

High performance computing & data sciences for reactor systems

Workshop on Computational Nuclear Science and Engineering

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Center for Exascale Radiation Transport
Texas A&M University**



TEXAS A&M UNIVERSITY
Department of
Nuclear Engineering

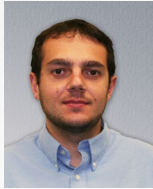
July 16, 2021 IAEA (online)

Outline

- Brief (picturesque) bio
- High-performance computing (HPC)
 - Some history
 - Some well-recognized software used in nuclear engineering
 - A few application examples:
 - Thermal-hydraulics (from Argonne Nat'l Lab)
 - Neutron Transport (from Argonne Nat'l Lab)
 - Neutral-particle Transport (from **Texas A&M U.**)
 - Multiphysics simulations of molten salt reactor (from CNRS/**Texas A&M U.**)
- Data sciences with HPC
 - Motivations (multi-query problems)
 - Data-driven model-order reduction
 - Application to multiphysics simulation of molten salt reactor (from **Texas A&M U.**)
- Conclusions and Outlook

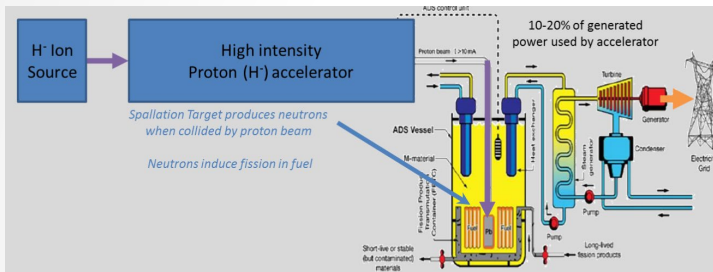


← That's me (on GitHub )

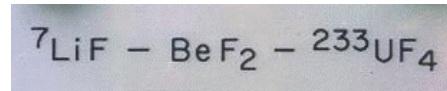


← That's me (in real life)

- Accelerator-driven production of tritium



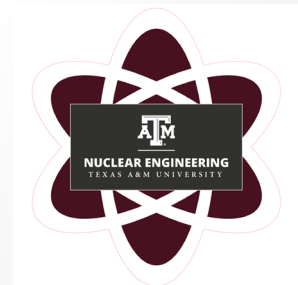
+



- Near-real-time PWR accident simulator for crisis management
Reactor physics and Applied Math Department



- 2004-present: Nuclear engineering, Texas A&M U.
Computational radiation transport, Multiphysics, and
Predictive science <https://multiphysics.engr.tamu.edu/>



My research interests

- Radiation transport

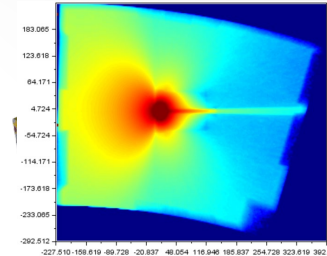
Predictive Science Academic Alliance Program (PSAAP)



CERT

Center for Exascale Radiation Transport

<http://class.tamu.edu/cert>



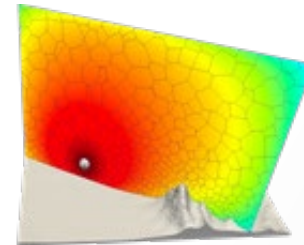
Stockpile stewardship 

- Multiphysics software development (RELAP-7, RattleSnake, Pronghorn)

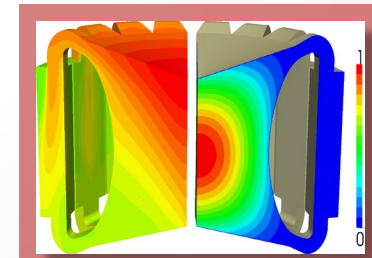
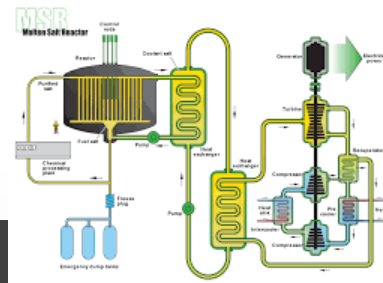


- Data sciences and machine-learning

Nuclear radiation effects



Multiphysics model reduction



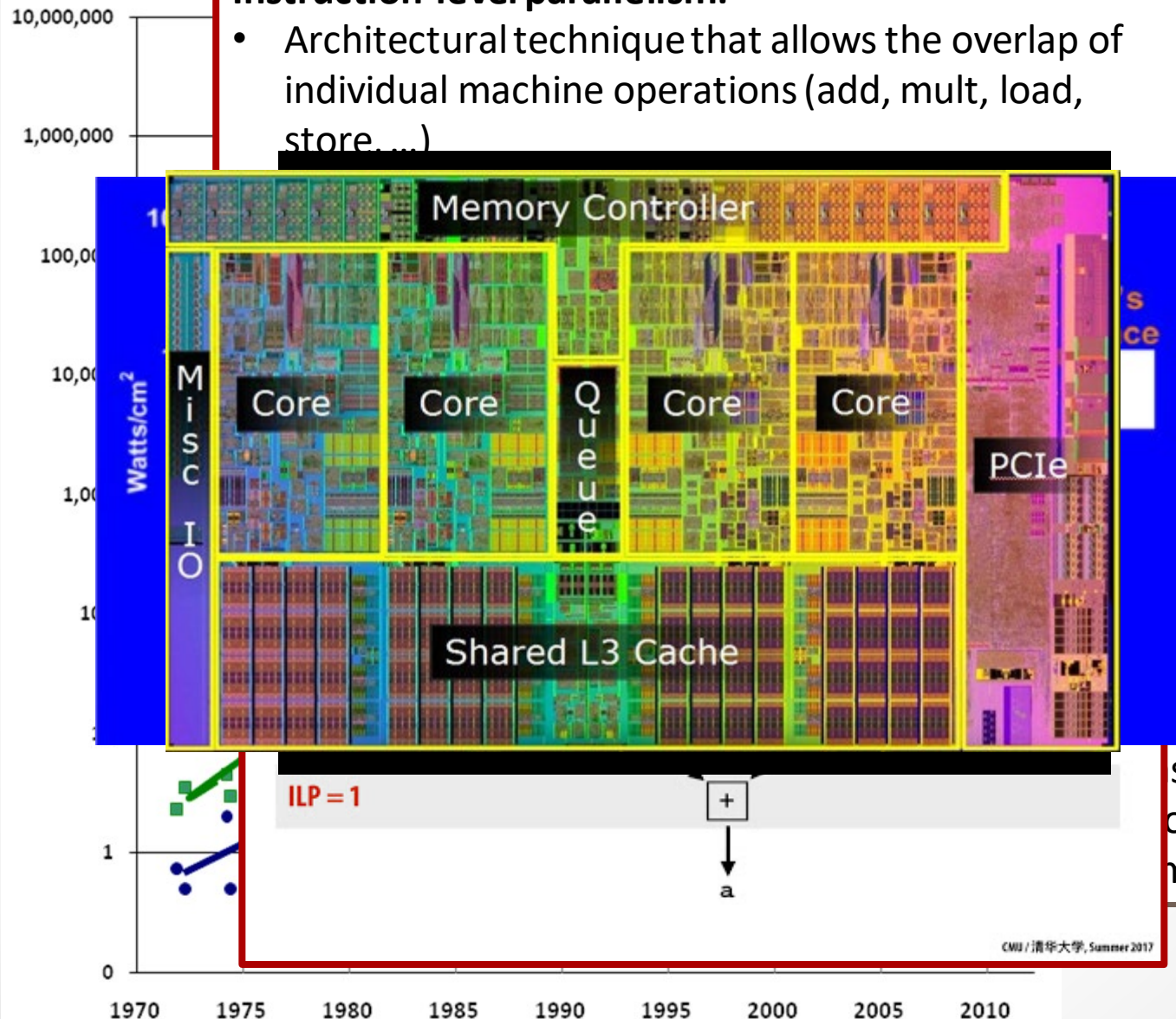
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Evolution of processor speeds

Instruction-level parallelism:

- Architectural technique that allows the overlap of individual machine operations (add, mult, load, store...)



...ant still rising
...esigns);
...re-interpreted"

...d has flattened

...nsumption
...ne issue)

...structions
...on-level
...m or ILP)

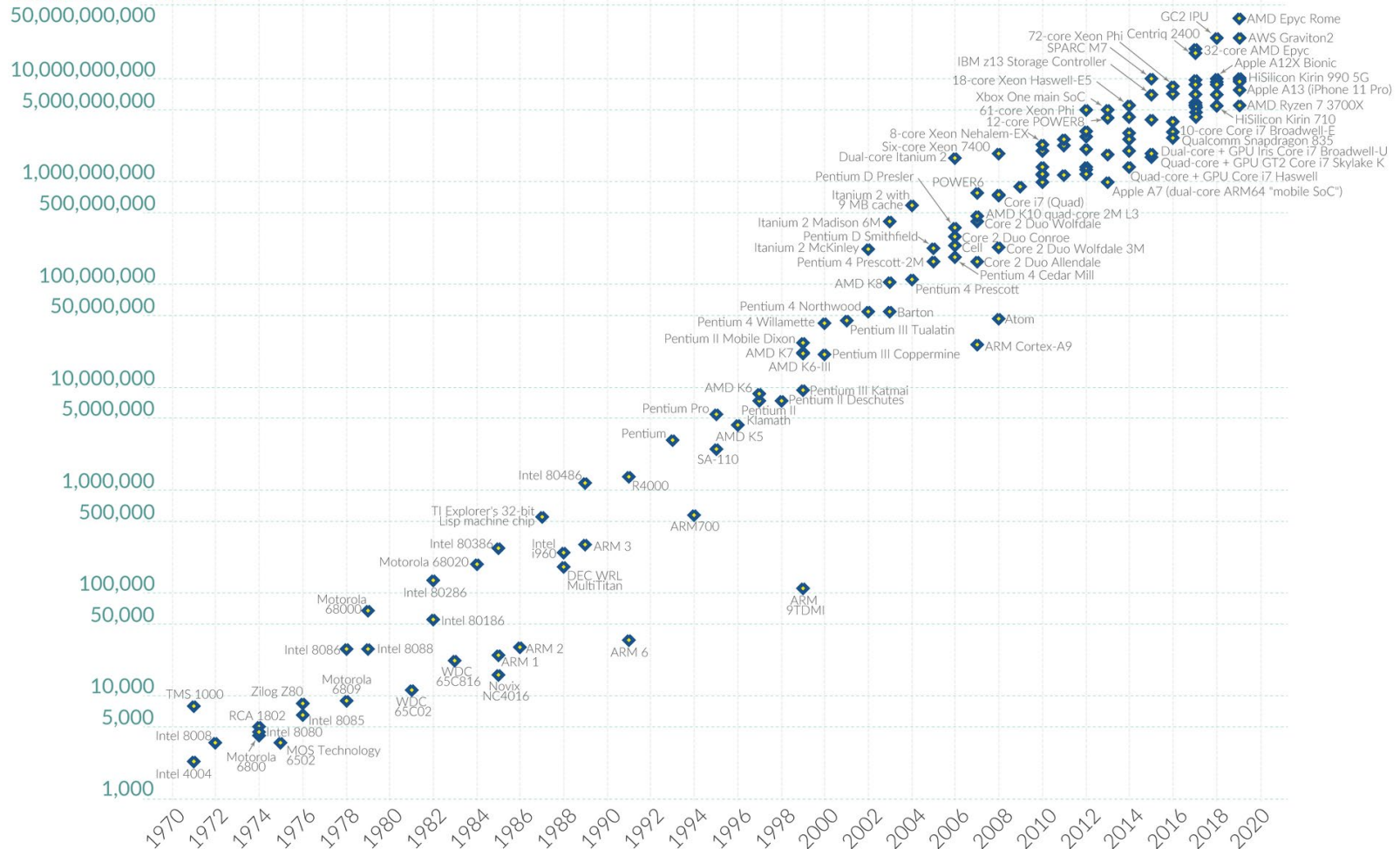
Moore's law: ~straight line on semilog scale

Moore's Law: The number of transistors on microchips doubles every two years

Moore's law describes the empirical regularity that the number of transistors on integrated circuits doubles approximately every two years. This advancement is important for other aspects of technological progress in computing – such as processing speed or the price of computers.

