core cycle

### RESEARCH REACTOR

- Fuel: highly enriched uranium,  $>20\% ^{235}\text{U}$
- Low power :  $\sim 0.1 \text{ kW}_{\text{th}} - 100 \text{ MW}_{\text{th}}$  but very short baseline accessible
- Wide array of designs & fuel contents + reactor specific structural material activation

⇒ Reactor-specific  $\bar{\nu}_e$  spectra



~69%  $\bar{\nu}_e$ : 94% fission + 6% capture

#### Fission fraction

$^{235}\text{U}$	0.993	} ~93% $\Phi_{\bar{\nu}_e}$
$^{239}\text{Pu}$	0.007	

#### Activation [ $\bar{\nu}_e$ /fission]

$^{239}\text{U}$	0.013	} ~7% $\Phi_{\bar{\nu}_e}$
$^{239}\text{Np}$	0.013	
$^{28}\text{Al}$	0.346	
$^{56}\text{Mn}$	0.058	

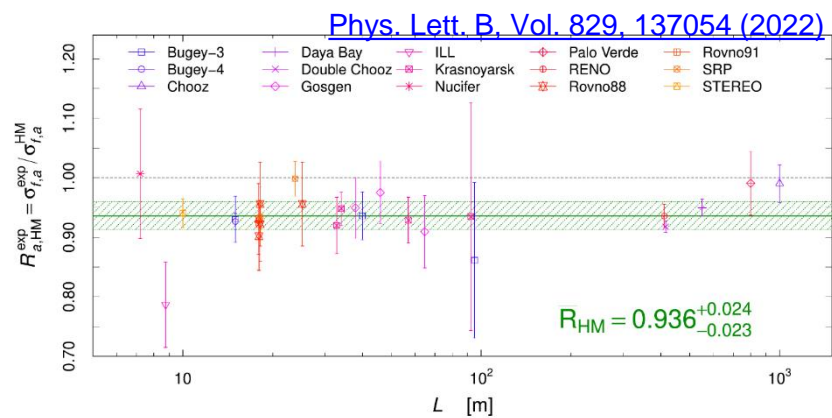
Average event/fission for the HFR at the ILL ( $\sim 93\% ^{235}\text{U}$ ) over a 50-day core cycle

⇒  $\bar{\nu}_e$  contribution depends on reactor type and changes with time

⇒ Prediction needed for fission and activation spectra

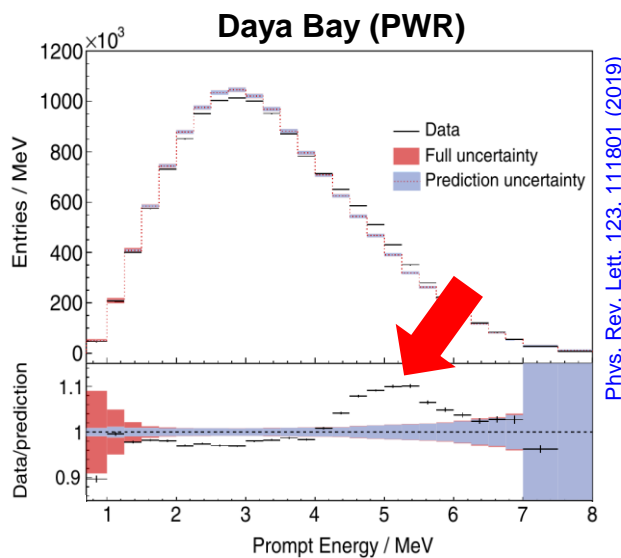
## REACTOR ANTINEUTRINO ANOMALY (RAA)

- Systematic IBD rate deficit vs to HM
- Measured/predicted IBD rate:  $0.936^{+0.024}_{-0.023}$  ( $2.5\sigma$ )
- RAA possible origins
  - ▶ Experimental bias *Unlikely*
  - ▶ New physics (sterile neutrino)
  - ▶ **Mismodeling / underestimation of  $\bar{\nu}_e$  spectrum uncertainty**
  - ▶ **Single / multiple actinide(s) ?**



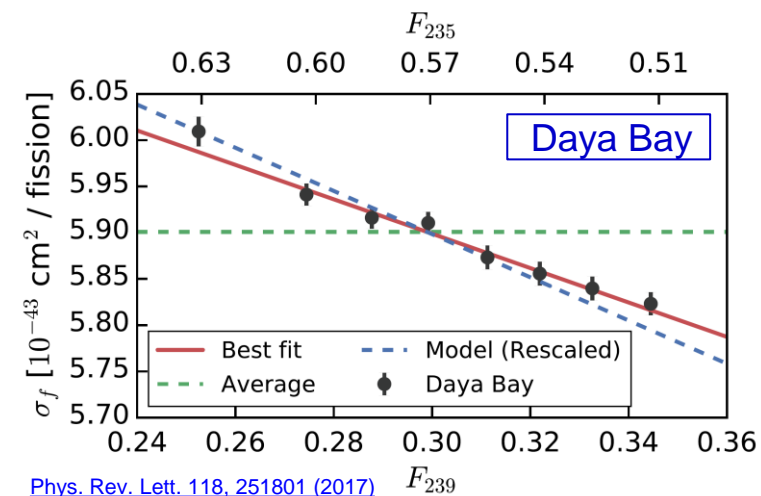
## SHAPE ANOMALY

- First observed by Double Chooz, Daya Bay; RENO
  - ▶ Confirmed by recent very-short baseline reactor exp. (NEOS, STEREO, PROSPECT, DANSS)
- Possible origins
  - ▶ Detector energy scale calibration *Checked*
  - ▶ Fuel composition
  - ▶ **Prediction issue, single / multiple actinide(s) ?**



## FUEL-DEPENDENT IBD RATE EVOLUTION

- IBD yield changes with fuel evolution of PWR
- Comparison between measured IBD yield evolution and predicted evolution
  - ▶  $3.1\sigma$  at Daya Bay
  - ▶  $1.3\sigma$  at RENO
- Induced by unequal fractional deficit among actinides



## REACTOR DATA-DRIVEN METHOD

- Unfolding **exp. prompt IBD** spectrum
  - ▷  $\bar{\nu}_e$  spectrum + covariance matrix



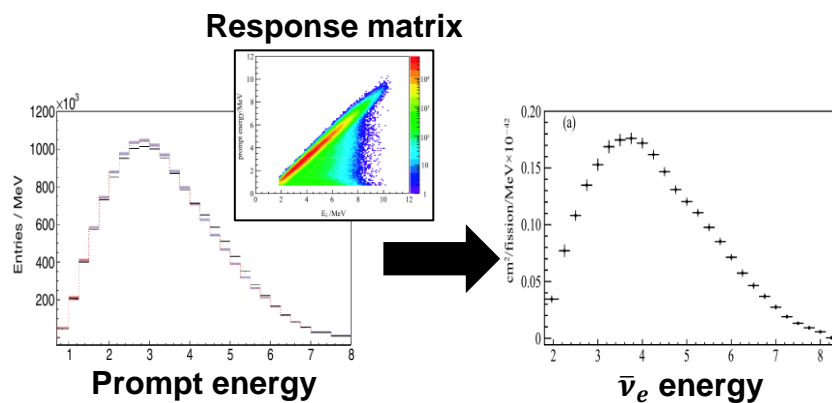
### PROS

- Model-independent (no anomalies)
- Small uncertainties



### CONS

- Limited to exp. range, 1.8-9 MeV
- Small number of available datasets
- **No activation spectrum**



## CONVERSION METHOD

- Measure **exp.  $\beta$  fission spectra**
- Convert virtual  $\beta$  branch fit to  $\bar{\nu}_e$  branches



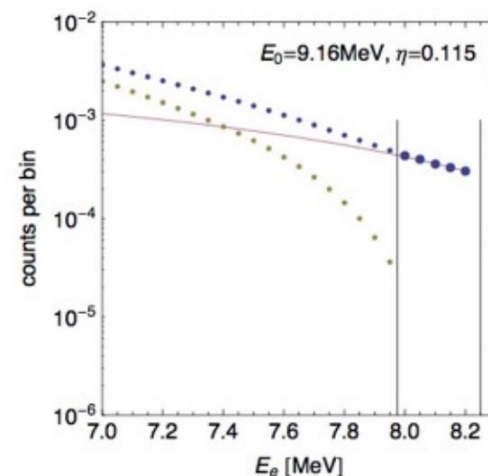
### PROS

- Small uncertainties  $\sim 2-3\%$
- Access total  $\bar{\nu}_e$  fission spectrum



### CONS

- Limited to exp. range, 2-8 MeV
- No activation spectrum
- **HM subject to the anomalies**
- BILL data questioned  $\rightarrow$  KI exp.
- Impact of forbidden branches on fit



## SUMMATION METHOD

- Fission spectrum prediction = **sum of all  $\beta$  branches** listed in nuclear databases
- +900  $\beta^-$  emitters  $\sim 10\,000$   $\beta^-$  transitions



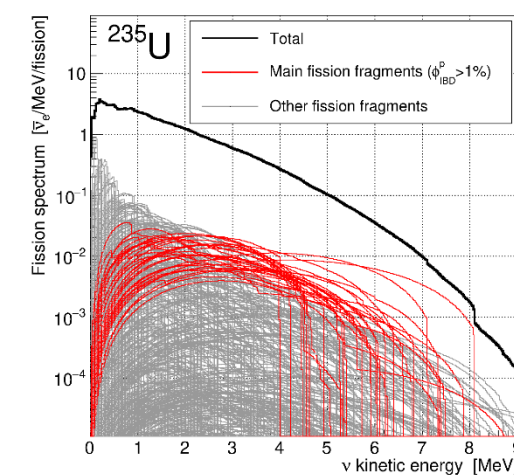
### PROS

- Prediction  $\forall$  energy,  $\forall$   $\beta$  emitter
  - ▷ CEvNS
- Convenient to understand physics
- **Mandatory for activation spectra**



### CONS

- Uncomplete/biased nuclear database
- Modeling approximations
- **Uncertainties very complex to estimate**



## REACTOR DATA-DRIVEN METHOD

- Unfolding **exp. prompt IBD** spectrum
  - ▷  $\bar{\nu}_e$  spectrum + covariance matrix



### PROS

- Model-independent (no anomalies)
- Small uncertainties



### CONS

- Limited to exp. range, 1.8-9 MeV
- Small number of available datasets
- **No activation spectrum**

Daya Bay: Total,  $^{235}\text{U}$ ,  $^{239}\text{Pu}$

RENO, NEOS: Total

STEREO, PROSPECT:  $^{235}\text{U}$

## CONVERSION METHOD

- Measure **exp.  $\beta$  fission spectra**
- Convert virtual  $\beta$  branch fit to  $\bar{\nu}_e$  branches



### PROS

- Small uncertainties ~2-3%
- Access total  $\bar{\nu}_e$  fission spectrum



### CONS

- Limited to exp. range, 2-8 MeV
- No activation spectrum
- **HM subject to the anomalies**
- BILL data questioned → KI exp.
- Impact of forbidden branches on fit

### Huber-Mueller model (+ KI data)

⇒  **$^{235}\text{U}$ ,  $^{239}\text{Pu}$  and  $^{241}\text{Pu}$  from P. Huber**  
[PRC 84, 024617 \(2011\)](#)

⇒  **$^{235}\text{U}/^{239}\text{Pu}$  data from KI**  
[PRD 104, L071301 \(2021\)](#)

## SUMMATION METHOD

- Fission spectrum prediction = **sum of all  $\beta$  branches** listed in nuclear databases
- +900  $\beta^-$  emitters ~ 10 000  $\beta^-$  transitions



### PROS

- Prediction  $\forall$  energy,  $\forall$   $\beta$  emitter
  - ▷ CEvNS
- Convenient to understand physics
- **Mandatory for activation spectra**



### CONS

- Uncomplete/biased nuclear database
- Modeling approximations
- **Uncertainties very complex to estimate**

⇒  **$^{238}\text{U}$  from Mueller *et al.***  
[PRC 83, 054615 \(2011\)](#)

## THE NE<sub>v</sub>FAR PROJECT

(New Evaluation of  $\nu$  Fluxes At Reactor)



- Revise summation method with BESTIOLE code
  - ▷ Improve  $\beta$ -decay modeling
    - Refine **non-unique forbidden transition** modeling
  - ▷ Impact of database incompleteness and quality
    - Update nuclear database with **Pandemonium-free data**
    - Adjusted effective modeling for **nuclides with no data**
  - ▷ Build a **comprehensive uncertainty** budget
    - Nuclear data and modeling uncertainties



**All results are preliminary**

## SUMMATION METHOD

- Fission spectrum prediction = **sum of all  $\beta$  branches** listed in nuclear databases
- +900  $\beta^-$  emitters  $\sim$  10 000  $\beta^-$  transitions



### PROS

- Prediction  $\forall$  energy,  $\forall$   $\beta$  emitter
  - ▶ CE $\nu$ NS
- Convenient to understand physics
- **Mandatory for activation spectra**



### CONS

- Uncomplete/biased nuclear database
- Modeling approximations
- **Uncertainties very complex to estimate**

**$\Rightarrow$  Reliable summation method required for multiple purposes**



## 1. Introduction & motivations

- a. Reactors as antineutrino sources
- b. Experimental anomalies
- c. Different modeling methods

## 2. Revised summation method

- a.  $\beta^-$  spectrum calculation
- b. Nuclear data content
- c. Uncertainty budget

## 3. Preliminary comparisons

- a. Integral measurements
- b. Spectrum shape

## 4. Conclusion & perspectives

W. Bühring and H. Behrens formalism (1982)

V-A THEORY OF  $\beta$ -DECAY

- $p$ :  $\beta$  momentum
- $W$ :  $\beta$  total energy
- $W_0$ : max available energy
- $E_0 = W_0 - m_e$ : max kinetic energy
- $K$ : normalization factor  $\int dW S_\beta = 1$

$$S_\beta(Z, A, W) = K pW(W_0 - W)^2 F_0(Z, A, W) C(Z, A, W) (1 + \delta_{WM} + \delta_{RC})$$

- **Phase space**

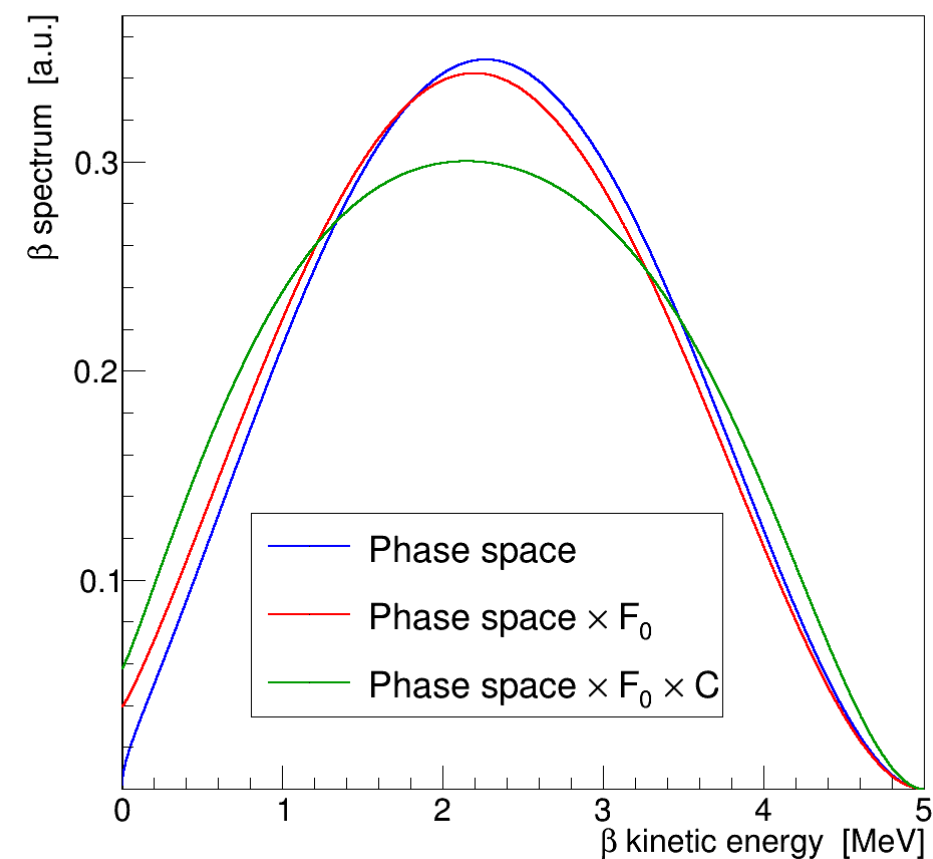
- ▷ Energy states accessible to the emitted  $\beta$

- **Fermi function**

- ▷ Electromagnetic interaction  $\beta$  / daughter nucleus
- ▷ Depends on  $\beta$  wavefunction

- **Shape factor**

- ▷ Nuclear structure effect, depends on spin-parity
- ▷ Depends on  $\beta$  wavefunction



## W. Bühring and H. Behrens formalism (1982)

V-A THEORY OF  $\beta$ -DECAY

$$S_\beta(Z, A, W) = K pW(W_0 - W)^2 \boxed{F_0(Z, A, W) C(Z, A, W)} (1 + \delta_{WM} + \delta_{RC})$$

