

# Nonlinear equilibria and transport processes in burning plasmas

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## ABSTRACT

- We introduce a theoretical framework to describe transport in the phase space based of the theory of Phase Space Zonal Structures (PSZS) [1-5]
- we extend the usual definition of plasma equilibrium in the presence of a residual level of electromagnetic fluctuations, i.e. the Zonal State (ZS)
- governing equations are derived by means of Gyrokinetic transport theory
- as a simple application, we describe ZS evolution in the absence of symmetry breaking fluctuations
- we show the evolution of PSZS during an EPM simulation by means of HMGC [6]

## BACKGROUND

- Predicting the dynamics of a burning plasma over long time scales, i.e. comparable with the energy confinement time or even longer, is essential to understand next generation fusion experiments
- most of the works for the study of core plasma transport are based on a systematic separation of scales between the reference equilibrium and fluctuations
- energetic particle (EP) transport in fusion devices is a spatiotemporal multi-scale process
- spatio-temporal mesoscales can be observed even in drift wave plasma turbulence simulations
- in a recent work [2] we have emphasized the fundamental importance of the self-consistency of the adopted description, including the determination of the characteristic spatiotemporal scales of the reference state

## PHASE SPACES ZONAL STRUCTURES (PSZS)

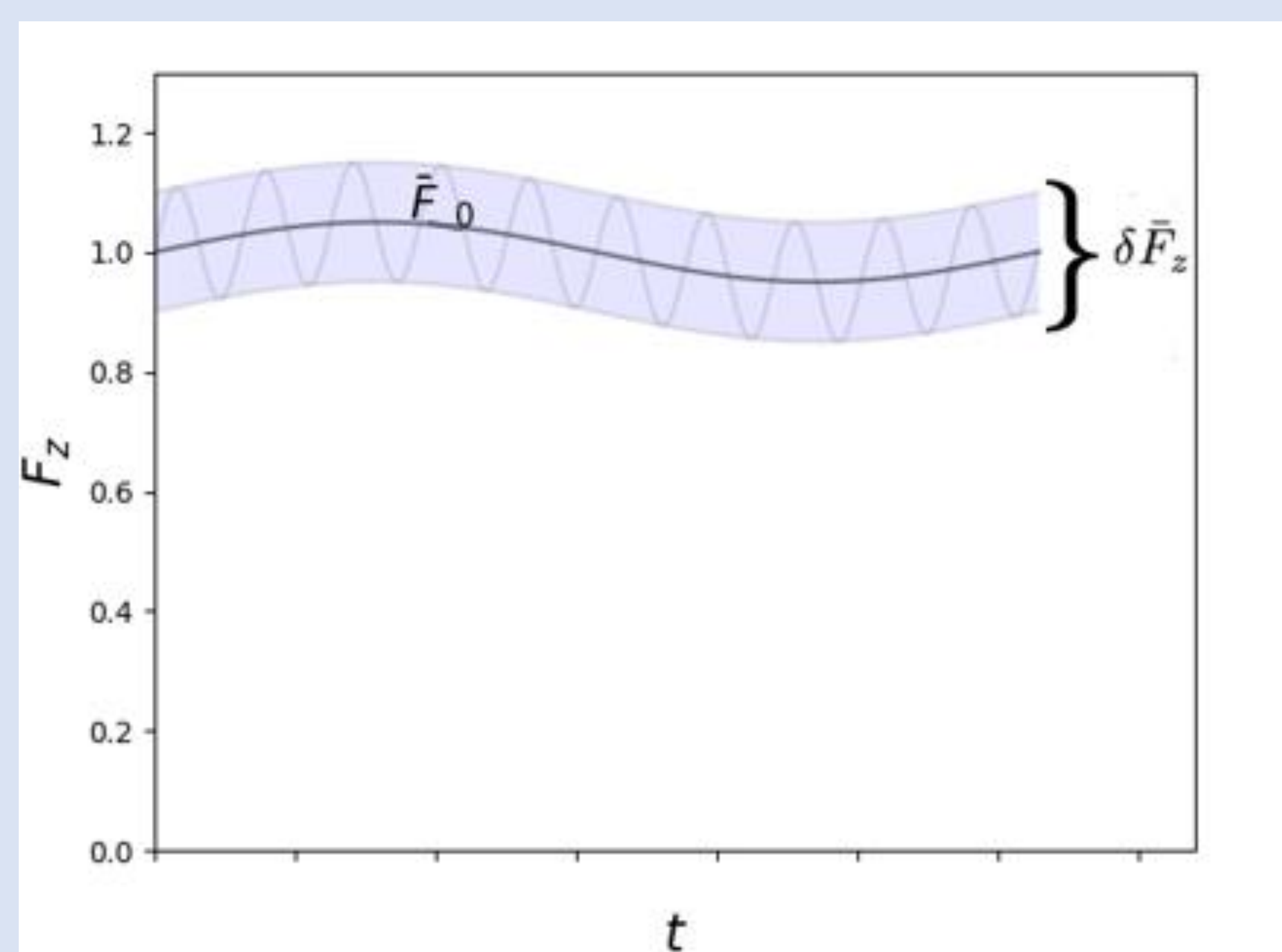
- PSZS equation is connected with the macro- meso-scopic component unperturbed orbit-averaged distribution function:

$$\frac{\partial}{\partial t} \overline{F_{z0}} + \frac{1}{\tau_b} \left[ \frac{\partial}{\partial P_\phi} (\tau_b \delta \dot{P}_\phi \delta F) + \frac{\partial}{\partial \mathcal{E}} (\tau_b \delta \dot{\mathcal{E}} \delta F) \right]_s = \overline{(\sum_b C_b^g [F, F_b] + \mathcal{S})}_{zS}$$

- we can decompose the toroidally symmetric distribution function

$$F_z = \overline{F_{z0}} + \delta \overline{F_z} + \delta \tilde{F}_z$$

- micro-scales are accounted by  $\delta \tilde{F}_z$  while macro- & meso-scales are described by PSZS



Equilibrium orbit averaged distribution

## ZONAL STATE (ZS)

- Computing the ZS dynamics require equations for the zonal field structures (ZFS), i.e. the long lived component of toroidal symmetric fields
- assume, for simplicity, that ZS is characterized predominantly by the scalar potential  $\delta \phi_z$
- we can study its self-consistent evolution in the absence of symmetry breaking fluctuations
- the scalar ZFS is obtained substituting the orbit averaged distribution function into the quasi neutrality condition:

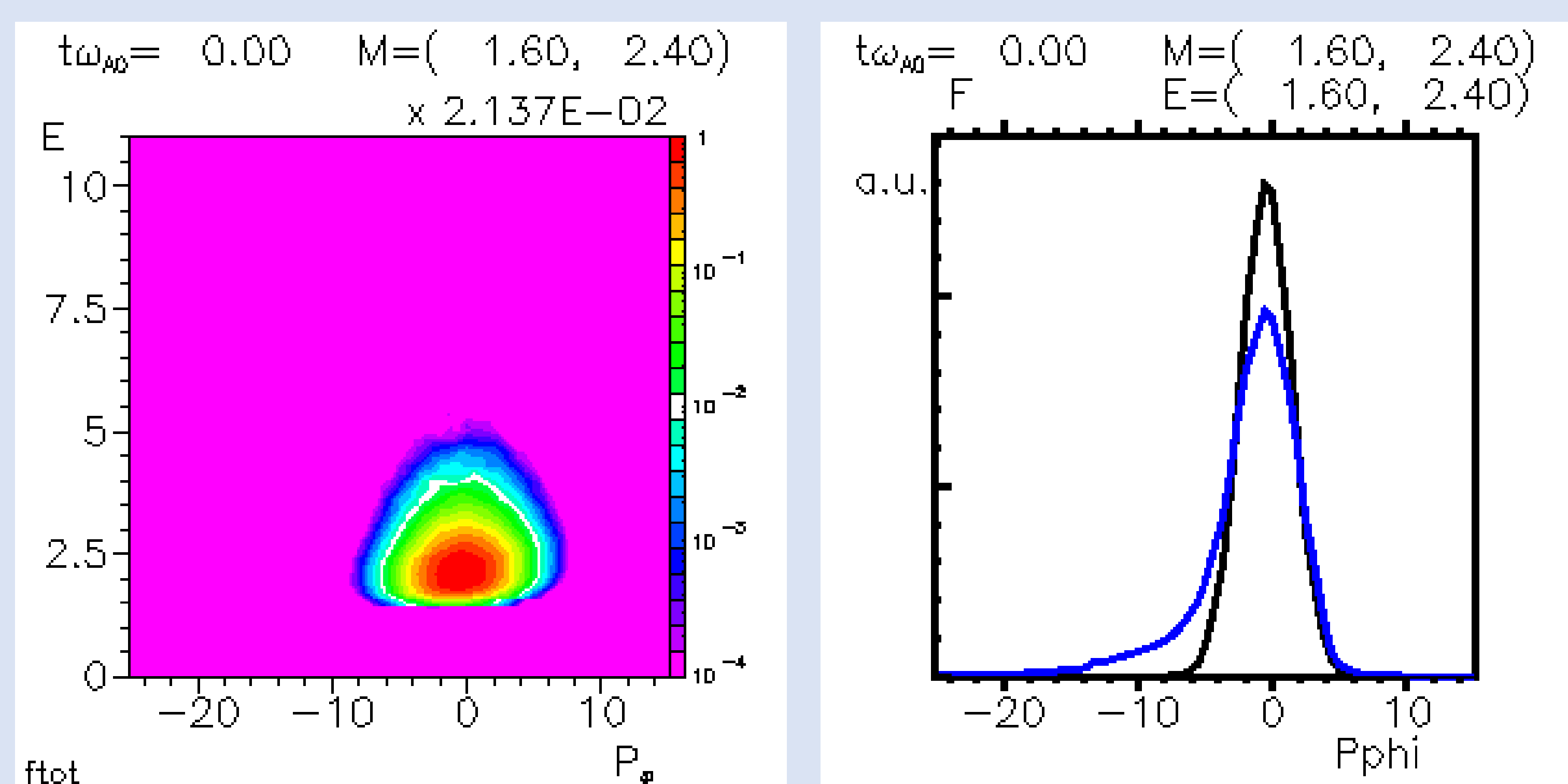
$$\sum_s \left\langle \frac{e^2}{m} \frac{\partial F_{z0}}{\partial \mathcal{E}} \right\rangle_v \delta \phi_z + \sum_s \langle e \hat{I}_0 \delta G_z \rangle_v = 0$$

$$(\partial_t + \omega_b \partial_{g_c}) \delta G_B = -e^{-iQ_z} \left[ \frac{e}{m} \frac{\partial F_{z0}}{\partial \mathcal{E}} \hat{I}_0 \partial_t \delta \phi_z + NL \right]$$

