

Impurity transport in collisionless trapped-particle-driven turbulence

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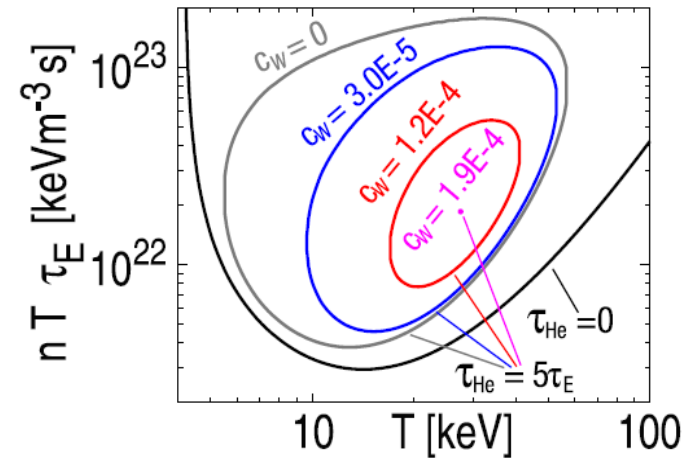
May 14th, 2021

Context: gyrokinetic simulations of impurity transport in the core of tokamaks

Fusion efficiency is sensitive to core impurity concentration

- Reduction of tungsten concentration from 1.2×10^{-4} to 0.3×10^{-4}
 - 40% decrease in required triple product
 - 40% decrease in required temperature
- ⇒ easier access to ignition

[Pütterich NF'10]



Challenge for gyrokinetic simulations

- Neoclassical and turbulent transport [Romanelli NF'98]
- Synergistic coupling [Estève NF'18]
- Disparate timescales

Focus on dynamics of trapped particles

⇒ bounce-averaged gyrokinetics

Objectives: Qualitative impacts of impurity concentration, charge, mass, and gradients

1. Impact of concentration

- In general, turbulence \rightleftharpoons impurities \Rightarrow self-consistent (active) treatment
- But if concentration $\rightarrow 0$, passive treatment is a promising approach. **Limit of validity?**
Smooth transition or critical threshold?

2. Diffusion, thermo-diffusion, and curvature pinch

- Total density flux of impurity with charge Z

$$\Gamma_Z = -D_Z [\nabla n_Z + C_T \nabla T_Z + C_P \nabla q]$$

Diffusion Thermodiffusion Curvature

- Each contribution can be isolated by varying the density and temperature gradients, and by artificially switching on/off the curvature drift

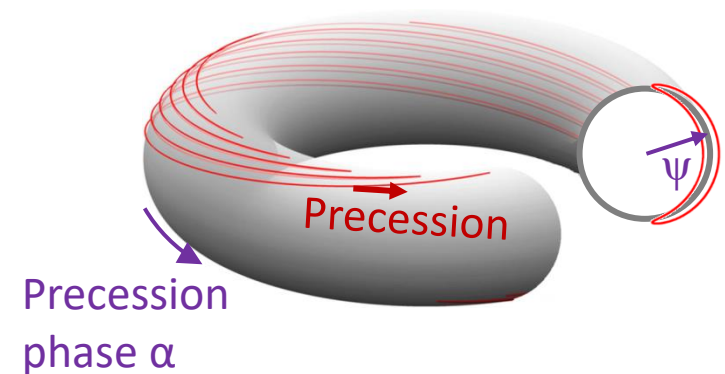
\Rightarrow **parameter scans in charge, mass, gradients, and magnetic shear**

Reduced model for trapped-particle-driven turbulence

Bounce-averaged gyrokinetic model

- Based on frequency ordering for TIM and TEM
 $\Omega \sim \Omega_{\text{precession}} \ll \Omega_{\text{bounce}} \ll \Omega_{\text{cyclotron}}$
- Kinetics of trapped particles only
 (adiabatic passing particles)
- 2D phase space (angle α , radius ψ)
 + 2 parameters (energy and pitch-angle)