- $p$ :  $\beta$  momentum
- $W$ :  $\beta$  total energy
- $W_0$ : max available energy
- $E_0 = W_0 - m_e$ : max kinetic energy
- $K$ : normalization factor  $\int dW S_\beta = 1$

## • Phase space

- ▷ Energy states accessible to the emitted  $\beta$

## • Fermi function

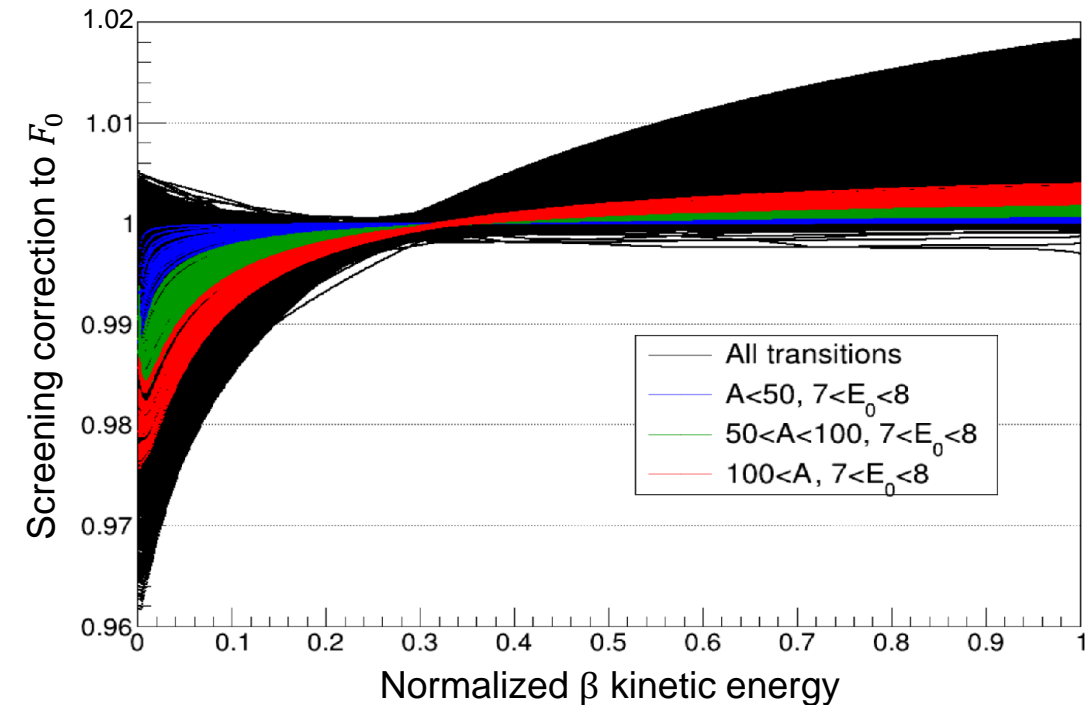
- ▷ Electromagnetic interaction  $\beta$  / daughter nucleus
- ▷ Depends on  $\beta$  wavefunction

## • Shape factor

- ▷ Nuclear structure effect, depends on spin-parity
- ▷ Depends on  $\beta$  wavefunction

Behrens & Bühring algorithm (1982)

- ✓  $\beta$  wavefunction computation depends on nuclear potential
- ✓ Reproduce Behrens & Jänecke tables
  - Finite-size and screening corrections to **Fermi functions** and to **unique forbidden shape factors**
- ✓ Extended to any energy, for any spherical nuclear potential



⇒ Impact of more realistic nuclear potential modeling <0.2% on fission spectrum shape and IBD yield

## W. Bühring and H. Behrens formalism (1982)

V-A THEORY OF  $\beta$ -DECAY

$$S_\beta(Z, A, W) = K pW(W_0 - W)^2 F_0(Z, A, W) C(Z, A, W) (1 + \delta_{WM} + \delta_{RC})$$

- $p$ :  $\beta$  momentum
- $W$ :  $\beta$  total energy
- $W_0$ : max available energy
- $E_0 = W_0 - m_e$ : max kinetic energy
- $K$ : normalization factor  $\int dW S_\beta = 1$

## • Phase space

- ▷ Energy states accessible to the emitted  $\beta$

## • Fermi function

- ▷ Electromagnetic interaction  $\beta$  / daughter nucleus
- ▷ Depends on  $\beta$  wavefunction

## • Shape factor

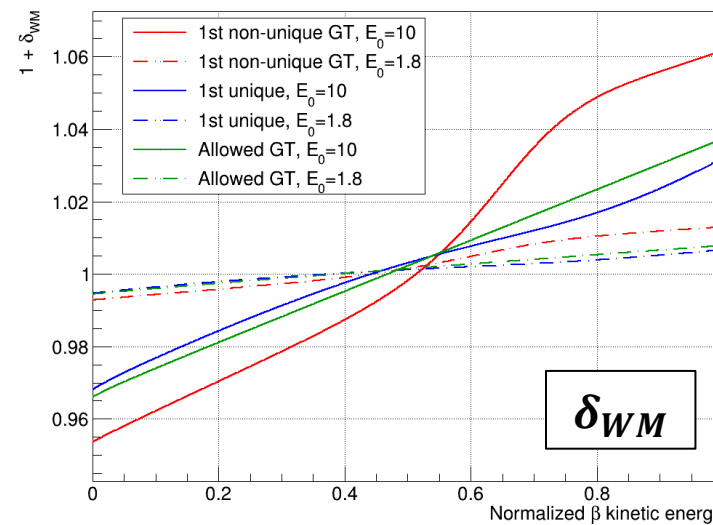
- ▷ Nuclear structure effect, depends on spin-parity
- ▷ Depends on  $\beta$  wavefunction

## • Radiative correction (RC)

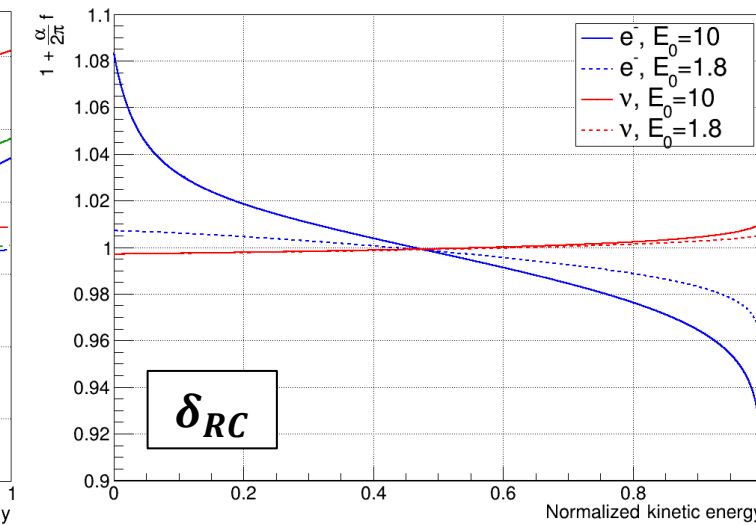
- ▷ QED effect from virtual photon exchange
- ▷  $\beta$  correction  $\gg \bar{\nu}_e$  correction

## • Weak magnetism correction (WM)

- ▷ Nucleon structure effect
- ▷ Depends on spin-parity info



Hayes et al., Phys. Rev. Lett. 112, 202501 (2014)



Correction  $\beta$ : [Sirlin, Phys. Rev. 164, 1767 \(1967\)](#)

Correction  $\bar{\nu}_e$ : [Sirlin, Phys. Rev. D 84, 014021 \(2011\)](#)

WM correction in Behrens & Bühring  $\rightarrow$  allowed GT and non-unique forbidden

✓ Apply WM correction of allowed GT to non-unique forbidden branches

✓ Uncertainty derived for fission spectra  $\rightarrow \sigma_{IBD}(WM) = 0.3\%$

CLASSIFICATION OF  $\beta^-$  TRANSITIONS

*Fluxes for typical PWR  
fission fractions*

$\beta$ -decay type	$\Delta J$	$\pi_i \pi_j$	Shape factor	Calculation	$\bar{\nu}_e$ [%]	IBD [%]
Allowed	0,1	+1	1	<i>Robust and accurate</i>	61	47
Unique forbidden	$n + 1$	$(-1)^n$	Polynomial in $p_\nu$ & $p_e$		10	9

CLASSIFICATION OF  $\beta^-$  TRANSITIONS

$\beta$ -decay type	$\Delta J$	$\pi_i \pi_j$	Shape factor	Calculation	$\bar{\nu}_e$ [%]	IBD [%]
Allowed	0,1	+1	1	<i>Robust and accurate</i>	61	47
Unique forbidden	$n + 1$	$(-1)^n$	Polynomial in $p_\nu$ & $p_e$		10	9
1 <sup>st</sup> non-unique forbidden	0,1	-1	Nuclear struct. calcul.	<i>Advanced calculation</i>	24	38
Main ( $\varphi_{IBD} \geq 1\%$ )					6	27
Others					18	11
$n^{\text{th}}$ non-unique forbidden	$n$	$(-1)^n$	$\xi$ -approximation	<i>Unknown accuracy</i>	3	1

## NON-UNIQUE FORBIDDEN SHAPE FACTOR

- No simple expression
  - ▷ Depends on **transition matrix elements** connecting nuclear states
  - ▷ Nuclear structure calculations or  $\xi$ -approximation

Fluxes for typical PWR fission fractions

### CLASSIFICATION OF $\beta^-$ TRANSITIONS

$\beta$ -decay type	$\Delta J$	$\pi_i \pi_j$	Shape factor	Calculation	$\bar{\nu}_e$ [%]	IBD [%]
Allowed	0,1	+1	1	<i>Robust and accurate</i>	61	47
Unique forbidden	$n + 1$	$(-1)^n$	Polynomial in $p_\nu$ & $p_e$		10	9
1 <sup>st</sup> non-unique forbidden	0,1	-1	Nuclear struct. calcul.	<i>Advanced calculation</i>	24	38
Main ( $\varphi_{IBD} \geq 1\%$ )					6	27
Others					18	11
$n^{\text{th}}$ non-unique forbidden	$n$	$(-1)^n$	$\xi$ -approximation	<i>Unknown accuracy</i>	3	1

#### NON-UNIQUE FORBIDDEN SHAPE FACTOR

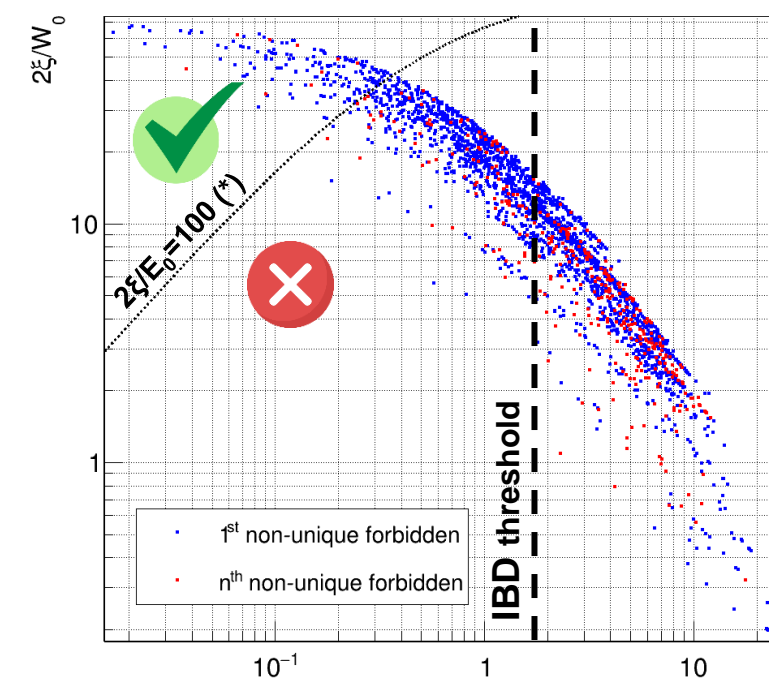
- No simple expression
  - Depends on **transition matrix elements** connecting nuclear states
  - Nuclear structure calculations or  $\xi$ -approximation

#### $\xi$ -approximation

$$2\xi = \alpha Z / R_n \gg W_0$$

- $\alpha$ : fine structure constant
- $R_n$ : radius of the daughter
- $W_0$ : max available energy for the transition

- If verified:  $n^{\text{th}}$  non-unique  $\sim (n - 1)^{\text{th}}$  unique
- Applied to all non-unique transitions  $\rightarrow$  **induce mismodeling**
  - Except 23 important non-unique transitions**



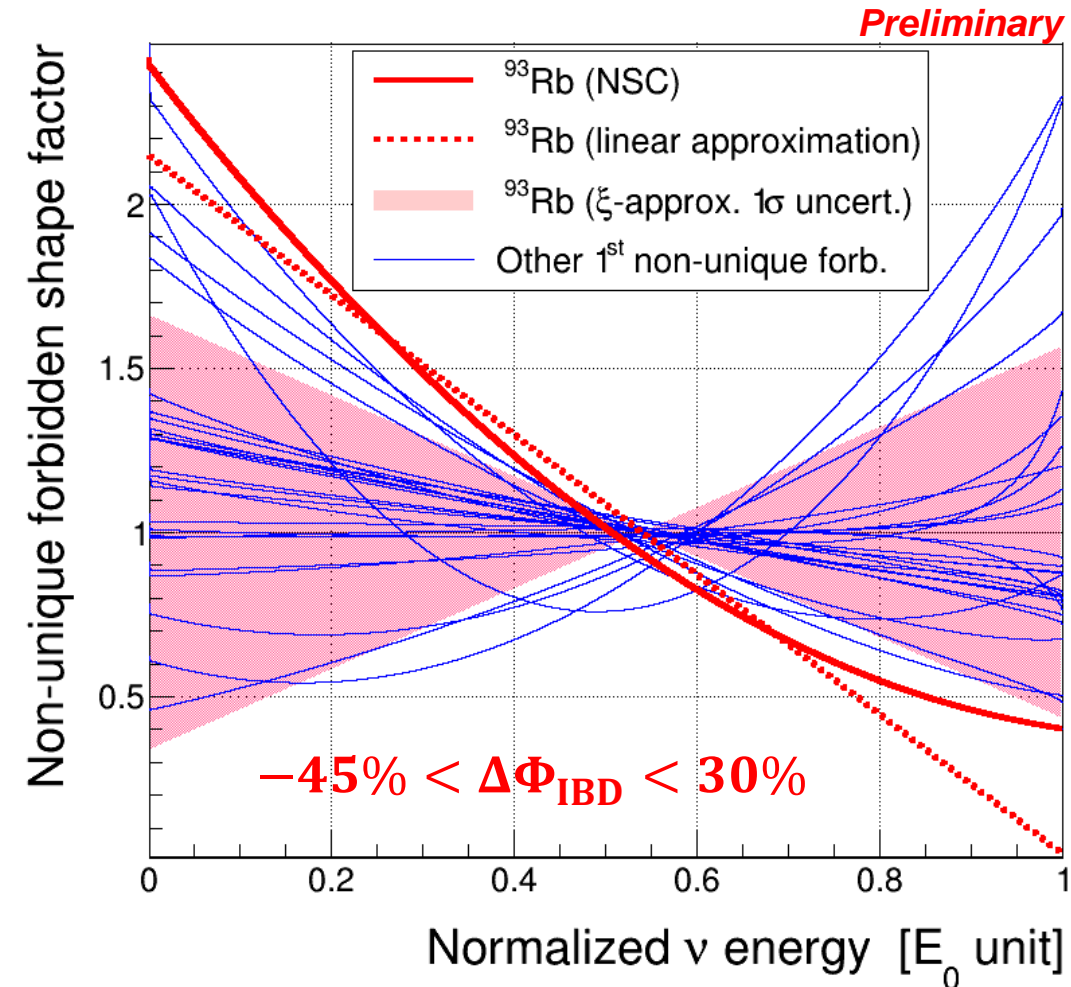
(\*): Criterion from X. Mougeot, Phys. Rev. C 91, 055504

## NUCLEAR STRUCTURE CALCULATION (NSC)

- $\beta$ -decay = single nucleon transition
- Nuclear state = superposition of nucleon states
- **Non-unique shape factor** calculation with NuShellX program
  - ▷ NSC very time consuming (man & cpu)
  - ▷ Comprehensive calculation for **23 important non-unique transitions**
  - ▷ Uncertainty derived from comparison to allowed spectrum
  - ▷ No general nor systematic trend in non-unique shape factors

