

A New Hybrid Model for Efficient Simulation of Ion Scale Electromagnetic Turbulence in Tokamak Plasma

Janghoon Seo, Jae-Min Kwon, Sumin Yi, Kimin Kim, and Lei Qi

Korea Institute of Fusion Energy

seojh@kfe.re.kr

ABSTRACT

- A new hybrid gyrokinetic model is developed and implemented for the electromagnetic turbulence simulations.
- In this model, a massless fluid model is adopted for passing electrons, while the conventional gyrokinetic model and the bounce kinetic model are applied to ions and trapped electrons, respectively.
- Linear growth rates of ITG, TEM and KBM are benchmarked with other numerical codes, which shows reasonable agreement.
- The stabilizing effect of plasma elongation on KBM is studied by using this model.

BACKGROUND

- There are a lot of difficulties in developing a feasible simulation model for electrons, mainly due to their fast time scale compared to the ion dynamics.
- A mixture of the bounce averaged model for trapped electrons and a massless fluid model for passing electrons were suggested previously. [Hinton F.L. et al., PoP (2003)]
- In this work, the model is implemented numerically into the gyrokinetic code gKPSP and tested for the linear growth rate of electromagnetic instabilities.

NUMERICAL METHODS

• Electron model

1. Continuity equation

$$\begin{aligned} \frac{\partial}{\partial t} \delta n_e &= [\mathbf{B}_0 + \delta \mathbf{B}_\perp] \cdot \nabla \left(\frac{\delta j_{\parallel e}}{e_c B_0} \right) + \frac{1}{m_e |\Omega_e| B_0^2} \mathbf{B}_0 \times \nabla B_0 \cdot \nabla (\delta P_{\perp e} + \delta P_{\parallel e}) \\ &+ \frac{\nabla \times \mathbf{B}_0}{m_e |\Omega_e| B_0^2} \cdot [(\delta P_{\perp e} - \delta P_{\parallel e}) \nabla B_0 + B_0 \nabla \delta P_{\parallel e}] - c \frac{\mathbf{B}_0 \times \nabla \Phi}{B_0^2} \cdot \nabla (n_{e0} + \delta n_e) \\ &- c \frac{n_{e0} + \delta n_e}{B_0^2} \left[2 \frac{\mathbf{B}_0}{B_0} \times \nabla B_0 + \nabla \times \mathbf{B}_0 \right] \cdot \nabla \Phi \end{aligned}$$

2. Faraday's law combined with Ohm's law

$$\frac{1}{c} \frac{\partial}{\partial t} A_{\parallel} = \frac{T_{e0}}{e_c B_0} \delta \mathbf{B}_\perp \cdot \nabla (\ln n_{ep0}) + \frac{\mathbf{B}_0 + \delta \mathbf{B}_\perp}{B_0} \cdot \left[\frac{T_{e0}}{e_c} \nabla \left(\frac{\delta n_{ep}}{n_{ep0}} \right) - \nabla \Phi \right]$$

• Time integration method

: The IMEX (implicit-explicit) Runge-Kutta algorithm is used to mitigate the severe time step restriction related to the shear Alfvén wave propagation.

1. stiff linear parts of the field equations -> treated by the implicit method
2. nonlinear parts -> treated by the explicit method

