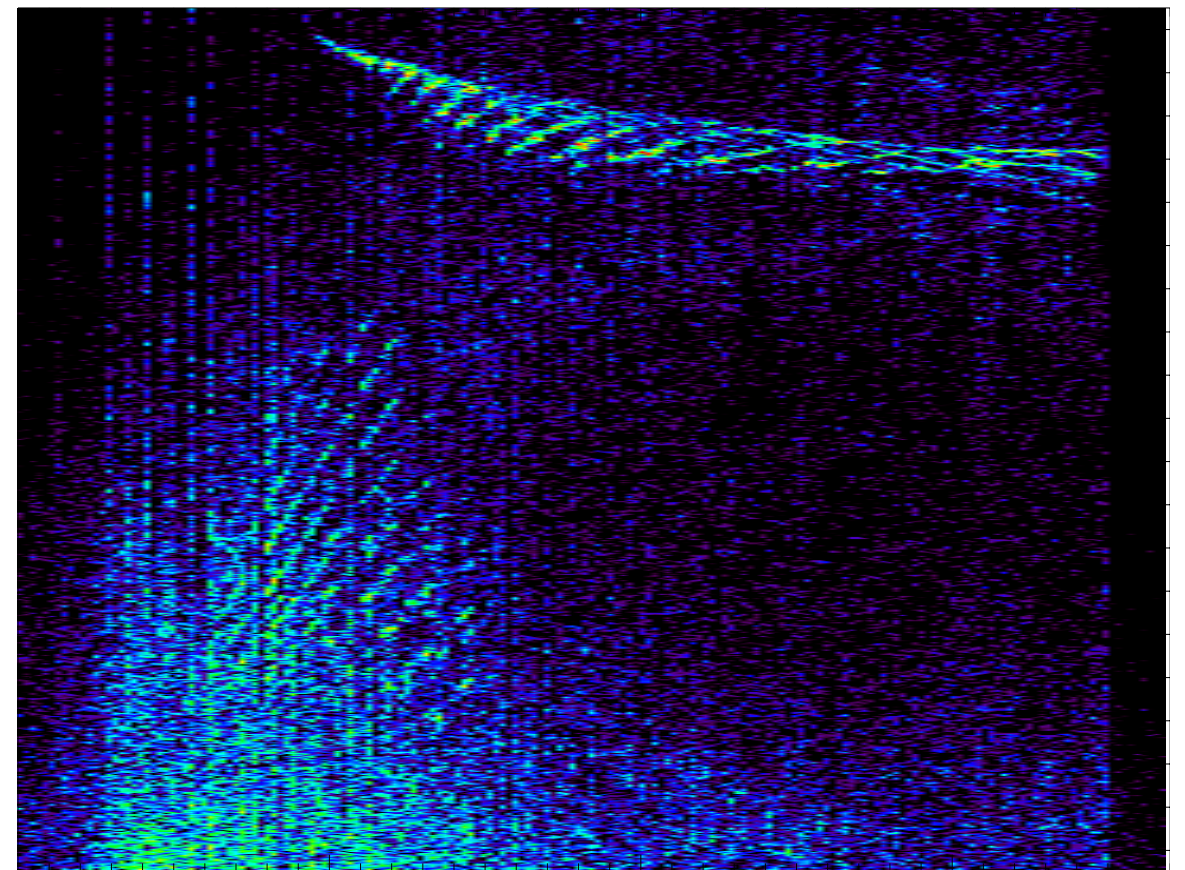


Observation and interpretation of tornado modes coupled to near-axis Alfvén cascade eigenmodes in JET sawtoothing plasmas

R. Calado, F. Nabais,
S. Sharapov, J.P. Bizarro

GTM meeting

28/05/2021

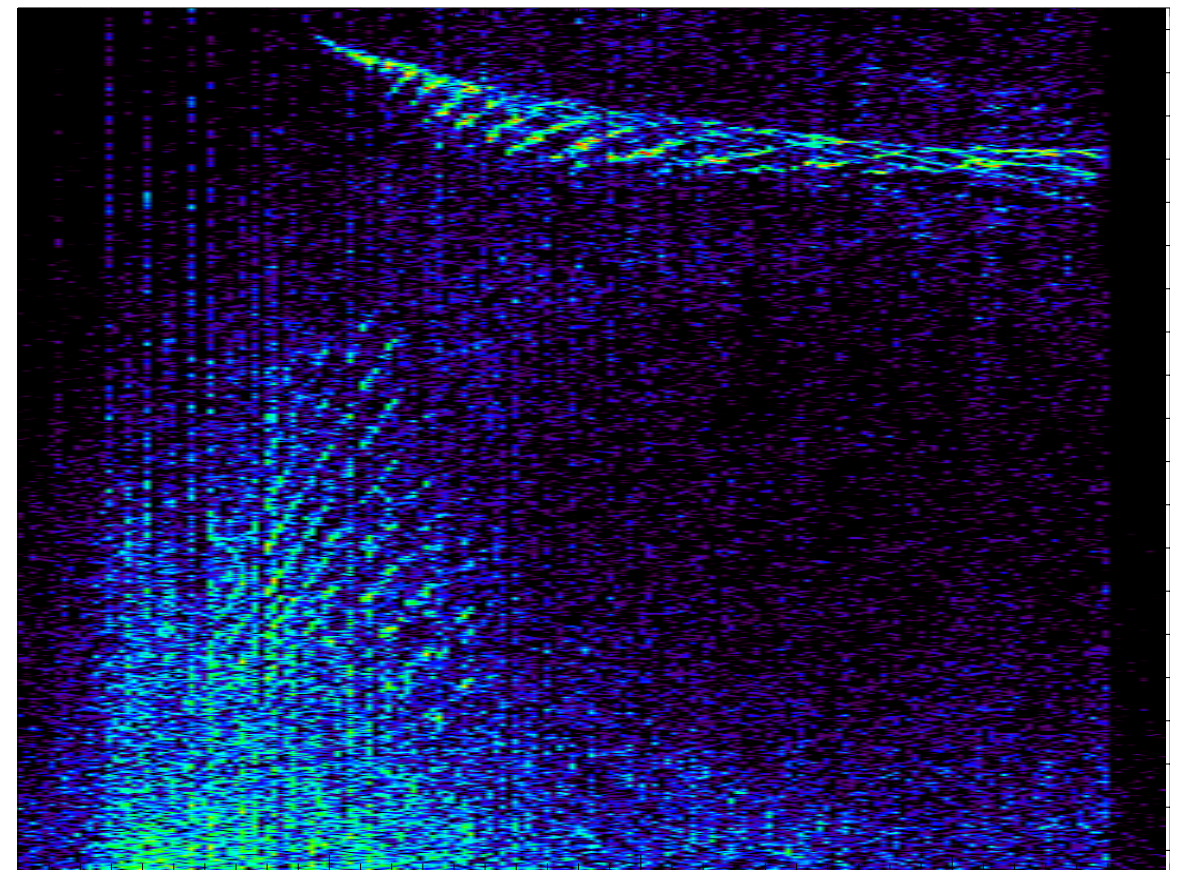


Observation and interpretation of tornado modes coupled to near-axis Alfvén cascade eigenmodes in JET sawtoothed plasmas

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Motivation

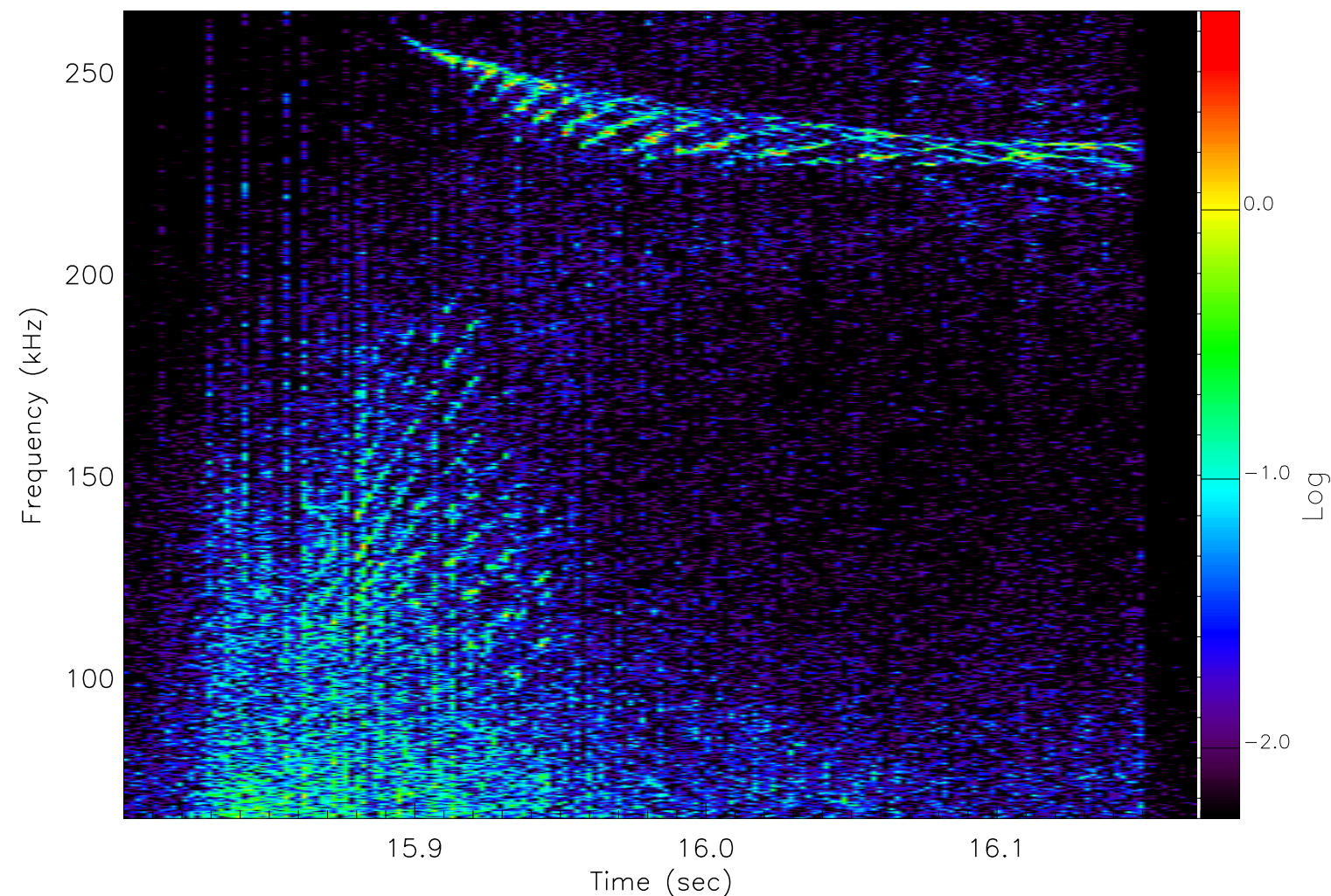
Two types of modes seemingly coupled:

- Upward frequency sweeping modes in the range 100-200 kHz
- Modes within the frequency range 225-250 kHz with some frequency modulation

1st type resembles Alfvén
Cascades (ACs)

2nd type was previously identified
as tornado modes*

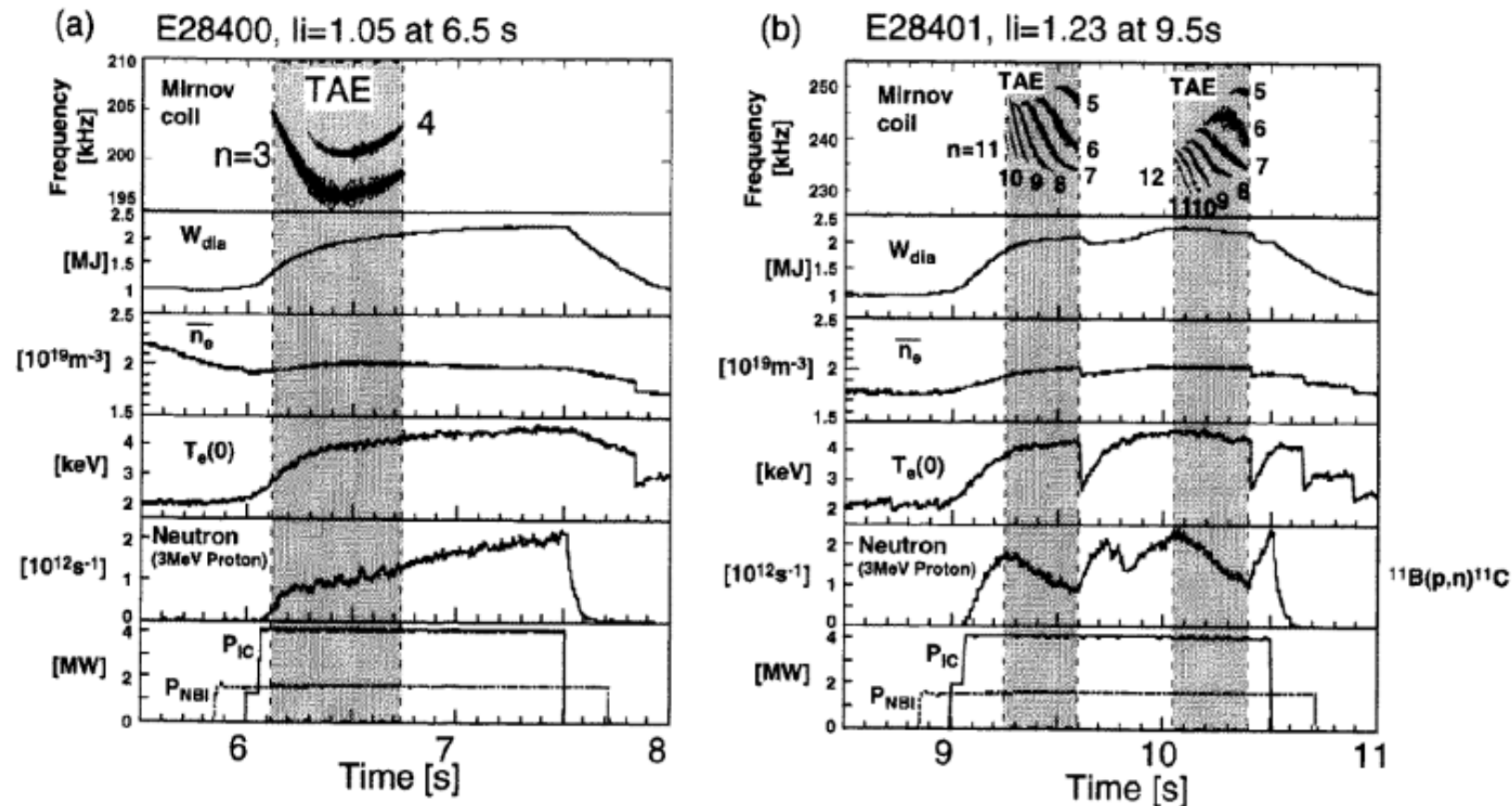
Applicability to MHD spectroscopy
of post-sawtooth dynamics?