⇒ **Non-unique forbidden branches treated as uncorrelated**

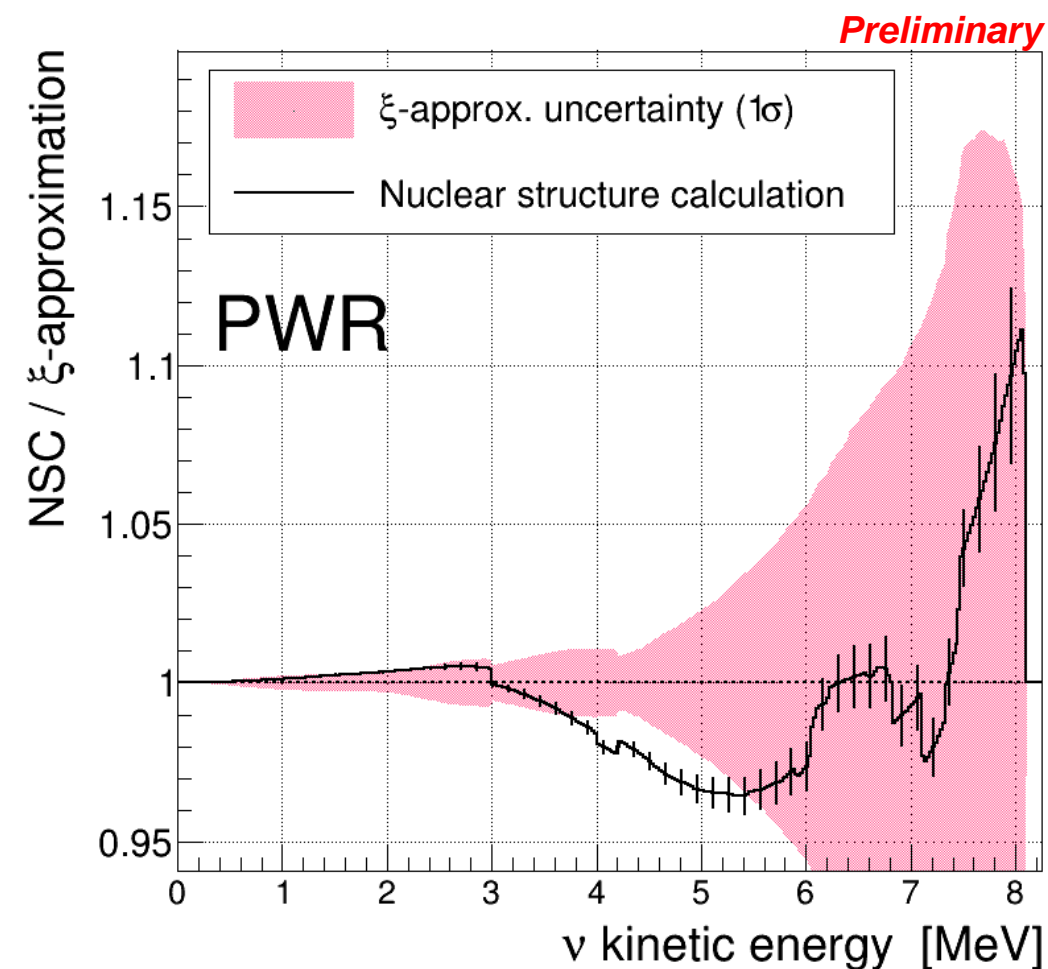
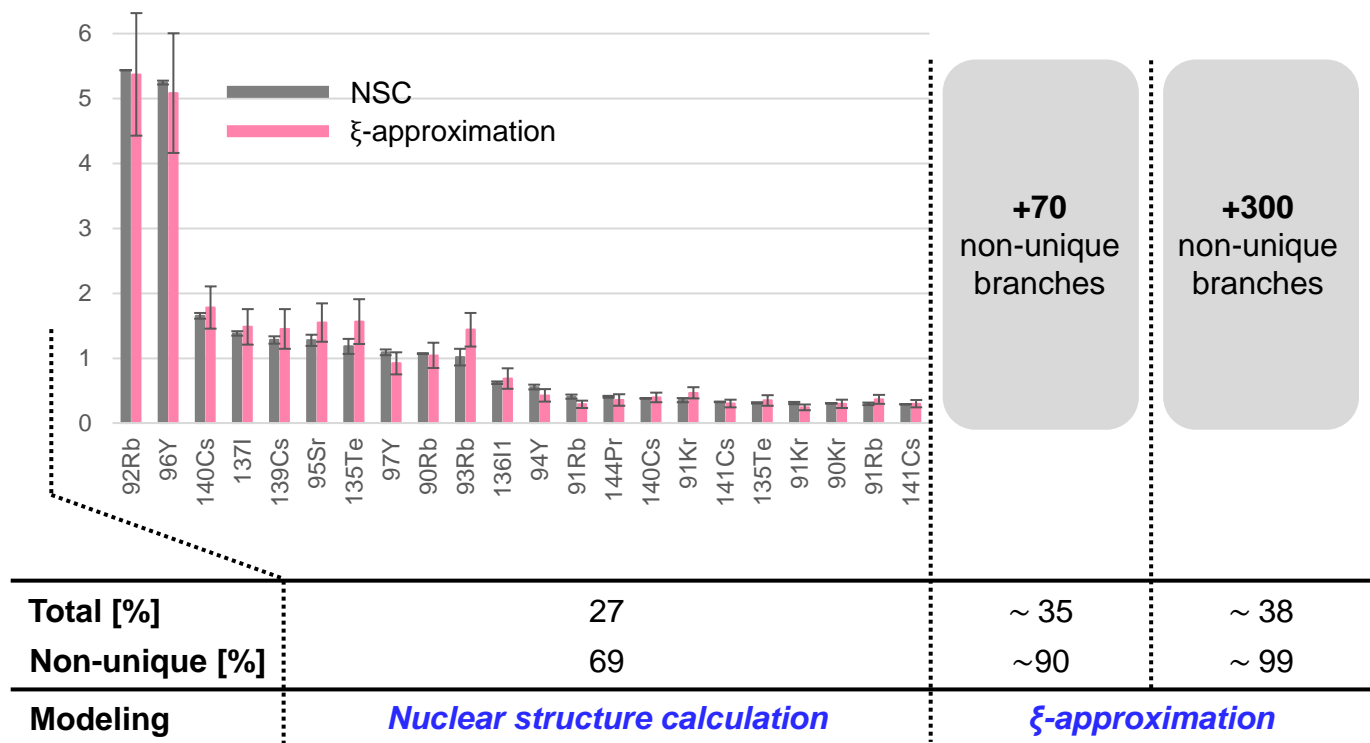
⇒ **Simplistic linear model used for uncertainty of  $\xi$ -approx. non-unique transitions**





## NUCLEAR STRUCTURE CALCULATION (NSC)

IBD contributions of non-unique transitions for a Chooz-like PWR



$\Rightarrow$  IBD yield decreased by  $(1.3 \pm 0.2)\%$  compared to full  $\xi$ -approximation

**Angeli 2013**

- Nuclear radius ( $R_n$ )  
[Angeli et al., At. Data Nucl. Data Tables 99\(1\):69-95 \(2013\)](#)

**ENSDF-2020**

- Branching ratio (BR)
- $\beta^-$  intensity ( $I_\beta$ )
- Spin-parity ( $J\pi$ )
- Parent energy ( $E_{parent}$ )
- Daughter level energy ( $E_{lvl}$ )

**NUBASE-2020**

- $\beta^-$  intensity ( $I_\beta$ )
- Parent energy ( $E_{parent}$ )

**AME-2020**

- $Q_\beta$  energy

**JEFF-3.3**

- Fission yield (FY)

**Branch spectrum**

$$S_\beta = K pW(W_0 - W)^2 F_0 C (1 + \delta_{WM} + \delta_{RC})$$

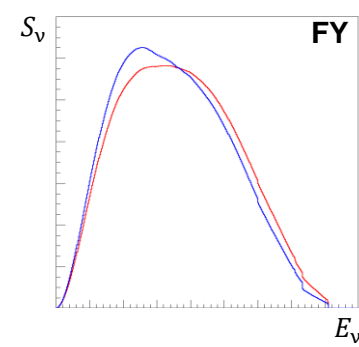
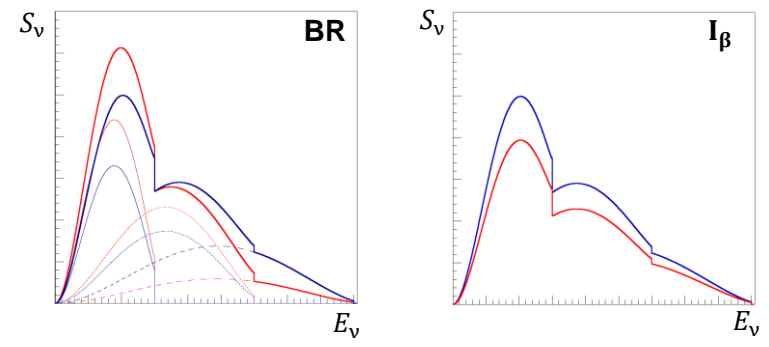
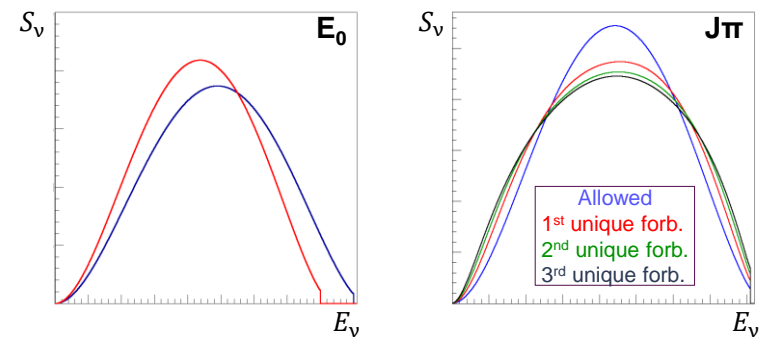
**Isotope spectrum**

$$S_i = \sum_b BR_i^b S_\beta^b$$

**Fission spectrum**

$$S_f = \sum_i FY_f^i S_i$$

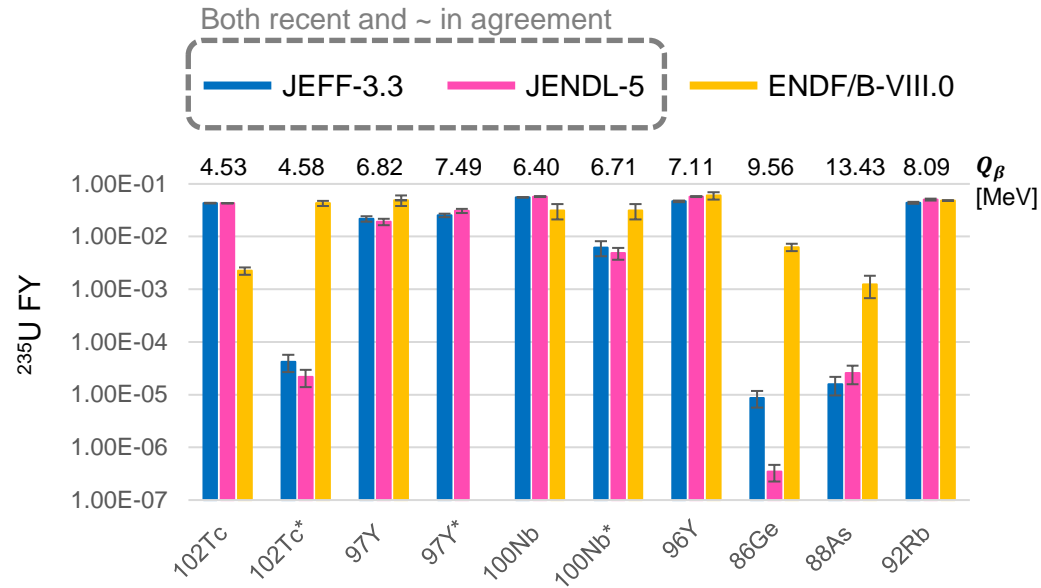
$$E_0 = Q_\beta + E_{parent} - E_{lvl}$$



⇒ Summation method requires many input data

FISSION YIELD DATA

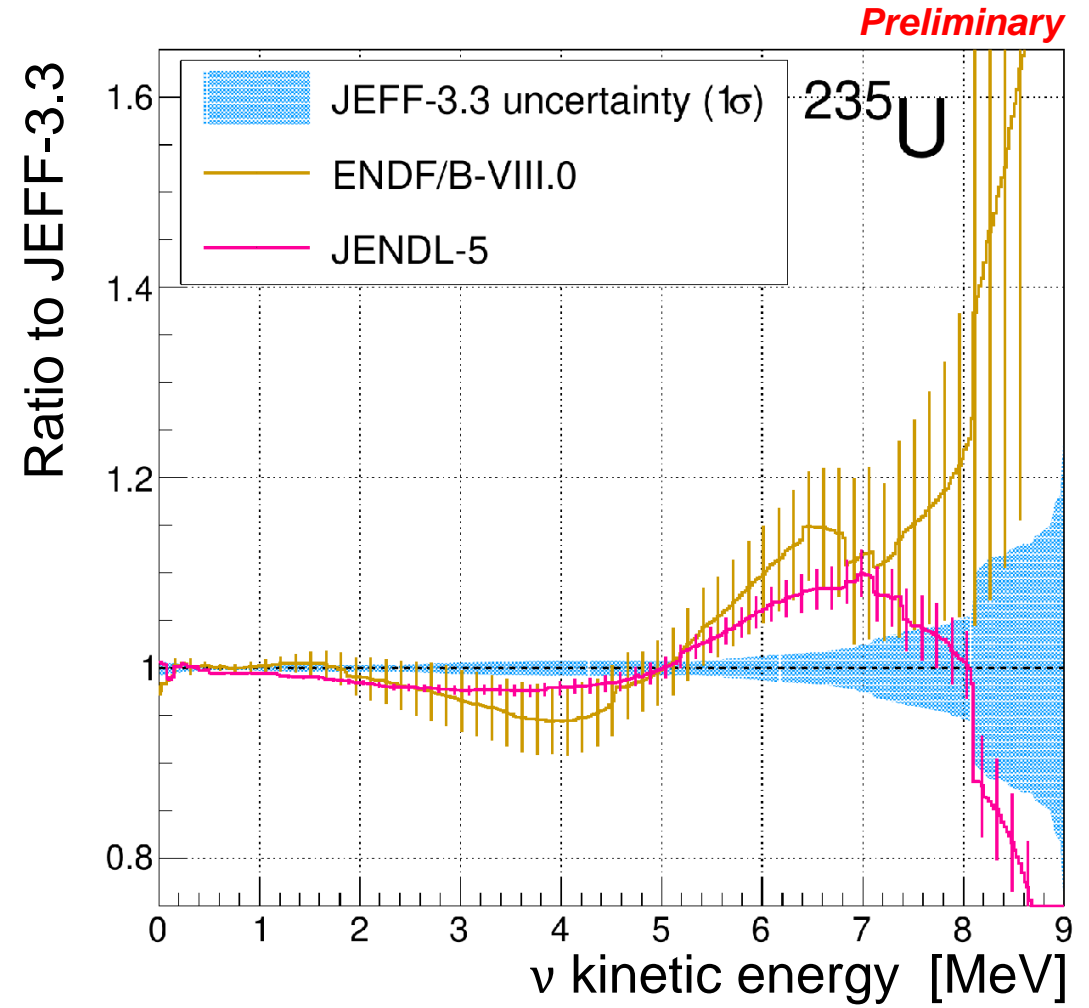
Discrepancies between cumulative FY data



⇒ Impacts fission spectrum shape

⇒ Impacts IBD yields

$^{235}\text{U} \sim 0.5\%$       $^{239}\text{Pu} \sim 2\%$   
 $^{238}\text{U} \sim 3\%$       $^{241}\text{Pu} \sim 2\%$

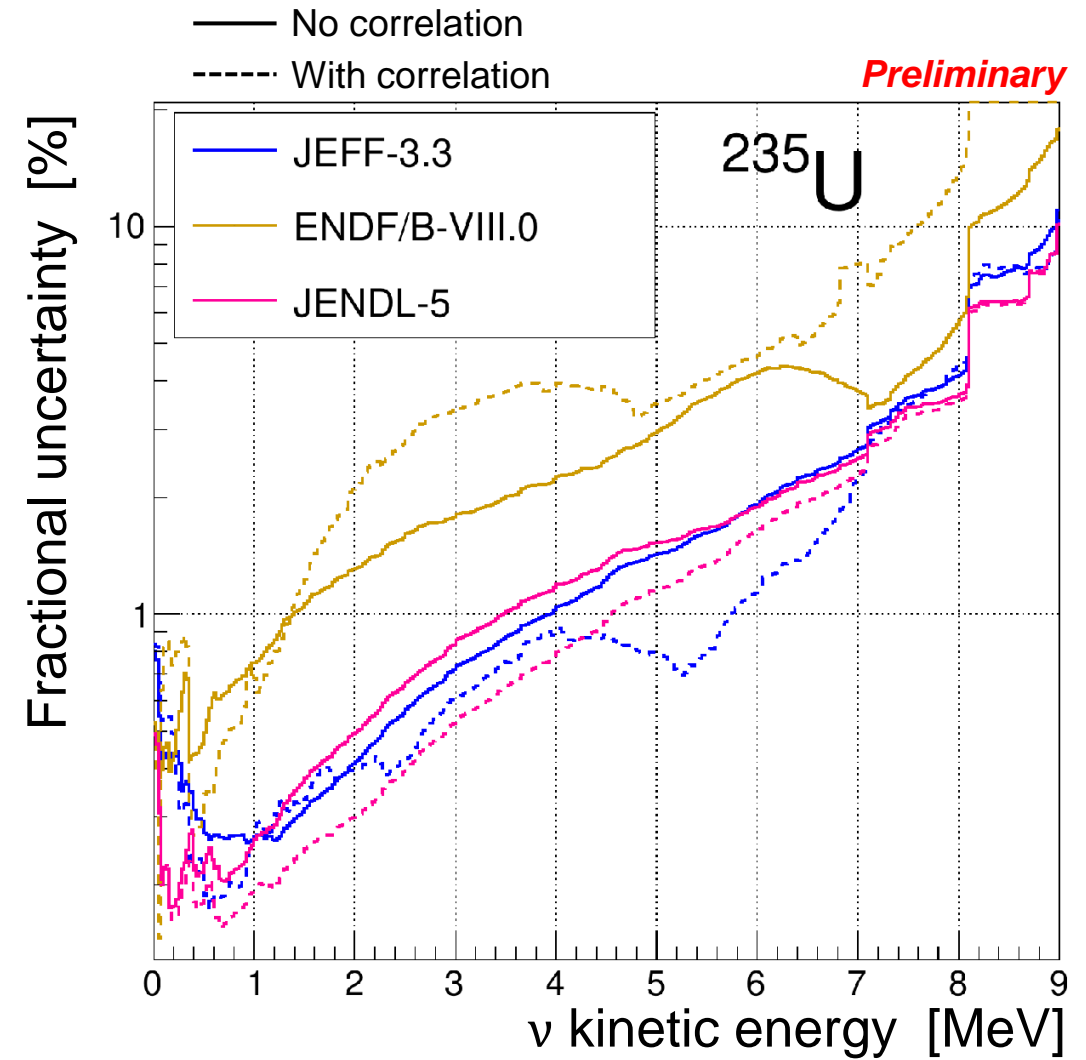


## FISSION YIELD DATA

Covariance matrix for cumulative FY

- Correlations derived from evaluation process
  - ▶ No correlation from fission process modeling and experimental data
- No inter-actinide correlations
  - ▶ Needed for PWR