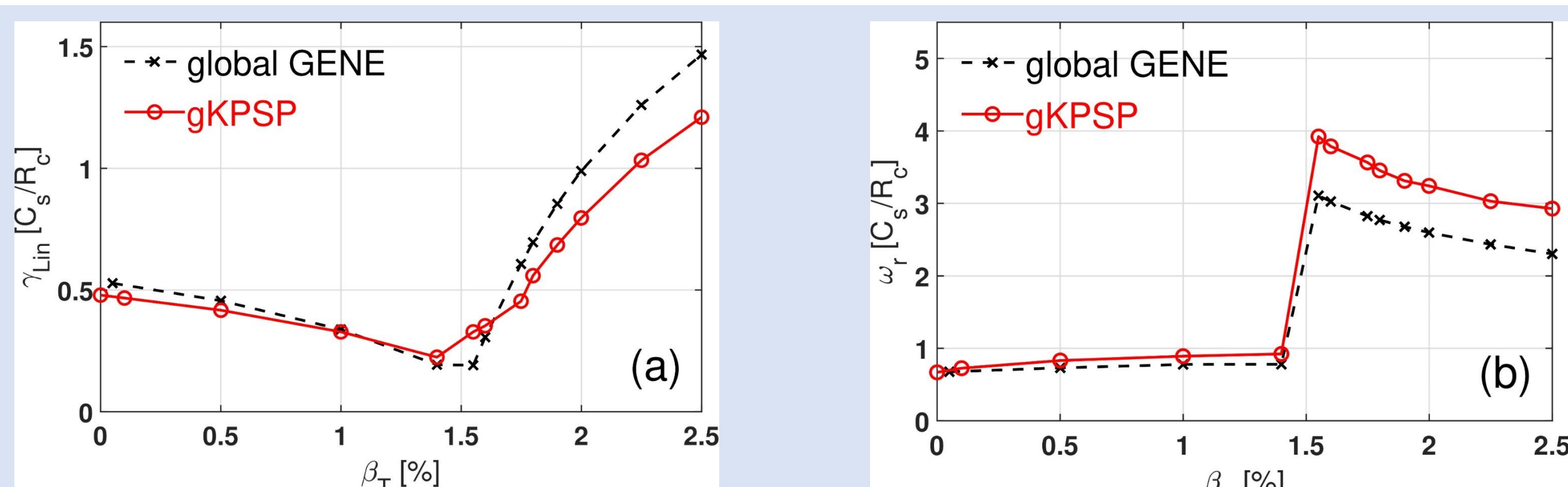


Fig 1. (a) γ_{Lin} (b) ω_{real} of ITG/KBM with varying plasma β

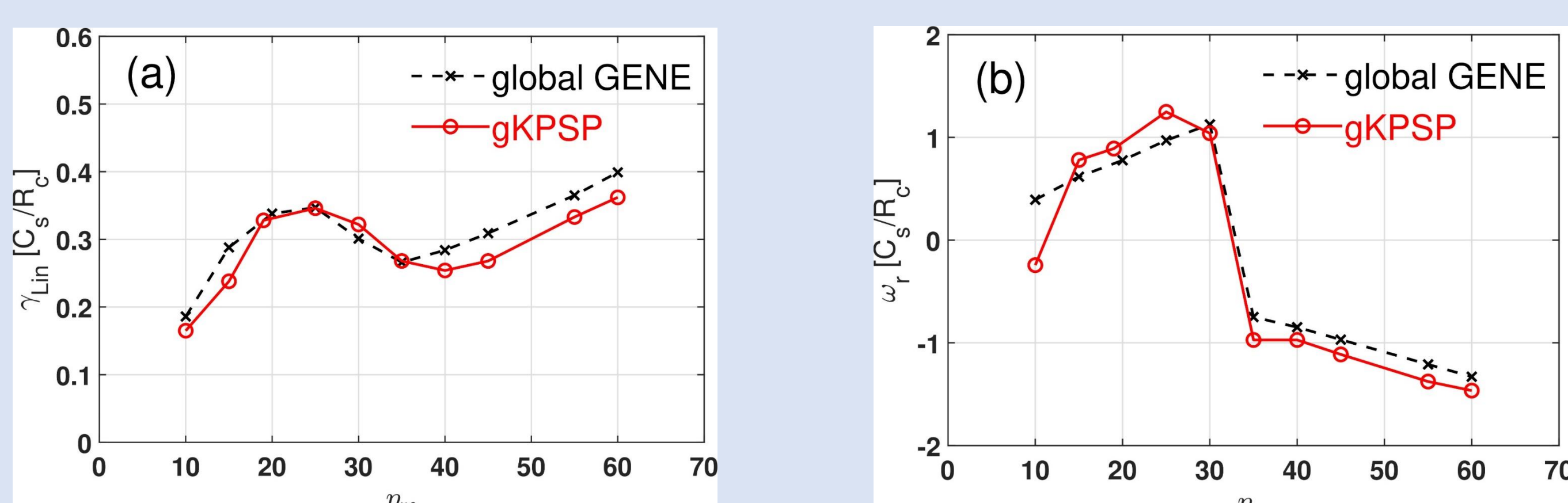


Fig 2. (a) γ_{Lin} (b) ω_{real} of ITG/TEM with varying toroidal mode number

RESULT

• γ_{Lin} benchmark for ITG-TEM-KBM

: The linear growth rates γ_{Lin} of ITG-TEM-KBM are benchmarked with GENE code results. [Görler, T. et al., PoP (2016)]

1. ITG/KBM with varying plasma β : Fig 1.
2. ITG/TEM with varying toroidal mode number : Fig 2.

: As can be seen in Fig 1 & 2, the newly developed model shows reasonable agreement with GENE results.

• Stabilizing effects of elongation

: The elongation κ has a stabilizing effect on KBM, as shown in Fig 3 (a).

: As κ increases, the magnitude of parallel wave number k_{\parallel}^2 also increases, which is shown in Fig 3 (b).

: Since k_{\parallel}^2 has a stabilizing effect on KBM [Kim J. et al., Phys. Fluids (1993)], the increased k_{\parallel}^2 is consistent with the stabilizing effect of the elongation.

• Linear TAE simulation

: The growth rate of TAEs driven by varying fast ion energies is tested with the parameters from [Könies A. et al., NF (2018)], which is shown in Fig 4.