Our World
in Data

Transistor count



Data source: Wikipedia (wikipedia.org/wiki/Transistor_count)

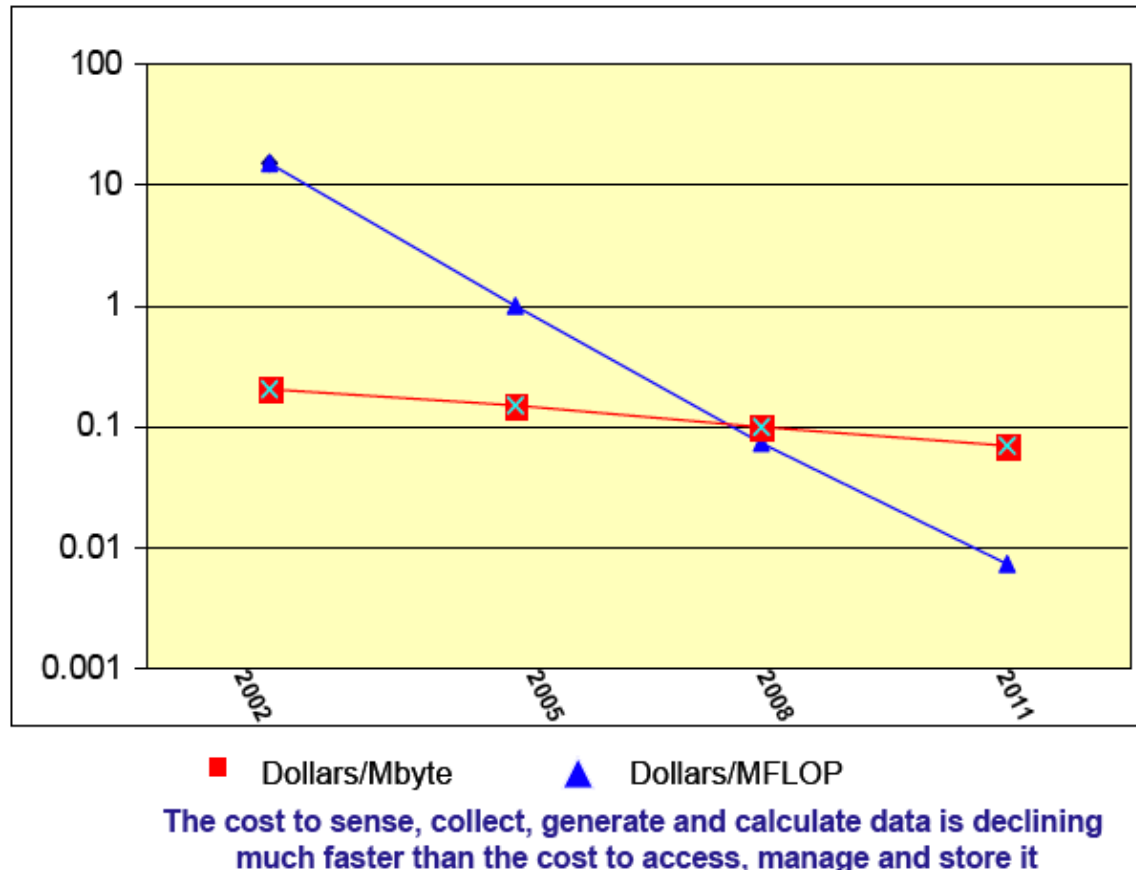
OurWorldinData.org – Research and data to make progress against the world's largest problems.

Licensed under CC-BY by the authors Hannah Ritchie and Max Roser.

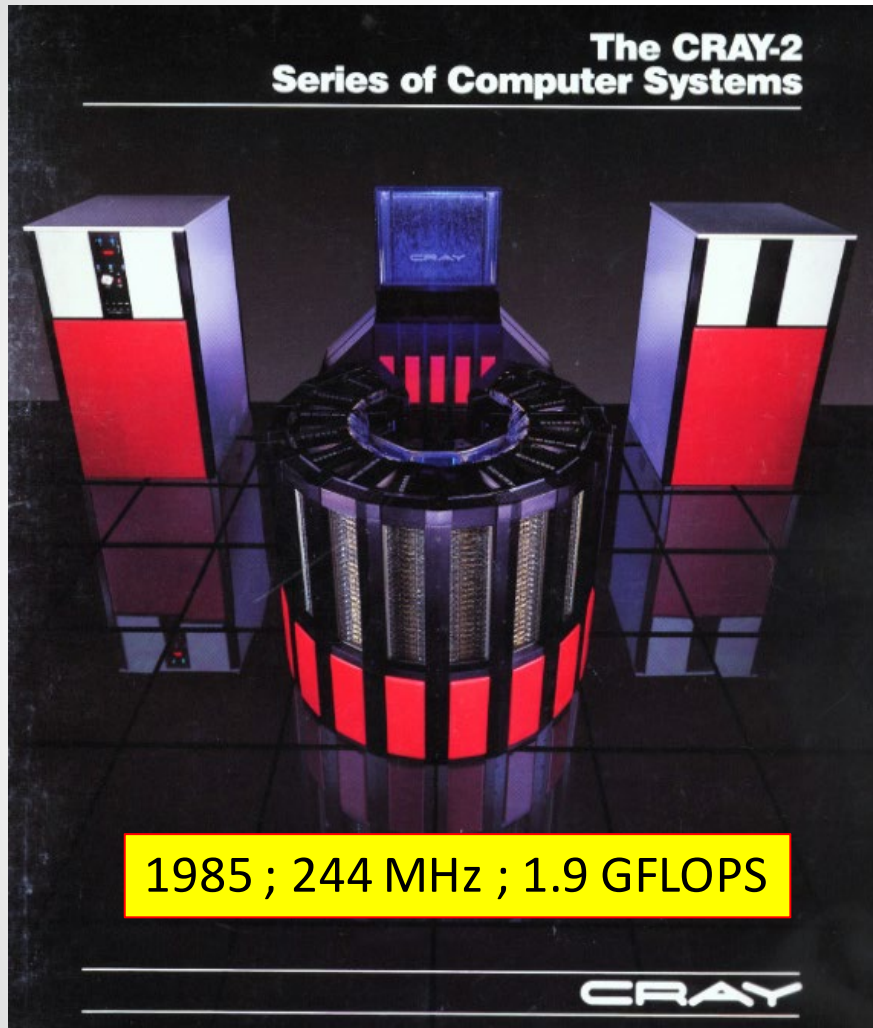
FLOP costs decreasing faster than RAM costs

- *Our ability to sense, collect, generate and calculate on data is growing faster than our ability to access, manage and even “store” that data*

Source: David Turek, IBM



Perspective



2010; 800 MHz ; 1.6 GFLOPS

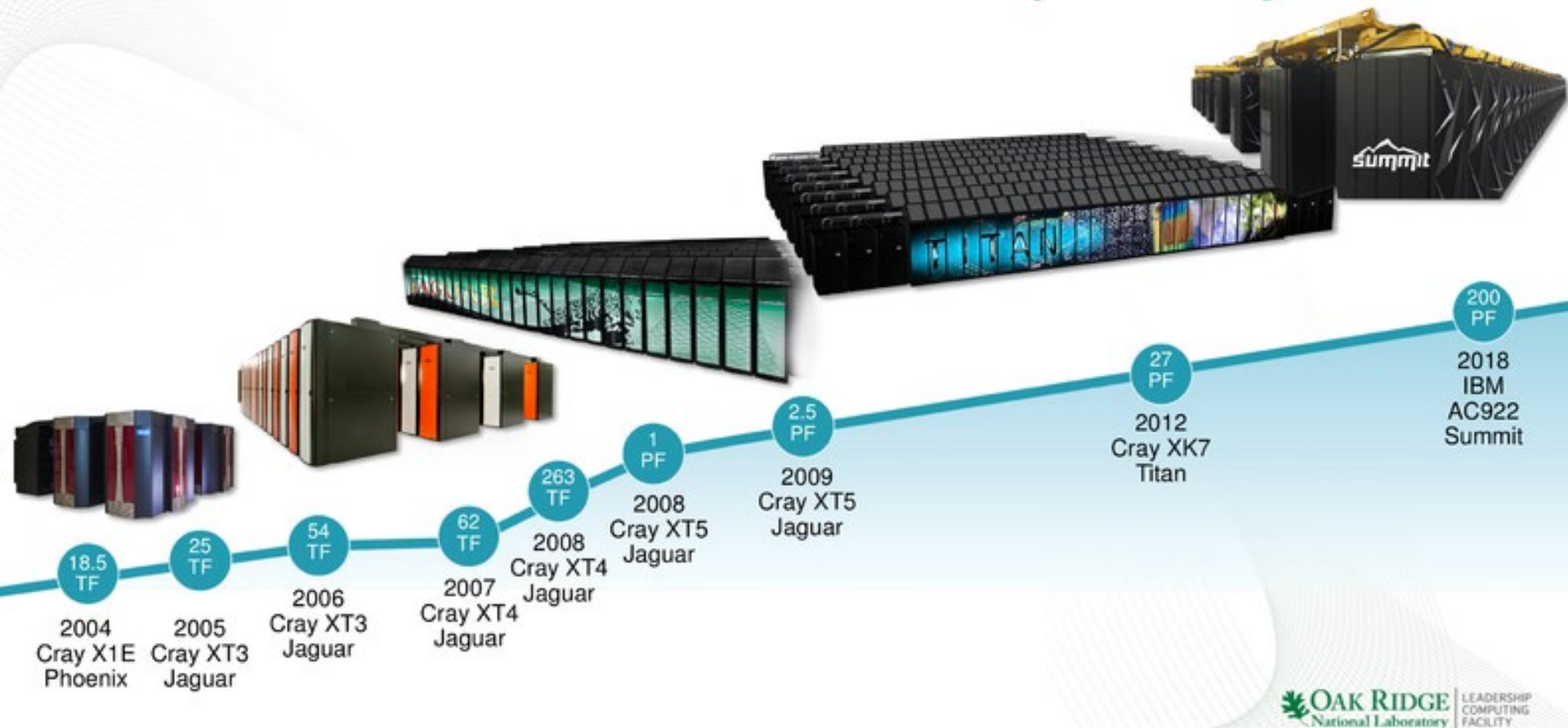


2015; 1,000 MHz ; 3 GFLOPS

Top 500 list

Rank	System	Rank	System	Cores	Rmax (TFlop/s)	Rpeak (TFlop/s)	Power (kW)	Rank	Power (kW)
1	Sunway National	1	Supercomputer Fugaku - Supercomputer Fugaku, A64FX 48C 2.2GHz, Tofu interconnect D, Fujitsu RIKEN Center for Computational Science	7,630,848	442,010.0	537,212.0	29,899	435.9	15,371

The Oak Ridge Leadership Computing Facility has enabled us to field a series of leadership-class systems



OAK RIDGE
National Laboratory
LEADERSHIP COMPUTING FACILITY

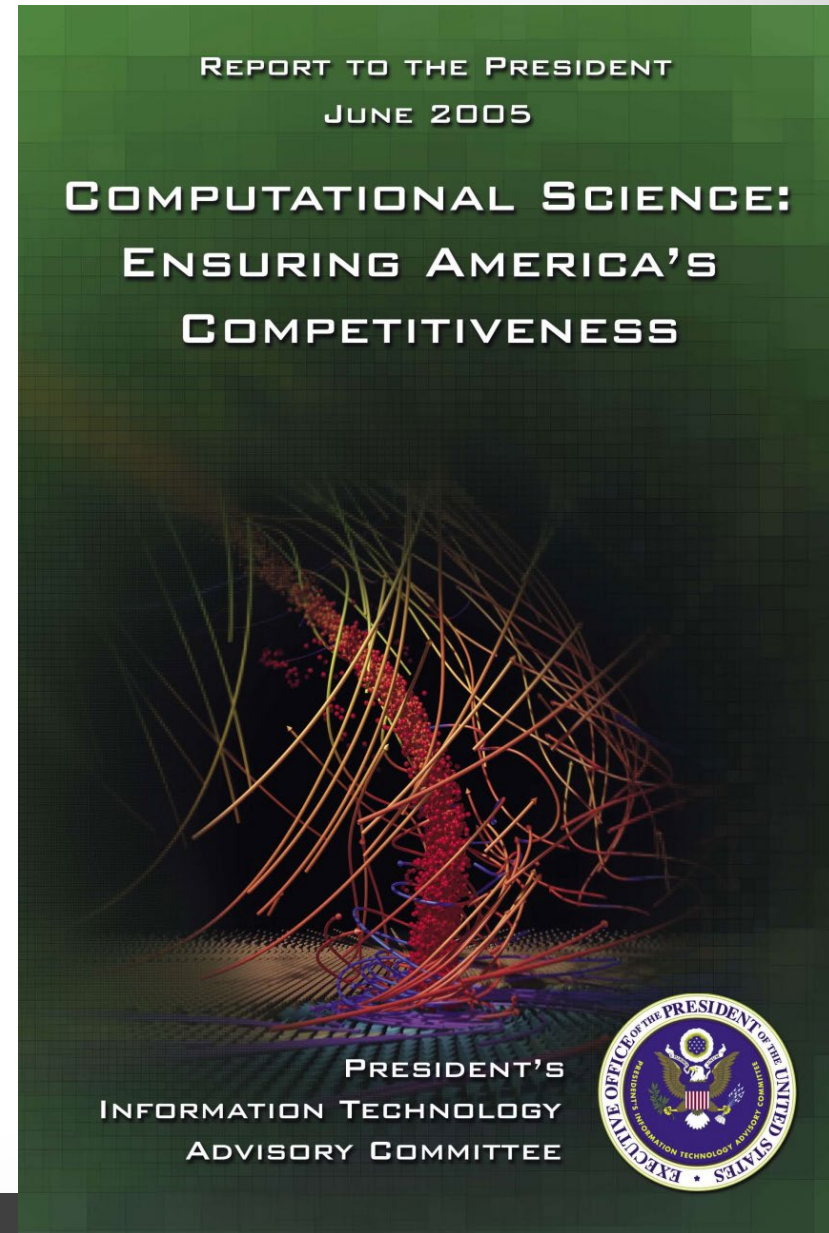
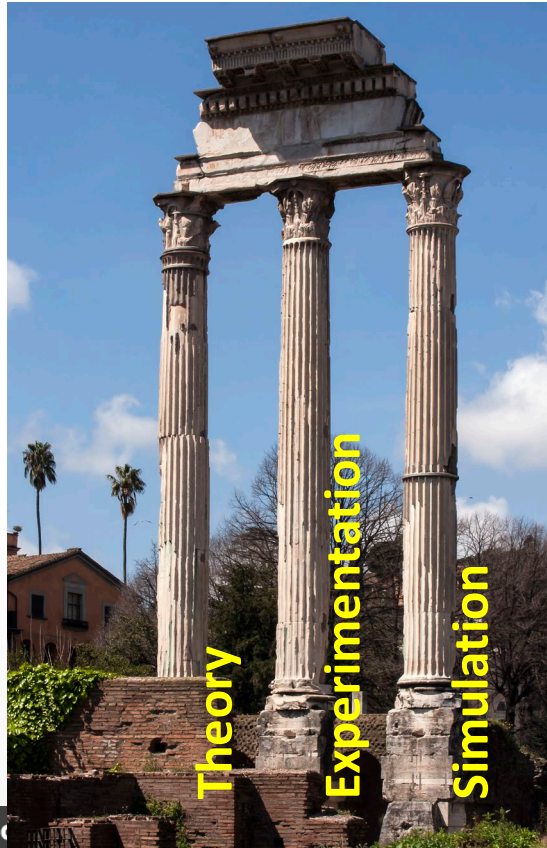


TEXAS A&M ENGINEERING
EXPERIMENT STATION

10	Komp RIKEN Japan	Eni S.p.A. Italy	10	Frontera - Dell C6420, Xeon Platinum 8280 28C 2.7GHz, Mellanox InfiniBand HDR, Dell EMC Texas Advanced Computing Center/Univ. of Texas	448,448	23,516.4	38,745.9	280.4	12,660
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U.S. Presidential Information Technology Advisory Committee (PITAC)

- Computational science is a rapidly growing multidisciplinary field that uses advanced computing capabilities to understand and solve complex problems.
- Requires advances in hardware and software.