[Depret PPCF'00]
[Sarazin PPCF'05]



$$\frac{\partial f_s}{\partial t} + [J_0 \phi, f_s]_{\alpha, \psi} + \omega_{d,s} \frac{\partial f_s}{\partial \alpha} = 0$$

$$\omega_{d,s} = E \Omega_d / Z_s$$

$$\underbrace{C_{ad} (\phi - \epsilon_\phi \langle \phi \rangle)}_{\delta \rho_{\text{passing}}} - \underbrace{C_{pol} \sum_s C_s \tau_s Z_s^2 \bar{\Delta}_s \phi}_{\delta \rho_{\text{polarization}}} = \underbrace{\frac{2}{\sqrt{\pi}} \sum_s \left(Z_s C_s \int_0^\infty J_{0,s} f_s E^{1/2} dE \right)}_{\delta \rho_{\text{trapped}}}$$

⇒ TERESA simulation code (N species)

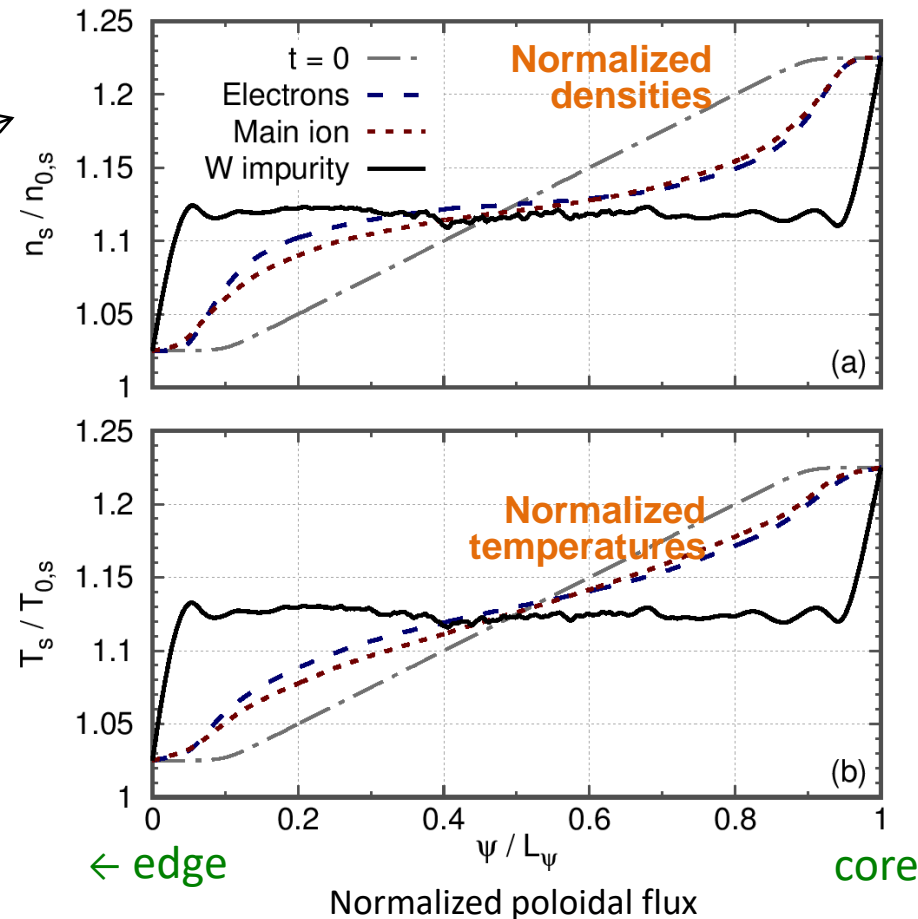
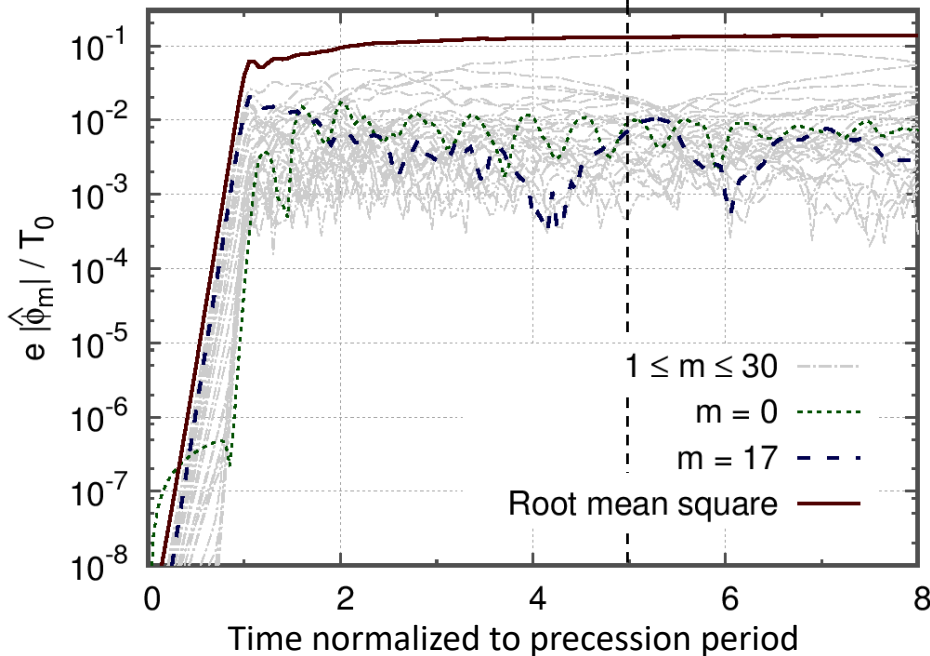
[Drouot EPJD'14]
[Cartier-Michaud JPCS'15]