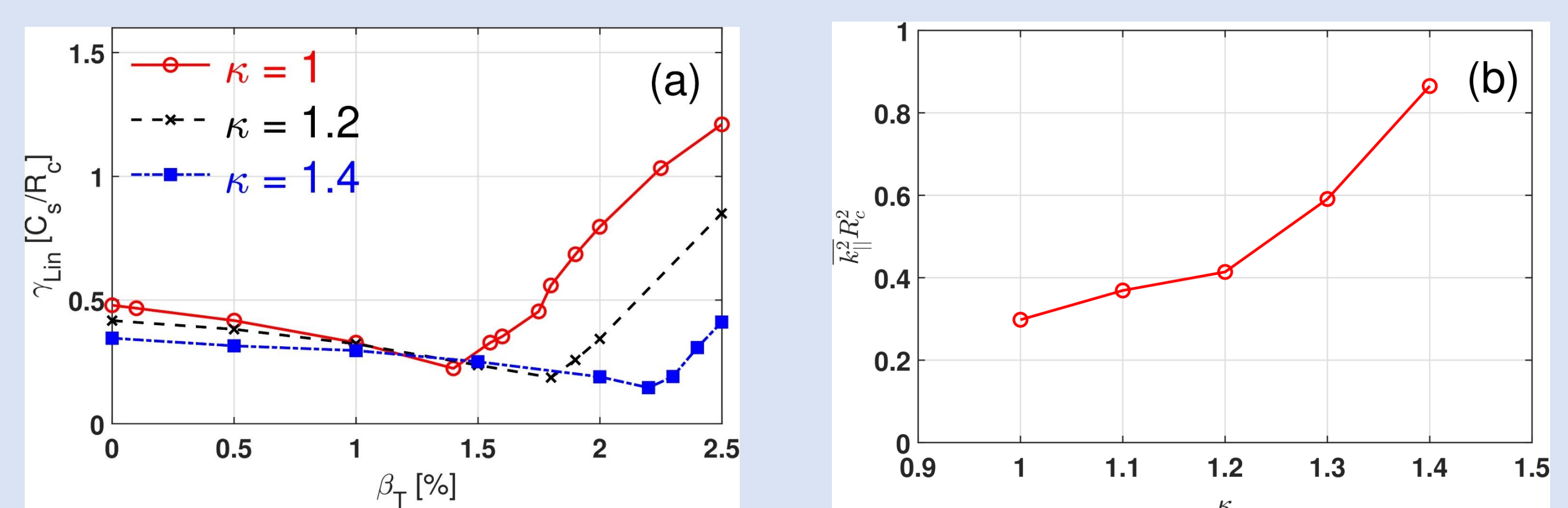


Fig 3. (a) γ_{Lin} of ITG/KBM with different κ
(b) the magnitude of parallel wavenumber with different κ

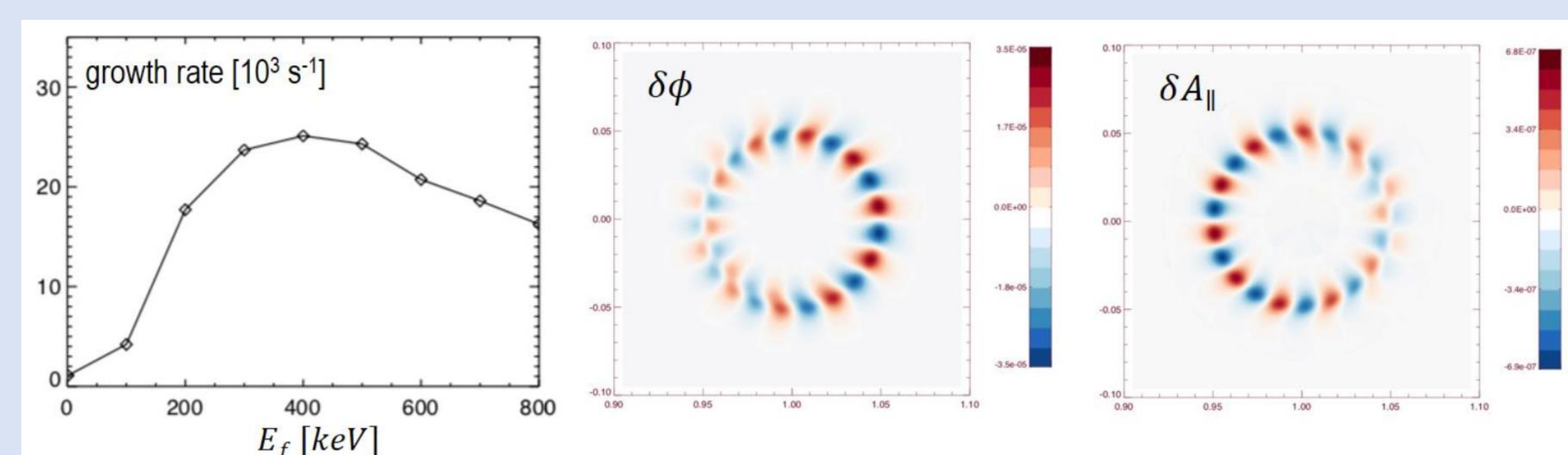


Fig 4. left : γ_{Lin} of TAE with varying temperature of fast ions
middle & right : electrostatic and electromagnetic potential, respectively

CONCLUSION

- A new hybrid electromagnetic scheme with a massless fluid model for passing electrons is implemented numerically.
- Benchmarks for linear growth rates with other codes show reasonable agreement.
- Elongation of magnetic geometry is shown to have a stabilizing effect on the KBM linear instability, which is consistent to the broadened k_{\parallel} spectrum with higher elongation.
- A nonlinear scheme with this hybrid model is under development.

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