*P. Sandquist, S. E. Sharapov, M. Lisak, T. Johnson, Phys. of Plasmas 14, 122506 (2007)

Tornado Modes Preceding Sawtooth Crashes

First reported by the JT-60U Team¹



Called “Tornado” because of non-Alfvénic frequency sweeping (not $\sim B/\rho^{1/2}$)

Identified as TAE inside the $q=1$ radius, with the “twist” frequency caused by the proximity to magnetic axis²

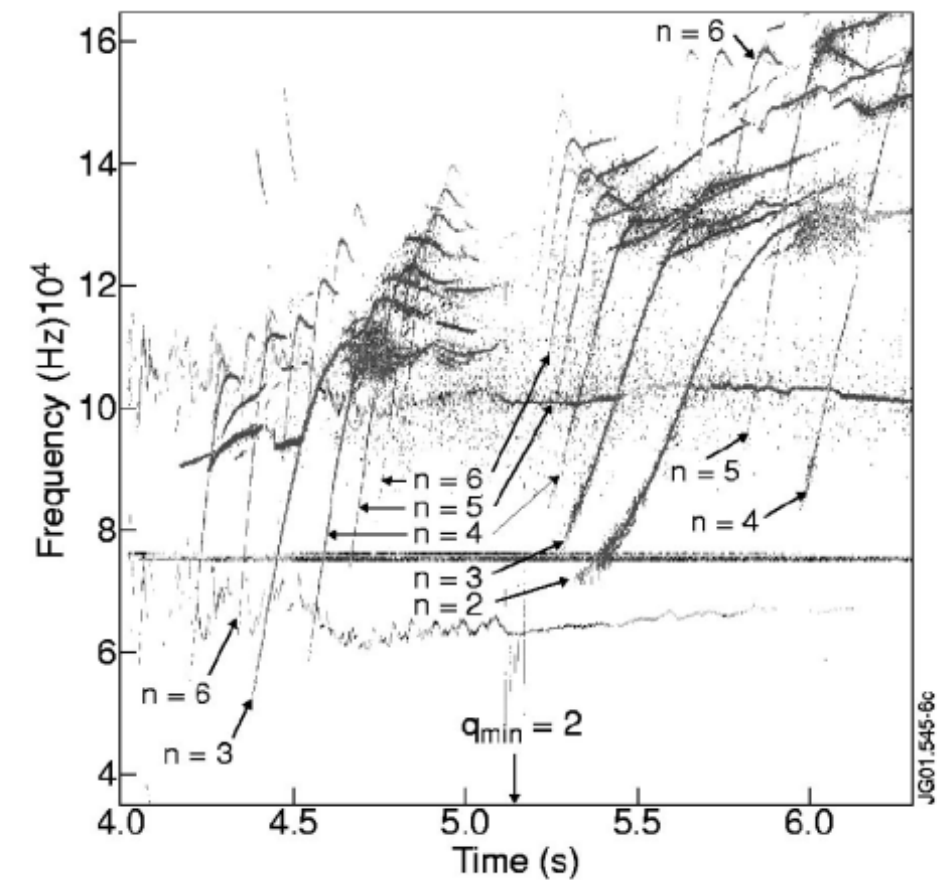
¹M.Saigusa et al., PPCF 40 (1998) 1647

²G.Kramer, S.Sharapov et al., Phys. Rev. Lett. 87 92 (2004) 015001

The “Alfvén Cascade” Modes in Reversed Shear Discharges

First observed in JT-60U negative shear plasmas¹

Observed then in JET, DIII-D, ASDEX-Upgrade, C-MOD, MAST, NSTX, TCV...



Interpreted as Eigenmodes residing at maximum points of Alfvén continuum caused by the zero magnetic shear^{2,3}

ACs are usually associated with non-monotonic $q(r)$ -profiles. However, the possibility of AC existence in plasmas with monotonic but very flat q -profiles was predicted in [B.Breizman et al., Phys. of Plasmas 10 (2003) 3549]

¹Y.Kusama et al., PPCF 38 (1998) 1215

²H.Berk et al., Phys. Rev. Lett. 87 (2001) 185002

³S.Sharapov et al., Phys. of Plasmas 9 (2002) 2027

Outline

Experimental conditions and observations

Identification of the modes

Numerical calculation of mode structure
and frequency

Energetic ion population drive

Resonances and orbits contributing to
mode drive along its evolution

Conclusion

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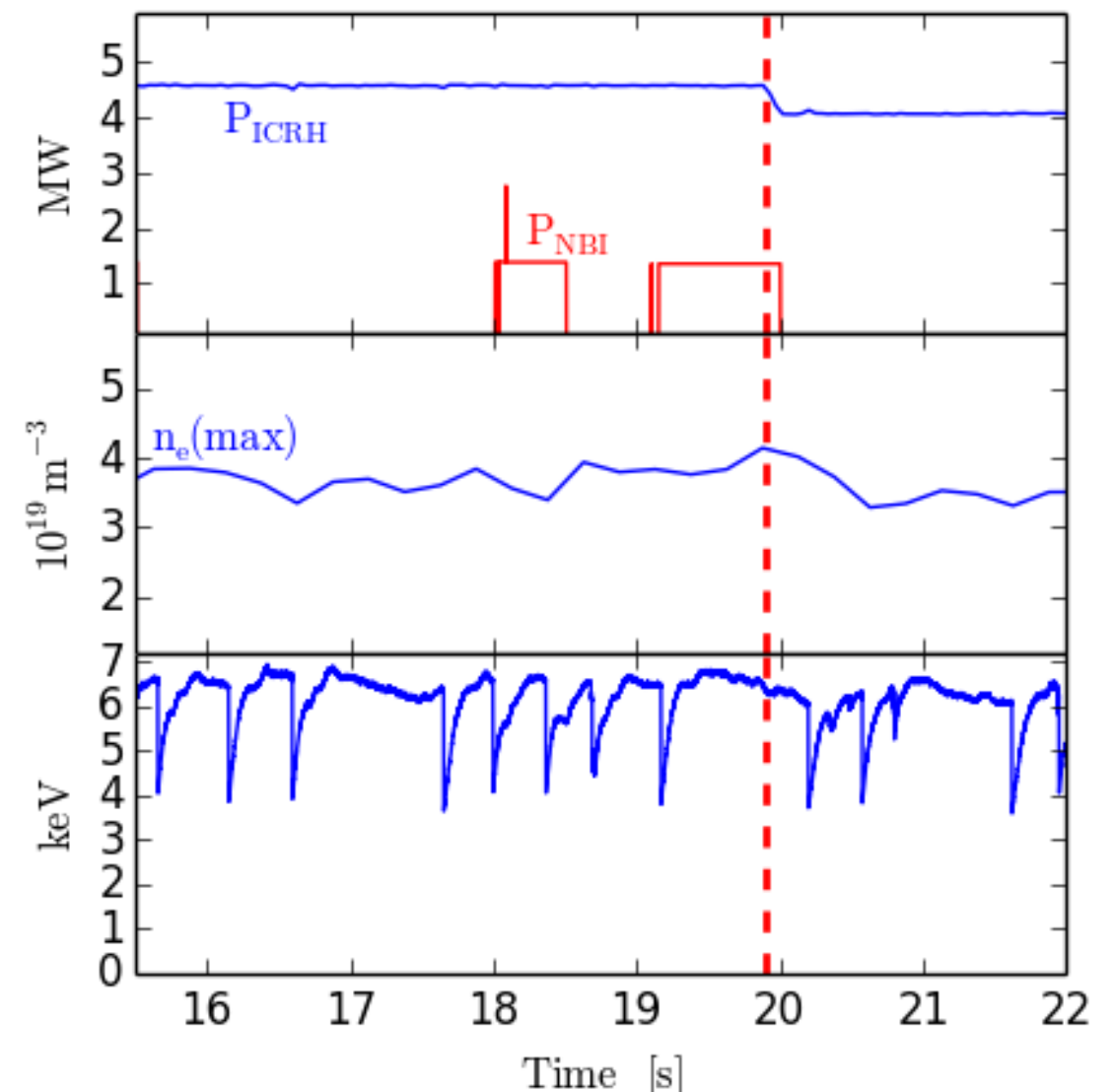
Conclusion

Experimental conditions

Auxiliary plasma heating was on-axis ICRH of hydrogen minority ($n_H/n_e=2.5\%$) with flat power waveform

Diagnostic NBI blips necessary for MSE measurements crucial for reconstruction of q-profile close to the axis

Density approximately constant; temperature evolution indicates sawtooth oscillation



JET machine parameters: 2.7 T magnetic field, 2 MA plasma current

Observation of near-axis coupled AC type and tornado modes

Tornado modes are TAEs and so they are associated with specific $q_{n,m}=(m-1/2)/n$

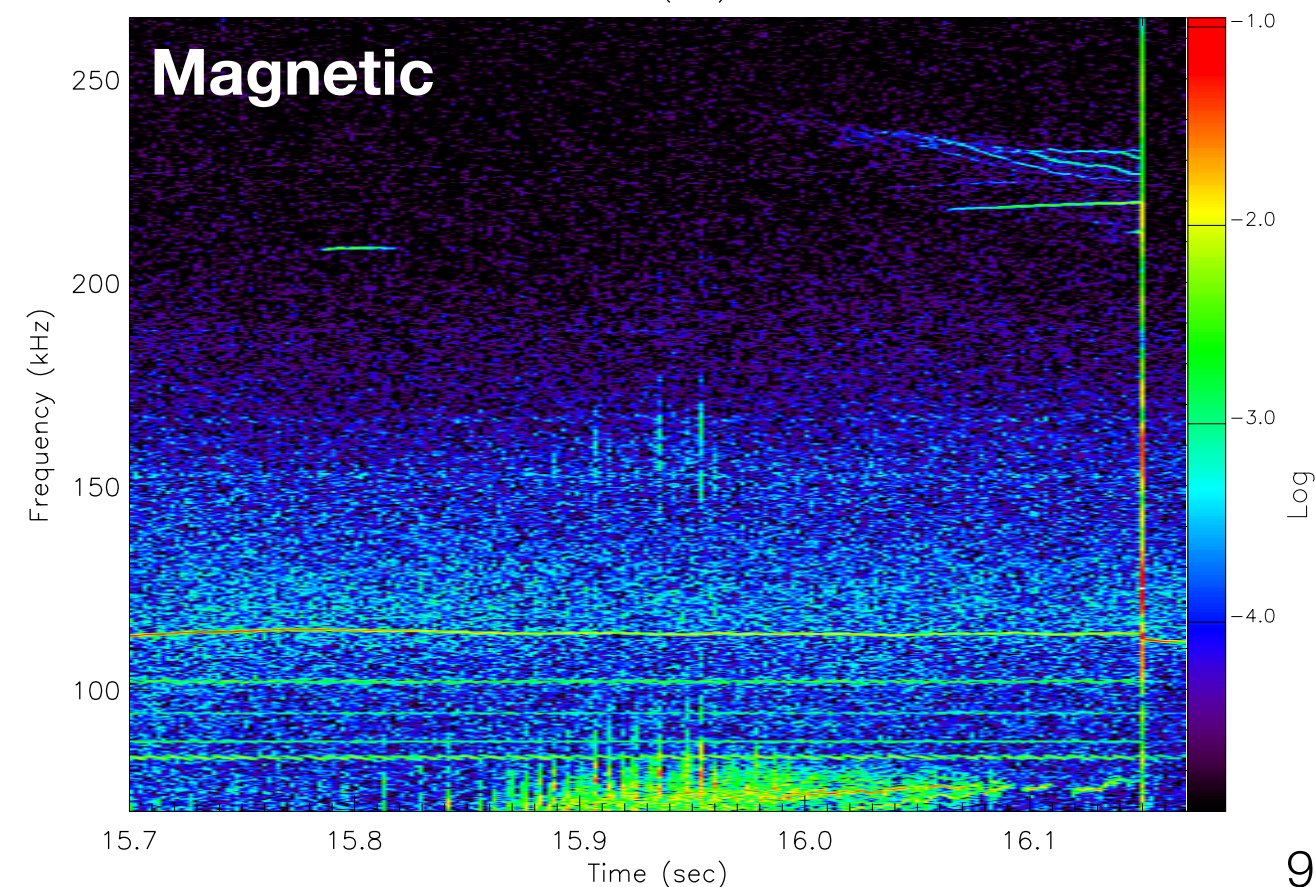
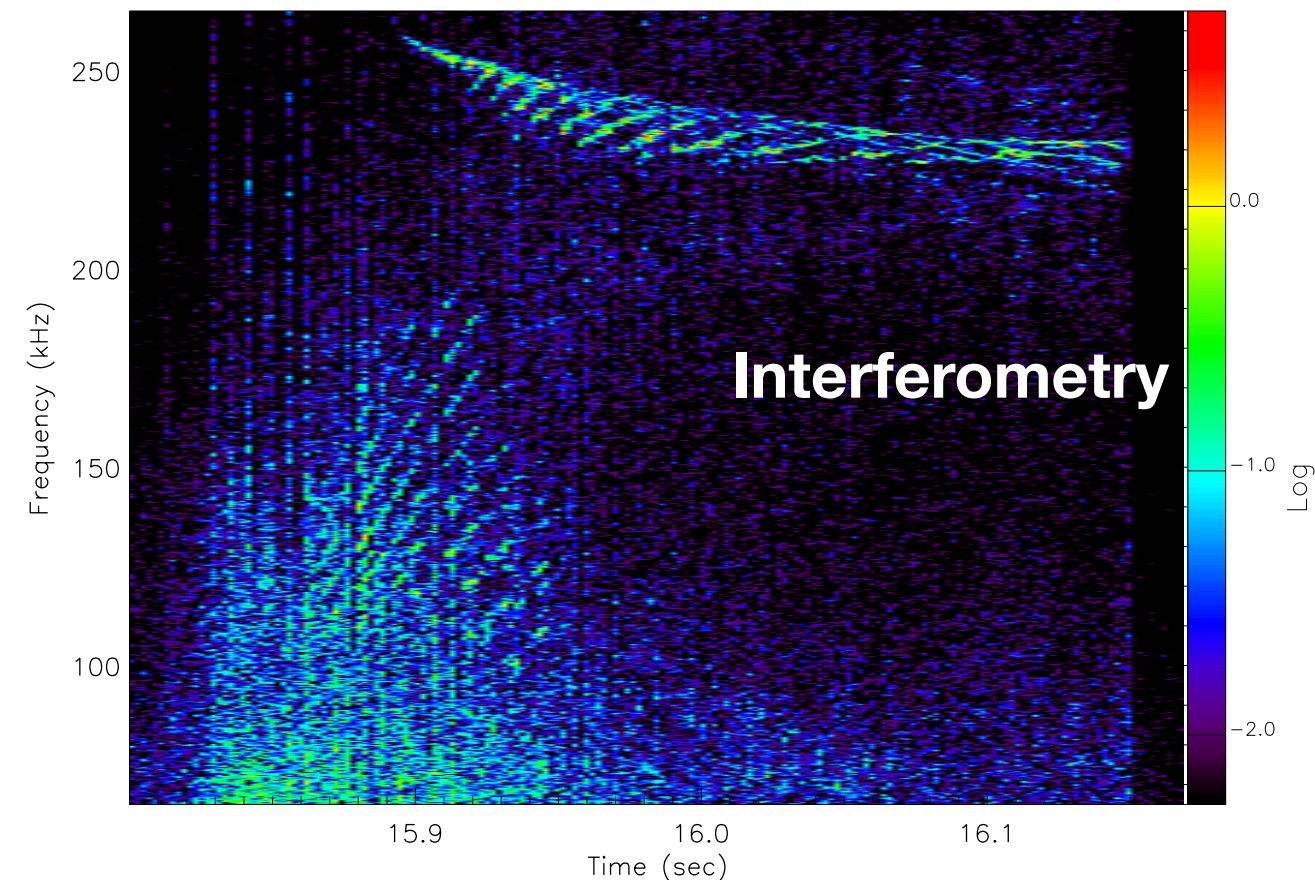
We are between sawteeth so q_0 is close to unity but gradually decreasing in time, and the modes have $m=n$