High Performance Scientific Computing

Introduction to HPSC

What is High Performance Scientific Computing?

single process

Multi-process

Multi-process

What is Scientific Computing

Scaling Challenge

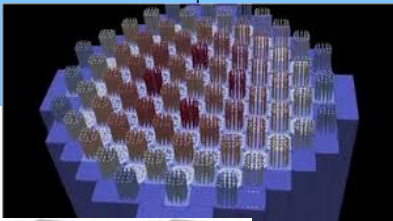
Overview of computational landscape

application takes too long to run

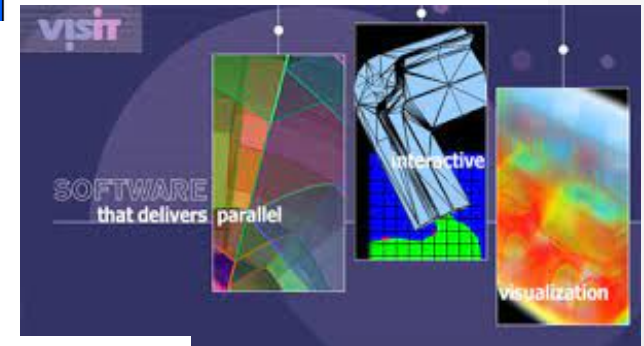
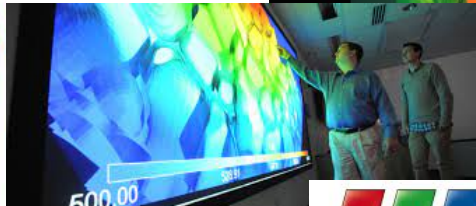
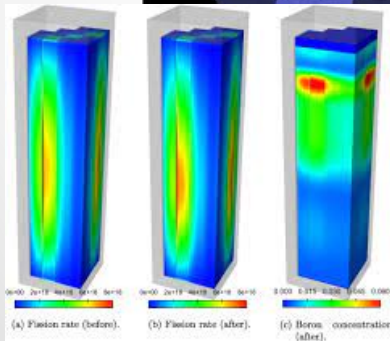
Application doesn't fit in memory of single machine

Application doesn't fit & takes too long

Scientific Simulations Examples



Data Analytics and Knowledge Extraction

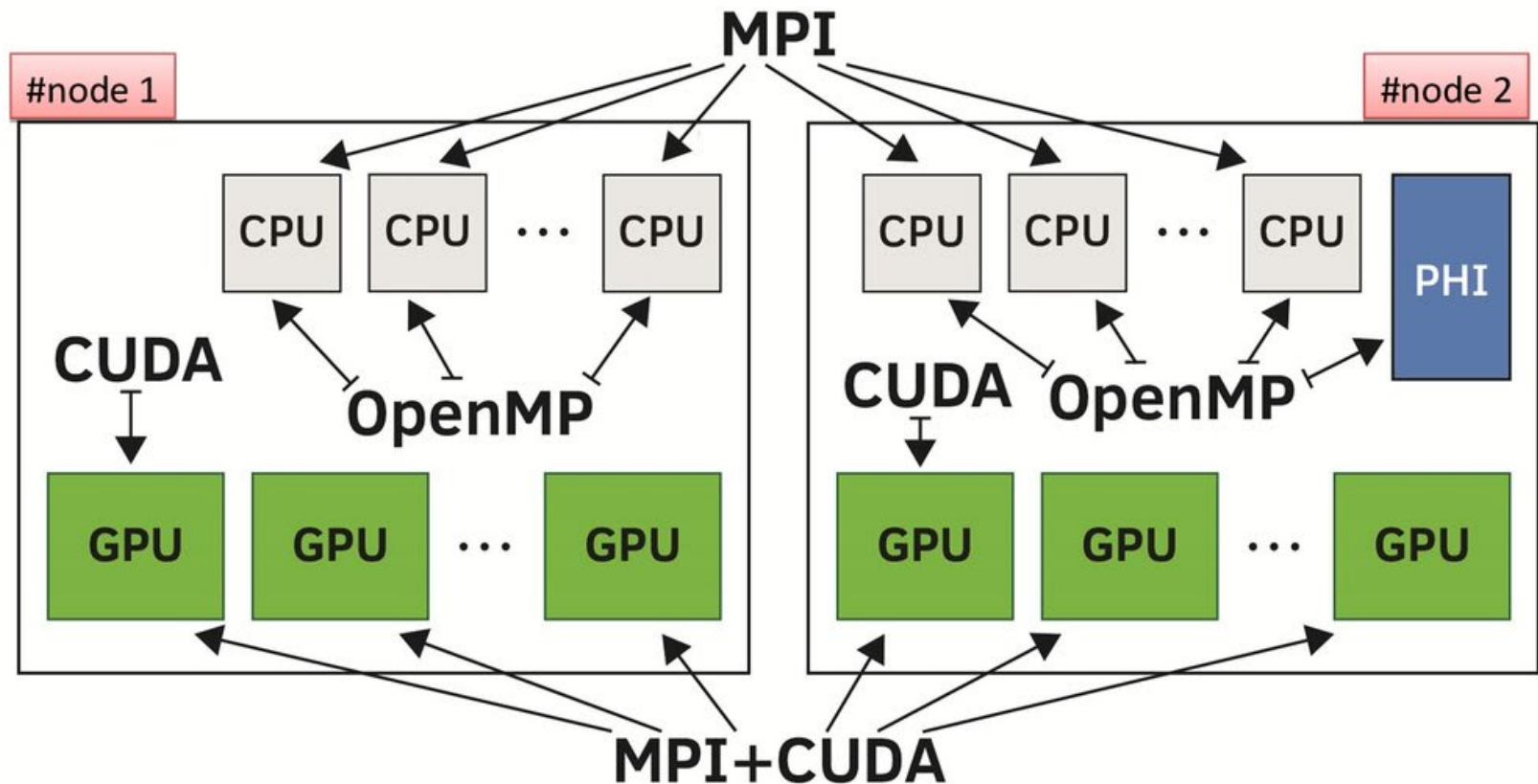


ParaView
Parallel Visualization Application

Partially adapted from the Lincoln Laboratory Supercomputing Center (MIT)



Parallel technologies: levels of parallelism



How to control hybrid hardware:
MPI – OpenMP – CUDA - OpenCL ...

OpenMP

What is Scientific Computing?

Single process

What is High Performance Scientific Computing?

Multi-process

Multi-process

how do we address the parallel computing challenges

Why High Performance Scientific Computing?

why?

how

What is an Interactive Supercomputing Environment

mas

```
main()
{
```

```
#pragma omp parallel
```

```
{
  cout << "Hello World!";
}
```

```
}
```

PARALLEL {

OMP_NUM_THREADS

T₀ T₁ T₂

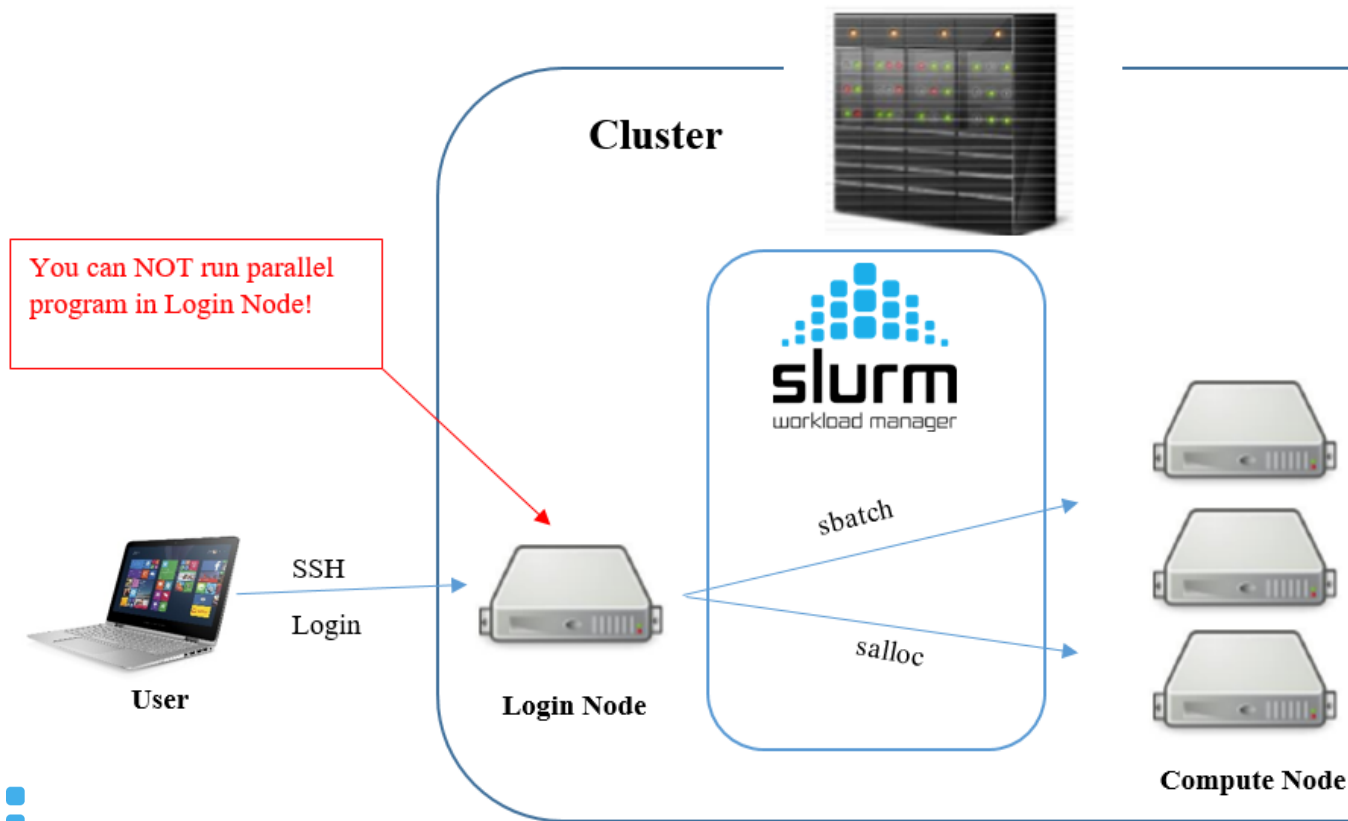
Thread Team

}

T₀

Interacting with a supercomputer:

Job scheduling



HPC for Scientific computing (SC)

Verification

(Am I solving the equations correctly?)