1. Impact of impurity concentration

Timescale of flattening of impurity profiles depends on concentration

Typical simulation with low tungsten concentration $C_W=10^{-5}$

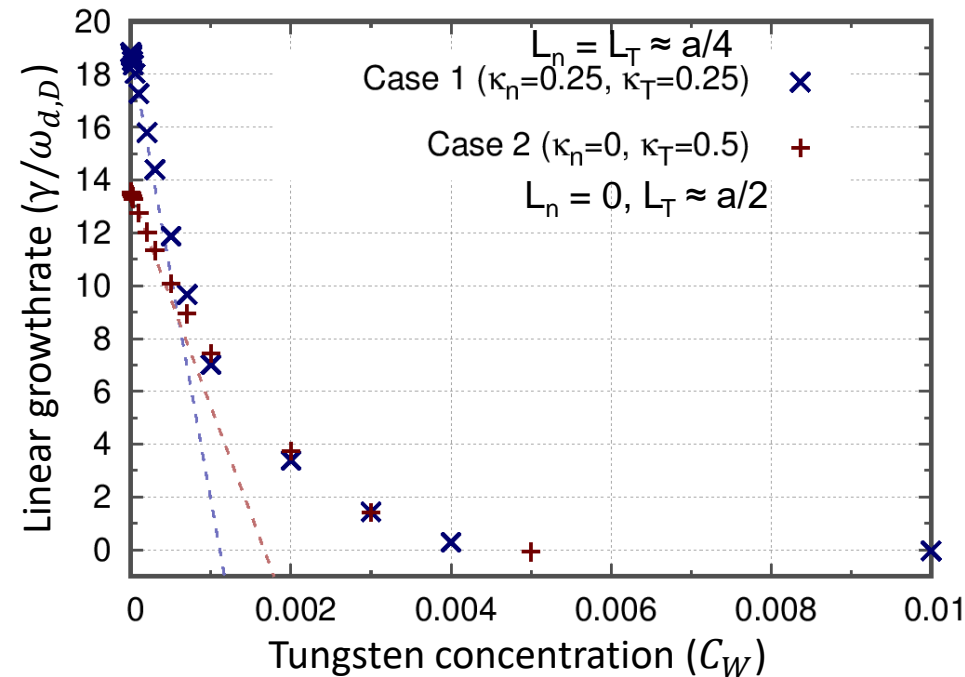
- Initial gradient lengths $L_n = L_T \approx a/4$



Timescale of flattening or impurity profiles

- Trace concentration \rightarrow within a fraction of a precession period
- Non-trace concentration \rightarrow several precession periods (similar to main species)

Growth rate and turbulence intensity decrease with increasing C_W , linear for $C_W < 5 \cdot 10^{-4}$