As the q -profile decreases q_0 crosses $q_n=(n-1/2)/n$ and the corresponding tornado mode is then allowed to exist, which explains why they appear one by one from high to low toroidal mode numbers

ACs and tornado modes are observed in interferometry diagnostics but not in magnetics which are peripheral



Modes very close to magnetic axis



Outline

Experimental conditions and observations

Identification of the modes

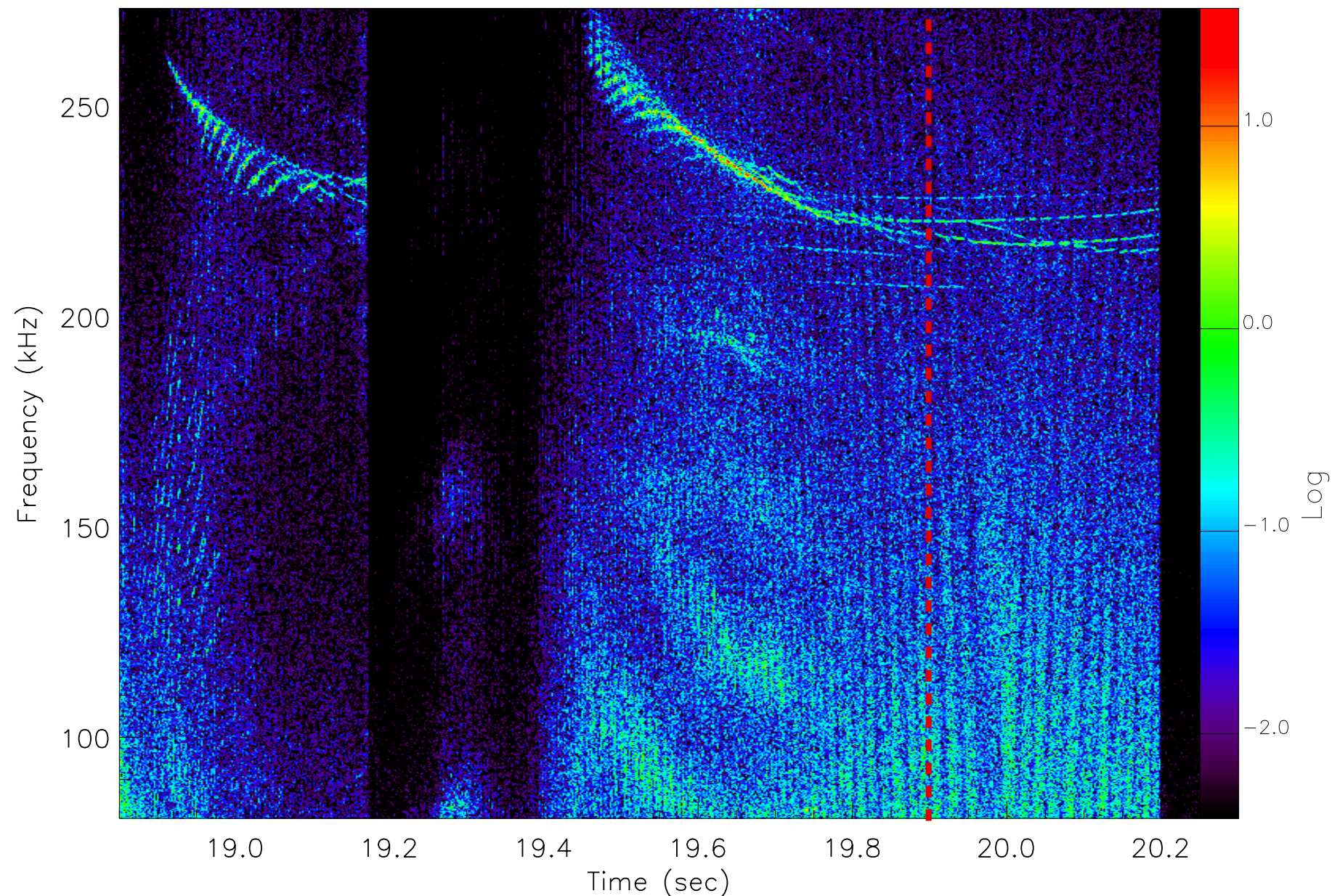
Numerical calculation of mode structure
and frequency

Energetic ion population drive

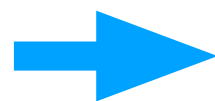
Resonances and orbits contributing to
mode drive along its evolution

Conclusion

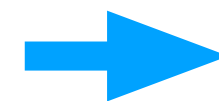
Retrace back from late stage tornado



Starting point in final stage of tornado modes



Retrace back plasma evolution



Establish connection between ACs and tornado modes

Rescaling q_0 to mimic post-sawtooth plasma evolution

Before sawtooth crash $q_0 < 1$, crash raises q_0 , then it gradually decreases

We have EFIT equilibrium reconstruction with MSE measurements refined with HELENA for $t=19.9\text{s}$

Equilibrium reconstructed q -profile is rescaled to reproduce plasma evolution after sawtooth crash

Raise q_0  Move backwards in time

For each step (i.e. for each q_0) MHD code MISHKA is used to scan for the existence of modes close to the axis

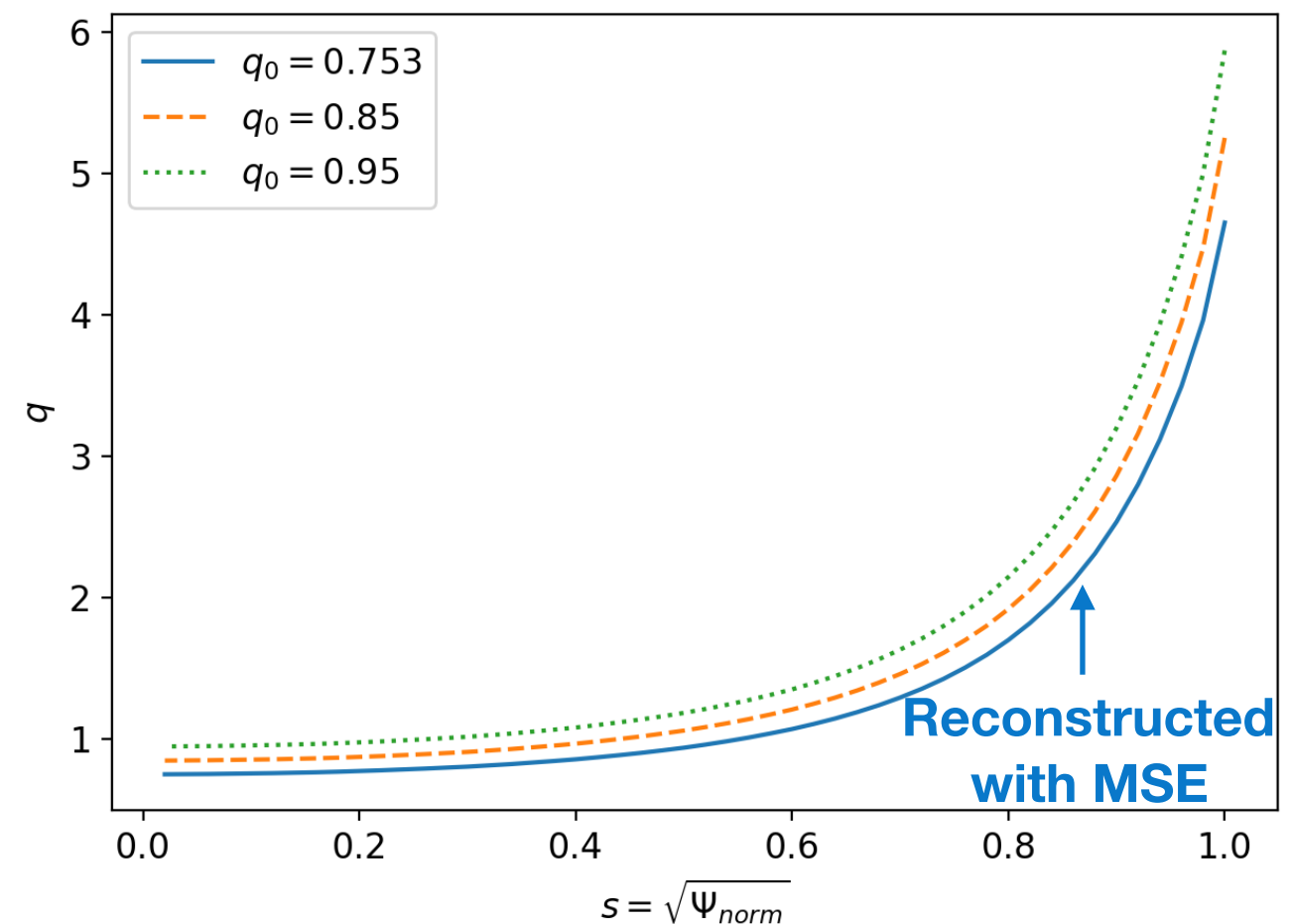
Near-axis cascades in very flat q-profile

q-profile is very flat near the axis but nonetheless monotonic

ACs are usually connected to shear reversal; however, they can be allowed in the right conditions if q-profile is sufficiently flat*

Tornado modes: TAEs inside $q=1$ **

AC modes: near-axis, flat q cascades



*B. N. Breizman, H. L. Berk, M. S. Pekker, S. D. Pinches, and S. E. Sharapov, Phys. of Plasmas 10, 3649 (2003)