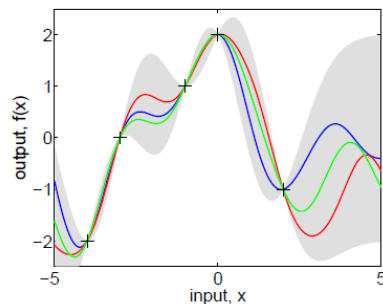
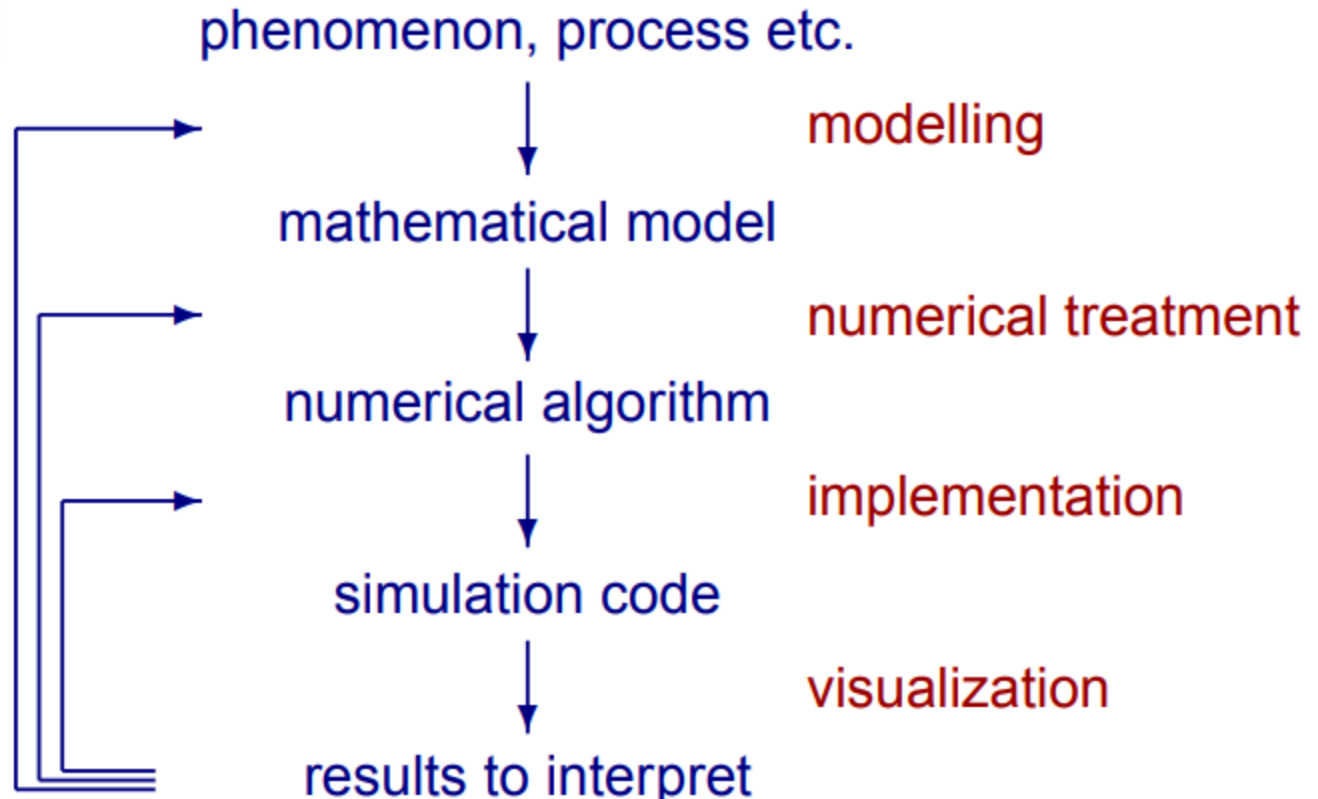
Validation

(Am I solving the correct equations?)

Uncertainty

Quantification

(What is the goal of my simulation? What are the QoI's?)



FastMath: Frameworks, Algorithms and Scalable Technologies for Mathematics



 **PETSc**

 **TAO**

Portable, Extensible Toolkit for Scientific Computation

Toolkit for Advanced Optimization

PETSc							
Vectors	Matrices						
	Compressed Sparse Row (AIJ)	Blocked Compressed Sparse Row (BAIJ)	Compressed Block Diagonal (BDIAG)	Dense	Others		
Linear Solvers							
GMRES	CG	CGS	BiCGSTAB	TFQMR	Richardson	Chebyshev	Others
Preconditioners							
Additive Schwartz	Block Jacobi	Jacobi	ILU	ICC	Others		
Non-linear Solvers				Time Steppers			
Line Search	Trusted Region	Others		Euler	Backward Euler	Pseudo Time Stepping	Others



Example-1: Computational fluid dynamics

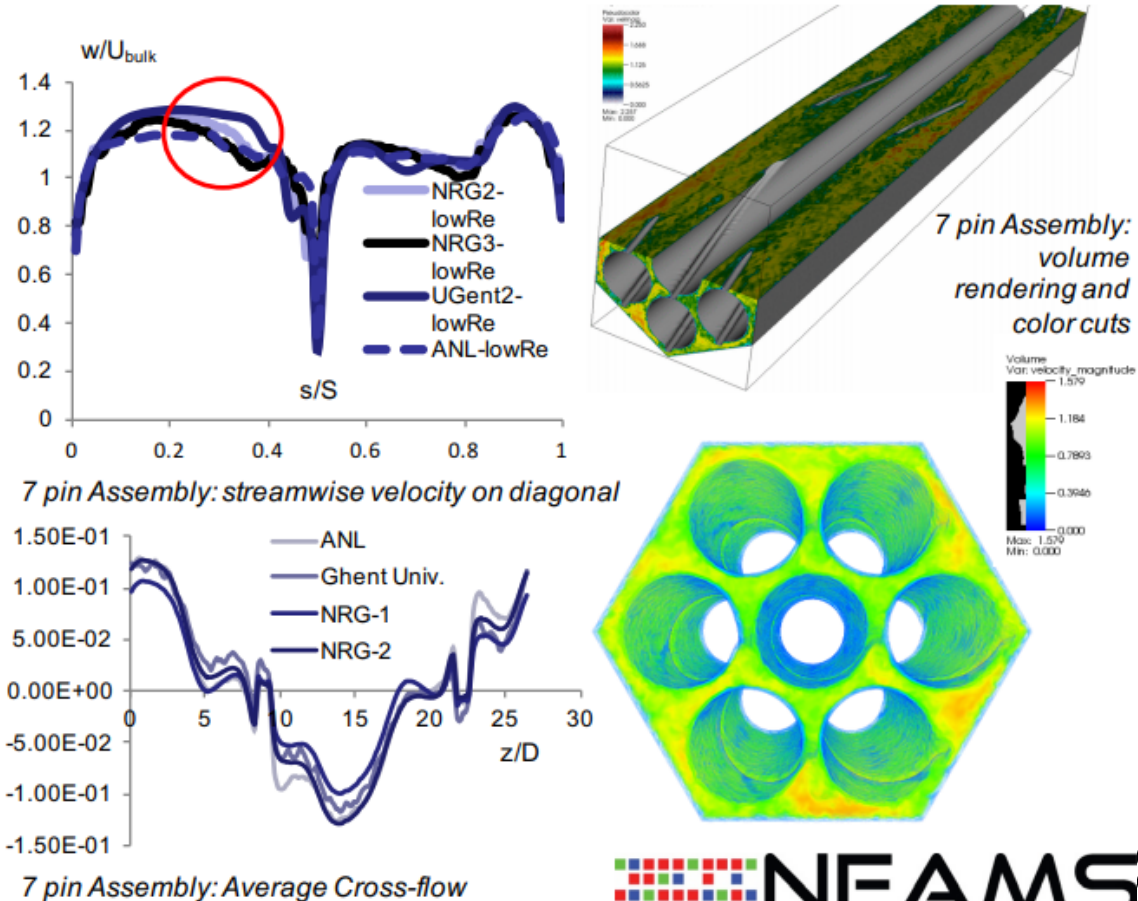
User case: Using higher-resolution approaches to inform lower-resolution methods - 1

For complex geometries CFD-grade data is often not available.

- RANS approaches can benefit from comparison with DNS/LES

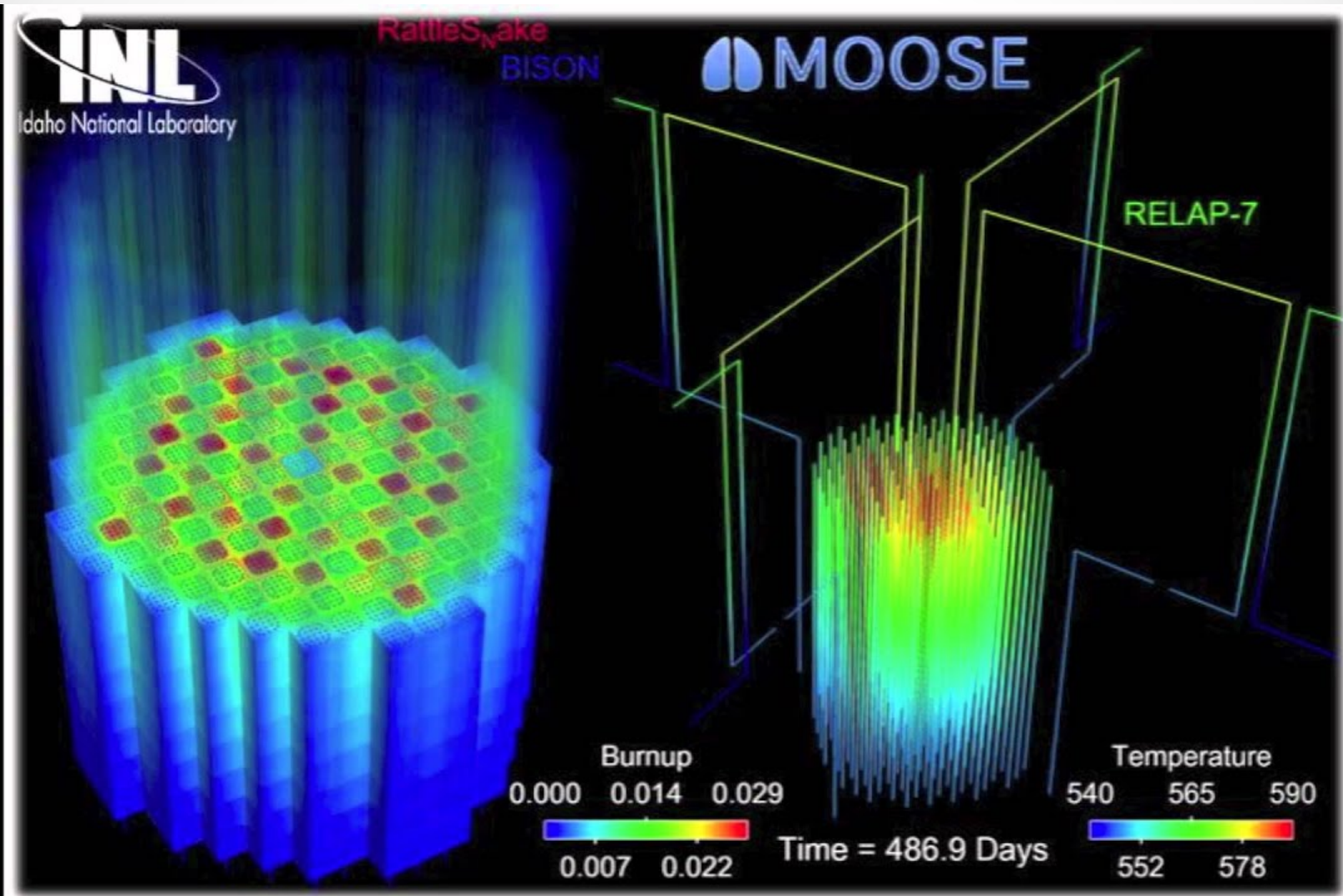
International collaboration (INERI) centered on wire-wrappers.

- Comparison between commercial codes and Nek5000
- Results are being used in the design of advanced reactors in Europe



[SFR]

Example-2: MOOSE, a Multiphysics HPC platform



Example-3: Massively parallel radiation transport

- neutron, thermal radiation, gamma, electron
- steady-state, time-dependent, criticality, adjoint, etc.
- advanced solution techniques
- discretization in space/angle/energy
 - **Largest problem we have done: 20.8 Trillion unknowns**