	JEFF-3.3	ENDF/B-VIII.0	JENDL-5
Source	<a href="#">Matthews et al. (2021)</a>		Provided in JENDL
$\sigma_{IBD}(FY)$ no cor.	~1%	~2%	~1%
$\sigma_{IBD}(FY)$ with cor.	~0.8%	~4%	~0.8%



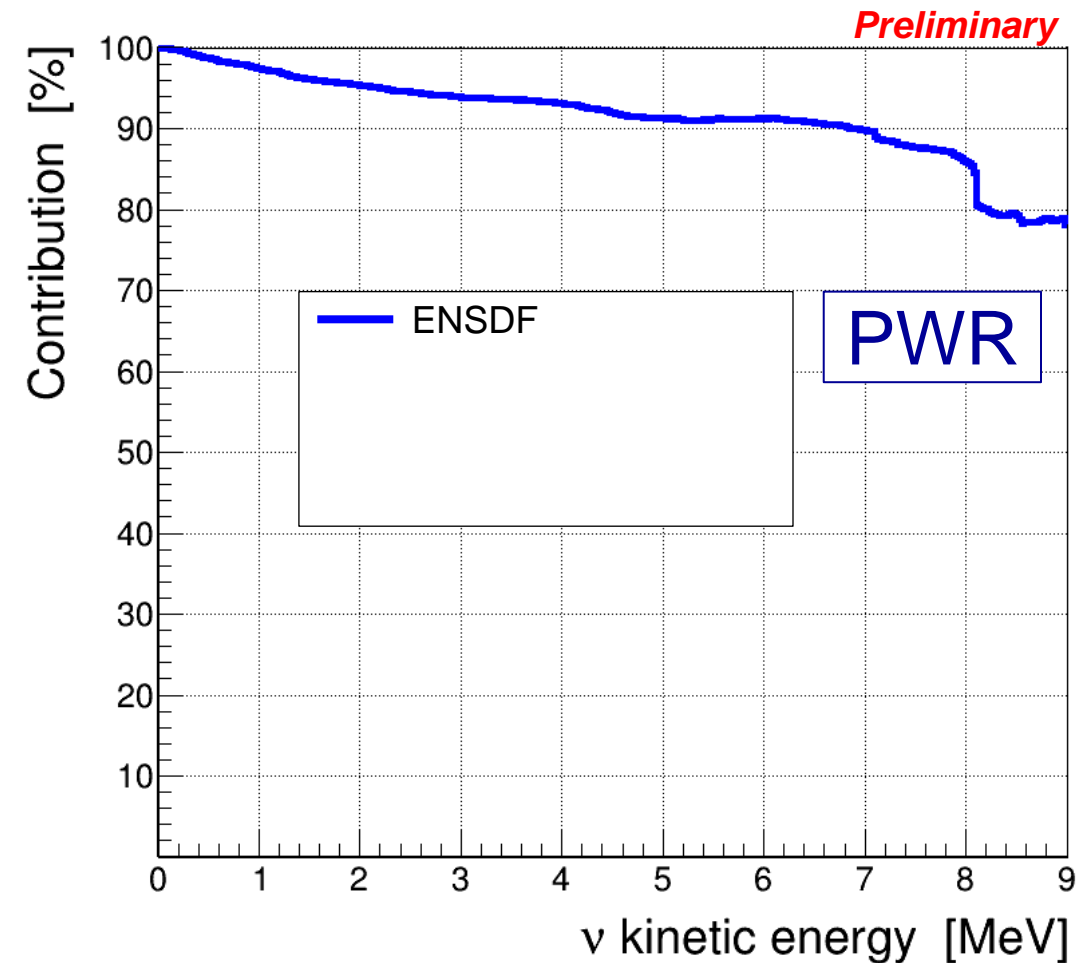
⇒ **Conservative choice for JEFF-3.3 is the « no correlation » case**

$\beta^-$ emitters from JEFF-3.3		
	NUBASE-2020	ENSDF-2020
$^{235}\text{U}$	793	566
$^{238}\text{U}$	778	536
$^{239}\text{Pu}$	851	625
$^{241}\text{Pu}$	860	603
<b>PWR</b> $\bar{\nu}_e$ flux contribution [%]		<b>97</b>
<b>PWR</b> IBD yield contribution [%]		<b>92</b>

### 2 issues with ENSDF database

- Database completeness
- Quality of experimental data and evaluation

⇒ **Pandemonium effect**

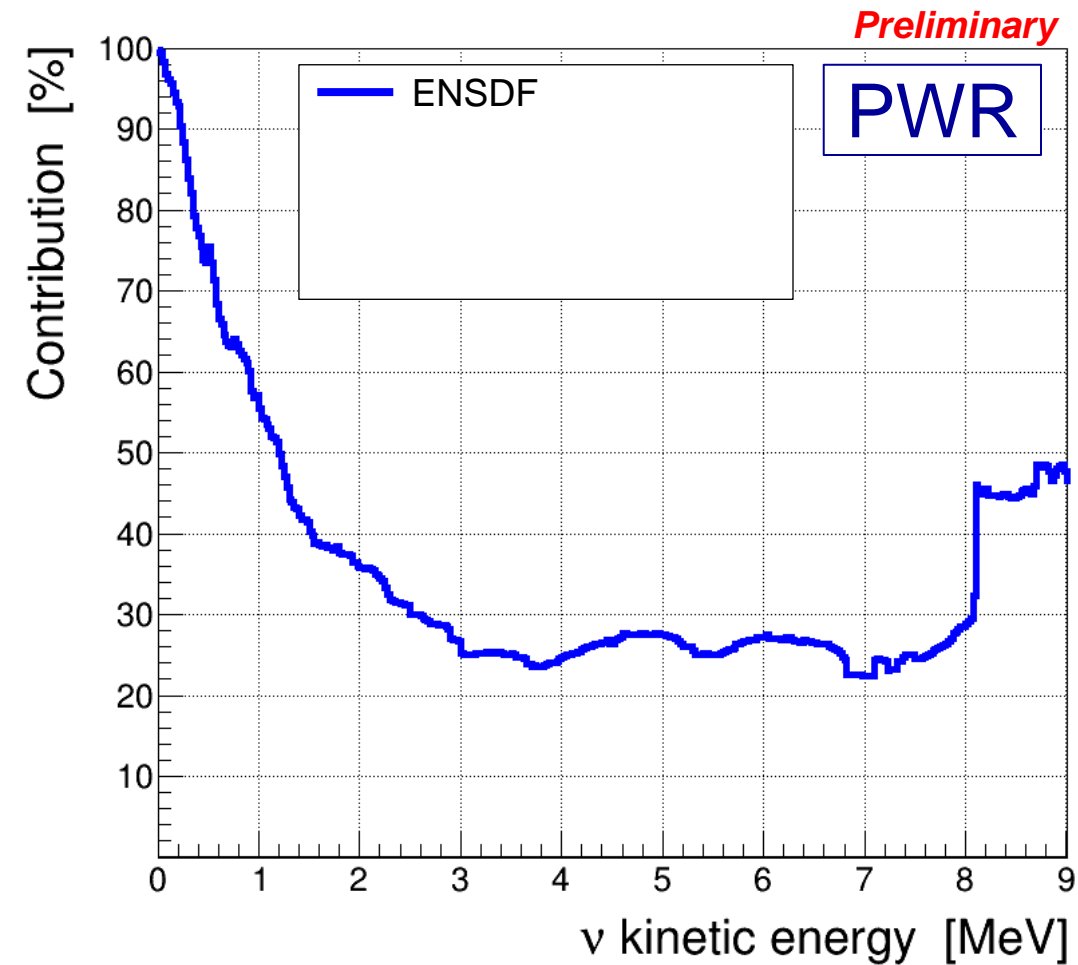


$\beta^-$ emitters from JEFF-3.3		
	NUBASE-2020	ENSDF-2020
$^{235}\text{U}$	793	↘ 448
$^{238}\text{U}$	778	↘ 419
$^{239}\text{Pu}$	851	↘ 507
$^{241}\text{Pu}$	860	↘ 485
<b>PWR</b> $\bar{\nu}_e$ flux contribution [%]		↘ <b>55</b>
<b>PWR</b> IBD yield contribution [%]		↘ <b>27</b>

### 2 issues with ENSDF database

- Database completeness
- Quality of experimental data and evaluation

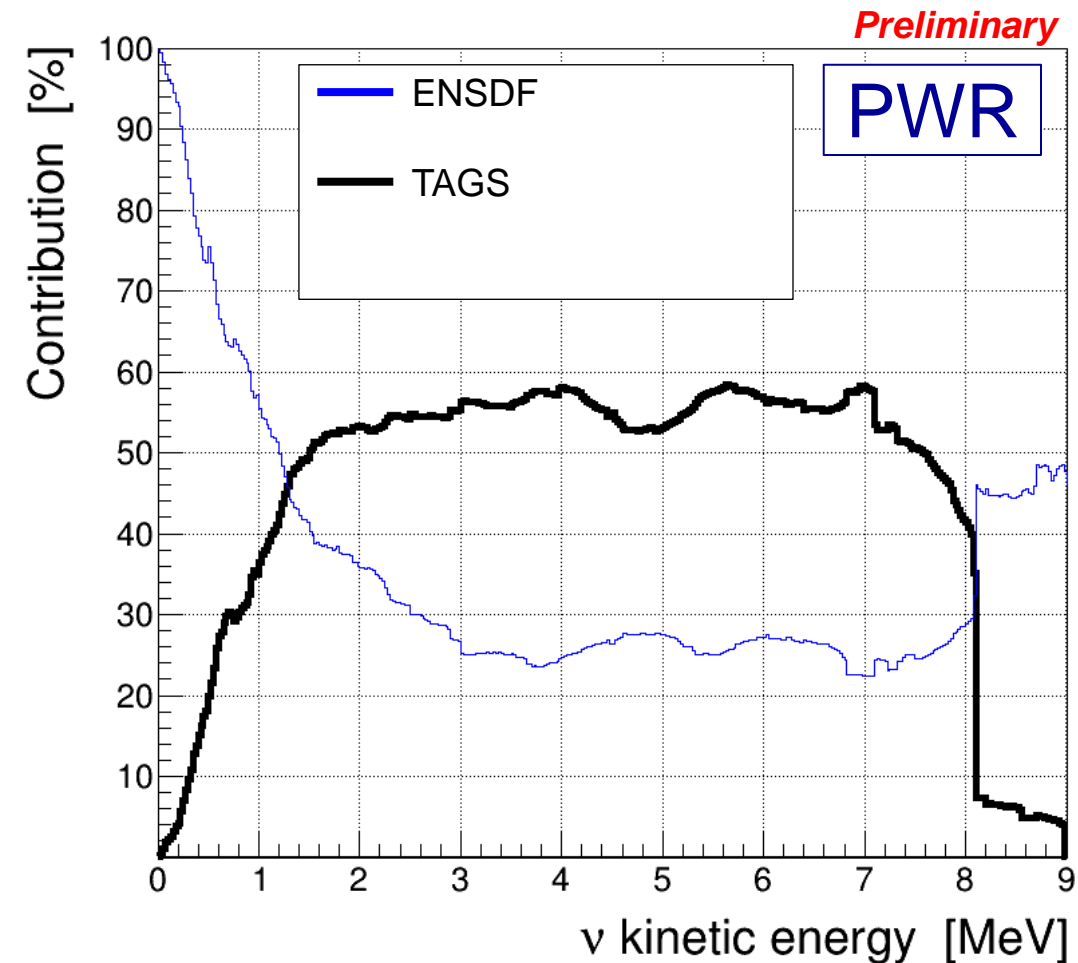
⇒ **Pandemonium effect**



$\beta^-$ emitters from JEFF-3.3			
	NUBASE-2020	ENSDF-2020	TAGS
$^{235}\text{U}$	793	448	84
$^{238}\text{U}$	778	419	83
$^{239}\text{Pu}$	851	507	84
$^{241}\text{Pu}$	860	485	84
<b>PWR <math>\bar{\nu}_e</math> flux contribution [%]</b>		<b>55</b>	<b>36</b>
<b>PWR IBD yield contribution [%]</b>		<b>27</b>	<b>55</b>

**TAGS data are Pandemonium-free**

- Priority over ENSDF data
- $\bar{\nu}_e$  spectra **shifts toward low energy**



**Quality of nuclear data**

- Acceptable: TAGS

**⇒ IBD yield decreased by 8% with TAGS data**

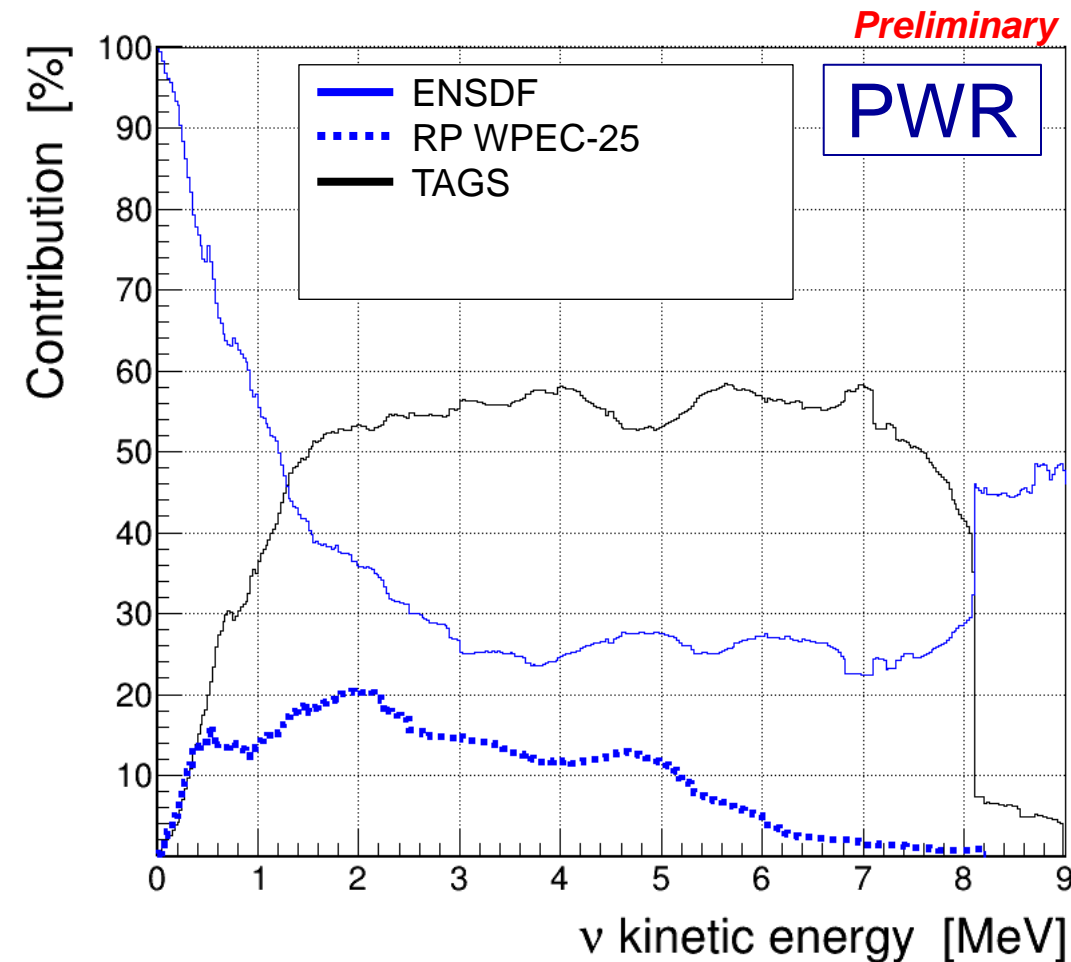
$\beta^-$ emitters from JEFF-3.3			
	NUBASE-2020	ENSDF-2020	TAGS*
$^{235}\text{U}$	793	448	84 (29)
$^{238}\text{U}$	778	419	83 (29)
$^{239}\text{Pu}$	851	507	84 (29)
$^{241}\text{Pu}$	860	485	84 (29)
<b>PWR</b>			
$\bar{\nu}_e$ flux contribution [%]		<b>55</b>	<b>36 (14)</b>
IBD yield contribution [%]		<b>27</b>	<b>55 (11)</b>

