

Bayesian probabilistic data analysis platform

R&D on HL-2A

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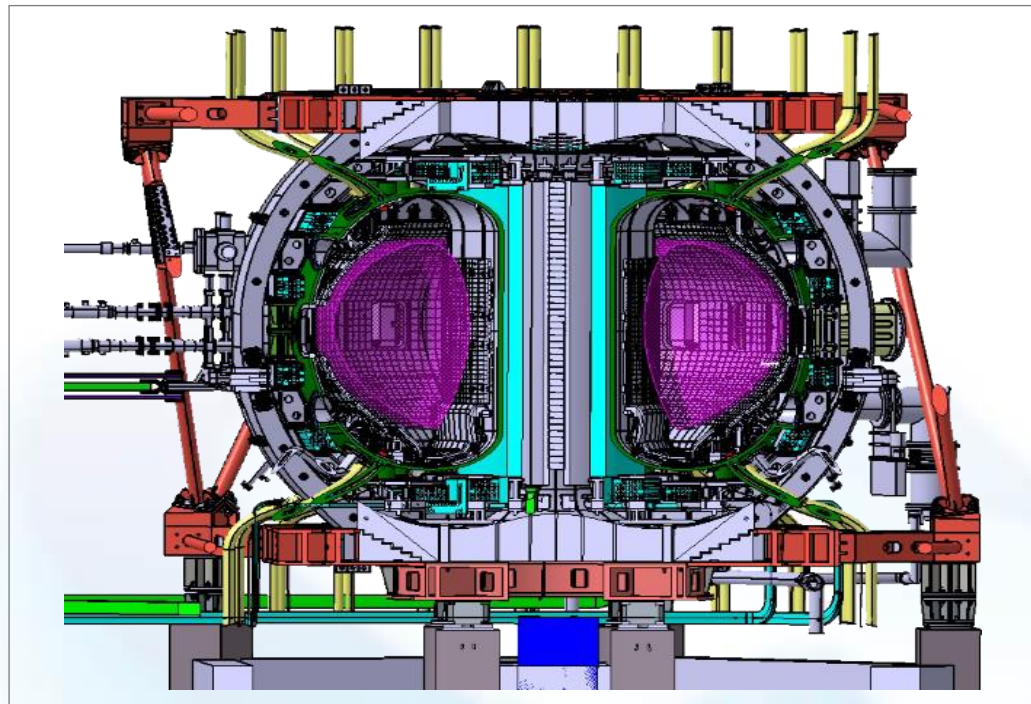
- **Motivation: HL-2A/2M experimental data analysis requirement**
- **Recent progress of HL-2A Bayesian probabilistic data analysis**
 - RETINA system
 - Plasma profiles inference & integrated data analysis
 - Tomography by using Soft X-ray / Bolometer / Magnetic coils
- **Summary**



Motivation

HL-2A/2M experimental **data analysis** requirement





Ion temperature
>150M Degree



Plasma current
6 times to HL-2A



Plasma volume
3 times to HL-2A



H&D power
2.5 times to HL-2A

| Parameters | HL-2A | HL-2M |
|-----------------------------|-----------------|-----------------|
| Major Radius, R | 1.65m | 1.78m |
| Minor Radius, a | 0.4m | 0.65m |
| Aspect ratio | 4.1 | 2.8 |
| Plasma current, I_p | 0.45MA | 2.5~3MA |
| Toroidal magnetic field, Bt | 2.8T | 2.2~3T |
| Triangularity, δ | <0.5 (DN) | >0.5 (DN) |
| Elongation, κ | <1.3 (DN) | 2 (DN) |
| Auxiliary heating power | >10MW | >25MW |



HL-2A has more than 30 physics diagnostics with different spatial-temporal resolution.

Conventional (individual) IDA (probabilistic combination)

Disadvantages:

- × (self-) consistent results?
- × error propagation
- × loss of information about the physics interdependency
- × often backward inversion techniques

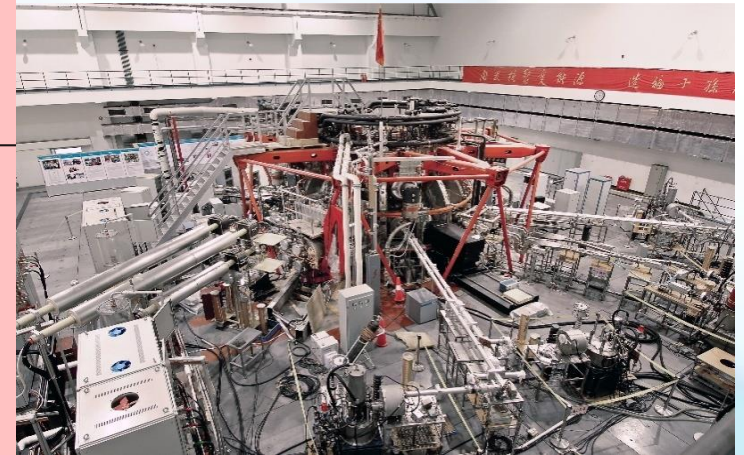
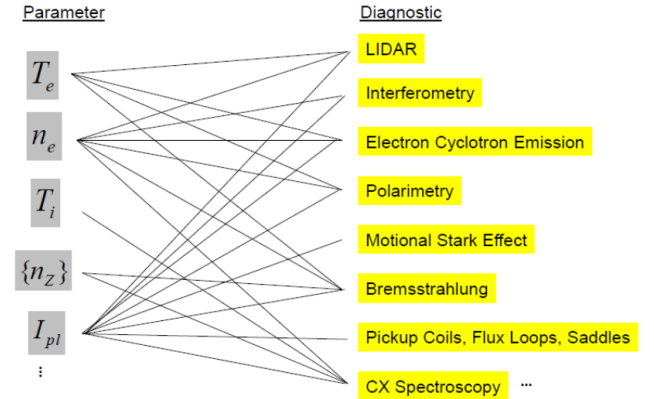
Advantages:

- ✓ avoids error propagation
- ✓ uses only forward modeling
- ✓ can easily integrate additional physical information and improve results
- ✓ result: probability distribution of parameters of interest

The Goal of IDA:

- **replace** combination of results from individual analysis
- **with** combination of measured data from heterogeneous diagnostics (one-step analysis of pooled data) to improve results.