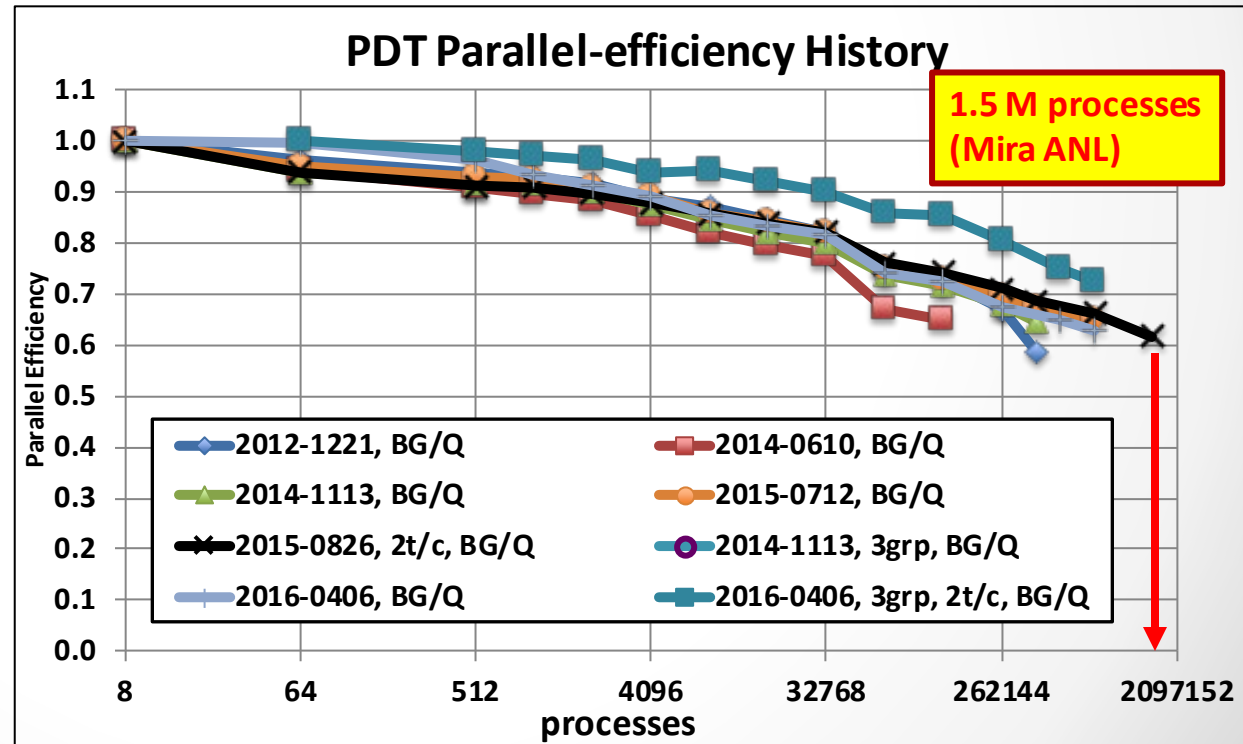
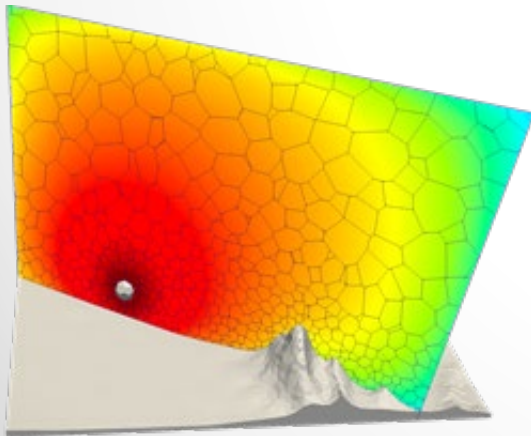
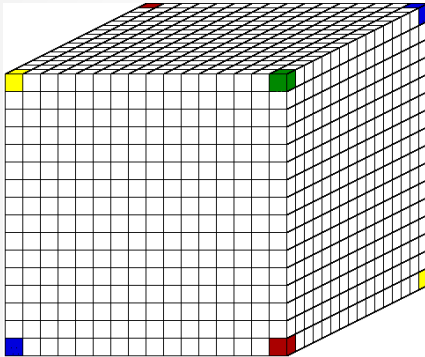
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Department of
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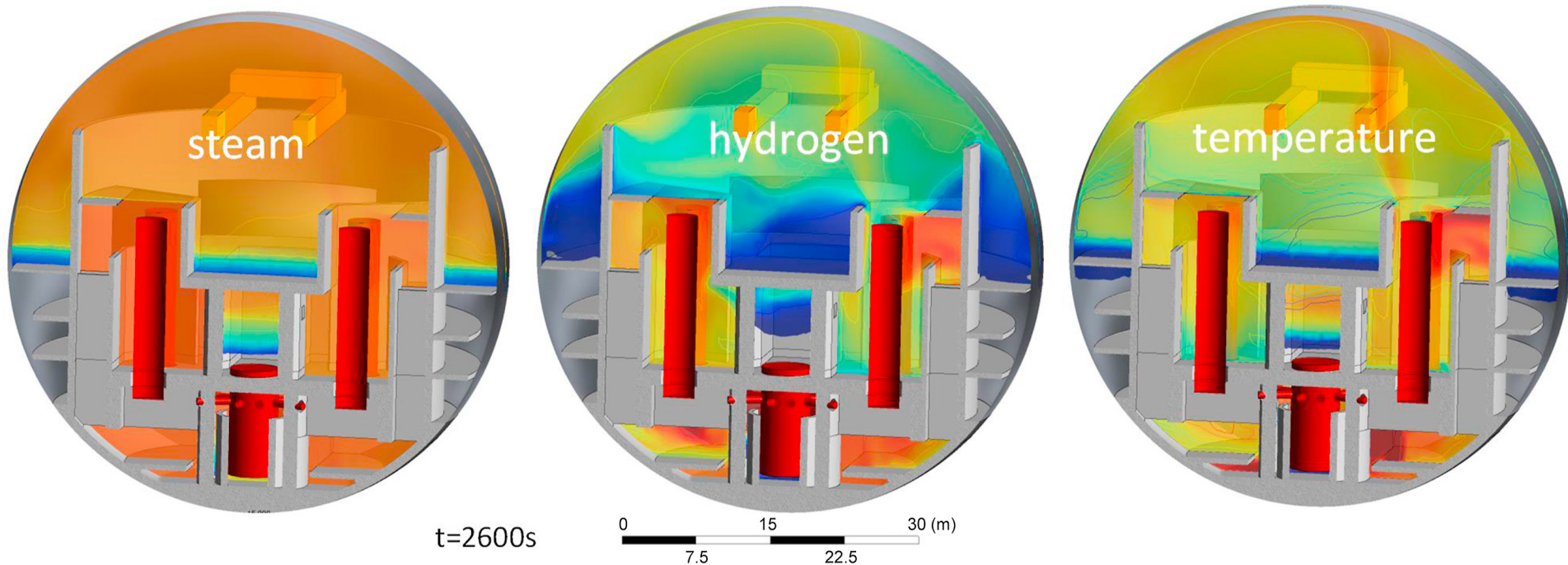
2018

NATIONAL DEBT OF UNITED STATES

\$ 20,502,740,304,411



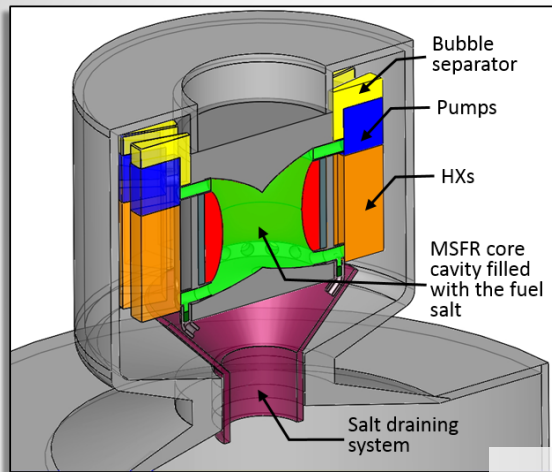
Example-4: Reactor containment



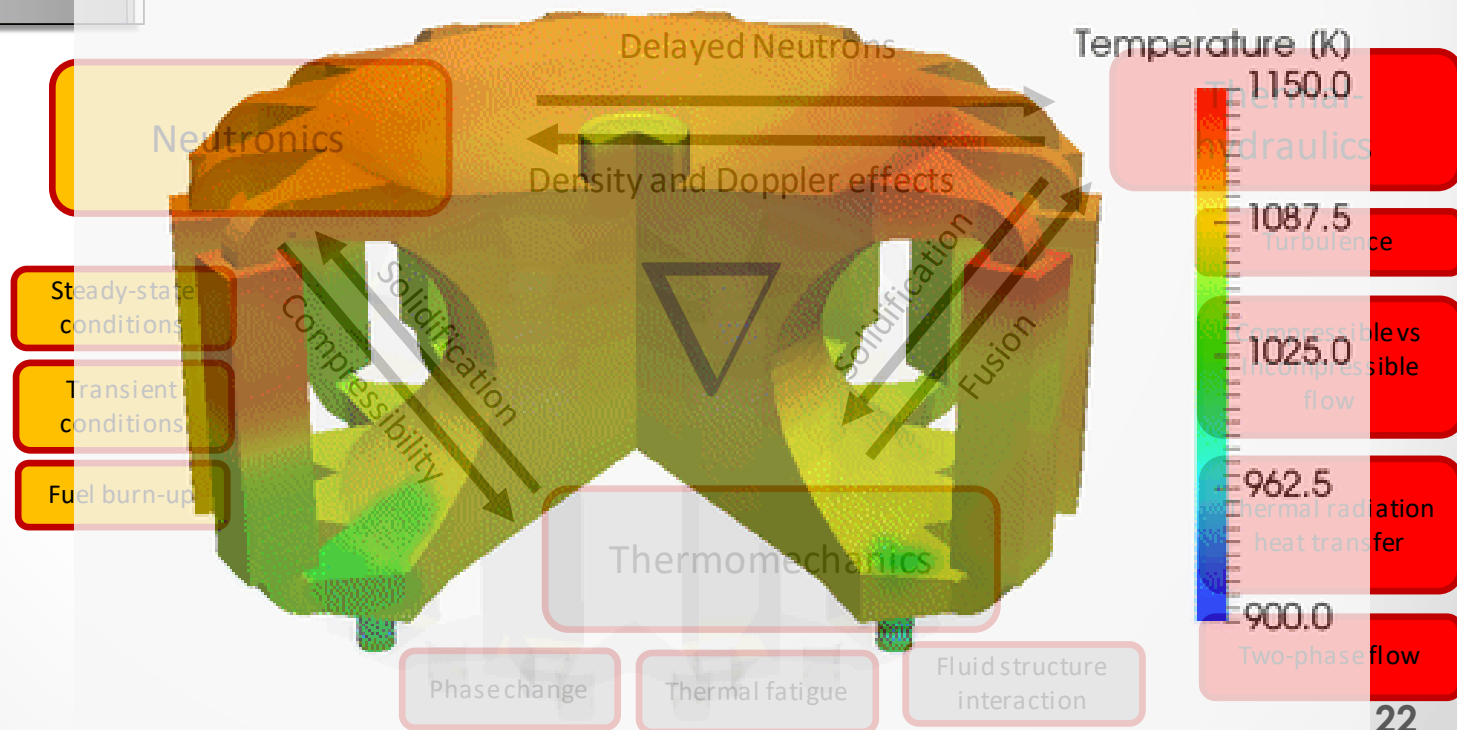
Gas distribution and pressurization inside the containment during an SB-LOCA (Julich, Germany, Kelm et al.).

Based on OpenFOAM for CFD

Example-5: Multiphysics of molten salt reactor



Conceptual Design of the MSFR core cavity



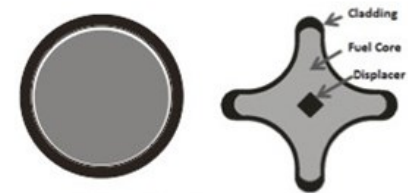
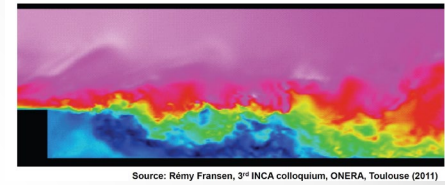
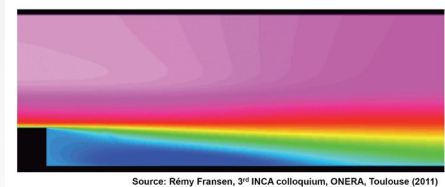
(CNRS, Tano)

Outline

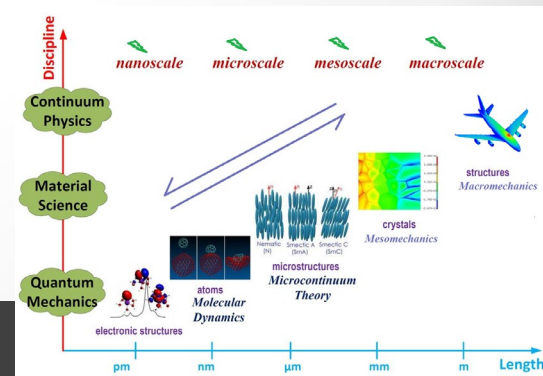
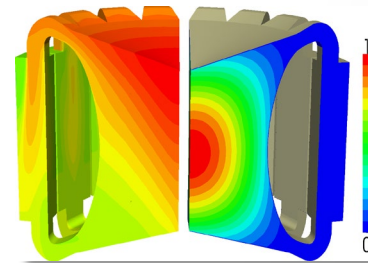
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What is SC/HPC for?

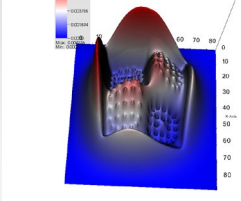
- Increase insight and understanding of physical phenomena
 - DNS > LES > RANS > lumped-parameter TH
- Provide layers in a **hierarchy** of increasingly complex models
 - Are we capturing the right physics?
 - First-principle simulations to ascertain the range of **applicability** of (cheaper) low-order models
 - New designs/configurations not handled by legacy codes
- Scaling bridging:
 - Material science <-> continuum FEM
 - NSF's Material Genome Initiative (MGI)
- Experimental design
 - simulation-informed experiments
- Sometimes, too costly/dangerous experiments:
 - Accidents (core meltdown), disasters, NW, ...



Standard Uranium Fuel Rods and Fuel Rods



What is SC/HPC **not** for?