\*Residual Pandemonium in parenthesis, list from [INDC\(NDS\) - 0551. IAEA \(2009\)](#) and [INDC\(NDS\) - 0676. IAEA \(2015\)](#)

### Residual Pandemonium effect (RP) in ENSDF data

- RP WPEC-25
  - ▷ **29 isotopes** identified by IAEA WPEC-25
  - ▷ IBD contribution: 10-12%

⇒ **Measurements needed, meanwhile RP correction is applied**



### Quality of nuclear data

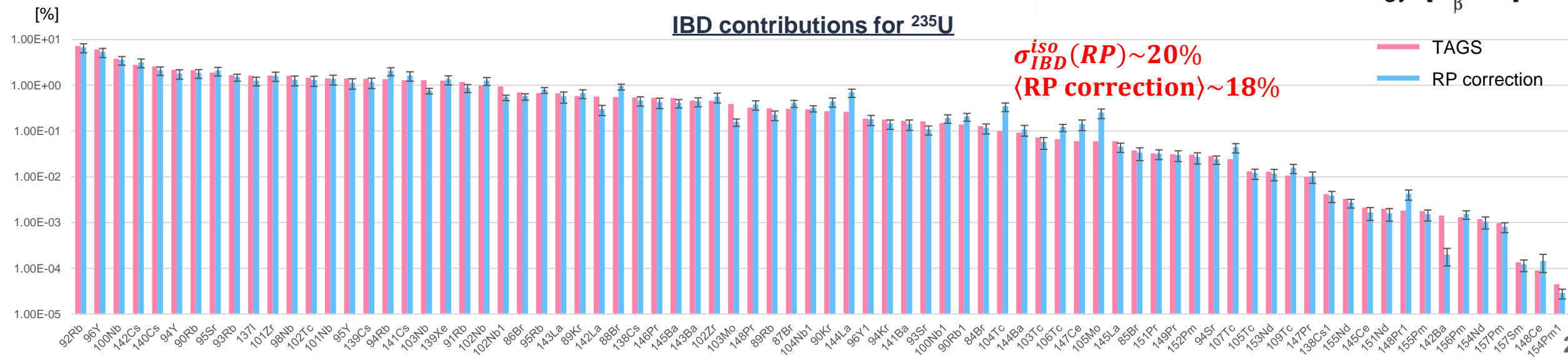
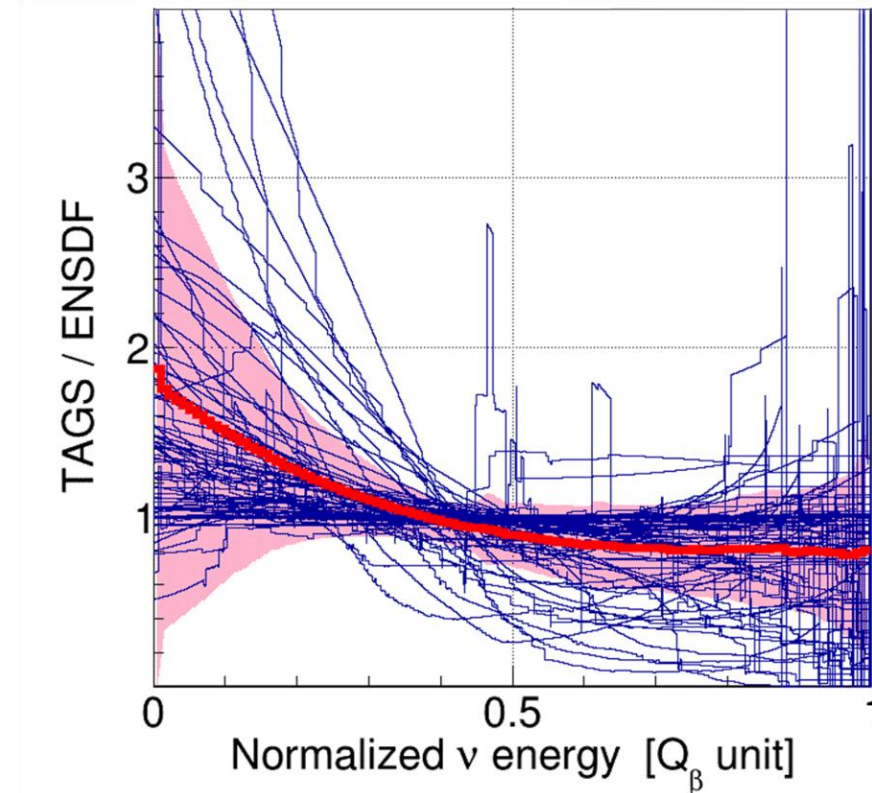
- Acceptable: TAGS, ENSDF
- Questionable: residual Pandemonium
  - ▷ **29 isotopes identified**
  - ▷ Measurement needed



## RESIDUAL PANDEMONIUM CORRECTION

### Buiding

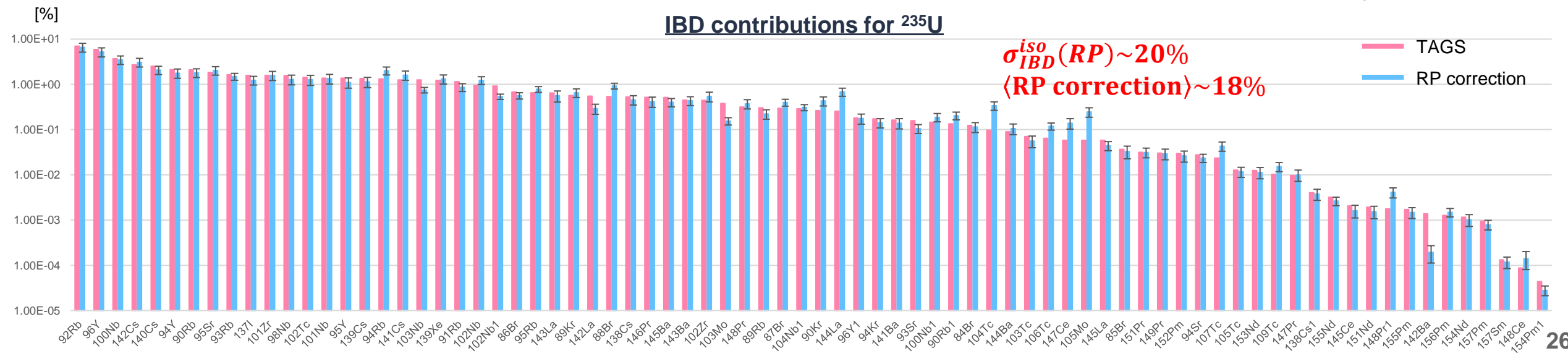
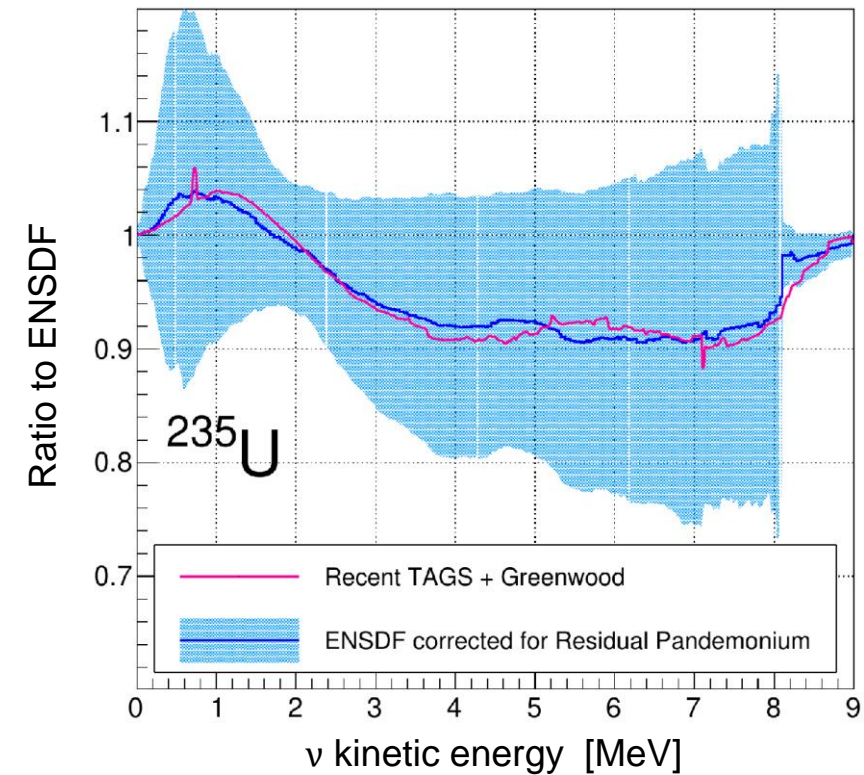
- Correction + uncertainty based on 81 isotopes having both TAGS and ENSDF data
- Correction = **average ratio** TAGS/ENSDF
- Uncertainty = **dispersion of ratios**
  - ▶ **Fully correlated** between isotopes and actinides



### RESIDUAL PANDEMONIUM CORRECTION

#### Testing on $^{235}\text{U}$

- $^{235}\text{U}$  IBD yield compared to using only ENSDF
  - ▶ Using TAGS data  $\rightarrow -7.7\%$
  - ▶ Using RP correction  $\rightarrow (-7.2 \pm 10.5)\%$



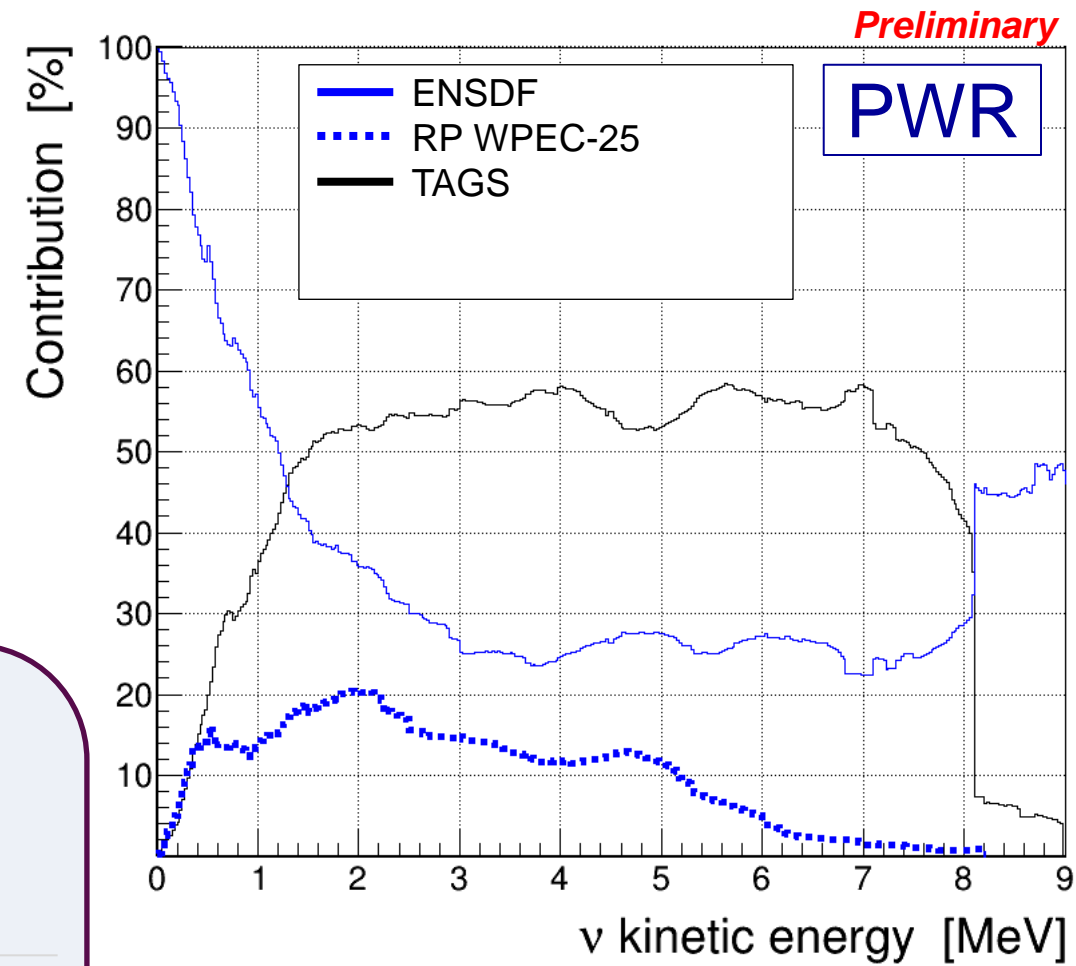
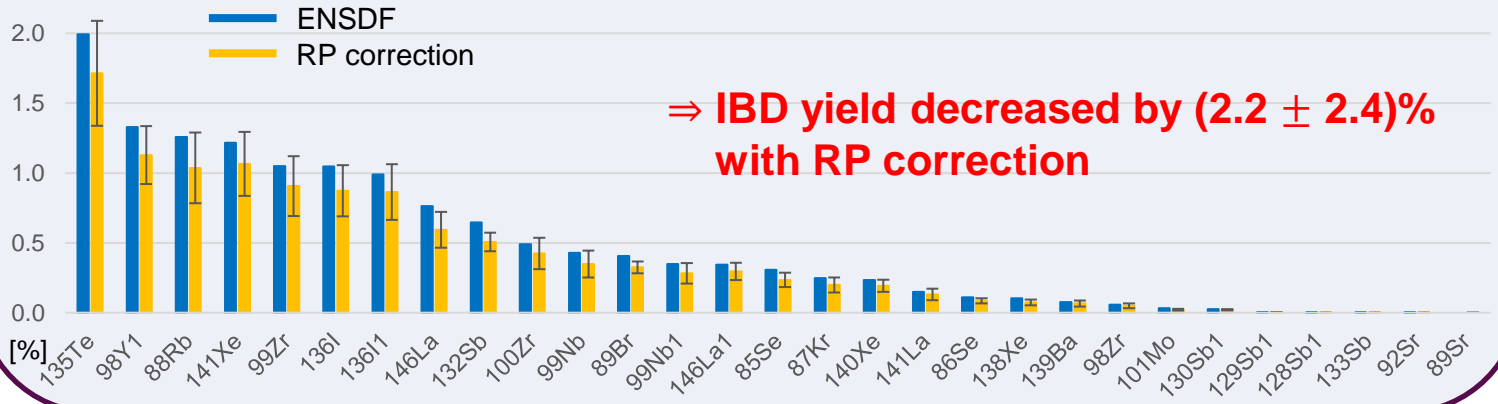
$\beta^-$ emitters from JEFF-3.3			
	NUBASE-2020	ENSDF-2020	TAGS*
$^{235}\text{U}$	793	448	84 (29)
$^{238}\text{U}$	778	419	83 (29)
$^{239}\text{Pu}$	851	507	84 (29)
$^{241}\text{Pu}$	860	485	84 (29)
<b>PWR <math>\bar{\nu}_e</math> flux contribution [%]</b>		<b>55</b>	<b>36 (14)</b>
<b>PWR IBD yield contribution [%]</b>		<b>27</b>	<b>55 (11)</b>

\*Residual Pandemonium in parenthesis, list from [INDC\(NDS\) - 0551. IAEA \(2009\)](#) and [INDC\(NDS\) - 0676. IAEA \(2015\)](#)

### RESIDUAL PANDEMONIUM CORRECTION

- Apply RP correction on the 29 isotopes from WPEC-25

#### IBD contributions for a Chooz-like PWR



Preliminary

#### Quality of nuclear data

- Acceptable: TAGS, ENSDF
- Questionable: residual Pandemonium
  - ▷ 29 isotopes identified
  - ▷ Measurement needed