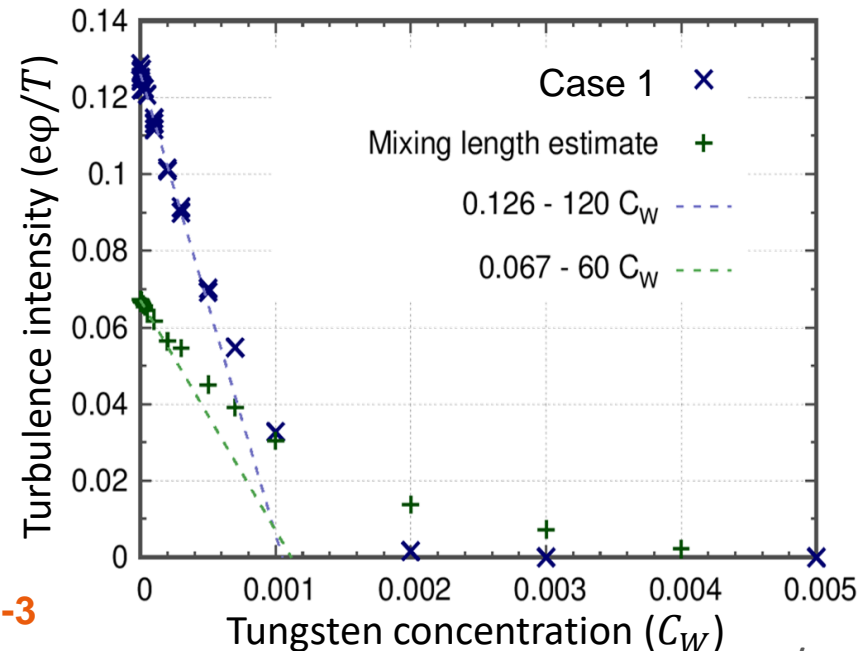
Linear growth rate ↓ with C_W ↑

- Consistent with linear GK [Dominguez NF'89]
- Due to dilution [Du NF'14]
- $\frac{\gamma - \gamma_0}{\omega_{d,D}} \sim -10^4 C_W$
- Quantitative agreement with analytic theory [Lesur NF'20]

Turbulence intensity ↓ with C_W ↑

- Qualitative agreement with mixing length estimate

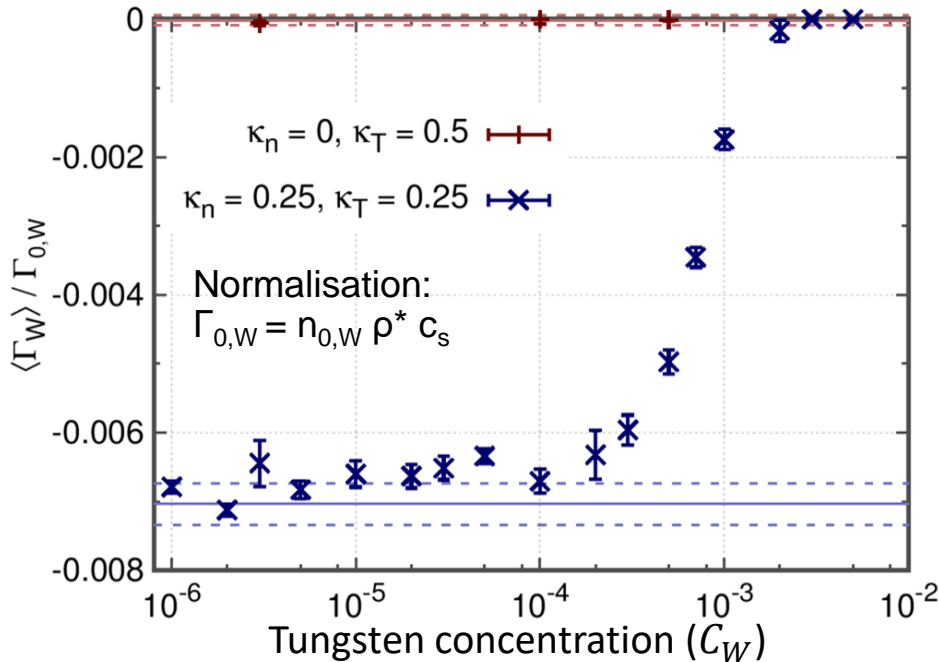
$$e\phi/T_0 = \gamma / (k_r \rho_{c,i} k_\theta c_s)$$
- But not simply proportional to γ