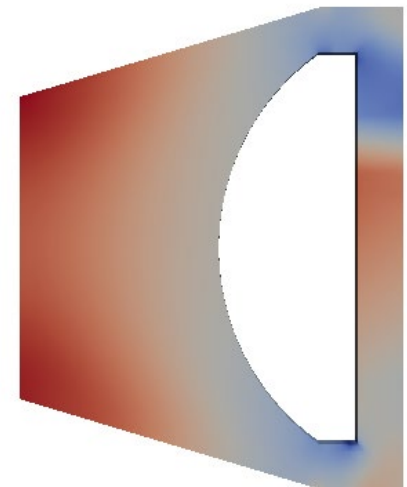
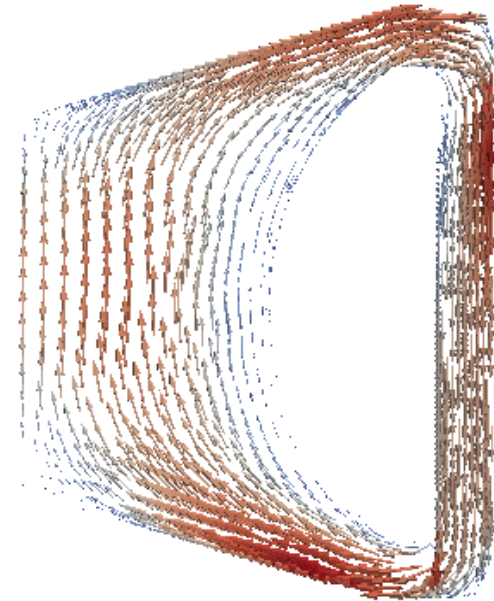
- Pretty pictures (the “viewgraph” norm = useless simulations).
- More demanding, complex simulations that **do NOT increase your ability to predict the outcome** (the quantities of interest)

$$\frac{\text{increased accuracy in prediction}}{\text{resources spent (\$)}}$$

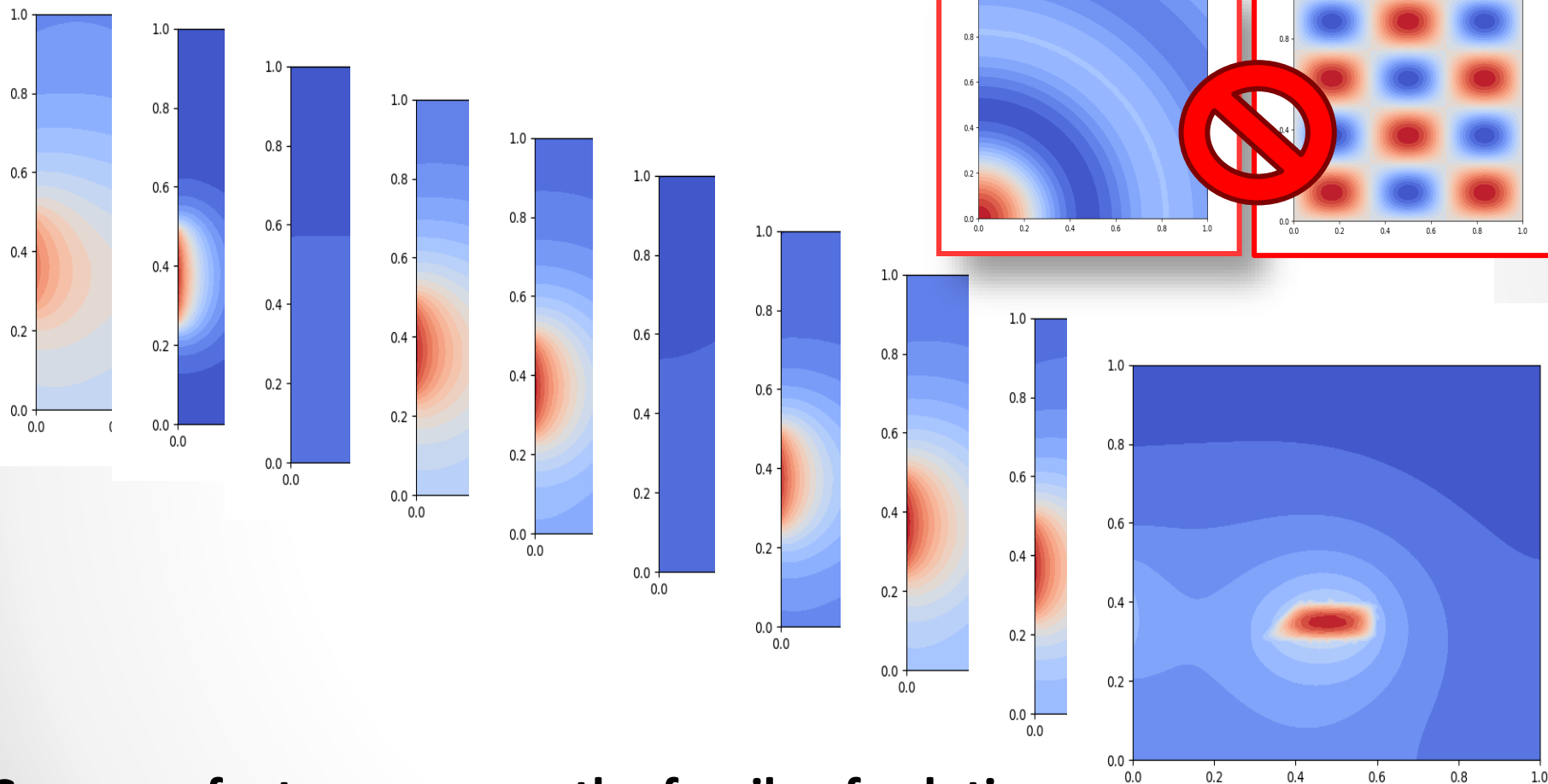
- Kord Smith (ANS M&C 2003)
 - PWRs: 3D reaction rates 3% pin power, axially integrated power: 1%
 - +/-10 ppm critical boron at start-up = “close to perfect”
- Uncertainties in some physics (e.g., XS evaluations, fuel thermo-mechanics, TH, ...) may overwhelm the accuracy of a solver for instance.

How about a much quicker turnaround for quality design calculations?

- High-dimensional (high-order/first-principles) models :
 - Generate a wealth of data
 - Require high-end HPC platforms
 - May need to be repeated for **every change in the input parameterspace**.
- Multi-query HPC problems (repeated calculations with changes in the input) can become expensive
 - **Design optimization**
 - **Uncertainty quantification**
- **Data Sciences:**
Learn from HPC simulations to predict new cheap HPC-quality simulations
→ Think data assimilation (“image/video compression”)



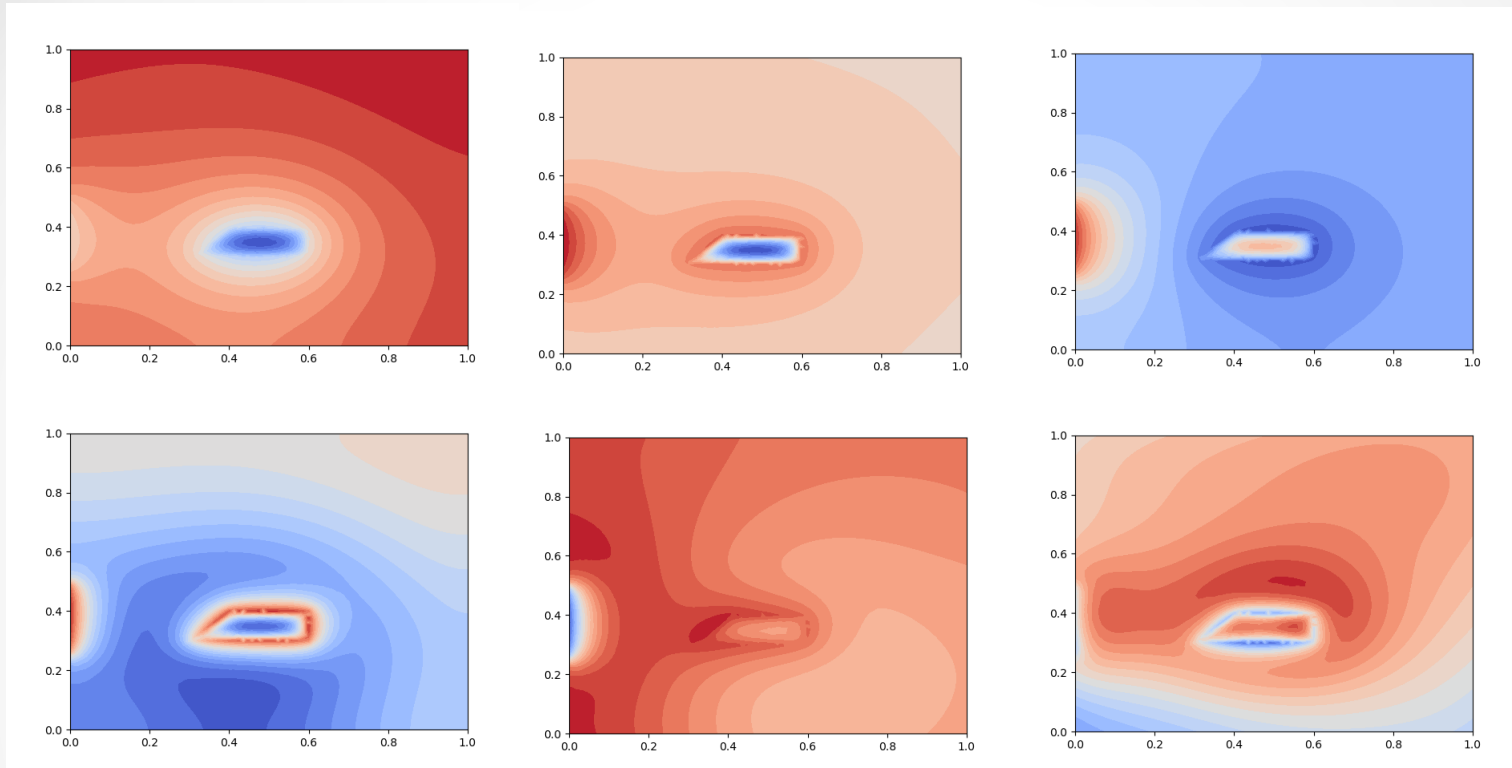
Many simulations with parametric variations



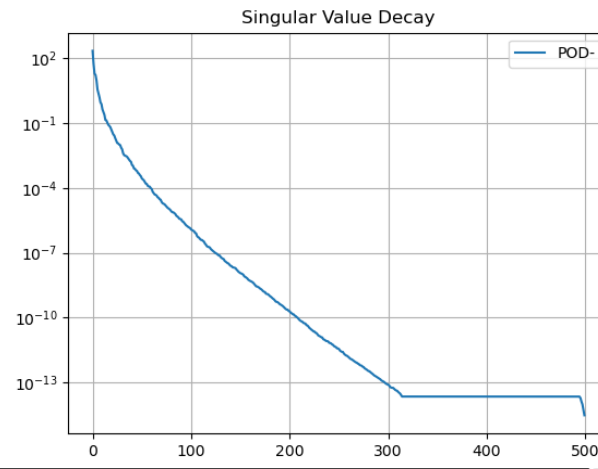
Common features among the family of solutions

Can we learn from that? → data-driven subspace discovery

Discovered subspace from learned data



- Obtained via **Singular Value Decomposition** of the snapshots (learned data)
- Reduction comes from the low number of modes needed



Model Order Reduction: to reduce the computational complexity

Definition

- Model order reduction (MOR) is a set of techniques aimed at reducing the computational complexity of mathematical models in numerical simulations.
- Description of reality (model) + problem input data (in) \rightarrow PDEs \rightarrow discretization \rightarrow large-scale model with a large number of unknowns (degrees of freedom, DoFs) N .

Full Order Model (FOM): Solve $\dot{x} = f(x(t), in(t))$ with $x \in \mathbf{R}^N$

- Model order reduction aims at lowering the computational complexity of such problems by reducing the # of DoFs ($r \ll N$)

Reduced Order Model (ROM): Solve $\dot{c} = f_r(c(t), in(t))$ $c \in \mathbf{R}^r$ with $r \ll N$

such that

$$\|x - Uc\| \leq C_r \|in\| \quad \text{with} \quad \lim_{r \rightarrow N} C_r = 0$$

U : reconstruction operator.

Key points:

- Full Order Model (FOM)

$$x \in \mathbf{R}^N$$

- Reduced Order Model (ROM)

$$c \in \mathbf{R}^r \quad \text{with} \quad r \ll N$$

- Reconstruction: $x \approx Uc$ where U (size $N \times r$) is a data-driven discovered basis.

Need to determine the expansion coefficients c (as functions of the input parameters)

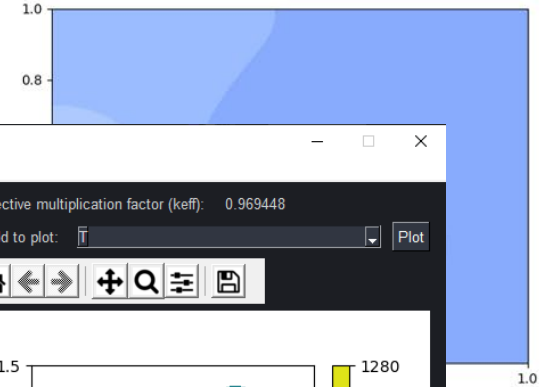
Data-driven sub-space discovery

Physical system

+

Data(*p*)

modeling



GeN-ROM - Model-Order Reduction tool for OpenFOAM

File Help

```

Loading fluid flow terms for precStar4.
Loading self matrices for precStar5.
Loading fuel temperature matrices for precStar5.
Loading coolant density matrices for precStar5.
Loading fluid flow terms for precStar6.
Loading self matrices for precStar6.
Loading fuel temperature matrices for precStar6.
Loading coolant density matrices for precStar6.
Loading fluid flow terms for precStar7.
Loading self matrices for precStar7.
Loading fuel temperature matrices for precStar7.
Loading coolant density matrices for precStar7.
Loading fluid flow terms for precStar7.
Loading reduced interpolation matrix for logTNeutro.
Loading reduced interpolation matrix for TCool.
*****
ROM Loaded!
*****
keff = 0.9694484165684509
    
```

Load

Solve

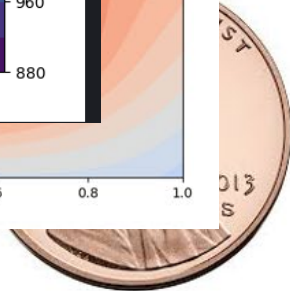
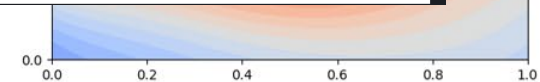
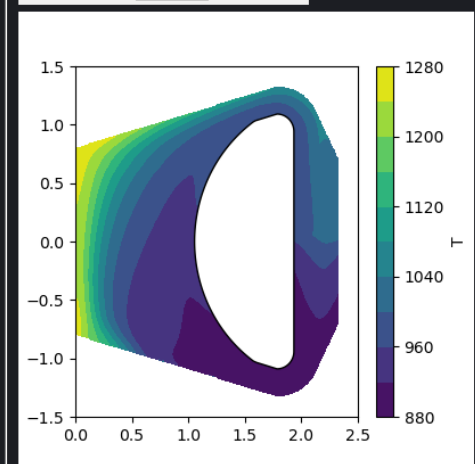
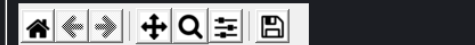
Reset