Dependencies




Recent progress of HL-2A Bayesian probabilistic data analysis



$$\underbrace{p(\text{profiles}|\text{diagnostics})}_{\text{posterior}} \sim \underbrace{p(\text{diagnostic}|\text{profiles})}_{\text{likelihood}} \cdot \underbrace{p(\text{profiles})}_{\text{prior}}$$

$p(\text{profiles}|\text{diagnostics}) \sim$

Individual diagnostic Forward models 

$$\begin{aligned}
 & p(\text{diagnostic No. 1}|\text{profile corresponding to diagnostic No. 1}) \\
 & \cdot p(\text{diagnostic No. 2}|\text{profile corresponding to diagnostic No. 1}) \\
 & \cdot p(\text{diagnostic No. 3}|\text{profile corresponding to diagnostic No. 3}) \\
 & \cdot p(\text{diagnostic No. 4}|\text{profile corresponding to diagnostic No. 4}) \dots \\
 & \cdot p(\text{profiles})
 \end{aligned}$$

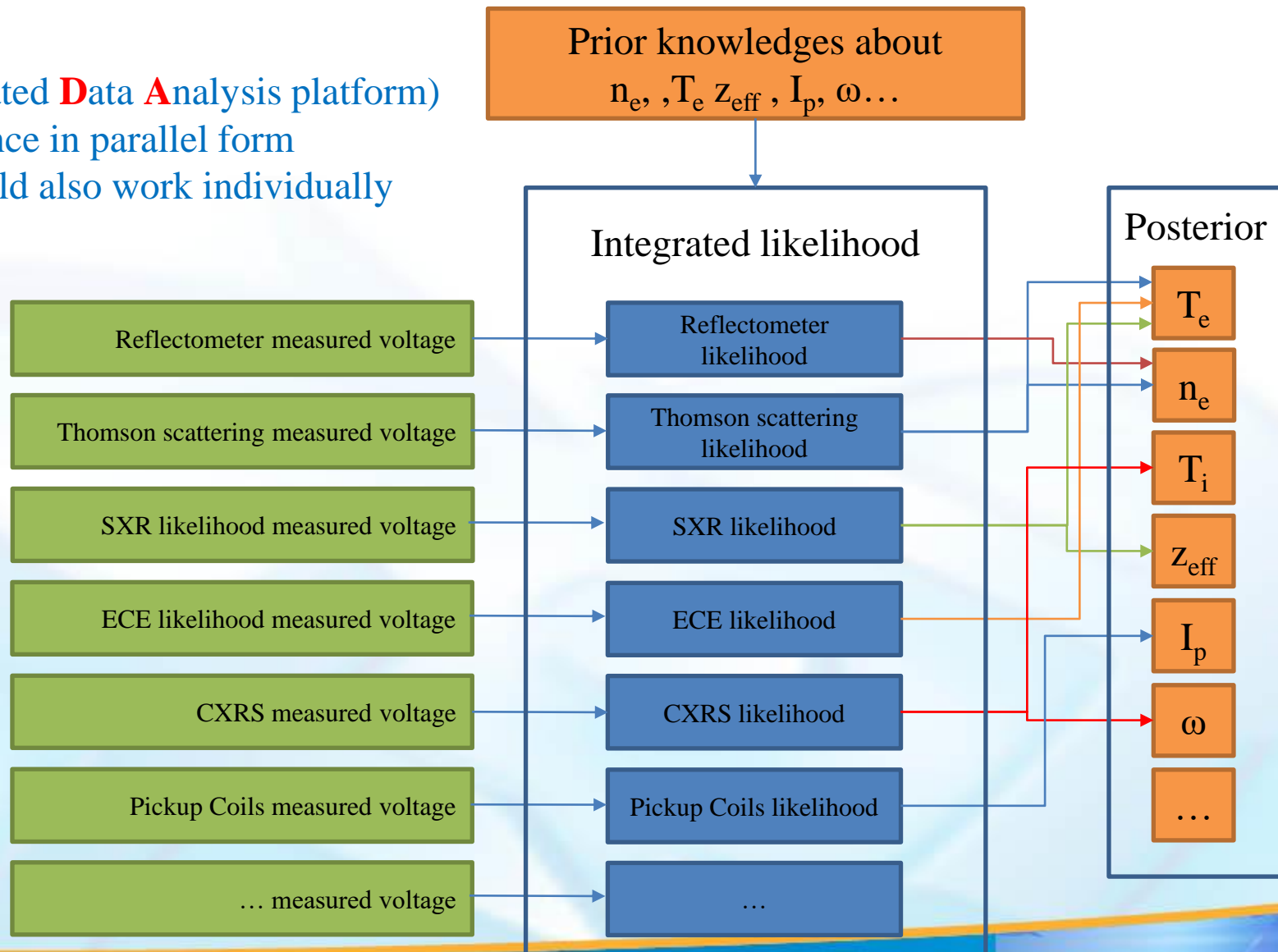
$$\begin{aligned}
 p(\bar{n}_e, \bar{T}_e, \bar{T}_i, \bar{\omega} \dots | \bar{d}_{ECE}, \bar{d}_{TS}, \bar{d}_{CXRS} \dots) & \sim p(\bar{d}_{ECE}, \bar{d}_{TS}, \bar{d}_{CXRS} \dots | \bar{n}_e, \bar{T}_e, \bar{T}_i, \bar{\omega} \dots) \cdot p(\bar{n}_e, \bar{T}_e, \bar{T}_i, \bar{\omega} \dots) \\
 & \sim p(\bar{d}_{ECE} | \bar{T}_e) \\
 & \cdot p(\bar{d}_{TS} | \bar{T}_e, \bar{n}_e) \\
 & \cdot p(\bar{d}_{CXRS} | \bar{T}_i, \bar{\omega}) \dots \\
 & \cdot p(\bar{n}_e) \cdot p(\bar{T}_e) \cdot p(\bar{T}_i) \cdot p(\bar{\omega}) \dots
 \end{aligned}$$