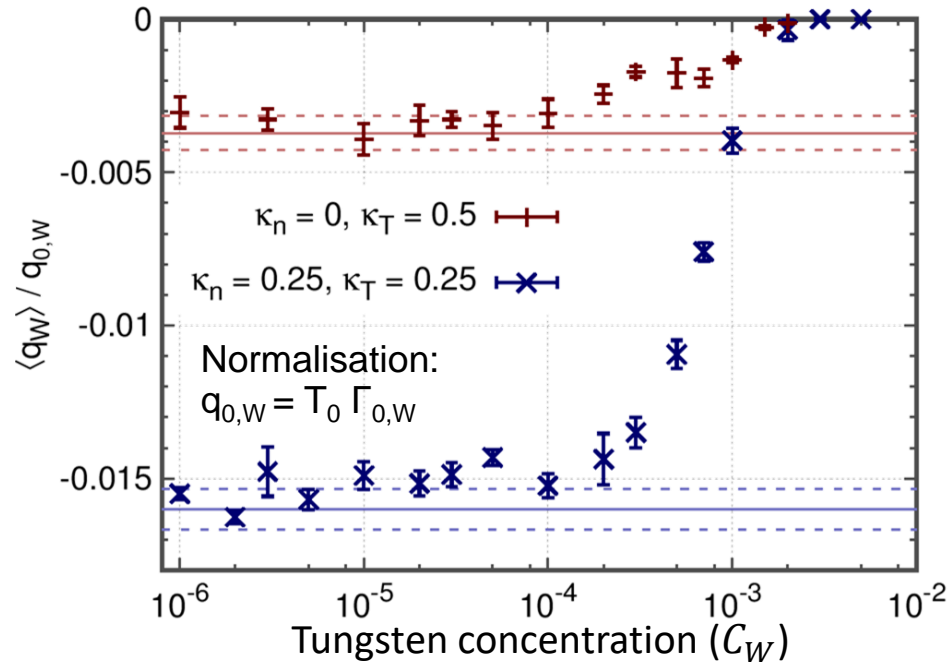
⇒ **Passive treatment valid for $C_W \ll 10^{-3}$**

$C_W = 2 \cdot 10^{-4}$ threshold for radial fluxes of W^{40+}

Radial density flux



Radial heat flux

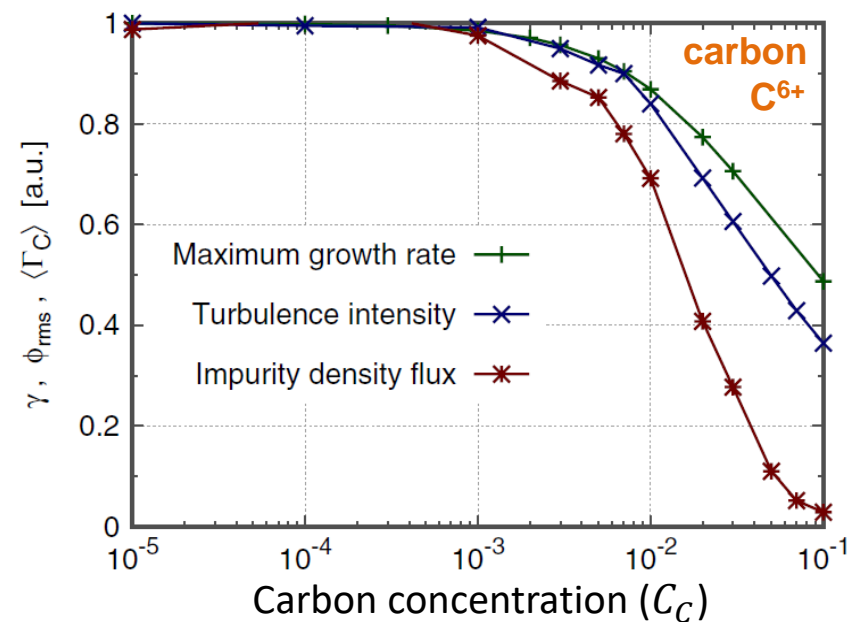
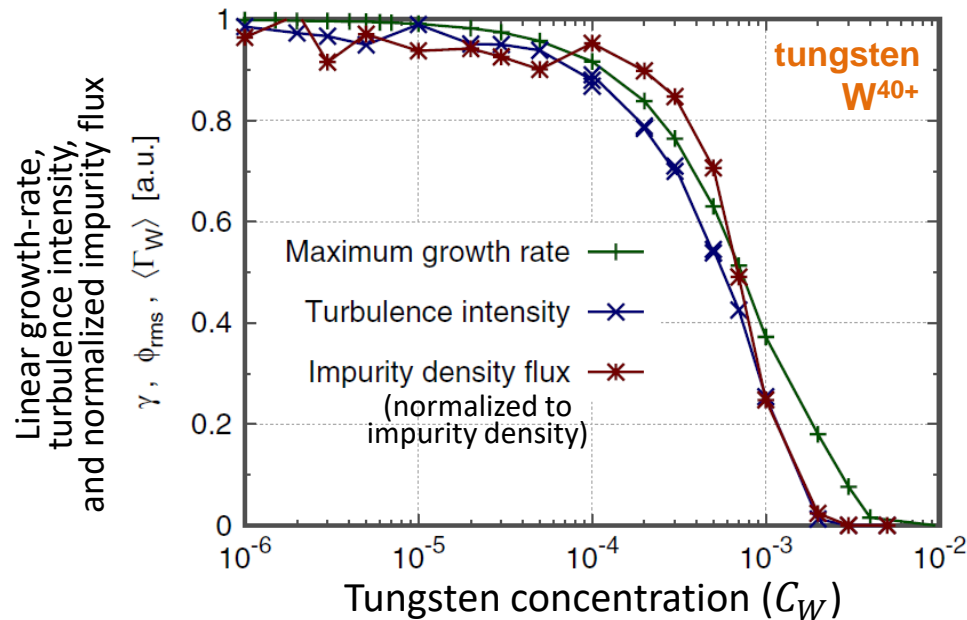