D_1	0.023720
D_2	0.015789
D_3	0.010024
D_4	0.012084
D_5	0.011534
D_6	0.011038
nuSigma_f_1	0.575548
nuSigma_f_2	0.375454
nuSigma_f_3	0.410838
nuSigma_f_4	0.622968
nuSigma_f_5	1.466770
nuSigma_f_6	4.758780

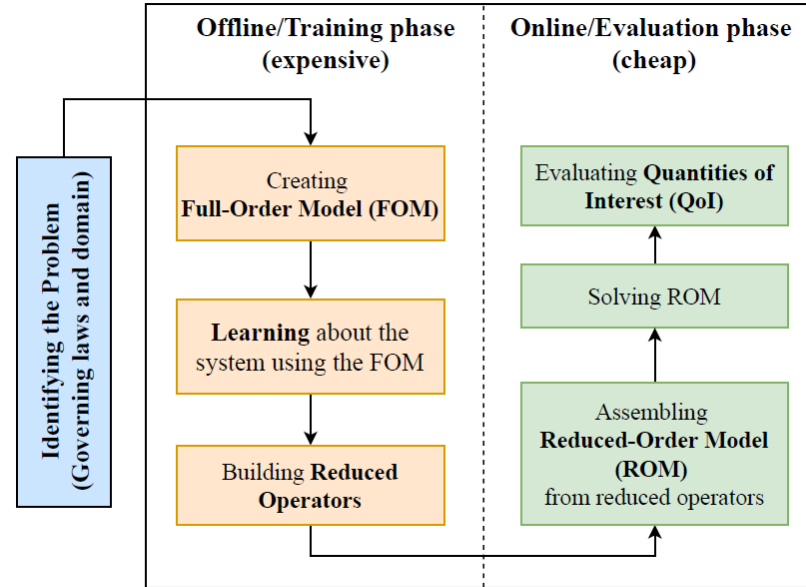
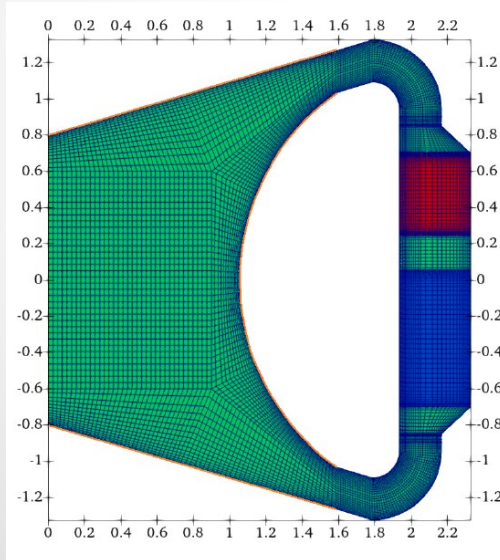
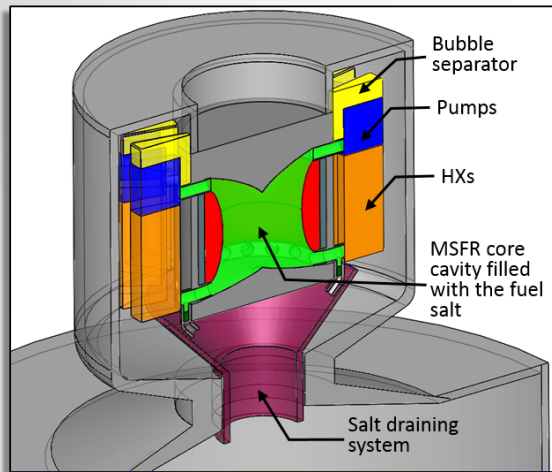
Sigma_r_1	6.899700
Sigma_r_2	3.955500
Sigma_r_3	1.774100
Sigma_r_4	1.983400
Sigma_r_5	1.637700
Sigma_r_6	3.566300
Fp	-80000.000000
T_HX	900.000000
alpha_HX	100000.000000
beta_th	0.000200
Pr	8.000000

Effective multiplication factor (keff): 0.969448

Field to plot: \bar{T}



Model-order reduction for advanced reactors



The reduced equation system

$$\rho M \dot{\mathbf{c}}^{uD} + \rho \mathbf{c}^{uD, T} \underline{\mathbf{C}} \mathbf{c}^{uD} - \mathbf{c}^{\eta, T} \underline{\mathbf{T}} \mathbf{c}^{uD} - \eta \mathbf{D} \mathbf{c}^{uD} + \mathbf{P} \mathbf{c}^p + \Gamma (\mathbf{B} \mathbf{c}^{uD} - |\mathbf{u}_{D, in}| \mathbf{S}_r^{BD}) - \sum_{z=1}^Z (|\mathbf{F}_{p,z}| \mathbf{S}_{p,z} - \mathbf{S}_{fr,z} \mathbf{c}_z^{Ffr}) - \rho \beta_e (\mathbf{A} \mathbf{c}^T - T_{ref} \mathbf{S}_T) = 0, \quad (16)$$

$$\rho \mathbf{G} \mathbf{c}^{uD} = 0 \quad (17)$$

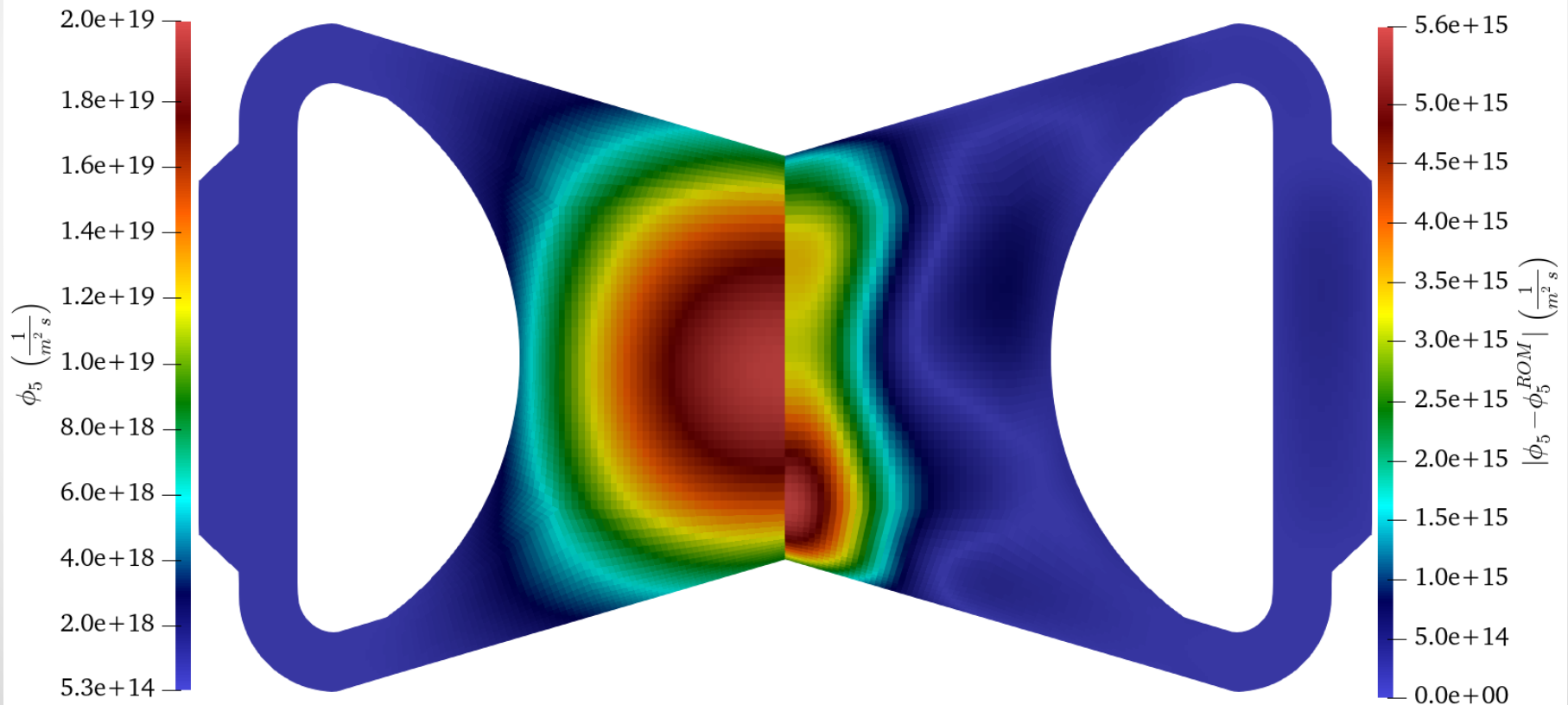
Some of the reduced operators

$$\begin{aligned} \mathbf{M}_{i,j} &= \langle \psi_i^{uD}, \psi_j^{uD} \rangle_{\mathcal{D}} & \underline{\mathbf{C}}_{i,j,k} &= \left\langle \psi_j^{uD}, \frac{1}{\gamma} \nabla \cdot (\psi_i^{uD} \otimes \psi_k^{uD}) \right\rangle_{\mathcal{D}} \\ \mathbf{D}_{i,j} &= \langle \psi_i^{uD}, \nabla \cdot [\nabla \psi_j^{uD} + (\nabla \psi_j^{uD})^T] \rangle_{\mathcal{D}} & \mathbf{P}_{i,j} &= \langle \psi_i^{uD}, \gamma \nabla \psi_j^p \rangle_{\mathcal{D}} \\ \mathbf{B}_{i,j} &= \langle \psi_i^{uD}, \psi_j^{uD} \rangle_{\Gamma_{in}} & \mathbf{S}_{p,z,i} &= \left\langle \psi_i^{uD}, \gamma \frac{\delta_z(r) \mathbf{F}_{p,z}}{|\mathbf{F}_{p,z}|} \right\rangle_{\mathcal{D}} \\ \mathbf{S}_{r,i}^{BD} &= \left\langle \psi_i^{uD}, \frac{\mathbf{u}_{in}}{|\mathbf{u}_{in}|} \right\rangle_{\Gamma_{in}} & \mathbf{G}_{i,j} &= \langle \psi_i^p, \nabla \cdot \psi_j^{uD} \rangle_{\mathcal{D}} \end{aligned}$$

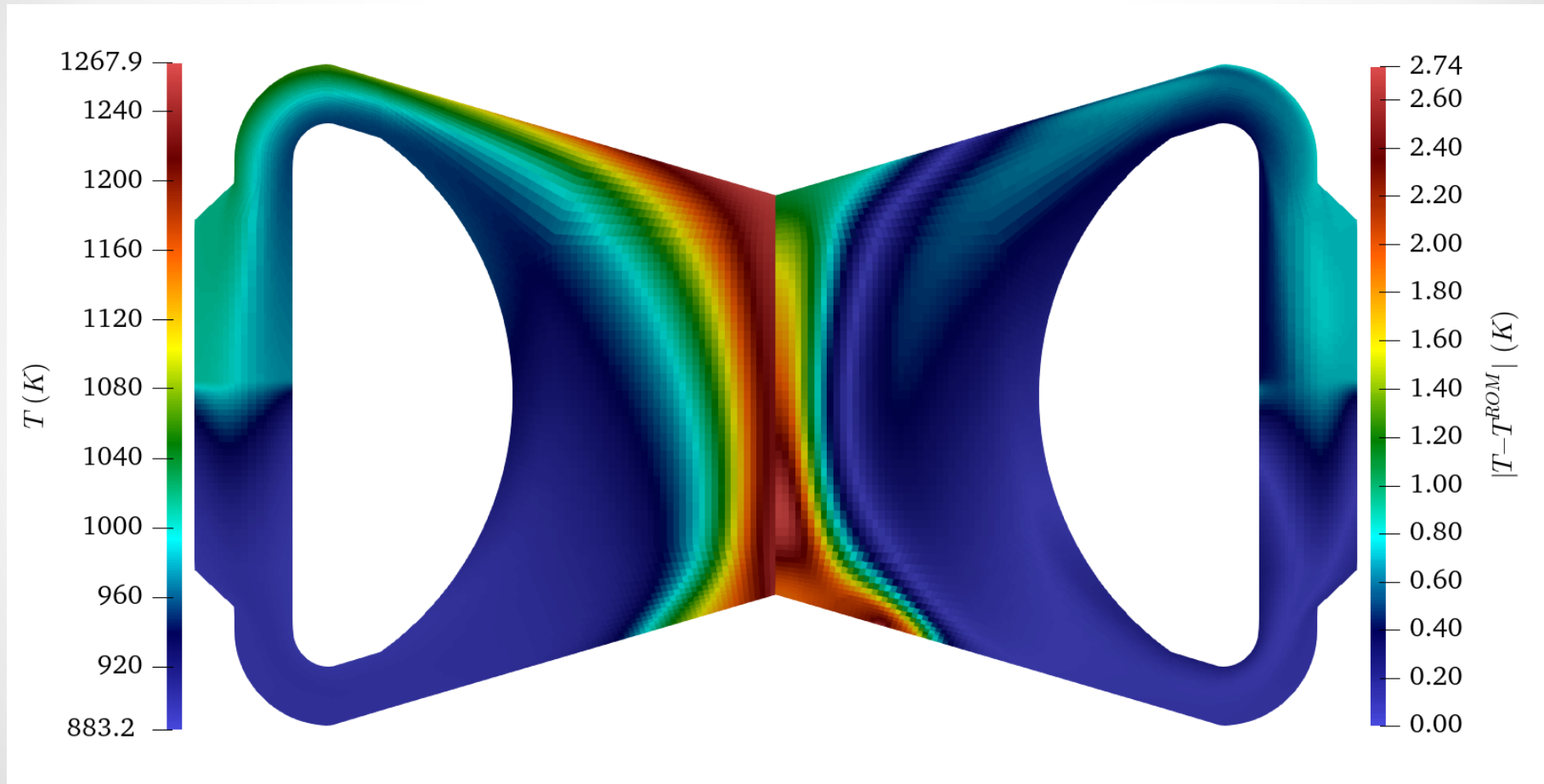
Reconstructed Flux (left) - Reconstruction Error (right)