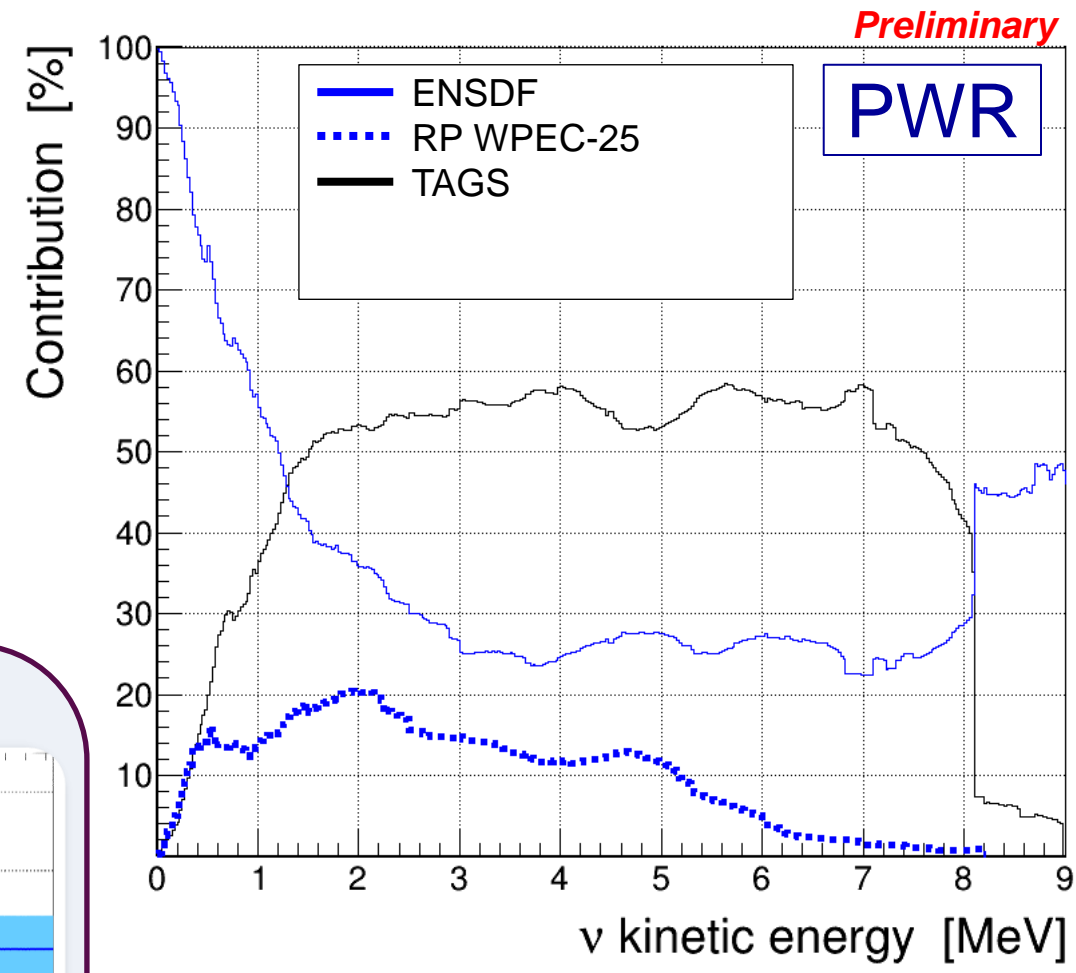
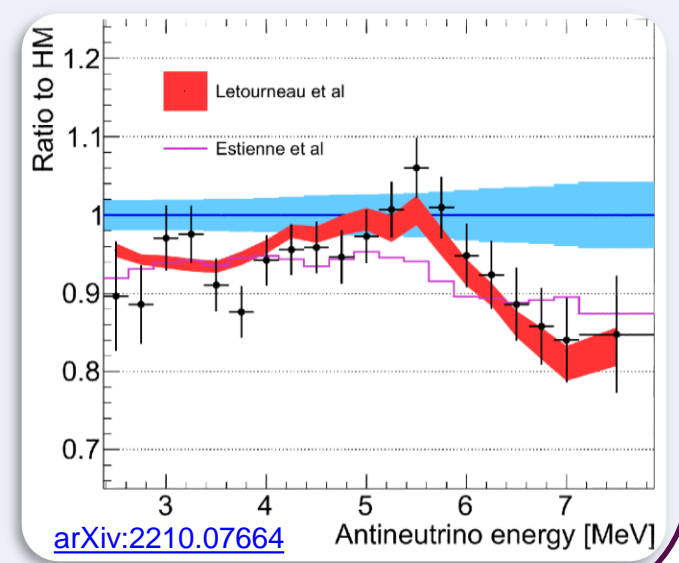
$\beta^-$ emitters from JEFF-3.3			
	NUBASE-2020	ENSDF-2020	TAGS*
$^{235}\text{U}$	793	448	84 (29)
$^{238}\text{U}$	778	419	83 (29)
$^{239}\text{Pu}$	851	507	84 (29)
$^{241}\text{Pu}$	860	485	84 (29)
<b>PWR <math>\bar{\nu}_e</math> flux contribution [%]</b>		<b>55</b>	<b>36 (14)</b>
<b>PWR IBD yield contribution [%]</b>		<b>27</b>	<b>55 (11)</b>

\*Residual Pandemonium in parenthesis, list from [INDC\(NDS\) - 0551. IAEA \(2009\)](#) and [INDC\(NDS\) - 0676. IAEA \(2015\)](#)

### PHENOMENOLOGICAL DECAY STRENGTH MODEL

- 1 parameter Gamow-Teller strength model
- Generate missing transitions for all fission products from ENSDF
  - ▶ Correct Pandemonium effect and missing transitions
- [Letourneau et al., PRL 130, 021801 \(2023\)](#)

⇒ **Very good agreement with STEREO**



#### Quality of nuclear data

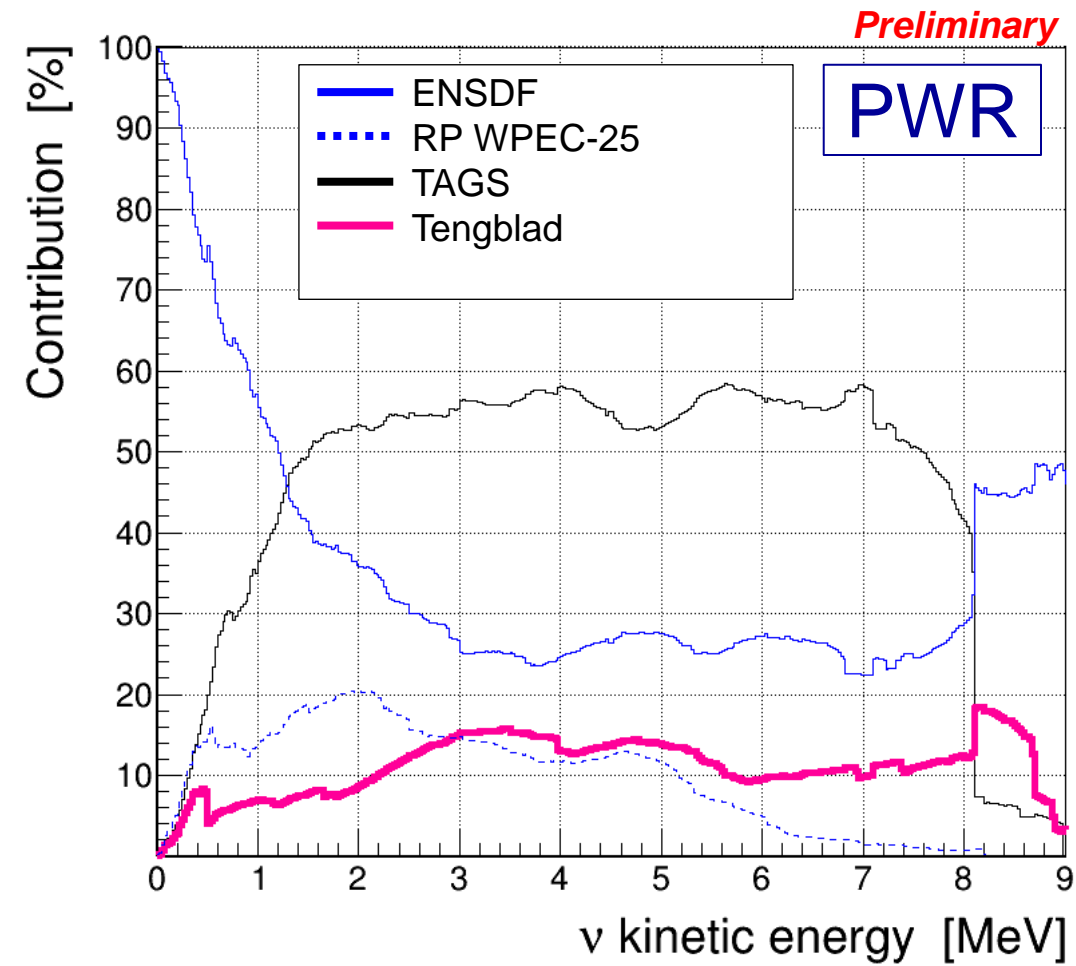
- Acceptable: TAGS, ENSDF
- Questionable: residual Pandemonium
  - ▶ **29 isotopes identified**
  - ▶ Measurement needed

		$\beta^-$ emitters from JEFF-3.3			
		NUBASE-2020	ENSDF-2020	TAGS	Direct $\beta^*$
$^{235}\text{U}$		793	448	84 (29)	44
$^{238}\text{U}$		778	419	83 (29)	44
$^{239}\text{Pu}$		851	507	84 (29)	44
$^{241}\text{Pu}$		860	485	84 (29)	44
<b>PWR</b>	$\bar{\nu}_e$ flux contribution [%]		<b>55</b>	<b>36 (14)</b>	<b>8</b>
	IBD yield contribution [%]		<b>27</b>	<b>55 (11)</b>	<b>13</b>

\*Rudstam et al., At. Data Nucl. Data Tables 45(2):239-320 (1990)

**Direct  $\beta$  measurements are Pandemonium-free**

- Priority over ENSDF but after TAGS
- $\beta$  spectra converted to  $\bar{\nu}_e$  spectra



**Quality of nuclear data**

- Acceptable: TAGS, ENSDF, Direct  $\beta$
- Questionable: residual Pandemonium

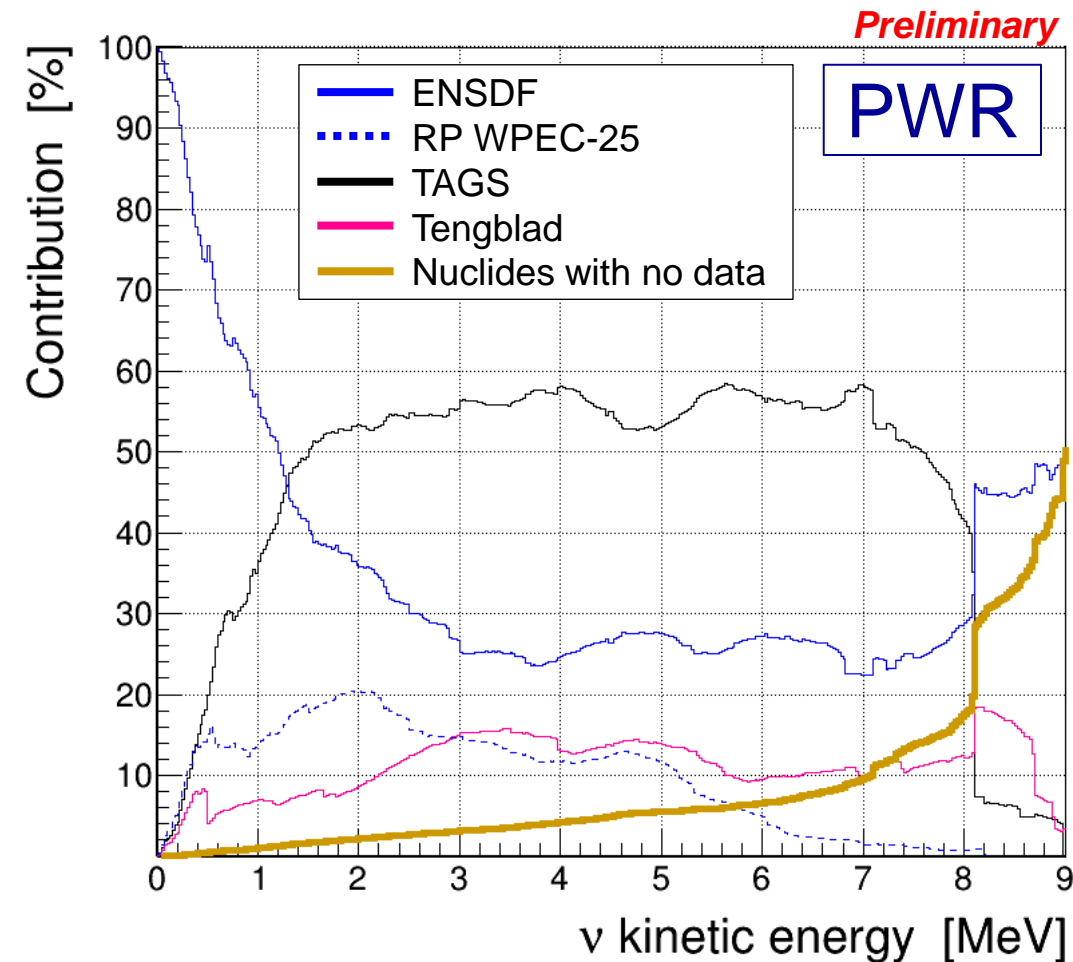
⇒ IBD yield decreased by  $(4.8 \pm 1.4)\%$  with Direct  $\beta$  measurements

		$\beta^-$ emitters from JEFF-3.3				
		NUBASE-2020	ENSDF-2020	TAGS	Direct $\beta$	No data
	$^{235}\text{U}$	793	448	84 (29)	44	217
	$^{238}\text{U}$	778	419	83 (29)	44	232
	$^{239}\text{Pu}$	851	507	84 (29)	44	216
	$^{241}\text{Pu}$	860	485	84 (29)	44	247
PWR	$\bar{\nu}_e$ flux contribution [%]		<b>55</b>	<b>36 (14)</b>	<b>8</b>	<b>1</b>
	IBD yield contribution [%]		<b>27</b>	<b>55 (11)</b>	<b>13</b>	<b>5</b>

### How to model nuclides with no data (NND) ?

- Different modelings already tested in other summation models
  - ▷  $Q_\beta$  model with n branches, Gross theory
  - ▷ No modeling uncertainty

⇒ **Measurements needed, meanwhile modeling of NND + uncertainty**



### Quality of nuclear data

- Acceptable: TAGS, ENSDF, Direct  $\beta$
- Questionable: residual Pandemonium
- Poor: nuclides with no data



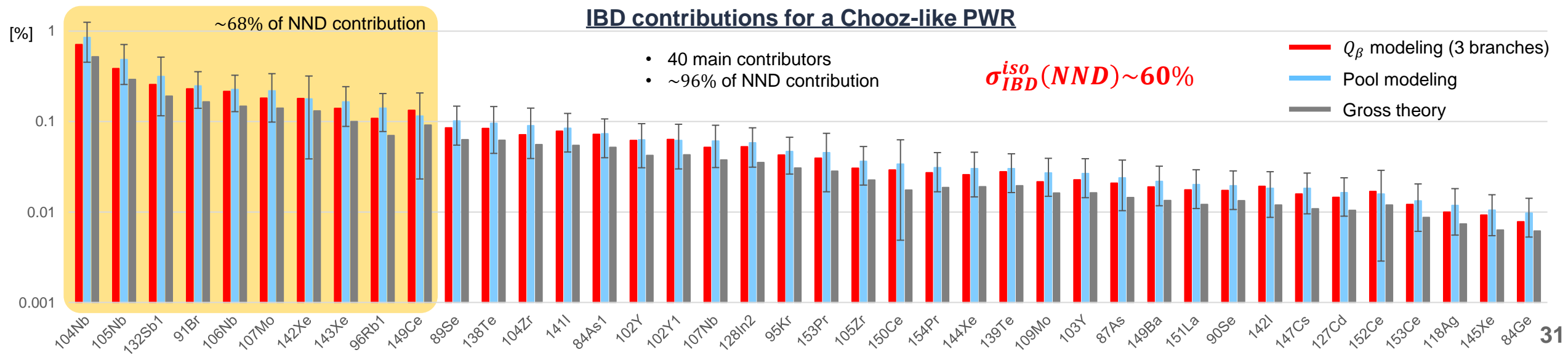
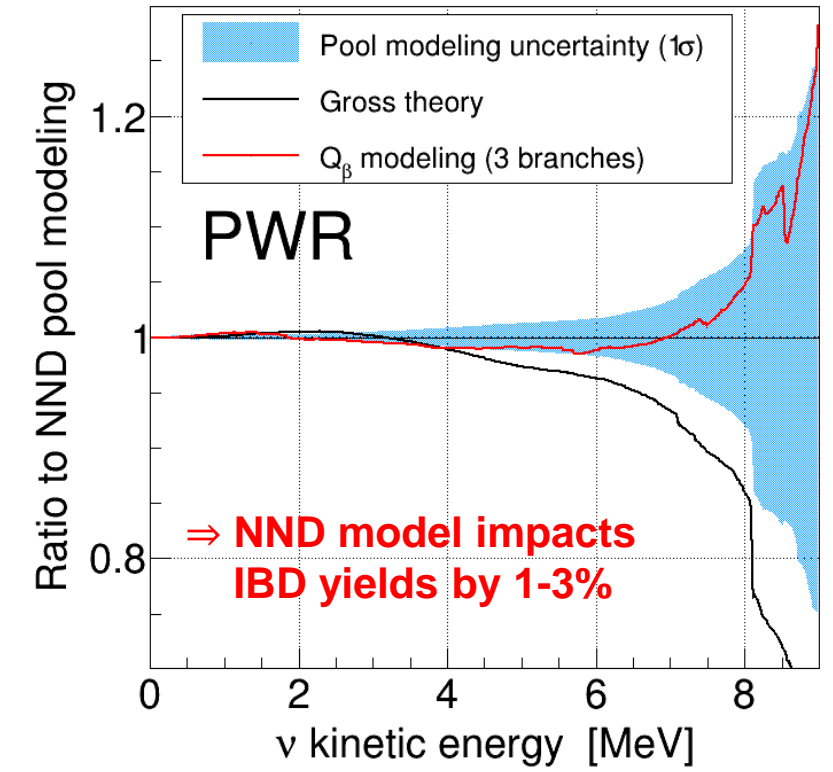
**Important >7 MeV**