Caveats

- Effect of low-frequency turbulence only, no neoclassical transport
- Small system size ($\rho^* \approx 1 / 30$), radial profiles constrained by thermal baths

Comparing the effects on linear modes, turbulence, and transport

Dependency of normalized impurity transport is more threshold-like than that of linear growth rate and turbulent intensity



- Here, all quantities are normalized to their value in the limit of zero impurity concentration

Transport quenching is due to phase synchronization

[Lesur NF'20]

- Electric potential fluctuations synchronize to impurity density fluctuations
- Occurs only above critical concentration

2. Diffusion, thermo-diffusion, and curvature pinch

Impact of charge and mass numbers on diffusive impurity transport

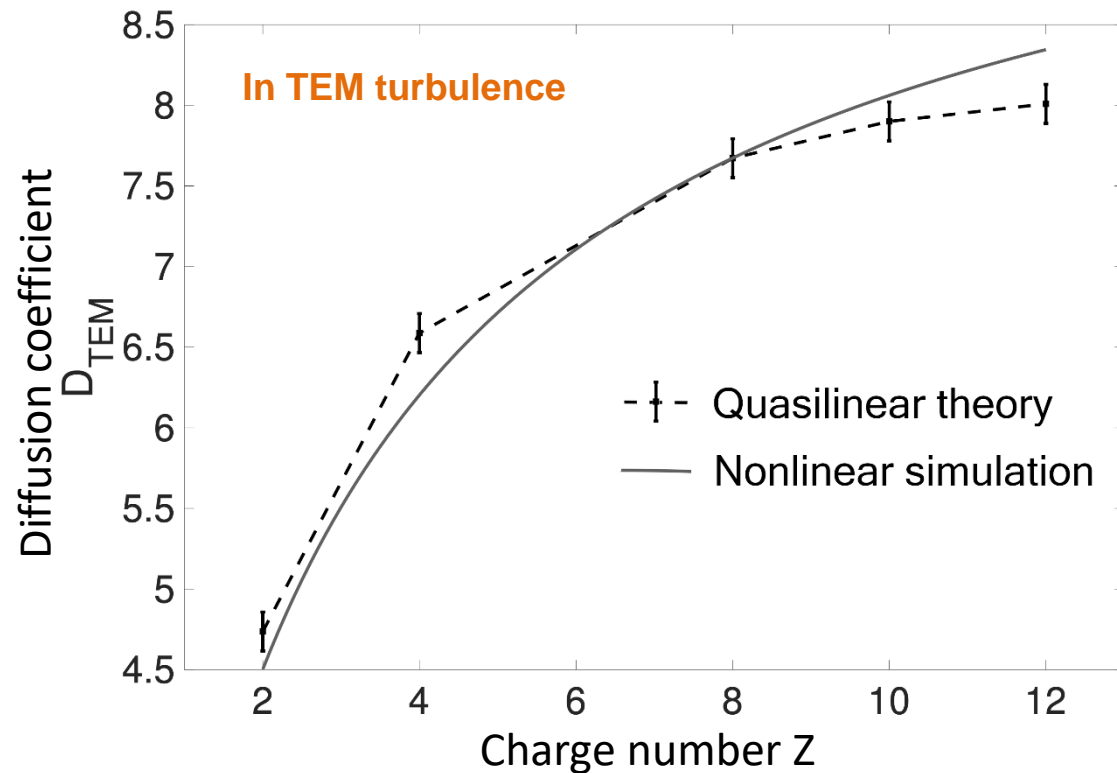
Isolating particle diffusion

- Flat impurity temperature profile
- Curvature drift artificially switched off

Scan in mass (A) and charge (Z) of impurities