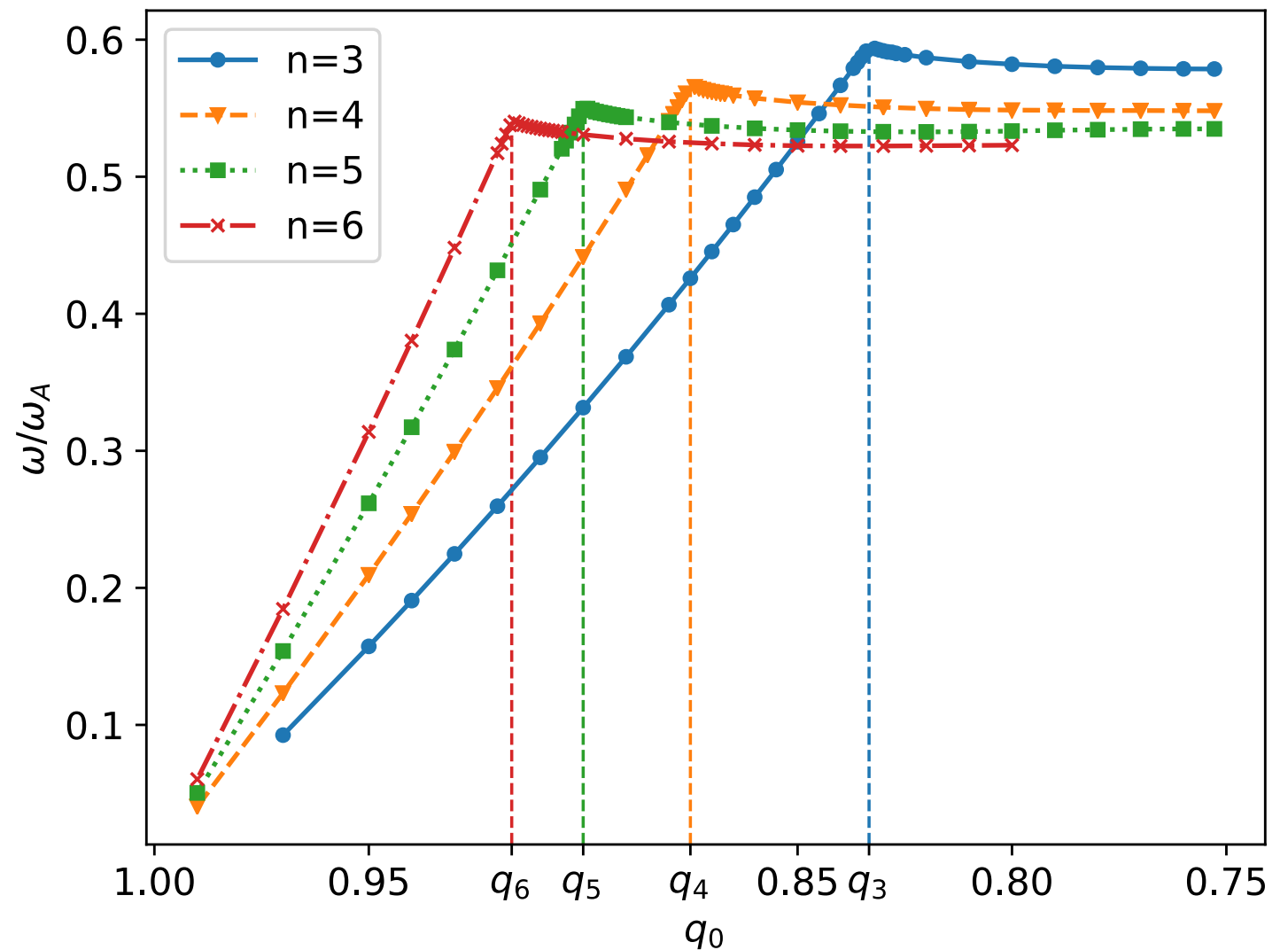
**T. Gassner et al., Phys. of Plasmas 19, 032115 (2012)

AC → tornado transition occurs at $q_0 = (n - 1/2)/n$

All modes have the same evolution

1st stage: grand cascade with higher n modes sweeping faster in frequency*

2nd stage: tornado mode



For mode with toroidal mode number n the transition point occurs at $q_0 = q_n = (n - 1/2)/n$

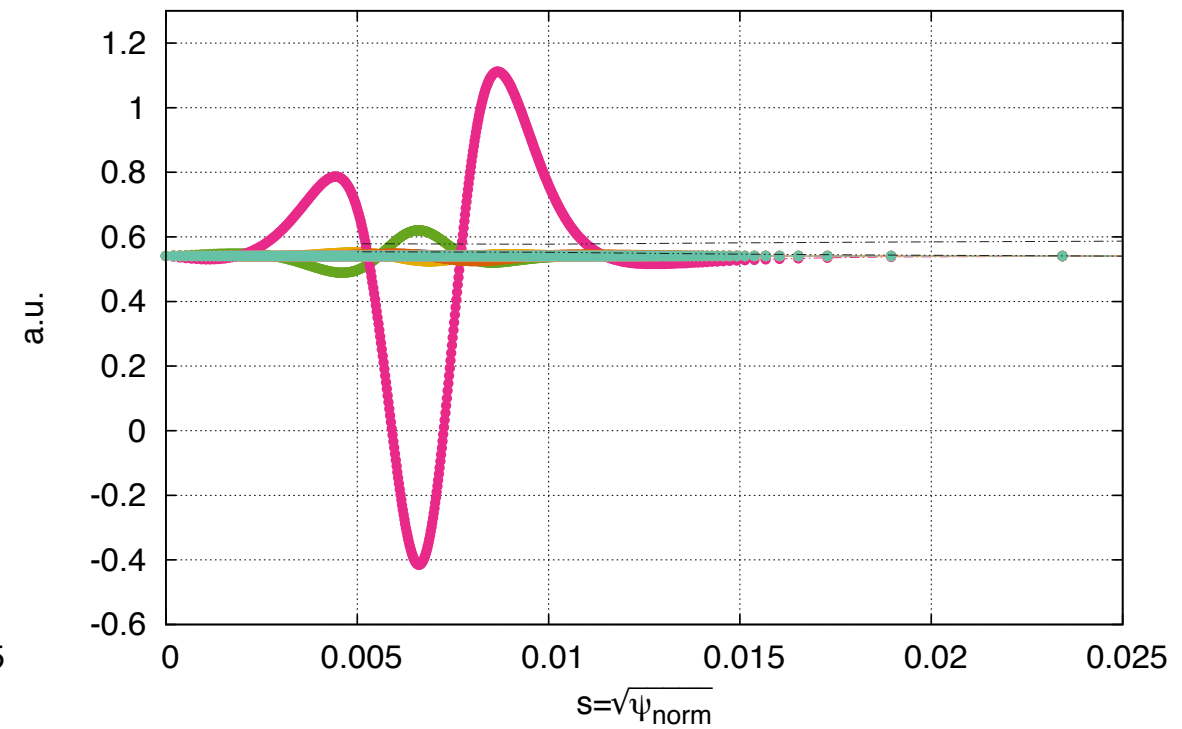
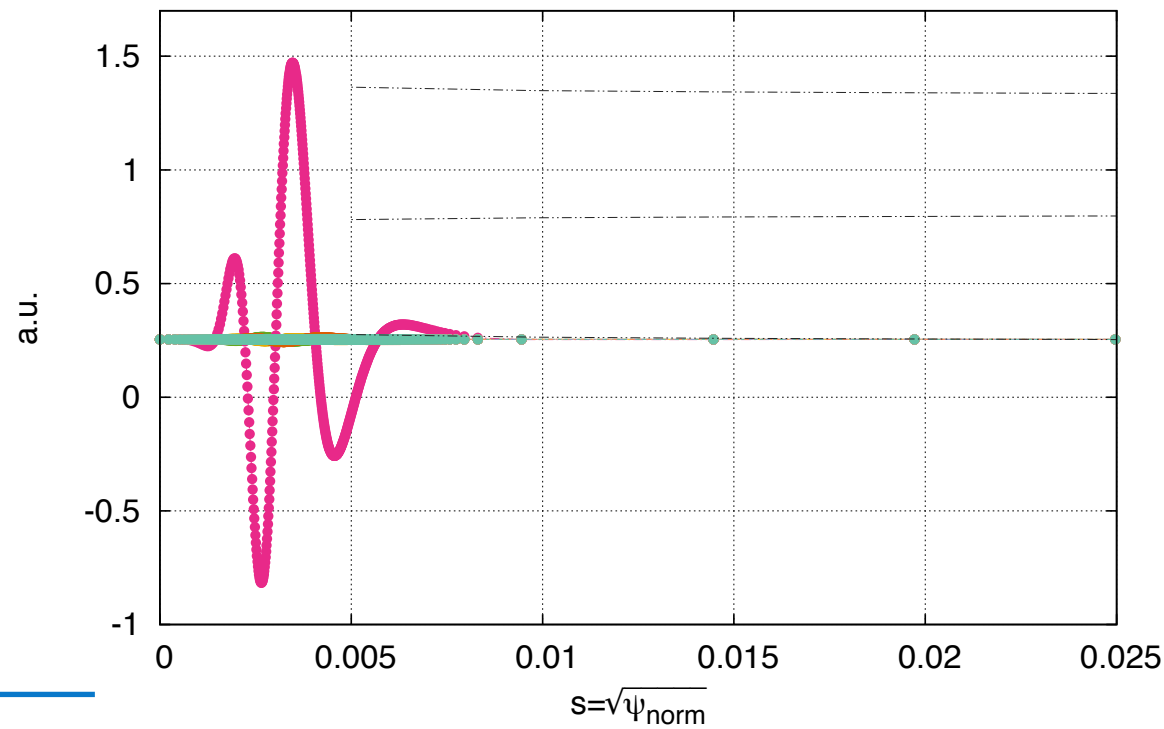


MHD spectroscopy of q-profile evolution after sawtooth crash:
 $q_6 = 0.917$; $q_5 = 0.9$; $q_4 = 0.875$;
 $q_3 = 0.833$

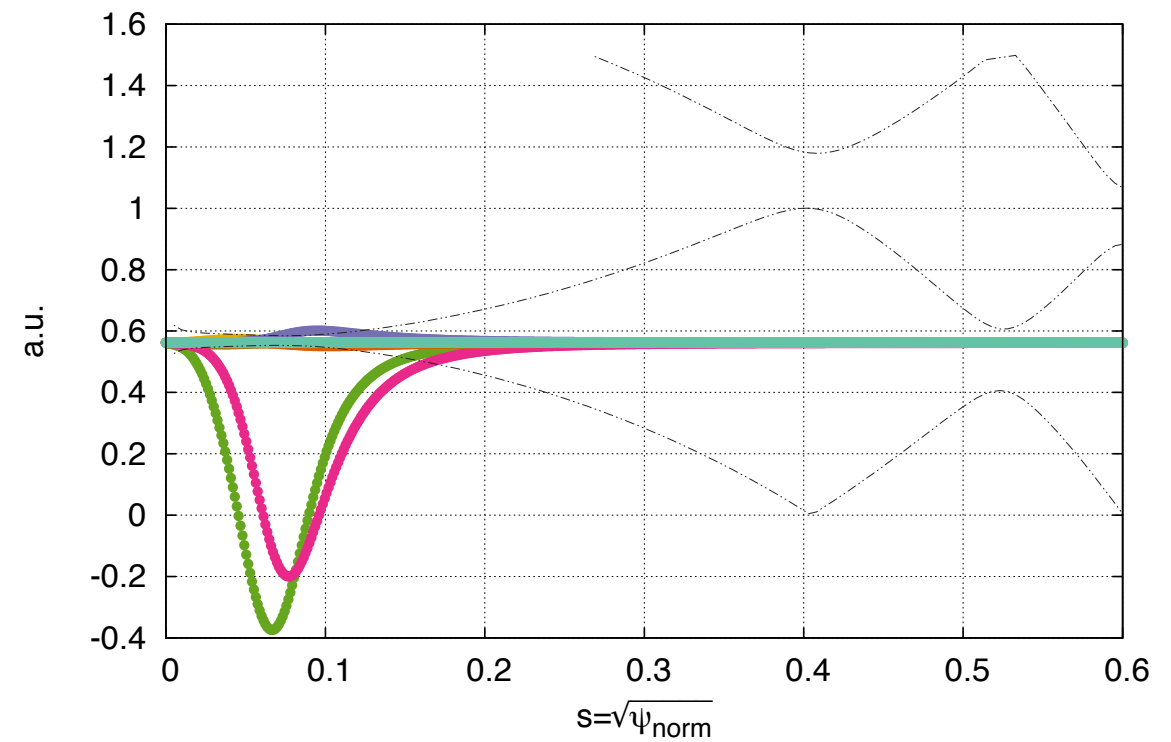
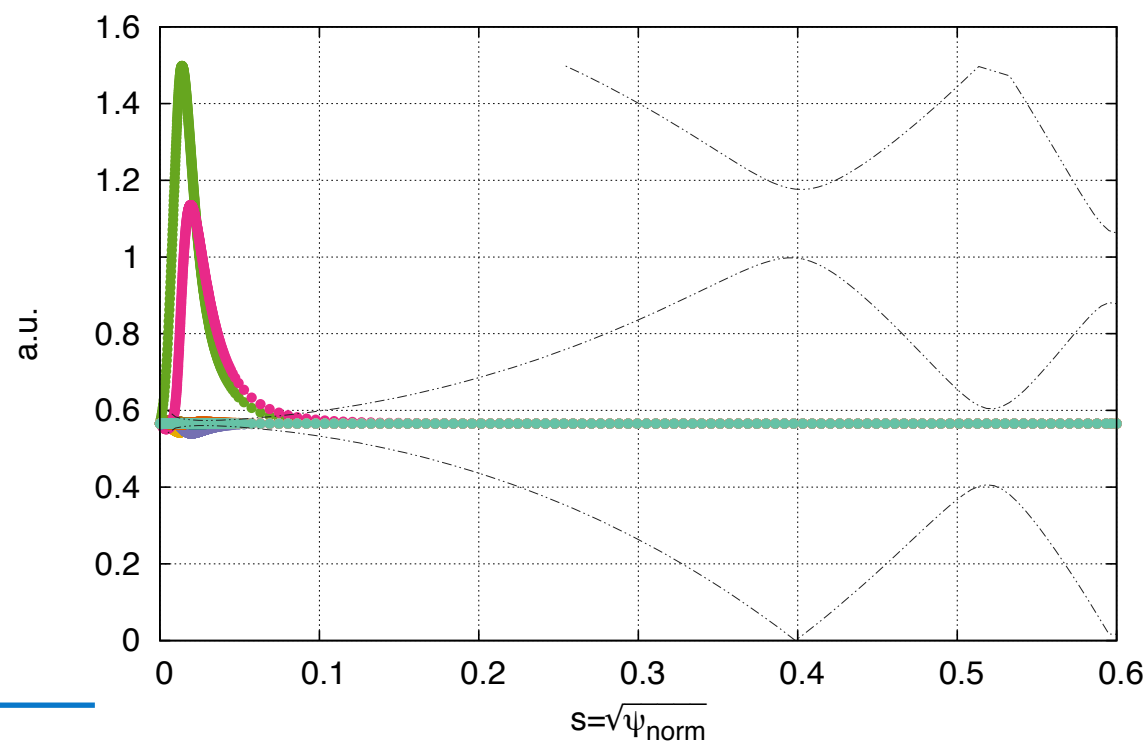
Highly localised AC, tornado modes larger radial extent