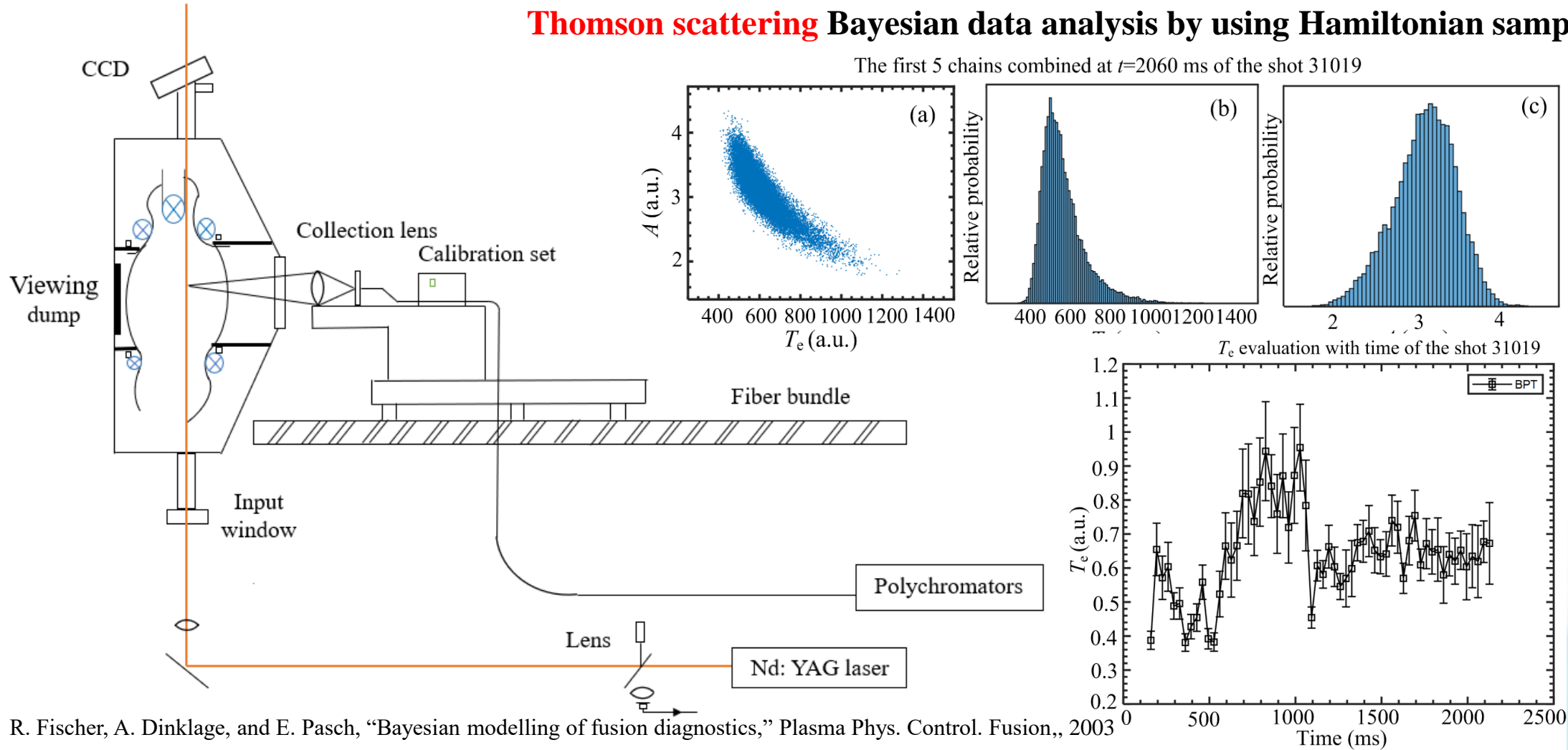
RETINA for HL-2A

(Recognitive **I**ntegrated **D**ata **A**nalysis platform)

- Integrated inference in parallel form
- Sub-modules could also work individually