- Dependency depends on the nature of dominant instabilities :
 - TEM → Diffusion ↑ as Z ↑
 - TIM → Diffusion ↓ as Z ↑
- Weak dependency on A (diffusion ↓ slightly as A ↑)
- Qualitative agreement with quasi-linear theory

$$\Gamma_Z = -D_Z [\nabla n_Z + \cancel{C_T \nabla T_Z} + \cancel{C_P \nabla q}]$$



[Gravier PoP'19]

Thermo-diffusion brings impurities inwards in TEM turbulence, but outwards for TIM

Isolating thermo-diffusion

- Curvature drift artificially switched off
- Impossible to maintain flat impurity density gradient

⇒ impurity density gradient such

that $\Gamma_z = 0$, then $V_z = D_z \frac{\nabla n_z}{n_z}$

obtained from density scan

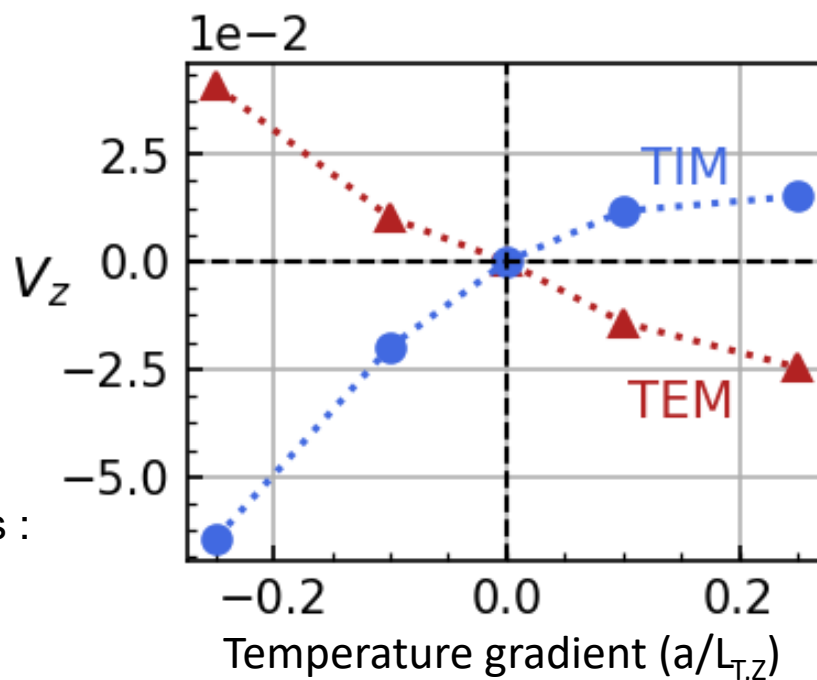
$$\Gamma_z = -D_z [\nabla n_z + \color{red}{C_T} \nabla T_z + \cancel{C_P \nabla q}]$$
$$= -D_z \nabla n_z + n_z V_z$$

Scan in temperature gradient

- For standard sign of impurity temperature gradient, thermodiffusion transport impurities :