$n=4$:

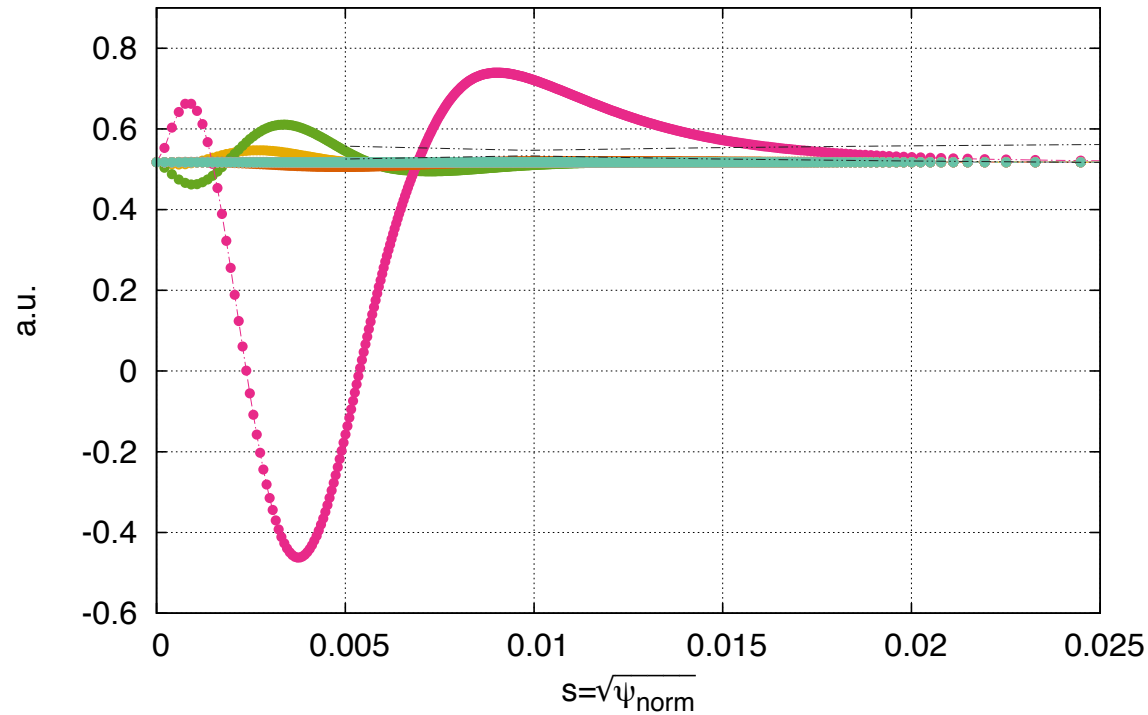
AC



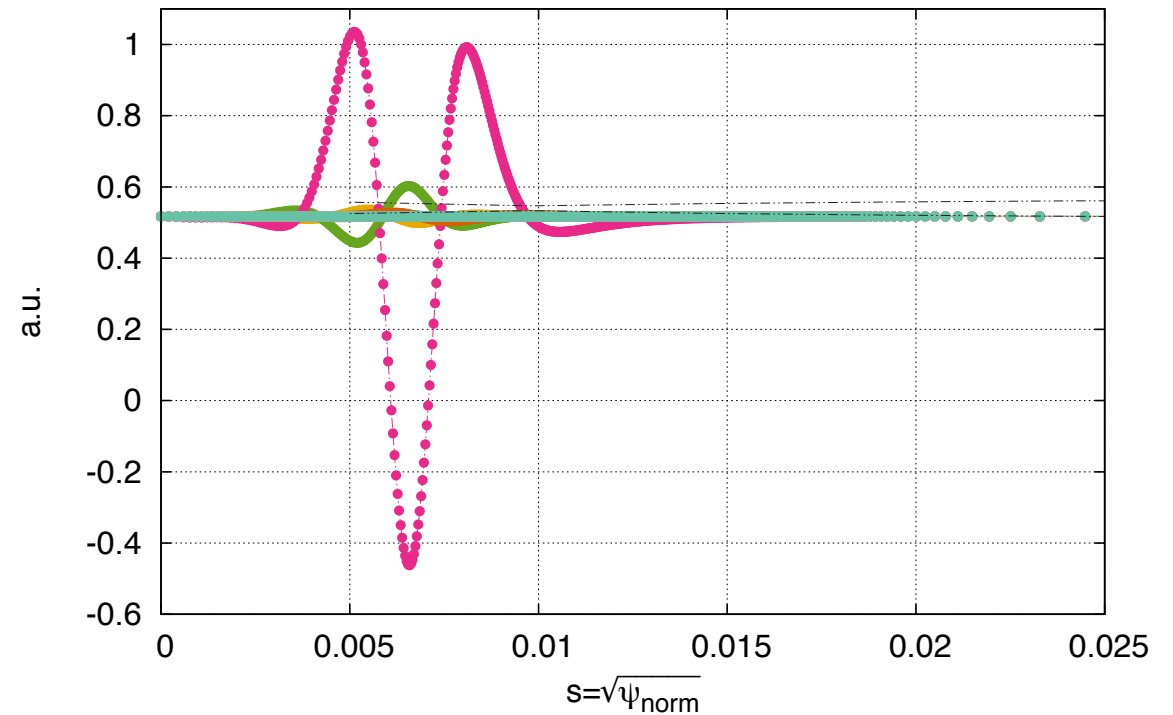
Tornado



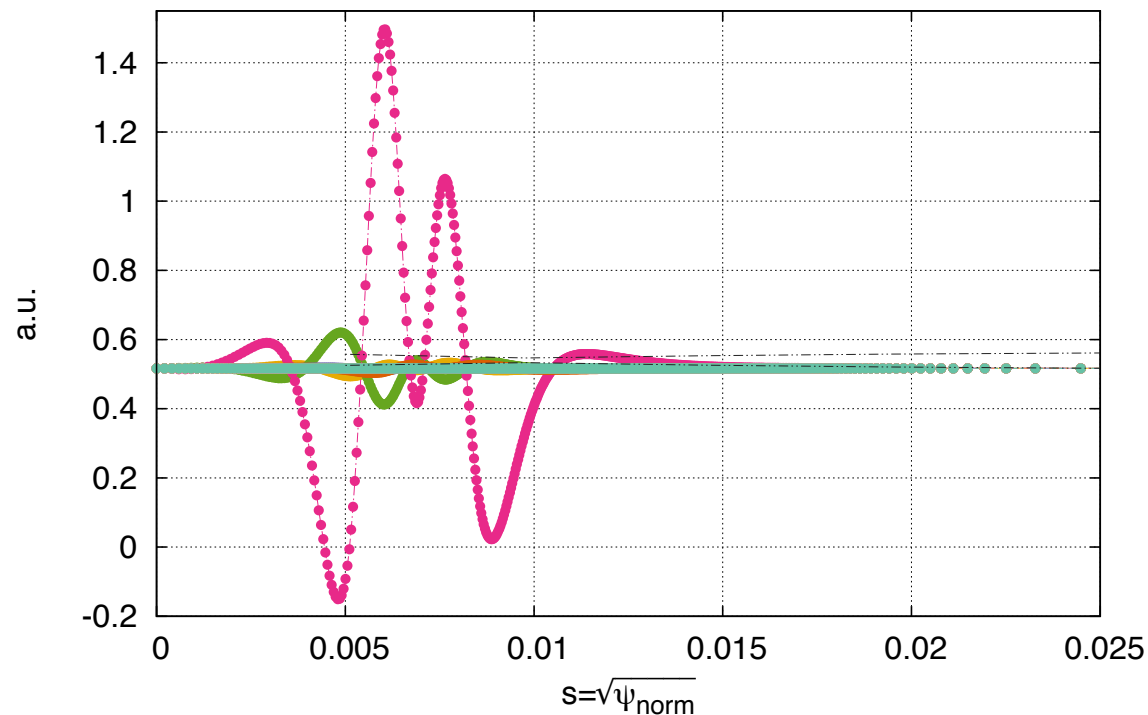
Multiple radial wavenumber modes exist in same “potential well”



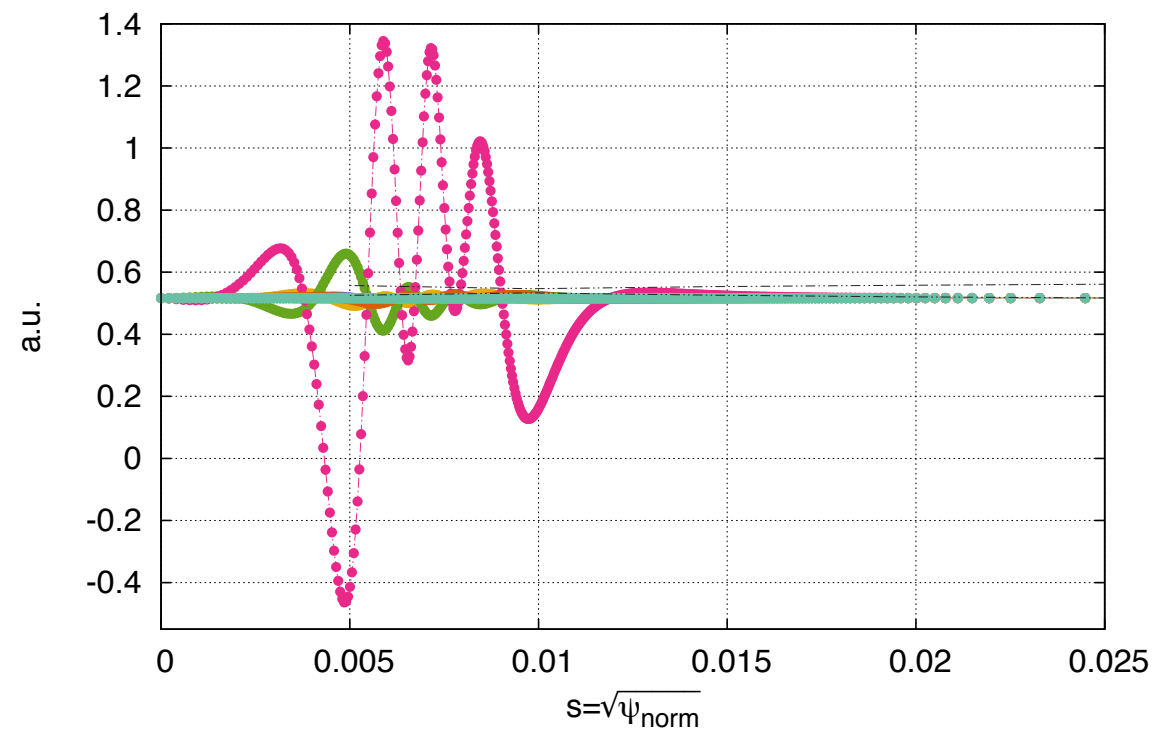
(a) $\omega/\omega_A = 0.5172$



(b) $\omega/\omega_A = 0.5170$



(c) $\omega/\omega_A = 0.5165$



(d) $\omega/\omega_A = 0.5163$

n=6 ACs

Outline

Experimental conditions and observations

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Numerical calculation of mode structure and frequency