Thomson scattering Bayesian data analysis by using Hamiltonian sampling



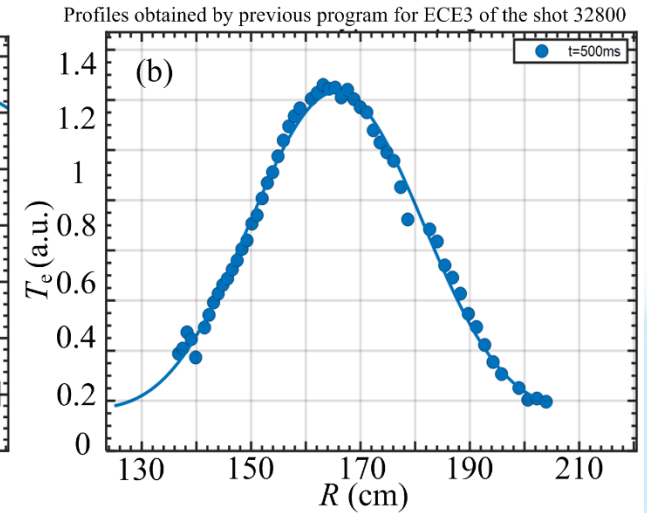
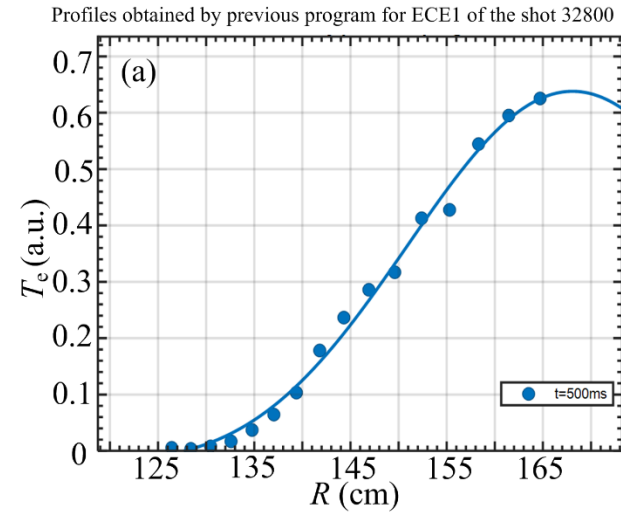
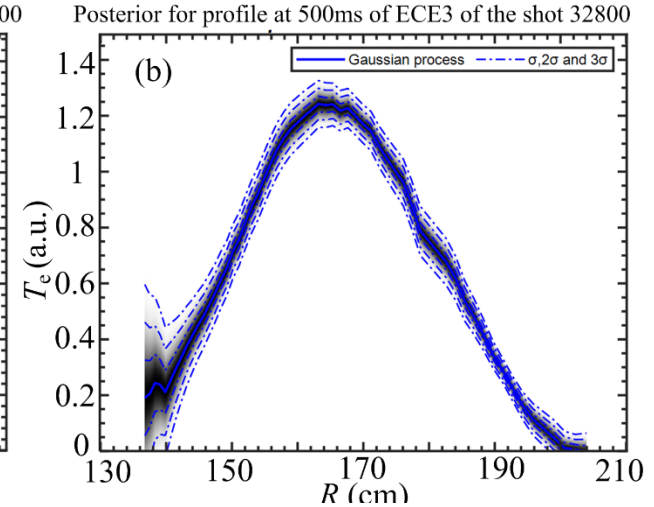
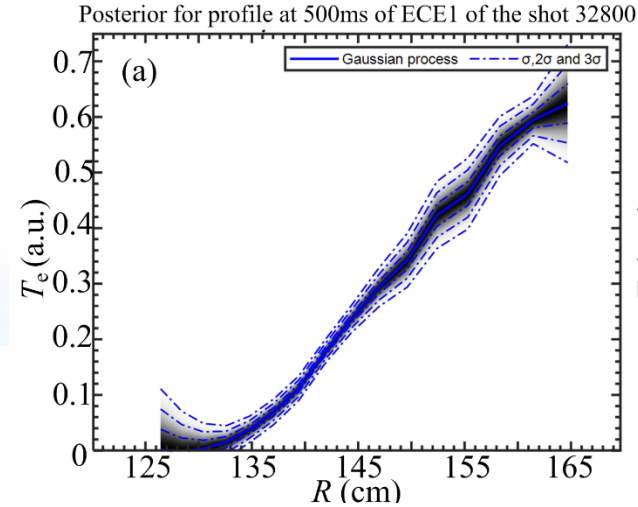
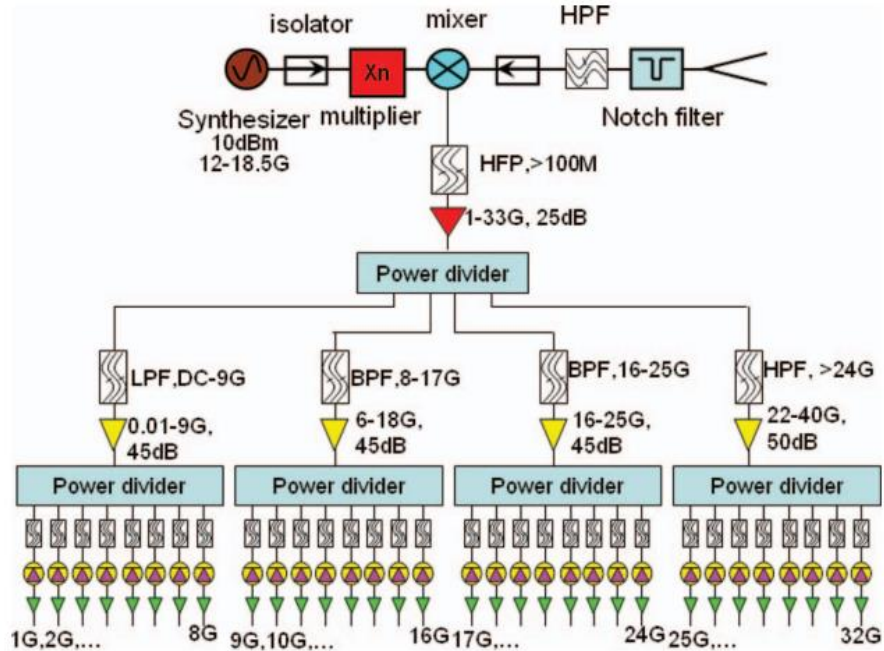
R. Fischer, A. Dinklage, and E. Pasch, "Bayesian modelling of fusion diagnostics," Plasma Phys. Control. Fusion., 2003

Wenan Pan, Tianbo Wang*, Zhibin Wang, Yonghao Yang, Hao Wu, Zengchen Yang, Chunhua Liu, Bingli Li, Zijie Liu, Wenbin Wu, Min Xu,

Integrated Data Analysis on the Electron Temperature profile of HL-2A with Machine Learning Method, submitted to Plasma Science and Technology.