**POOL MODELING OF NUCLIDES WITH NO DATA (NND)**

- For each NND, spectrum + covariance matrix derived from pool of isotopes with data

**Pool selection**

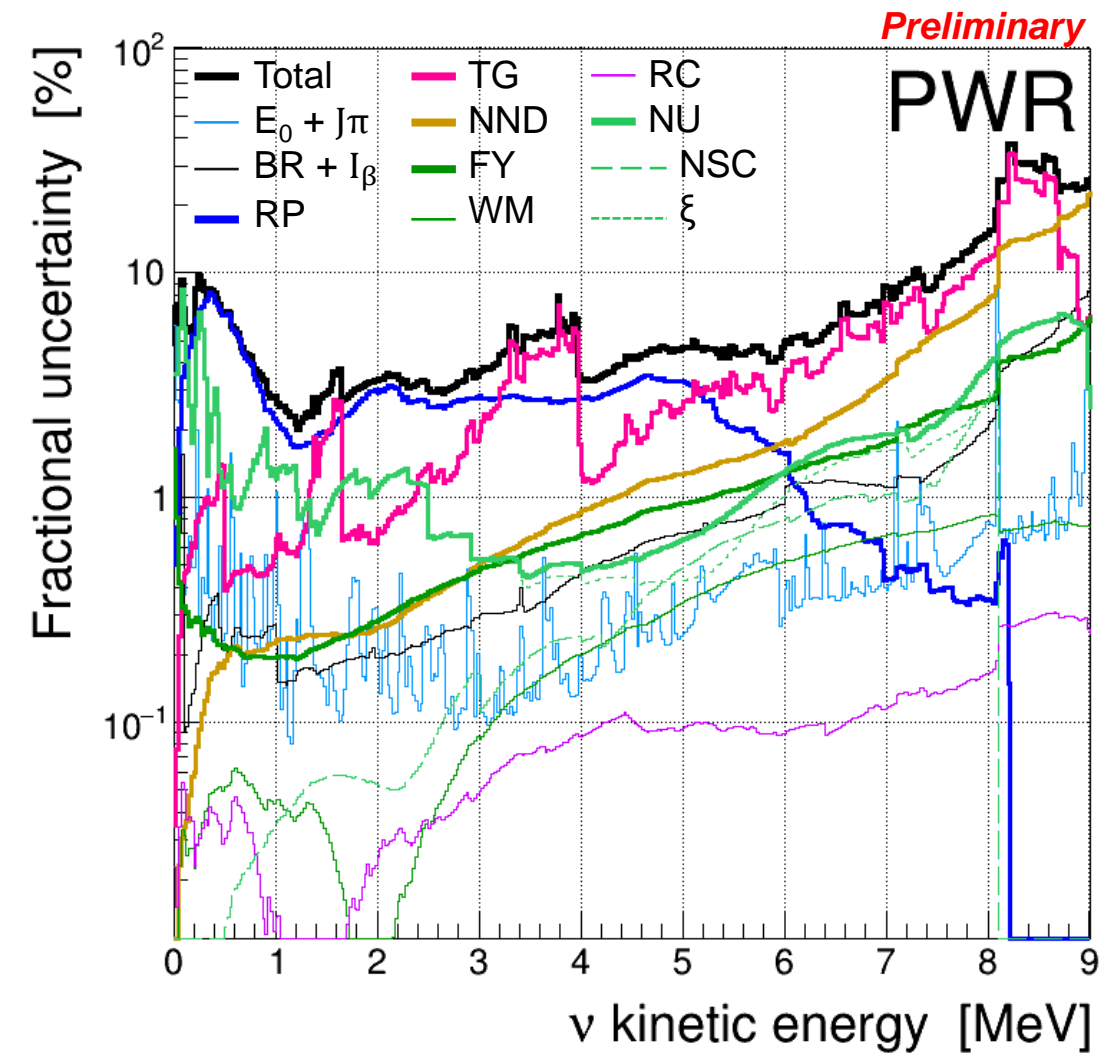
- Isotope with data such that  $Q_\beta$  within  $\pm 10\%$  of the NND  $Q_\beta$ 
  - ▶ 10-100 isotopes with data
- Spectrum = **pool average**
- Covariance matrix = **pool dispersion**
  - ▶ Uncertainties uncorrelated between isotopes
  - ▶ Cover other NND models at isotope level



### NORMALIZATION UNCERTAINTY

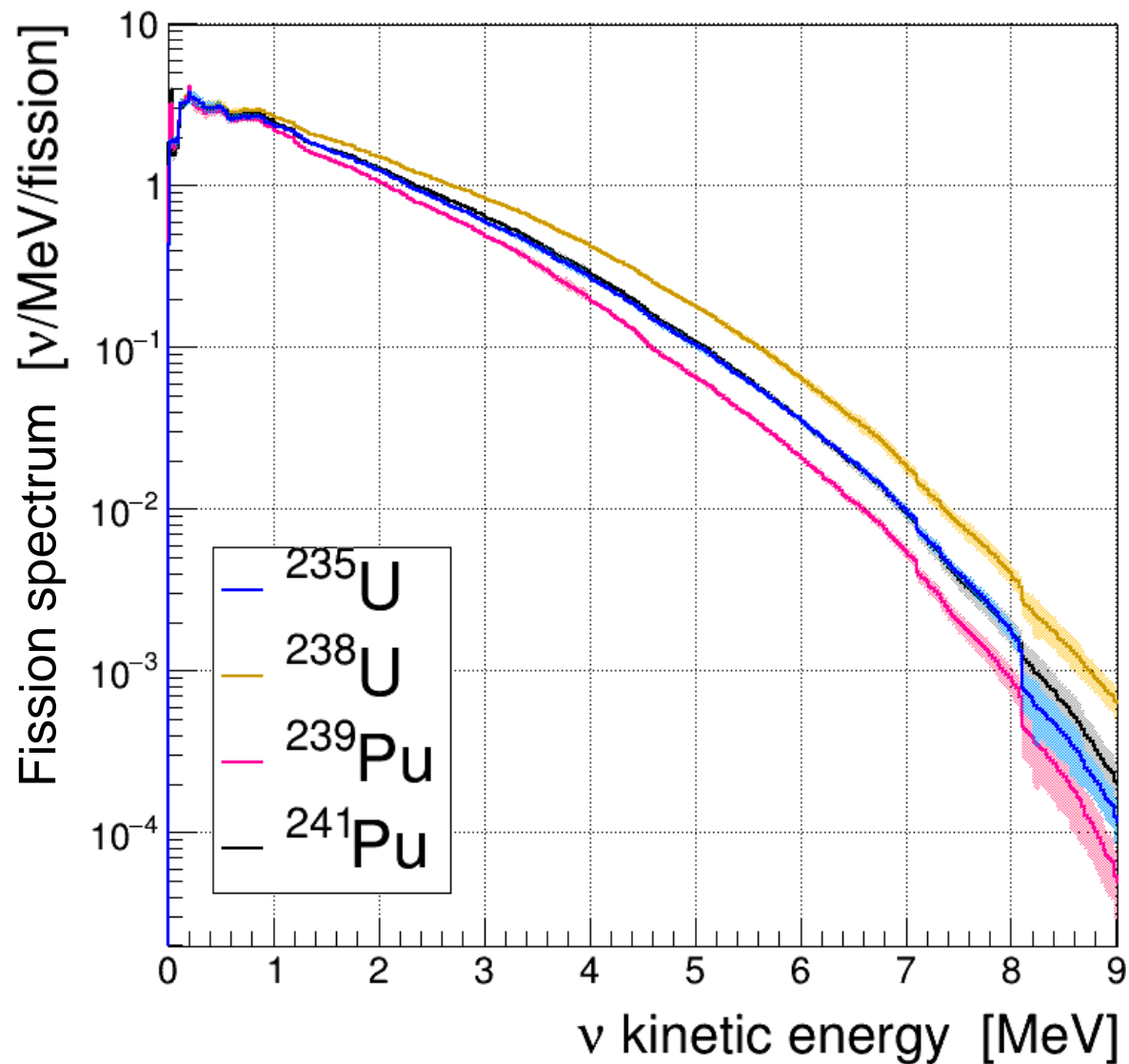
PWR				
$\langle \sigma_{IBD} \rangle$		6.08 x 10 <sup>-43</sup> cm <sup>2</sup> /fission		
	Uncertainty	Abbrev.	Method	[%]
DATA	Endpoint + Spin-parity	E <sub>0</sub> + J $\pi$	MC	0.1
	Branching ratio + $\beta^-$ intensity	BR + I $\beta$	MC + Analytic	0.4
	Residual Pandemonium	RP	Analytic	2.5
	Tengblad	TG	Analytic	1.5
	Nuclides with no data	NND	Pool modeling	0.8
	Fission yield	FY	Analytic	~0.7
	Fission fraction		Analytic	~0.7
MODELING	Weak magnetism	WM	Model comparison	0.3
	Radiative corrections	RC	Model comparison	0.1
	Non-unique transitions	NU	Model comparison	0.4
	• Nuclear struct. calcul.	NSC		0.2
	• $\xi$ -approximation	$\xi$		0.3
	IBD cross-section		Analytic	0.1
<b>TOTAL</b>				<b>3.1</b>

### FRACTIONAL UNCERTAINTY



**⇒ Uncertainty budget dominated by RP and TG (+ NND at high energy)**





### IBD yields ( $10^{-43} \text{ cm}^2/\text{fission}$ )

$^{235}\text{U}$ :  $6.25 \pm 0.21$

$^{238}\text{U}$ :  $10.01 \pm 0.32$

$^{239}\text{Pu}$ :  $4.48 \pm 0.15$

$^{241}\text{Pu}$ :  $6.58 \pm 0.21$

$\Rightarrow$  IBD yield uncertainty budget  $\sim 3\%$

- 1. Introduction & motivations**
  - a. Reactors as antineutrino sources
  - b. Experimental anomalies
  - c. Different modeling methods
  
- 2. Revised summation method**
  - a.  $\beta^-$  spectrum calculation
  - b. Nuclear data content
  - c. Uncertainty budget
  
- 3. Preliminary comparisons**
  - a. Integral measurements
  - b. Spectrum shape
  
- 4. Conclusion & perspectives**

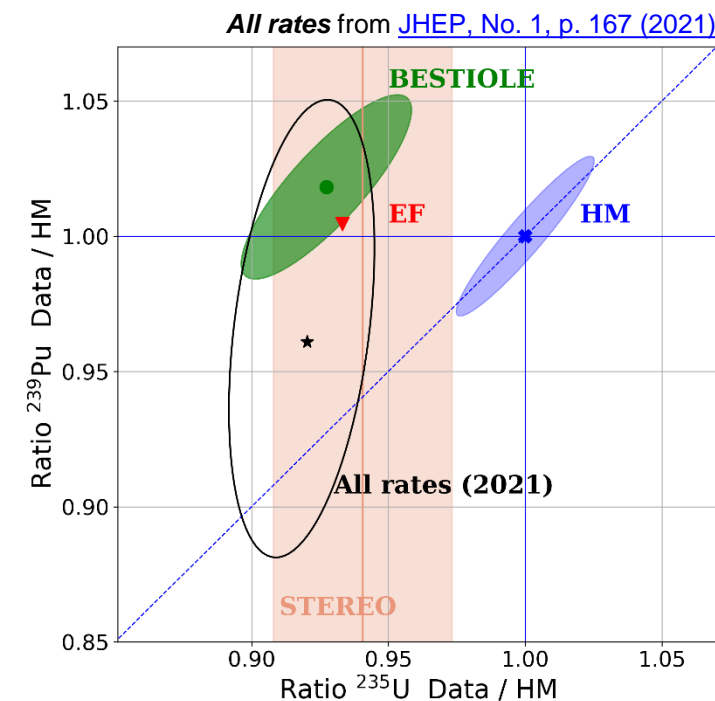
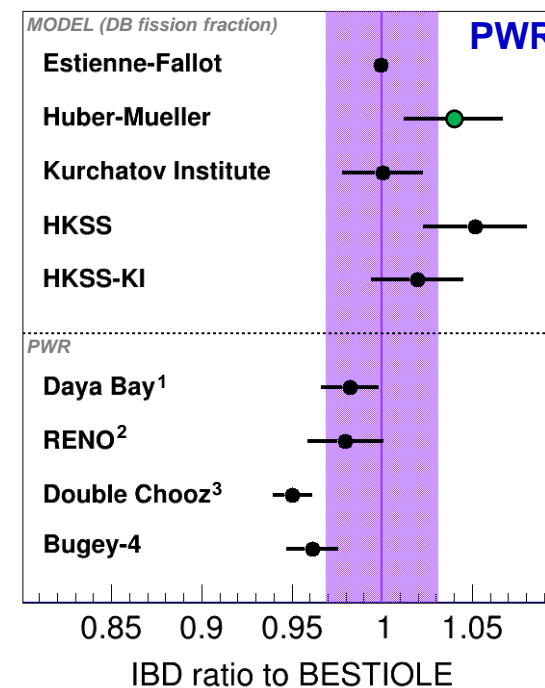
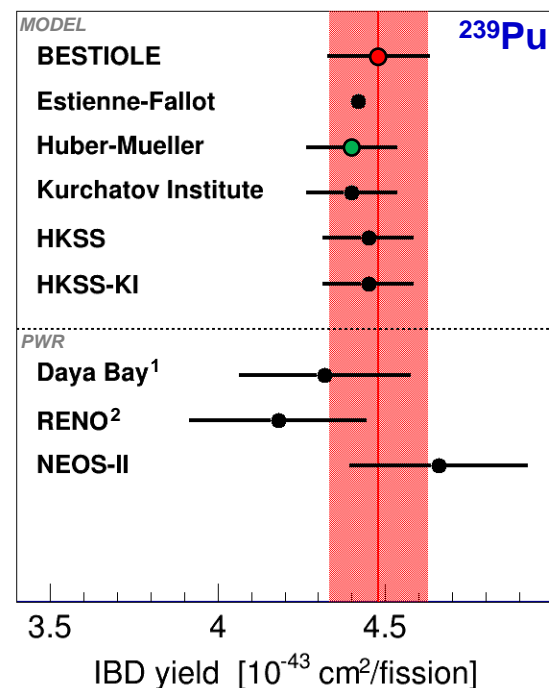
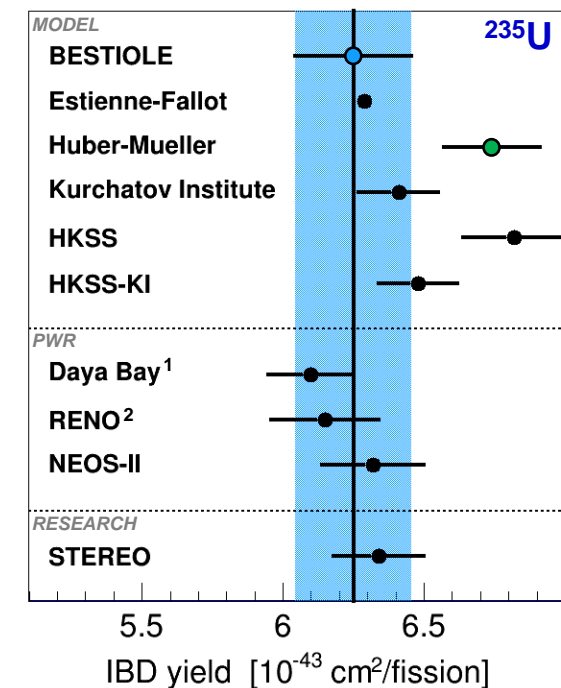
### 3. Preliminary comparisons

#### a. Integral measurements

*All plots are preliminary*

Predictions and Bugey-4 taken from [Giunti et al., Phys. Lett. B, 829, 137054 \(2022\)](#)

- 1: [Phys. Rev. Lett. 123, 111801 \(2019\)](#)
- 2: [Phys. Rev. D 104, L111301 \(2021\)](#)
- 3: [Phys. Rev. Lett. 125, 201801 \(2020\)](#)



- $^{235}\text{U}$ ,  $^{238}\text{U}$  and  $^{239}\text{Pu}$  : **BESTIOLE consistent within  $\sim 1\sigma$**  with other data
- $^{241}\text{Pu}$ : small tension with other data ( $1.5 - 2\sigma$ )
  - ▷ Important contribution of NND in BESTIOLE