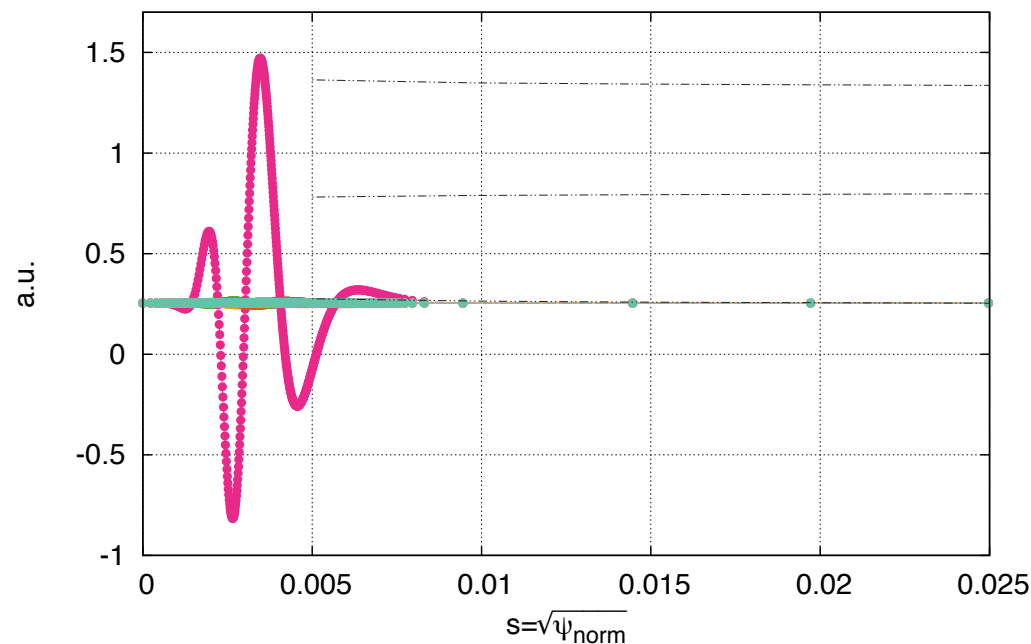
Energetic ion population drive

Resonances and orbits contributing to mode drive along its evolution

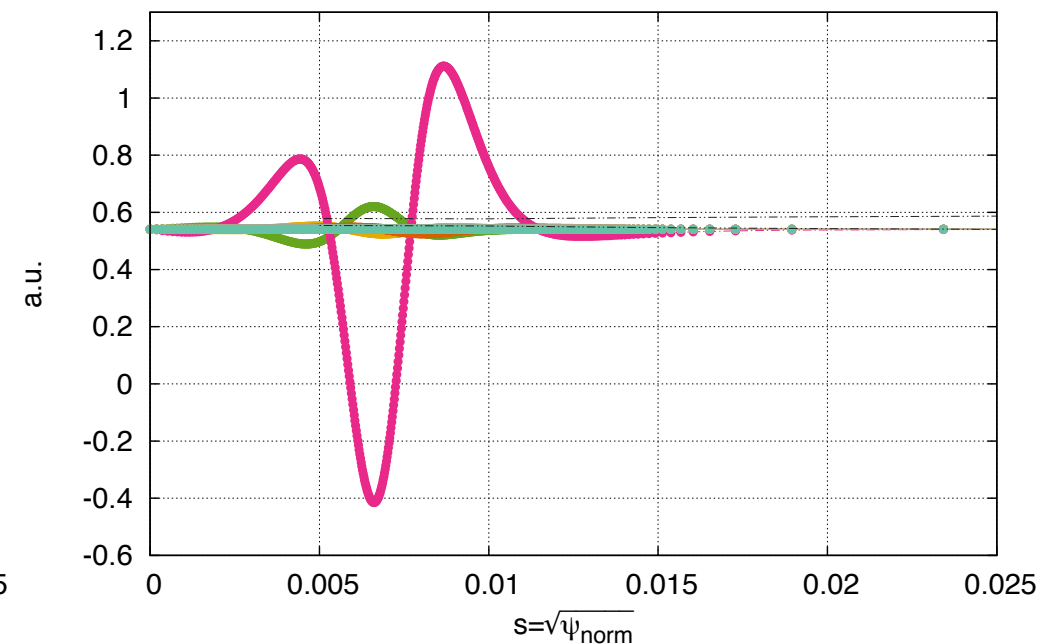
Conclusion

Assess energetic hydrogen minority drive of n=4 mode

$n=4$



(a) $q_0 = 0.94, \omega/\omega_A = 0.254$

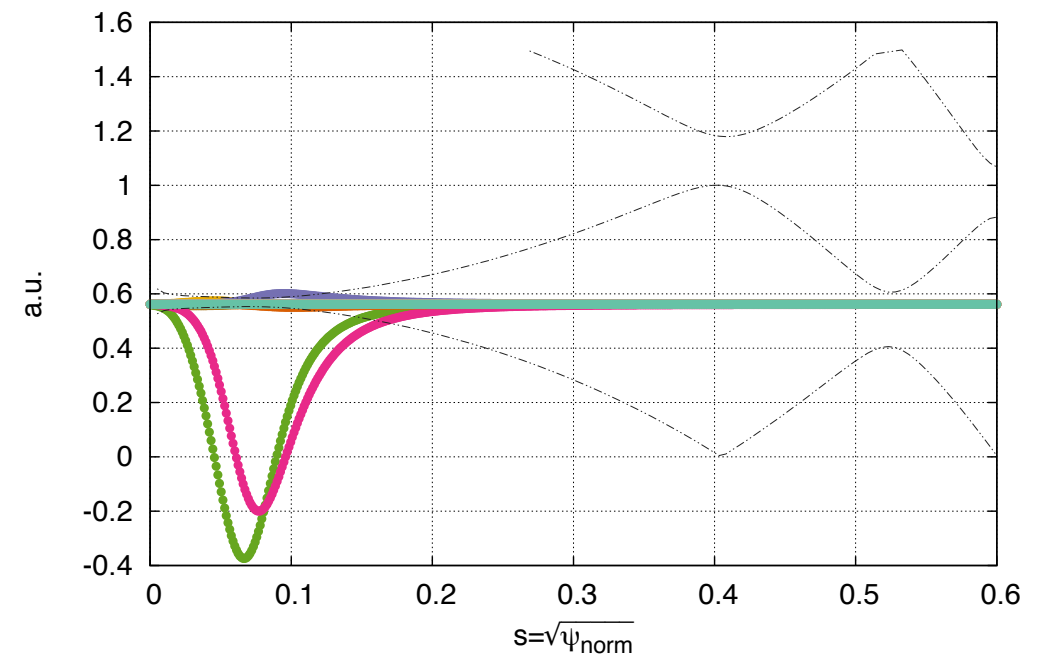


(b) $q_0 = 0.88, \omega/\omega_A = 0.541$

Ion orbits are characterised by the constants of motion (E, P_ϕ, Λ) , $P_\phi = Ze\Psi + v_{||}RB_\phi/B_0$, $\Lambda = \mu B_0/E$

Energetic ion population*:

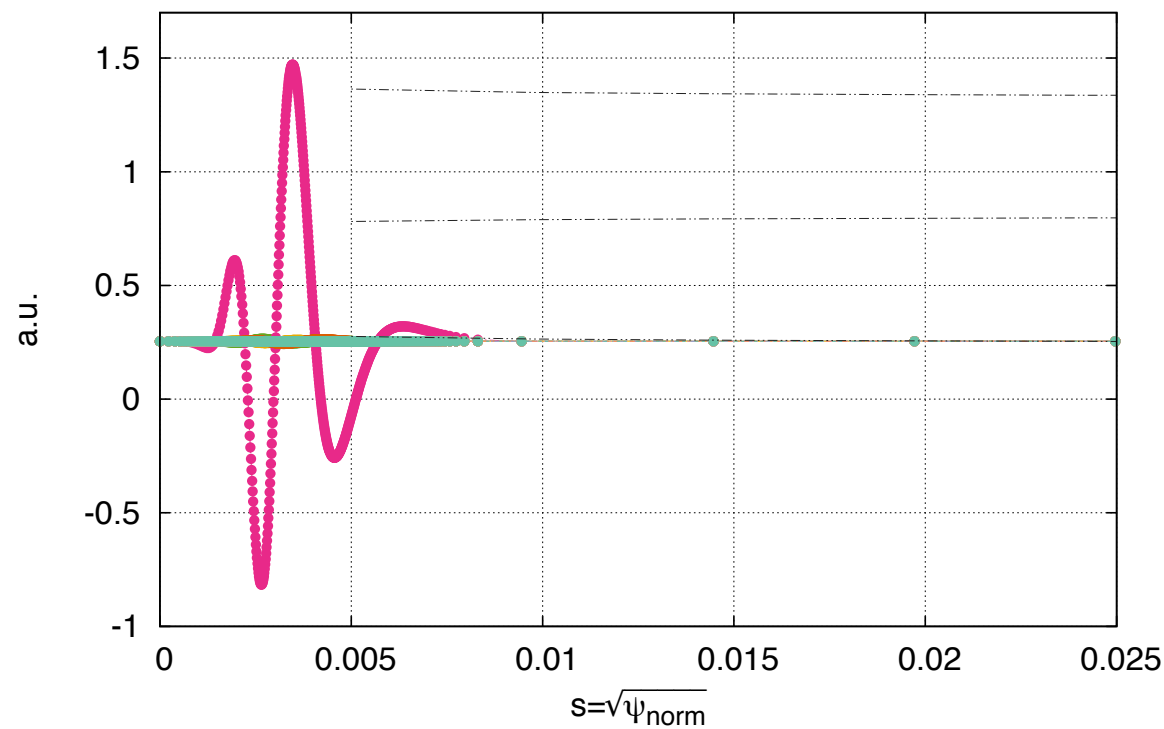
- single $\Lambda=0.96$
- Maxwellian distribution with temperature peaked on-axis of 527 keV
- radial density profile $\rho = \rho_0(1 - \Psi_{\text{norm}})^2$



(d) $q_0 = 0.87, \omega/\omega_A = 0.562$

Drive of n=4 mode is calculated with CASTOR-k at three steps of mode evolution

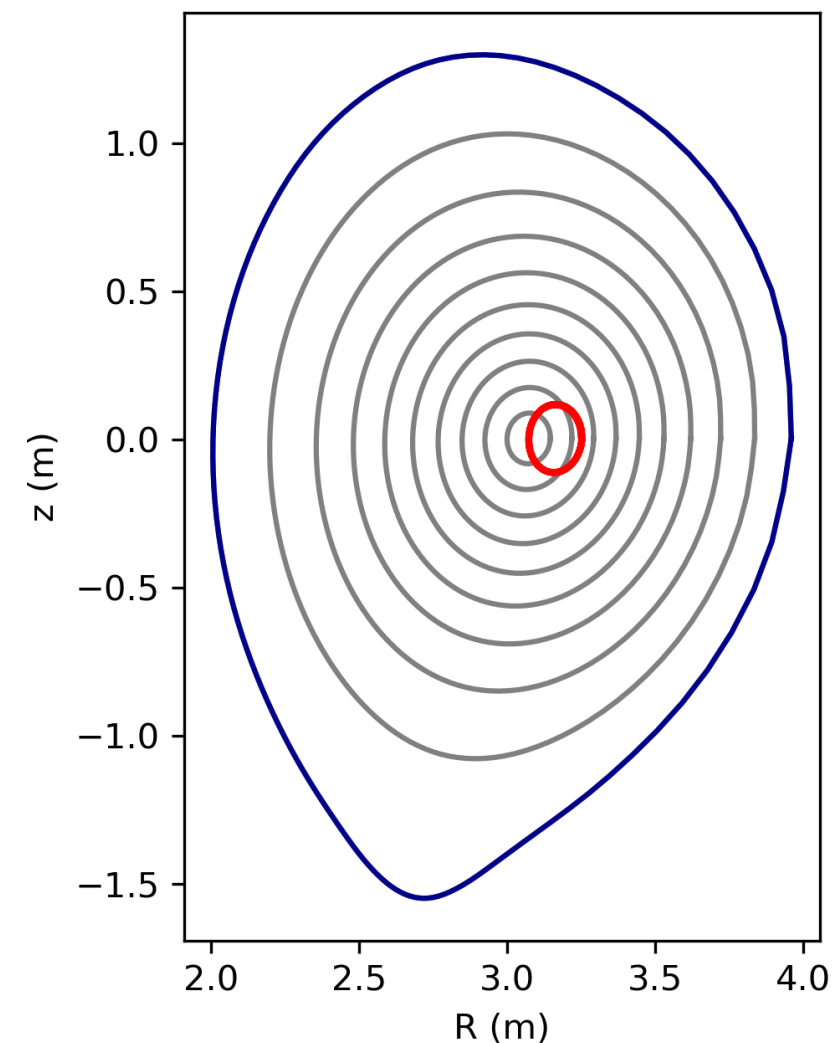
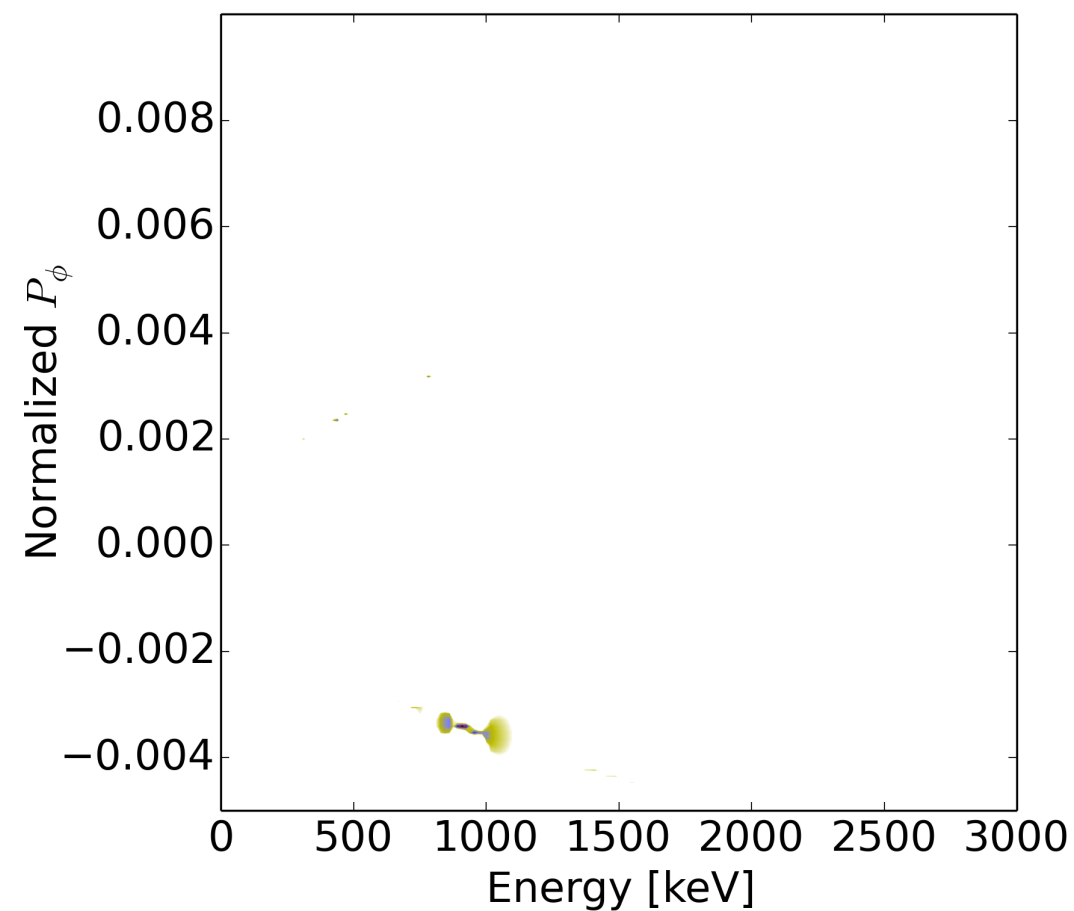
Low frequency cascade interacts with single, very narrow resonance