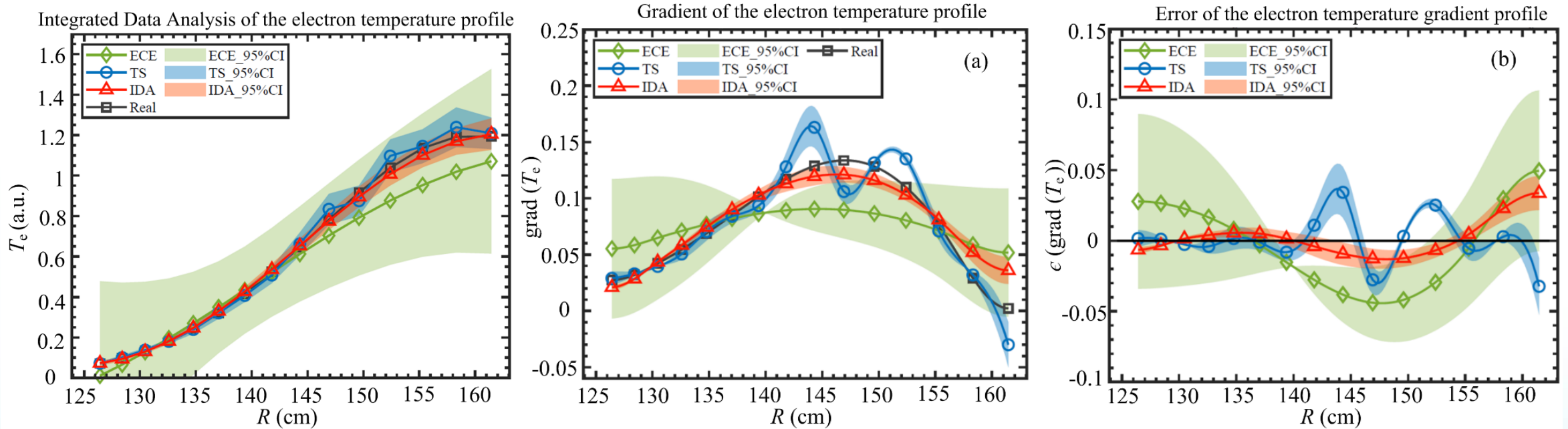
Electron Cyclotron Emission Bayesian data analysis on HL-2A



Bayesian

Conventional

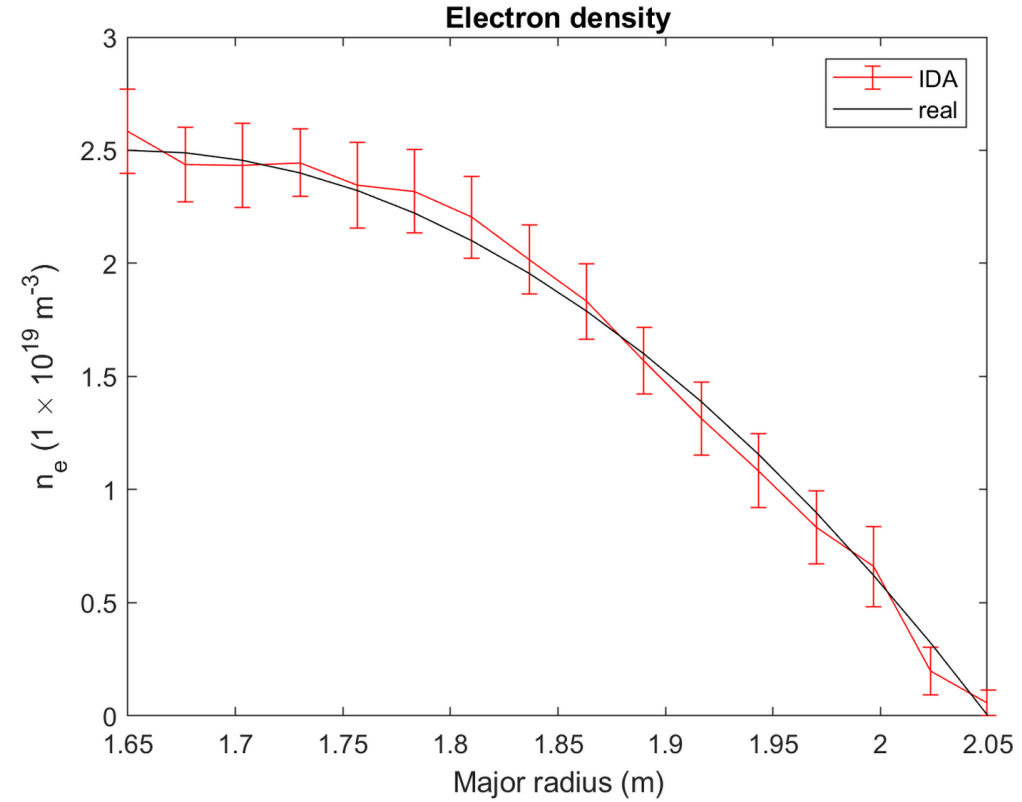
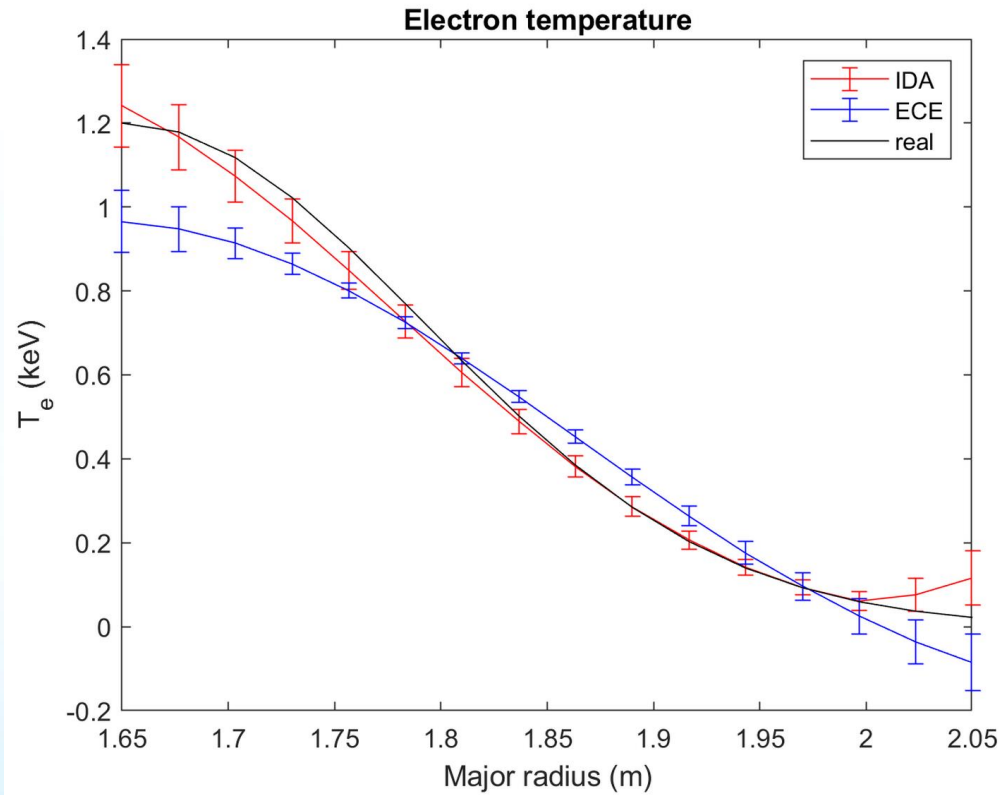
Electron temperature profile integrated data analysis by using ECE & TS