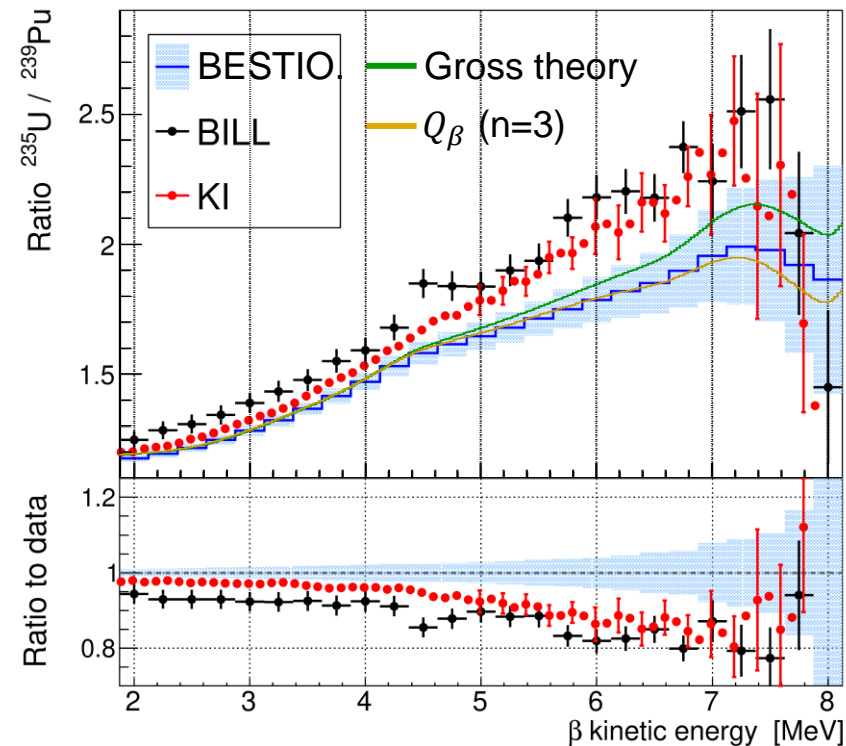
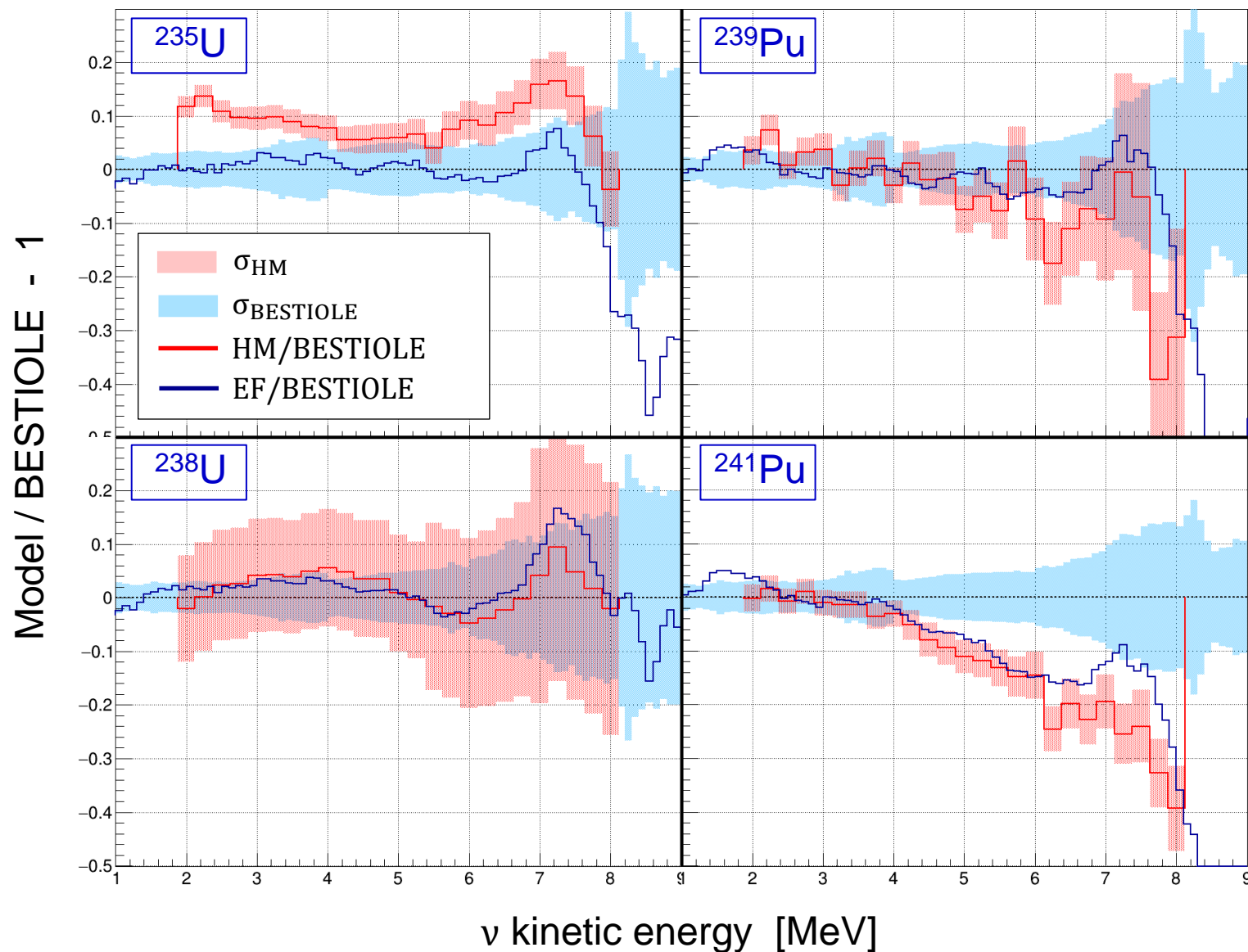
$$\text{DB / BESTIOLE} = 0.982 \pm 0.015 \text{ (exp)} \pm 0.031 \text{ (model)}$$

$$\text{DB / HM} = 0.945 \pm 0.014 \text{ (exp)} \pm 0.024 \text{ (model)}$$

⇒ **Significance at  $0.5\sigma$  for BESTIOLE and  $1.9\sigma$  for HM**

*All plots are preliminary*

**IMPACT OF NND MODEL**

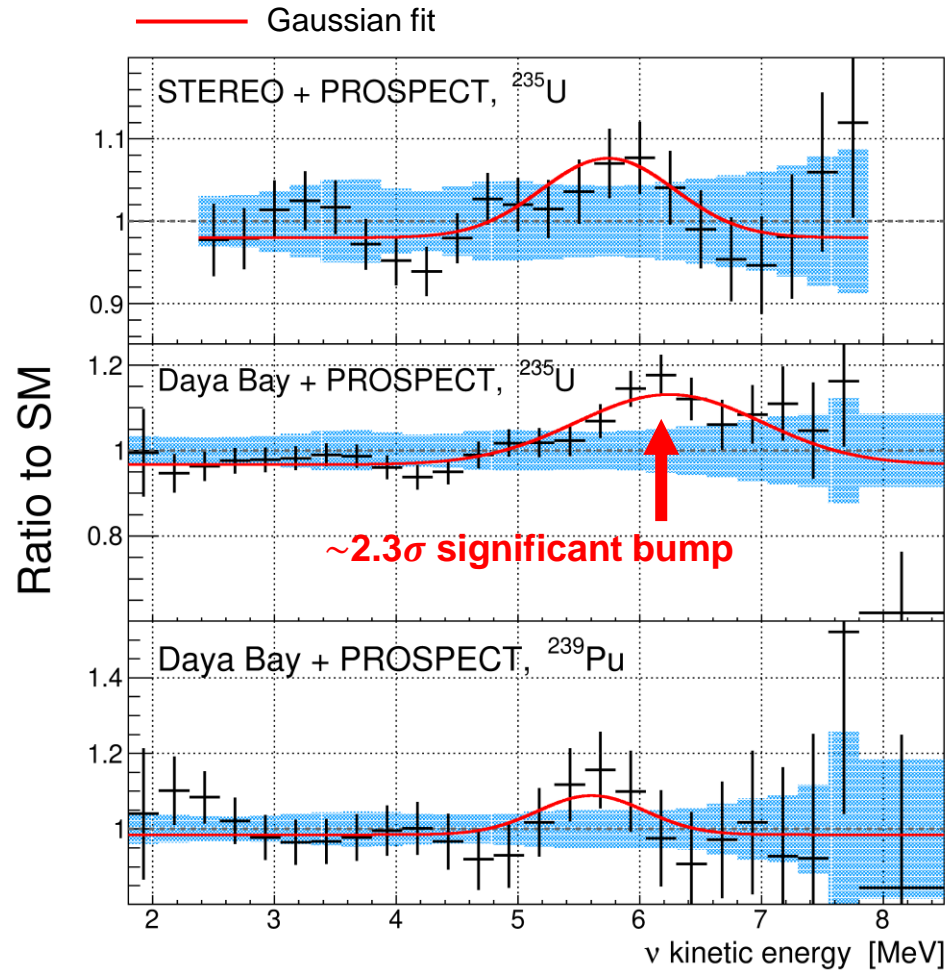


**⇒ Impact of NND modeling observed >6 MeV, important >7 MeV**

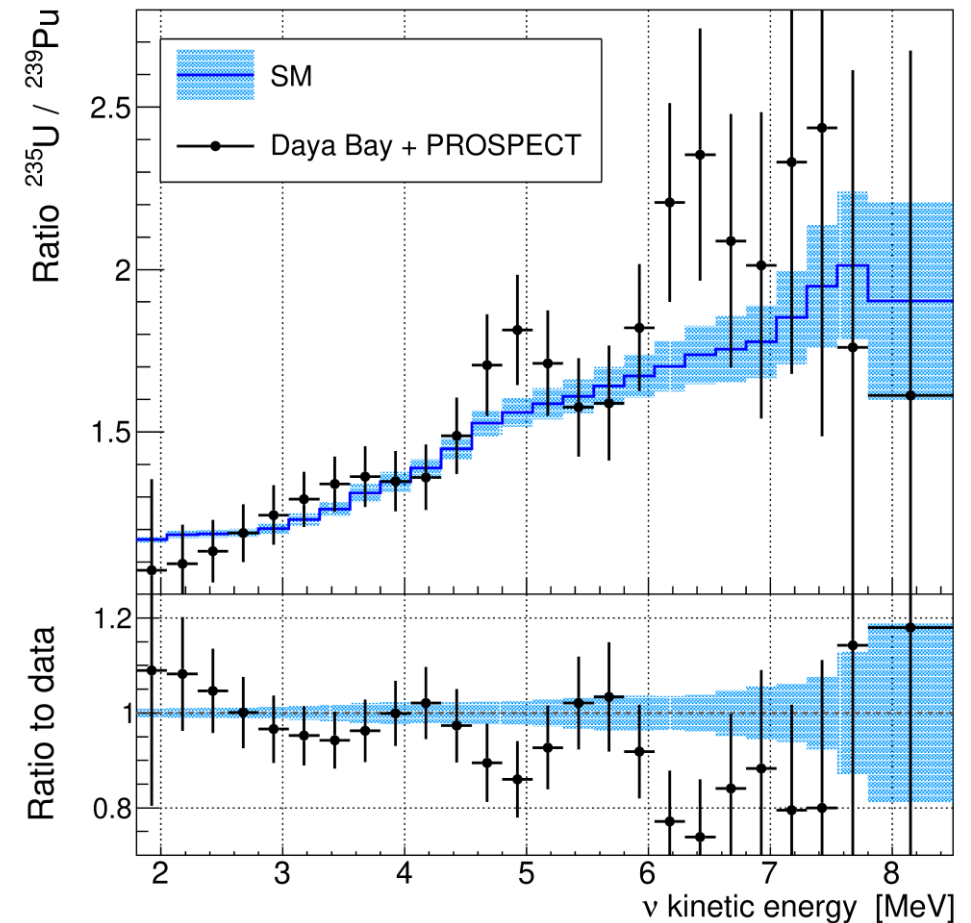
STEREO + PROSPECT data from [Almazán et al. \(2022\)](#)  
 Daya Bay + PROSPECT data from [An et al. \(2022\)](#)

*All plots are preliminary*

## RATIO OF IBD SPECTRA



## $^{235}\text{U}/^{239}\text{Pu}$ RATIO OF IBD SPECTRA



**$\Rightarrow$  Good agreement with experimental IBD spectra, no significant observation of deviation in 5-7 MeV**

## 1. Introduction & motivations

- a. Reactors as antineutrino sources
- b. Experimental anomalies
- c. Different modeling methods

## 2. Revised summation method

- a.  $\beta^-$  spectrum calculation
- b. Nuclear data content
- c. Uncertainty budget

## 3. Preliminary comparisons

- a. Integral measurements
- b. Spectrum shape

## 4. Conclusion & perspectives

# KEY POINTS OF BESTIOLE SUMMATION PREDICTION

## Modeling of non-unique forbidden transitions

- 23 non-unique forbidden branches computed with **nuclear structure calculation**
  - ▶ IBD yield **decreased by  $(1.3 \pm 0.2)\%$**
- $\xi$ -approximation uncertainty at fission spectrum level  **$\sim 0.3\%$  uncertainty**

## Impact of TAGS data

- IBD yield **decreased by 8%**
- Residual Pandemonium correction, IBD yield **decreased by  $(2.2 \pm 2.4)\%$** 
  - ▶ Measurement needed, can also be used to validate RP correction

## Modeling nuclides with no data

- Different NND modelings impact IBD yields by **1-3 %**
- Important for fission spectra **above 7 MeV**
  - ▶ Measurement needed, priority for high-energy spectrum comparison

## Comprehensive uncertainty budget

- Uncertainty budget of summation model for the **first time ever**
  - ▶ Impact of FY correlations to be confirmed

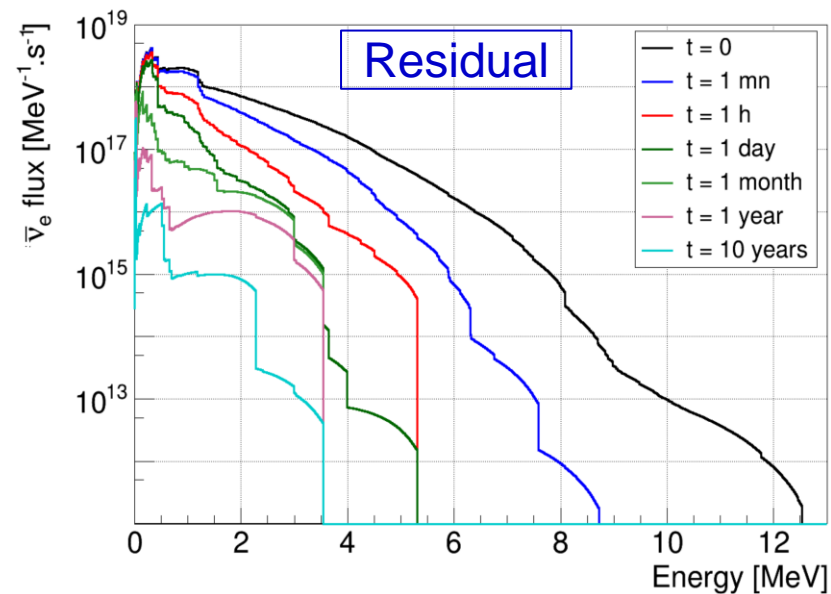
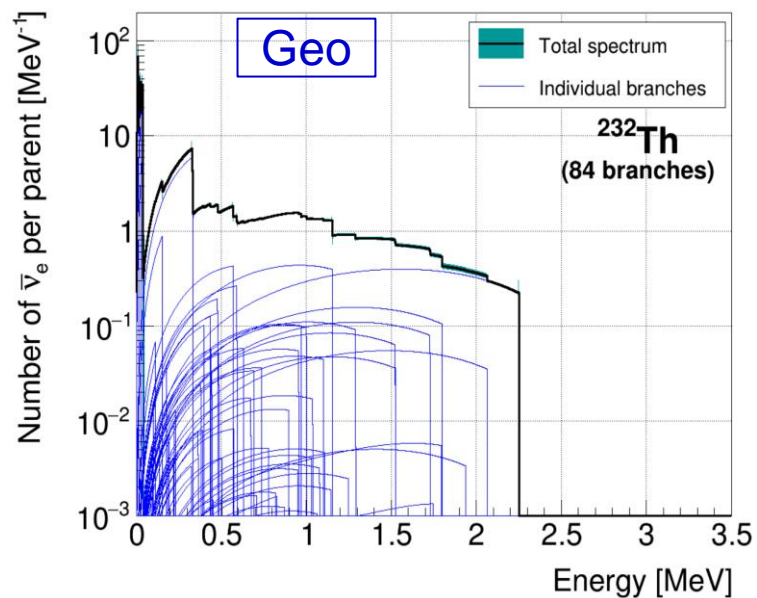
**Final uncertainty budget  $\sim 3\%$**

**Led by RP correction**

**$\Rightarrow$  more TAGS data should be the priority**

**$\Rightarrow$  Article in preparation, coming soon  
with supplementary materials**

## Reach of a comprehensive summation model, needed for validation



See talk by Anthony Onillon