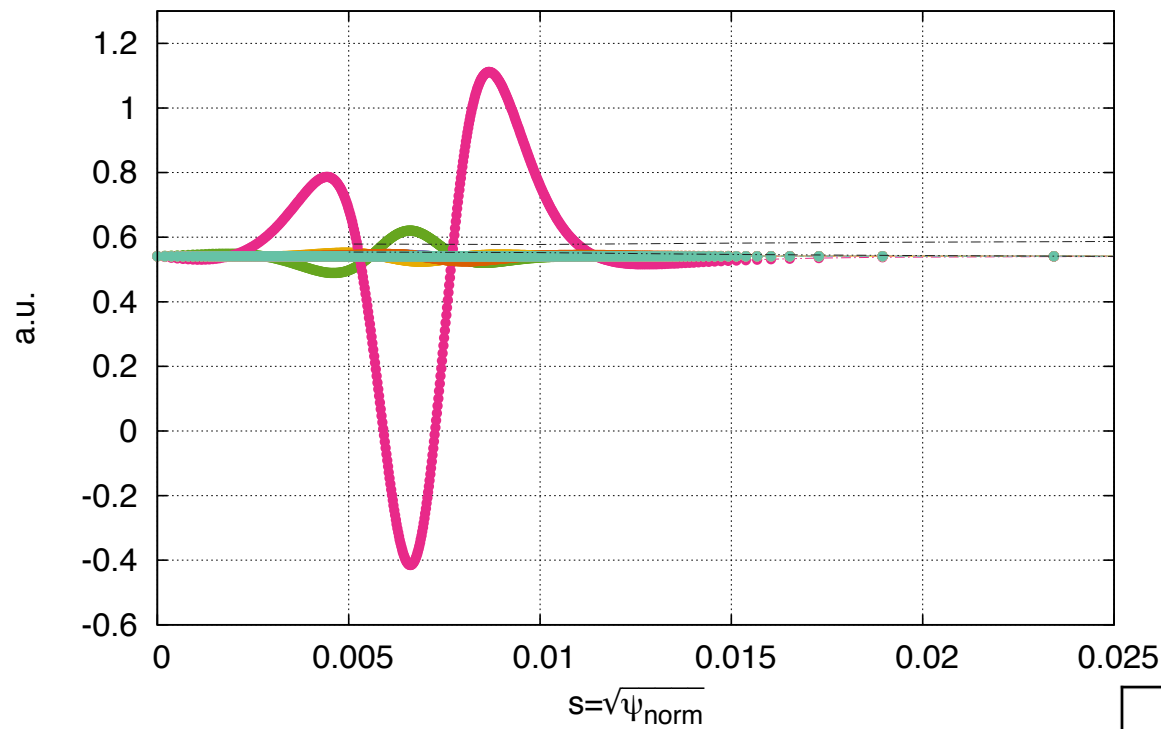
$$\omega/\omega_A = 0.254 \rightarrow f \approx 92 \text{ kHz}$$

Single relevant interaction in a very narrow resonance

Corresponding orbit is non-standard and close to the axis



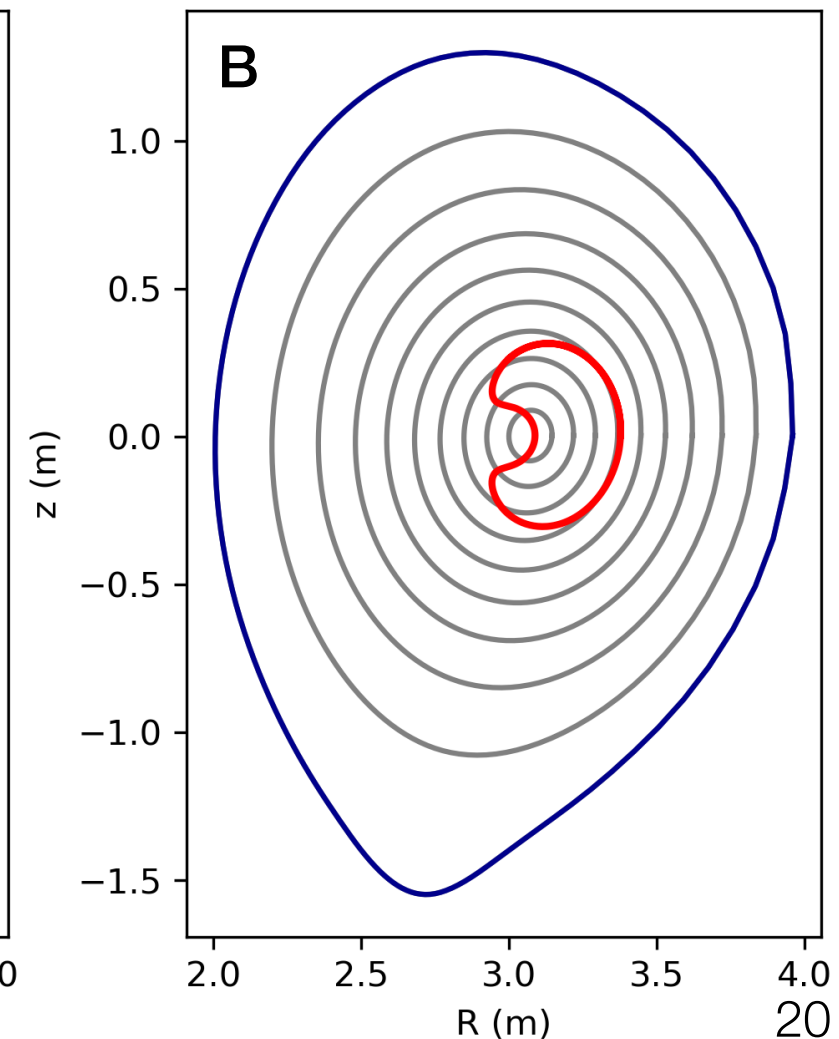
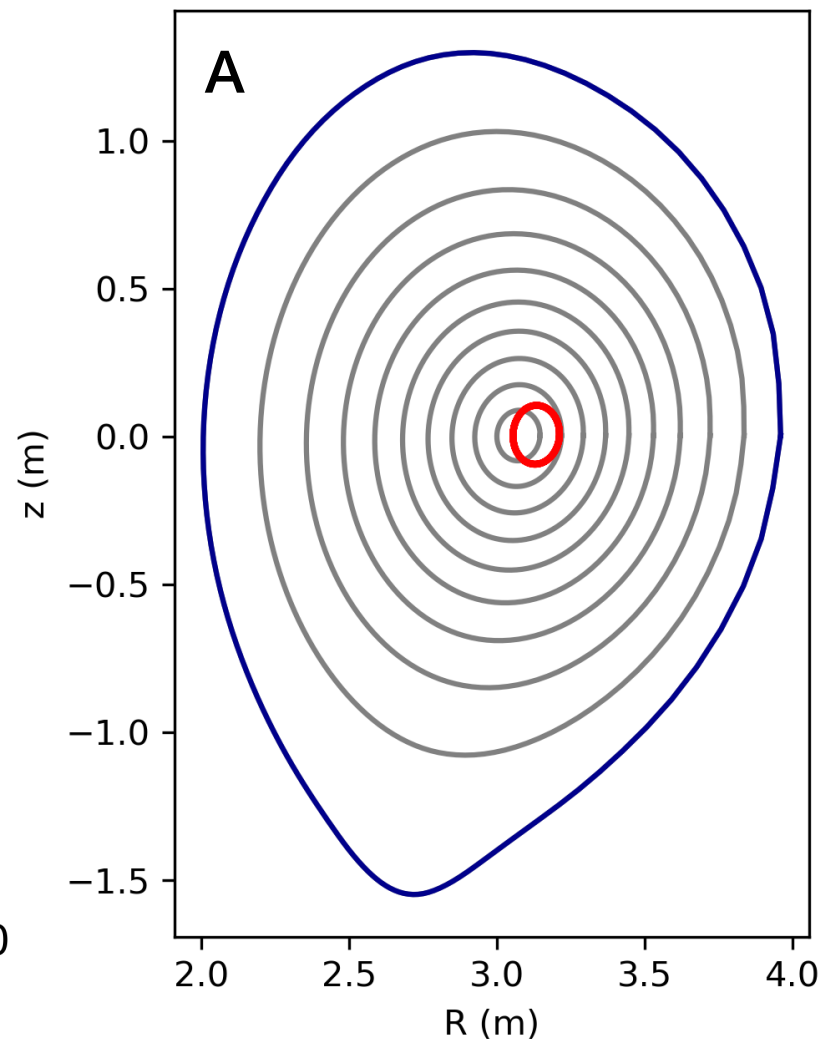
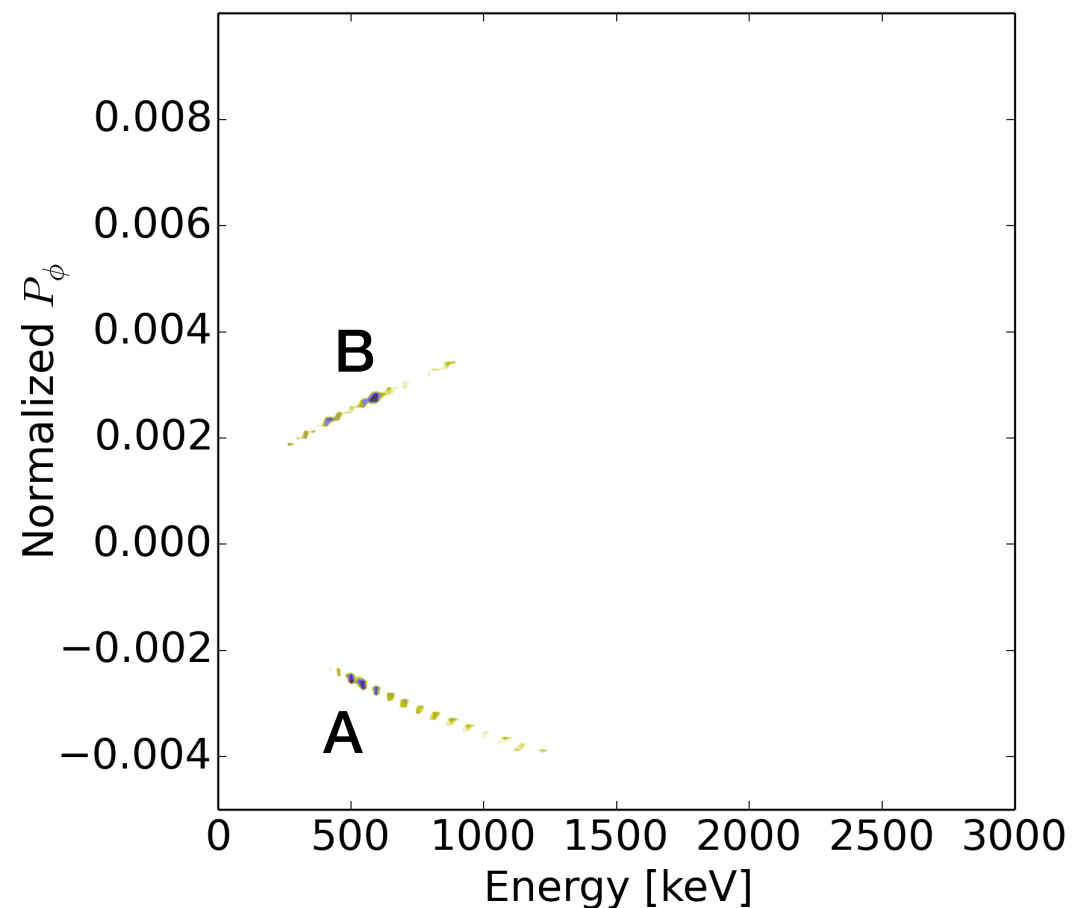
High frequency cascade interacts with two very narrow resonances



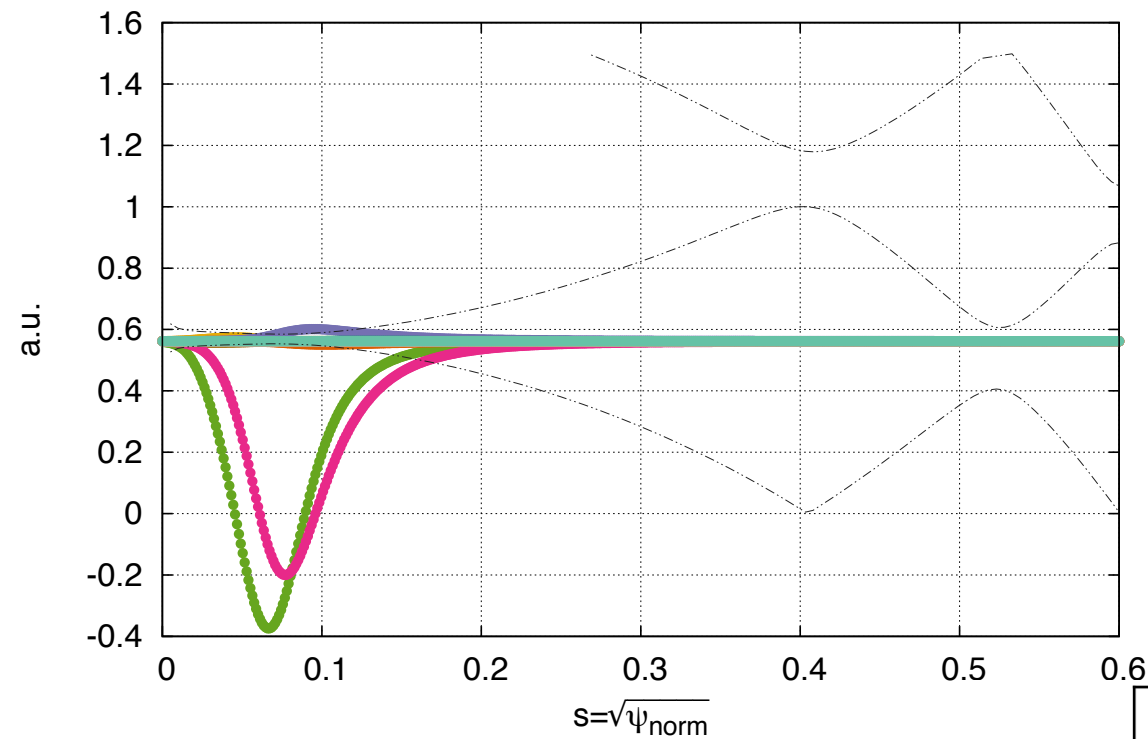
$$\omega/\omega_A = 0.541 \rightarrow f \approx 195 \text{ kHz}$$