Wenan Pan, Tianbo Wang*, Zhibin Wang, Yonghao Yang, Hao Wu, Zengchen Yang, Chunhua Liu, Bingli Li, Zijie Liu, Wenbin Wu, Min Xu, Integrated Data Analysis on the Electron Temperature profile of HL-2A with Machine Learning Method, submitted to Plasma Science and Technology.

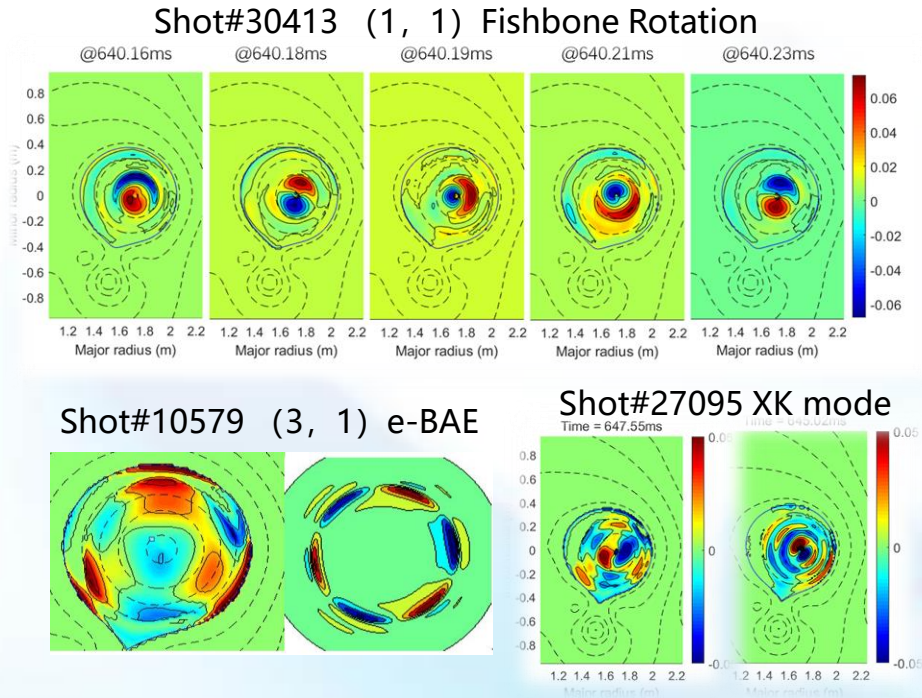


Electron temperature & density profiles integrated data analysis by using ECE & TS & Reflectometry
More difficult than single profile inference, and the prior selection plays an important role.
The work is still on going with optimization.