TEM → inwards

TIM → outwards



Scan in charge number

- The coefficient $\color{red}{C_T} \downarrow$ as $Z \uparrow$

[Lim PPCF'20]

Curvature pinch is inward except for reversed magnetic shear

Isolating curvature pinch

- Flat impurity temperature profile
- Focus near zero impurity density gradient

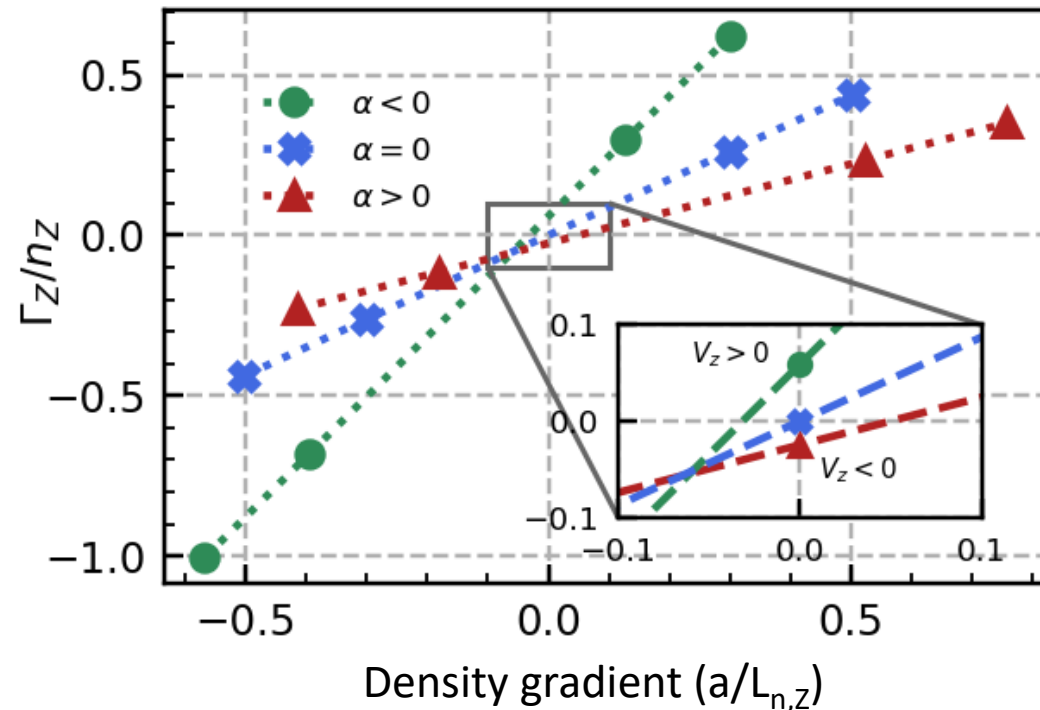
Role of magnetic shear

- Reversed magnetic shear can change the sign of precession frequency
- Artificial coefficient α in front of $\omega_{d,Z}$ to model this effect

Scan in density gradient

- Curvature pinch is inward except for reversed magnetic shear

$$\Gamma_Z = -D_Z[\nabla n_Z + C_T \nabla T_Z + C_P \nabla q]$$



[Lim PPCF'20]

Summary

Scan in impurity concentration

- TEM growth rate and turbulence intensity decrease with increasing tungsten concentration, linearly for concentrations below $5 \cdot 10^{-4}$
- For turbulent transport of W^{40+} , passive treatment valid for $C_W < 2 \cdot 10^{-4}$

Parametric dependencies of impurity transport

$$\Gamma_Z = -D_Z [\nabla n_Z + C_T \nabla T_Z + C_P \nabla q]$$

Increases (decreases) with increasing Z for TEM (TIM)

Thermodiffusion:

TEM → inwards

TIM → outwards

$C_T \downarrow$ as $Z \uparrow$

Curvature pinch: inward except for reversed magnetic shear

Acknowledgements

- Agence Nationale de la Recherche, project GRANUL (ANR-19-CE30-0005)
- Euratom research and training programmes, Grant Agreement No. 633053, project WP17-ENRCEA-02
- CINECA Marconi (projects GSNTIT and GSNTITS), EXPLOR (project 2017M4XXX0251), IDRIS