Two relevant interactions in very narrow resonances

Corresponding orbits are non-standard and close to the axis



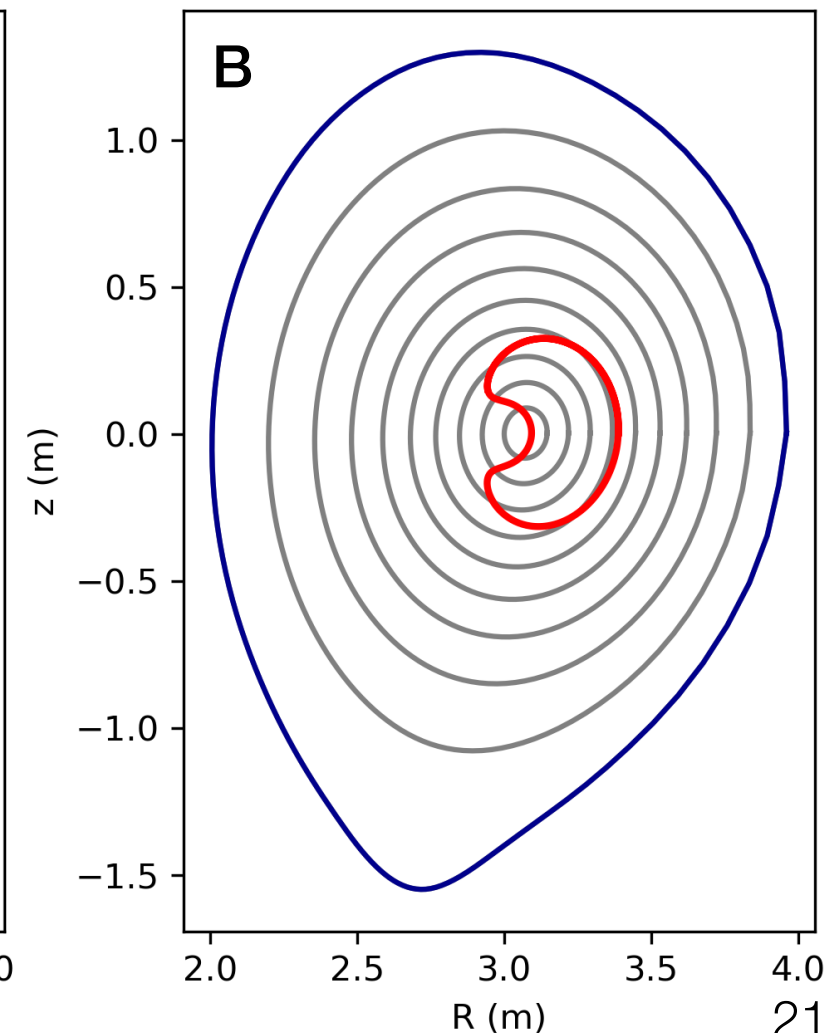
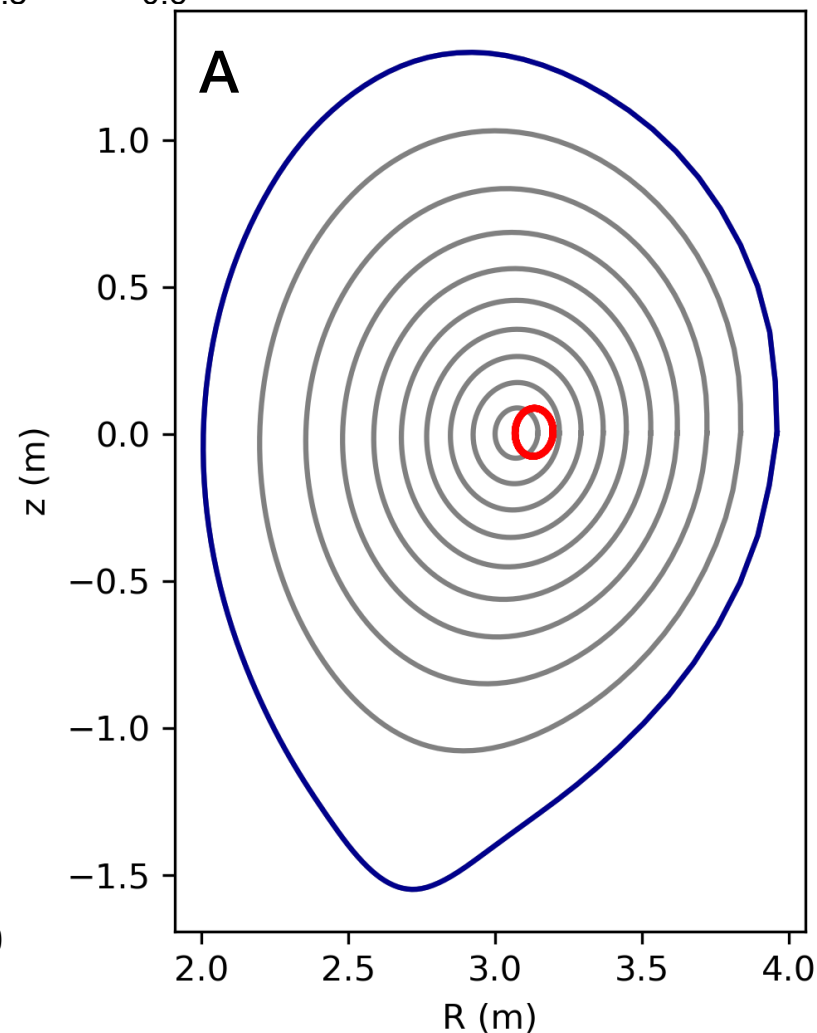
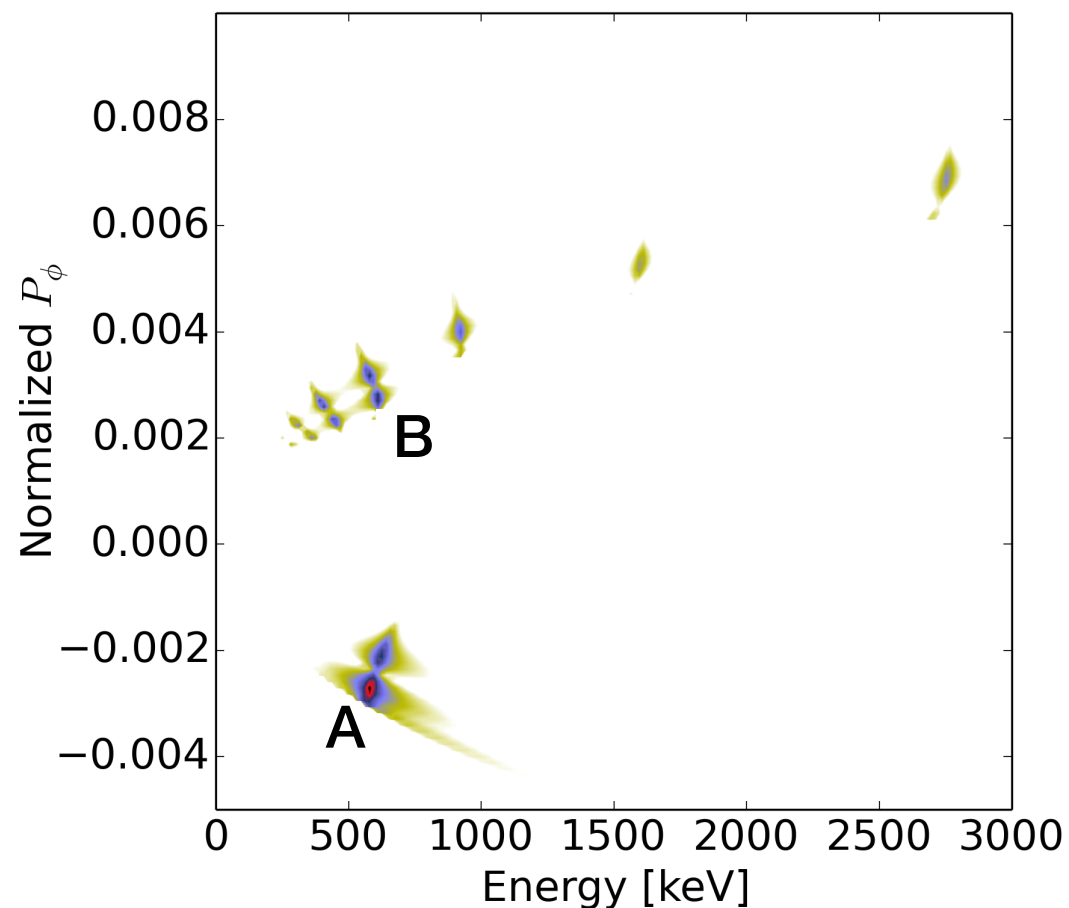
Tornado mode interacts with two broader resonances



$$\omega/\omega_A = 0.562 \rightarrow f \approx 203 \text{ kHz}$$

Two relevant interactions in broader resonances

Corresponding orbits are non-standard and close to the axis



Energetic minority drives the mode

Mode Type	q_0	ω/ω_A	γ/ω (%)
Low frequency AC	0.94	0.254	0.196
High frequency AC	0.88	0.541	0.0168
Tornado	0.87	0.562	3.07

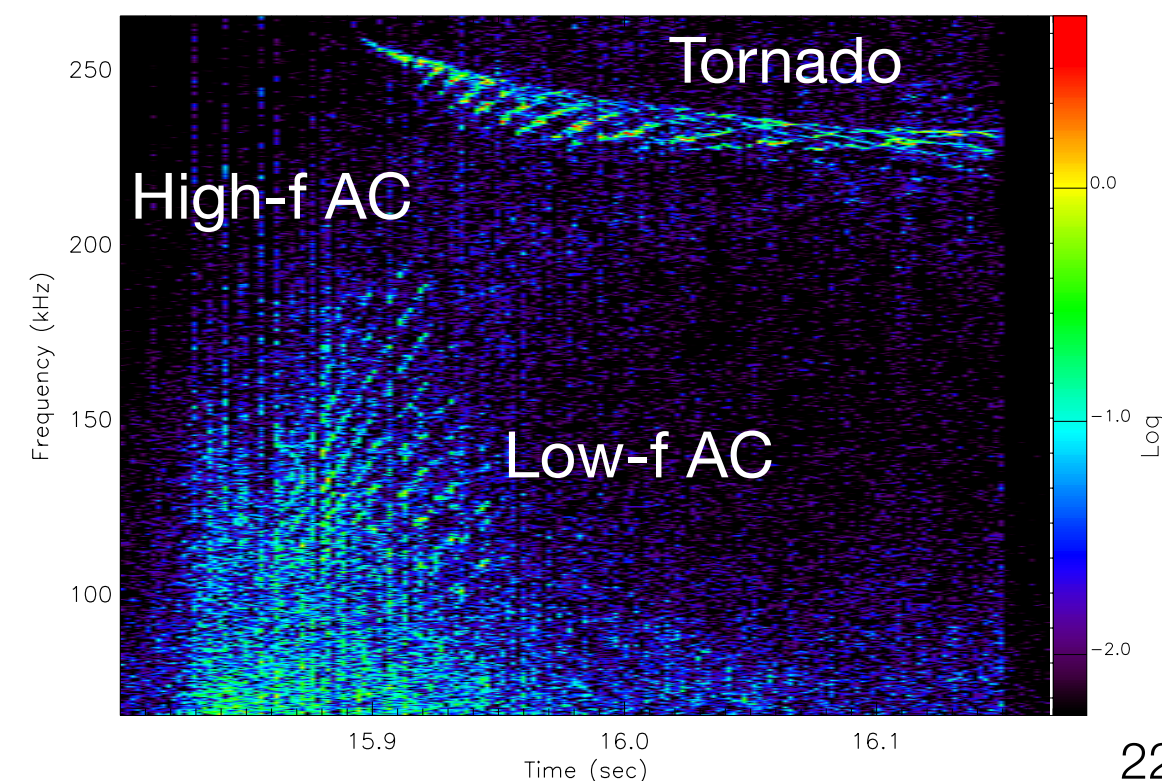
Intermediate drive in low frequency AC phase

Drive is weaker in high frequency AC phase

Drive is stronger during tornado phase

Mode experiences drive throughout its evolution

Lower drive in high frequency AC may explain why a gap is observed between ACs and tornado modes



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Conclusions

We have numerically reproduced mode evolution from the base of grand cascade to TAE frequency range followed by transition to tornado mode

Fast upward sweeping modes were identified as highly localised near-axis AC made possible due to the very flat q -profile

AC \rightarrow tornado mode transition occurs when $q_0=q_n=(n-1/2)/n$, which we propose to be used as an MHD spectroscopy technique to track q -profile evolution post-sawtooth crash. Only magnetics data is sufficient.

Throughout plasma evolution the mode is excited by energetic minority species, though high frequency AC phase experiences weaker drive which may explain gap between ACs and tornado modes observed in diagnostics