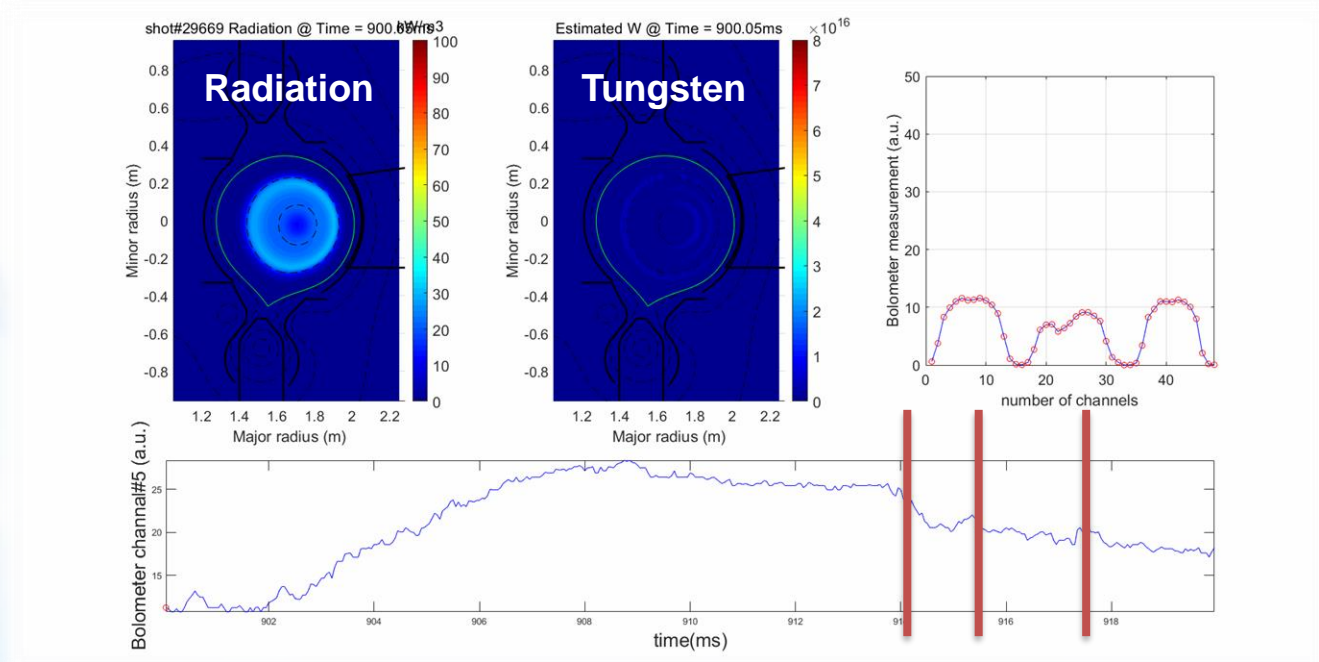
SXR tomography for MHD structure analysis

Bolometer tomography for tungsten monitoring with cooling factor



Yu Liming, Chen Wei, Shi Zhongbing, Wang Tianbo et al., Experimental observation of low-frequency magnetohydrodynamic instabilities driven by energetic electrons in low hybrid current drive plasmas, Nucl. Fusion, 2021, 61

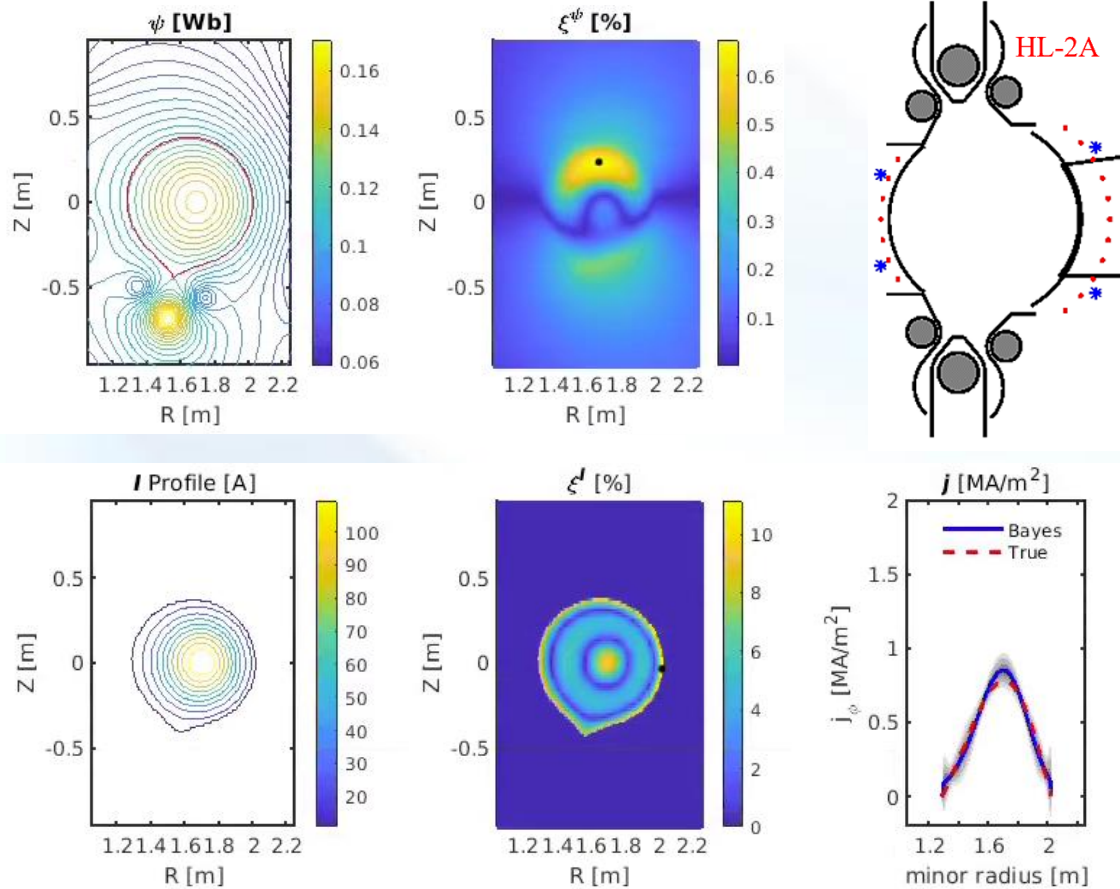
X X He et al., The ITB dynamics controlled by internal kink modes on HL-2A tokamak, Plasma Phys. Control. Fusion 64 (2022) 015007 (11pp)