- substituting the  $l = 0$  component into the flux surface averaged QN:

$$\sum_s \frac{V'_\psi}{4\pi^2} \frac{e^2}{m_s^2} \left\langle \left\langle \frac{\partial F_{z0}}{\partial \mathcal{E}} \delta \phi_z - e^{-iQ_z} \hat{I}_0 e^{iQ_z} \hat{I}_0 \frac{\partial F_{z0}}{\partial \mathcal{E}} \delta \phi_z \right\rangle_v \right\rangle_\psi = \sum_s \sum_\sigma \int d\mathcal{E} d\mu \tau_B e^{\frac{i}{\omega} \overline{e^{iQ_z} \hat{I}_0 e^{iQ_z} NL}}$$

- $F_{z0}$  is an arbitrary (renormalized) anisotropic distribution function;
- neglecting the non linear term we can study the polarizability in arbitrary geometry and realistic  $F_{z0}$ ;
- results known in literature, e.g. Wang and Hahm 2009 ; Lu et al. 2019 , are recovered in the proper limits;
- GAM/EGAM dispersion relations retaining finite Larmor radius and finite orbit width effects can be derived according to this expression;



PSZ evolution during an EPM simulation by HMGC [6]

## CONCLUSION

- we have introduced the concept of zonal state to describe the evolution of the plasma between neighboring nonlinear equilibria;
- governing equations for all the components of the ZS have been derived;
- the system is closed by the governing equations for em potentials.

## ACKNOWLEDGEMENTS / REFERENCES

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