Uncertain parameters (23 total):

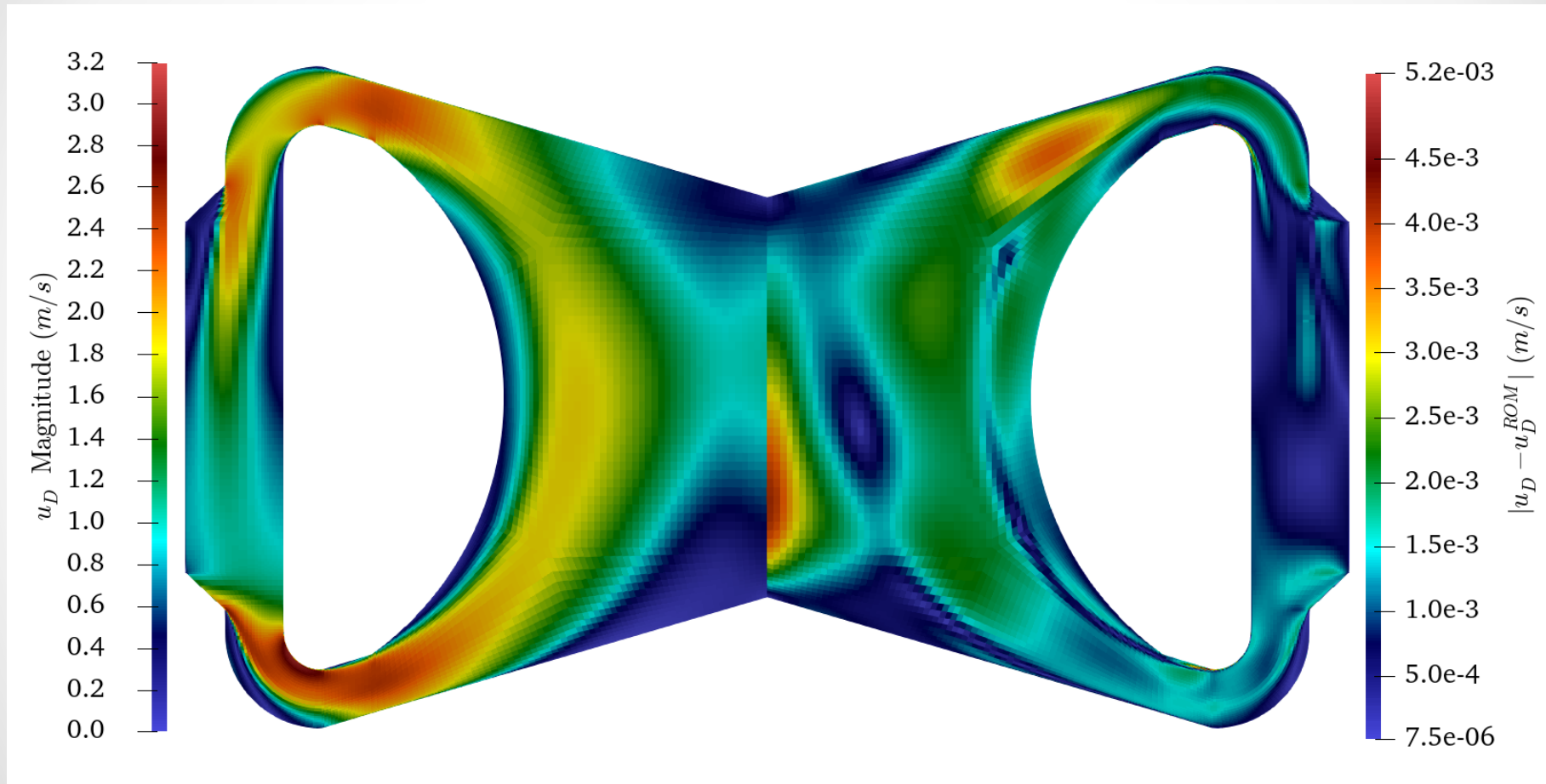
- Diffusion coefficients, fission and removal cross sections ($\pm 10\%$ around the nominal values)
- Pumping force, external coolant temperature, Heat transfer coefficient, Pr-number, thermal expansion coefficient



Reconstr. Temperature (left) – Reconstr. Error (right)

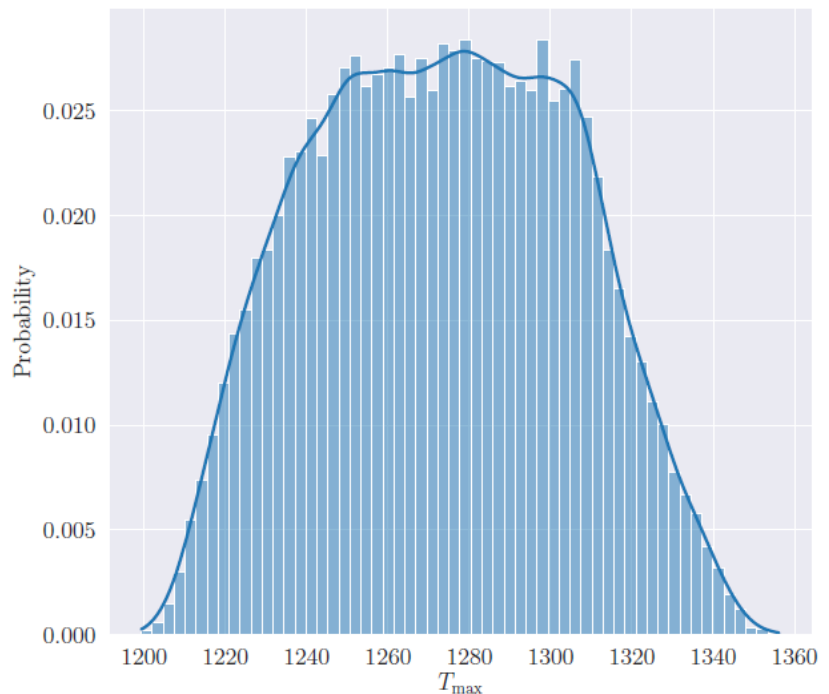
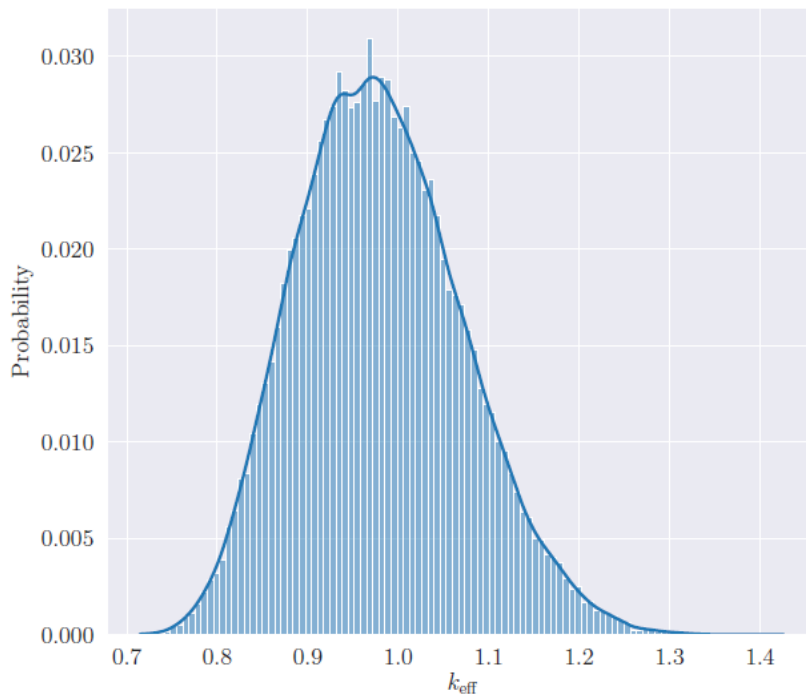


Reconst. Velocity (left) - Reconstruction Error (right)

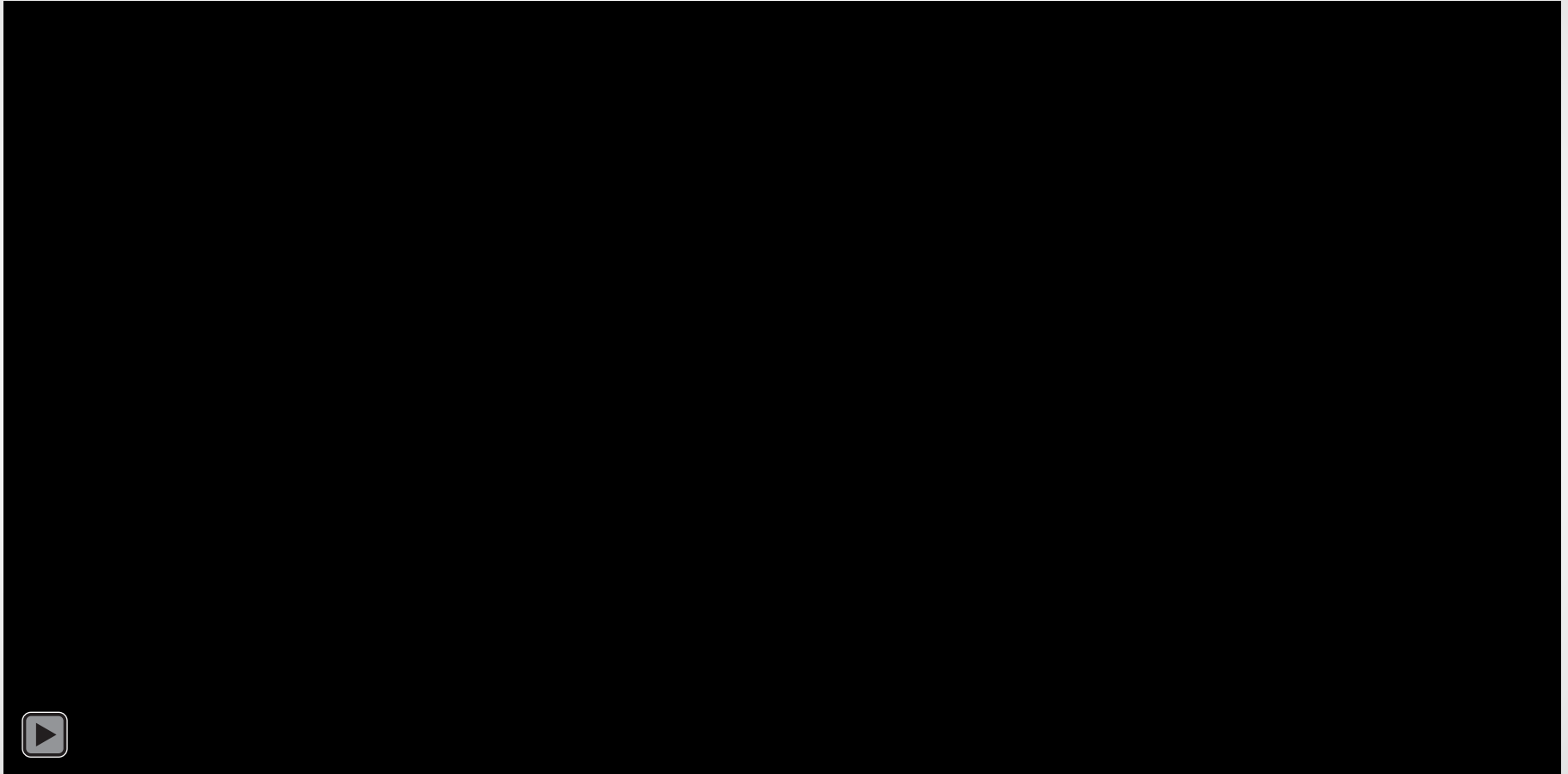


Model-order Reduction: huge speed ups

- Quantities of interest:
 - Effective multiplication factor (k_{eff})
 - Maximum temperature of the system (T_{max})
- Propagation of uncertainties: Monte Carlo approach with 50,000 samples
- **Speedup** in the UQ including training: approximately factor of **1,500**



Graphical User Interface Demo



Conclusions and EOF



- Intro to HPC for scientific computing in nuclear engineering and sciences
- Focus SC/HPC efforts where gains are visible/tangible
- Emphasize Predictive Science (VVUQ) and whether the simulation efforts will have an impact?
- Seek certifiable reduced-order models for quick design cycle
 - Borrow from machine-learning and big-data science.