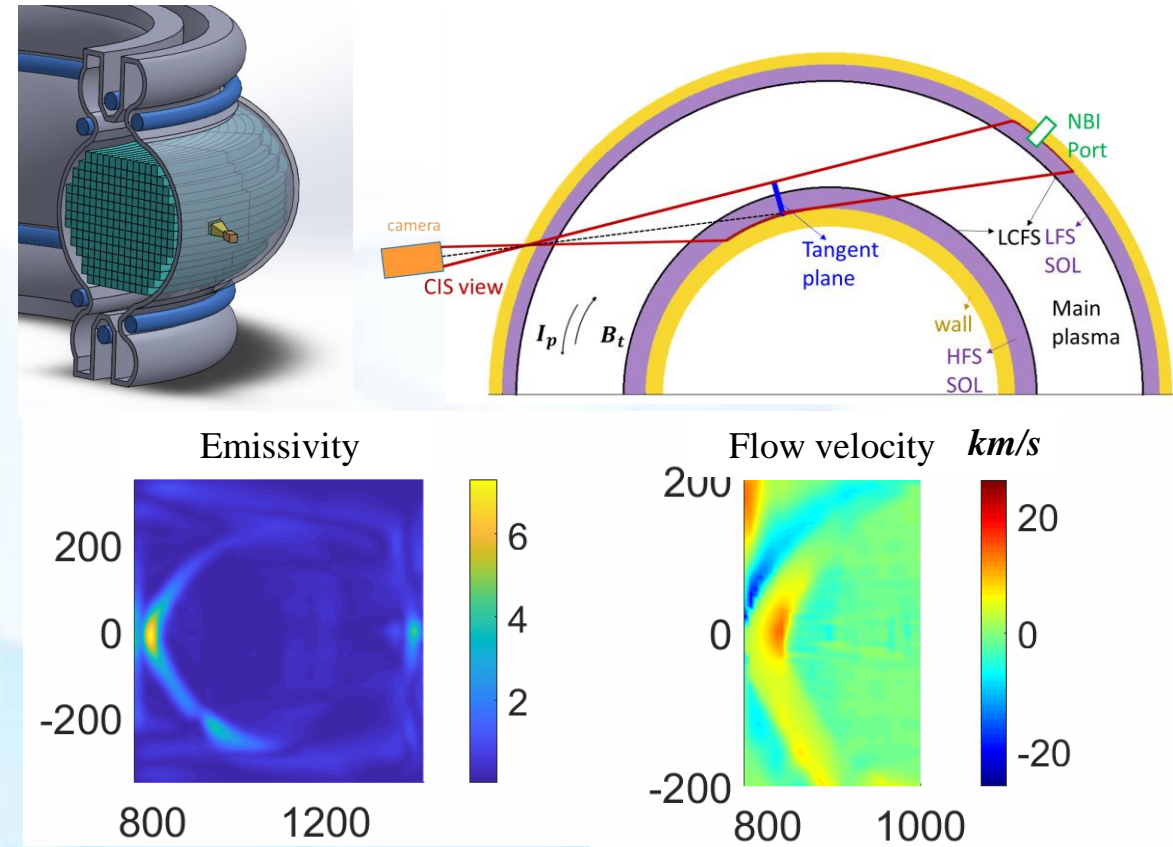
Tianbo Wang et al., Monitoring of two-dimensional tungsten concentration profiles on the HL-2A tokamak, under revision.



Magnetic flux & plasma current reconstruction by using pick-ups, flux & Rogowski loops on HL-2A



Magnetic flux & plasma current reconstruction by using Doppler coherence imaging spectroscopy (CIS) on HL-2A



Zijie Liu, Zhengping Luo*, Tianbo Wang* et al., Plasma current profile reconstruction for EAST based on Bayesian inference, Fusion Engineering and Design, 2021, 172

Li Bingli, Wang Tianbo* et al., Tomography of emissivity for Doppler coherence imaging spectroscopy diagnostic on HL-2A, Fusion Science and Technology 2021.

RETINA **available** modules on HL-2A:

Thomson scattering
ECE
Reflectometry
SXR
Bolometer
Passive visible spectroscopy
Magnetic diagnostics

RETINA **available** functions:

T_e profile
 n_e profile
 z_{eff} profile
SXR tomography
Bolometer tomography
Plasma current & magnetic flux reconstruction

RETINA **ongoing** modules on HL-2A:

Laser interferometry
CXRS
VUV

RETINA **ongoing** functions:

T_i profile
 ω profile
Multi-species/impurity profile by using cooling factors

Current technical challenge:

- The current sampling method (Hamiltonian Monte Carlo) is **computational expensive** and have to frequently deal with **convergence issue**.
- Since the RETINA is working on IDA in parallel structure, the parameter scale is very large. IDA in series structure or hybrid structure might be a potential option?



Summary



- The **Bayesian data analysis** has been applied on considerable number of diagnostics on HL-2A, and has doubtless delivered its value on experimental data analysis, especially on tomography applications.
- A set of individual Bayesian modules are being put together as a integrated data analysis platform, namely **RETINA**. This project is still ongoing in SWIP, aiming on inferences of basic experimental profiles of HL-2A, both for fresh experimental data and historical data base.
- A standardized data analysis platform could naturally deliver the desirable **data standard** on accuracy & consistency & uncertainty, which is extremely important for physics study.
- Giving a good data analysis standard is much more easier and cost-effective than historical data repairment.



Thank you!

