

Mechanical and Aerospace Engineering







## On Effect of n=2 RMP to Edge Pedestal in KSTAR with Nonlinear MHD Simulation

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RMP-induced pedestal degradation are successful explanation for ELM suppression, but have some difficulties in explaining experiment

- RMP is promising ELM suppression method [T. Evans 2004]
  - ✓ Linearly stabilized ELMs with degraded pedestal by RMP-induced islands and stochastic region [Q. Hu PRL 2020].
     → One of promising/successful explanation.
- Addition concept may be needed for full explanation
  - ✓ Possible difficulty to solely describe pedestal degradation with islands.
     → Additional transport induced by RMPs.
  - ✓ Limitations to explain ELM-like mode during suppression. [J. Lee PRL 2016].
    - Contradiction to linearly stabilized ELMs by Degraded pedestal.



Previous work reveals that RMP can induce other transport mechanism and directly affect ELM stability as well as pedestal degradation

- Previous studies on RMP-induced transport
  - ✓ Micro-instabilities [1,2].
  - ✓ Edge kink response [3,4].
  - ✓ Neoclassical toroidal viscosity (NTV) [5,6].
- Direct effect of RMPs on the ELM stability
  - ✓ Effect of RMP induced field structures on ELM stability [7,8].
  - $\checkmark$  ELM mitigation/suppression by RMP-ELM interaction [9-12].

RMP-driven ELM crash suppression considering these aspects.[1] I. Holod et al., Nucl. Fusion 57 (2017), 016005[5] Y.Liu et al., Nucl. Fusion 60 (2020), 036018[9] M. Becoulet et al., PRL 113 (2014), 115001[2] R. Hager et al., Nucl. Fusion 60 (2020),[6] J. Park et al., POP 16 (2009) 056115[9] M. Becoulet et al., PRL 113 (2014), 115001[10] F. Orain et al., Phys. Plasma (2019), 042503

[3] E. Nardon et al., Nucl. Fusion 50 (2010), 034002 [4] F. Orain et al., Nucl. Fusion 57 (2017), 102510

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[5] Y.Liu et al., Nucl. Fusion 60 (2020), 036018
[6] J. Park et al., POP 16 (2009) 056115
[7] M. Willensdorfer et al., PRL 119 (2017), 085002
[8] M. L. Mou et al., Phys. Plasma 25 (2018), 082518

Nonlinear MHD simulation is performed to investigate the

[9] M. Becoulet et al., PRL 113 (2014), 115001
[10] F. Orain et al., Phys. Plasma (2019), 042503
[11] J. Kim et al., Nucl. Fusion (2019), 096019
[12] S.K. Kim et al., Nucl. Fusion (2020), 026009





- 1. Simulation setup
- 2. Effect of RMP-induced plasma response on pedestal profile
- 3. RMP-induced ELM-crash suppression
- 4. Summary

### JOREK and PENTRC coupled simulation is developed to simulate RMP-ELM dynamics including RMP response and NTV transport

- JOREK (3D Nonlinear MHD) [G. Huysmans 2009]
  - ✓ Realistic geometries with scrape-off layer is included.
  - ✓ Reduced MHD equation [F. Orain 2013] is used.

 $\frac{\frac{1}{R^{2}}\frac{\partial\psi}{\partial t}}{\partial t} = \eta(T)\nabla \cdot \left(\frac{1}{R^{2}}\nabla_{\perp}\psi\right) - \vec{B} \cdot \left(\nabla u - \tau_{IC}\frac{\nabla p_{e}}{\rho}\right) \qquad Ohm's \ law \qquad w' \ toroidal \ rotation \\ w' \ ion \ diamagnetic \\ w' T_{i} = T_{e}$   $\frac{\partial\rho}{\partial t} = -\nabla \cdot (\rho\vec{v}) + \nabla \cdot (D\nabla\rho) + S_{\rho} \qquad Continuity \ eqn.$   $\frac{\rho\left(\frac{\partial}{\partial t} + \vec{v} \cdot \nabla\right)\left(\vec{v}_{E} + \vec{v}_{||}\right) = -\nabla(\rho T) + \vec{J} \times \vec{B} + S_{v} - \vec{v}S_{\rho} + \mu\Delta\vec{v} - \nabla \cdot \vec{\Pi}_{neo}}{\left(\nu_{||}, w\right)} \qquad Momentum \ eqn. \\
\frac{\partial(\rho T)}{\partial t} = -\left(\vec{v}_{E} + \vec{v}_{||}\right) \cdot \nabla\rho T - \gamma\rho T \ \nabla \cdot \left(\vec{v}_{E} + \vec{v}_{||}\right) + \nabla \cdot (\kappa\nabla T) + (1 - \gamma)S_{T}$   $\frac{d(\rho T)}{\partial t} = -\left(\vec{v}_{E} + \vec{v}_{||}\right) \cdot \nabla\rho T - \gamma\rho T \ \nabla \cdot \left(\vec{v}_{E} + \vec{v}_{||}\right) + \nabla \cdot (\kappa\nabla T) + (1 - \gamma)S_{T}$ 

- PENTRC (NTV) [N. Logan 2013]
  - ✓ NTV calculation code based on the given plasma equilibrium, profiles, and plasma displacements.
  - ✓ Inclusion of NTV by JOREK-PENTRC coupling.



## n = 2 RMP-driven ELM crash suppression in KSTAR is numerically reproduced

- Reference discharge
  - $\checkmark$  KSTAR ELM suppression discharge (#18594) with n=2 ( $\phi=90^{\circ}$ ) RMPs.

$$\checkmark I_{\rm p} = 690 \, {\rm kA}, \ q_{95} \sim 4, \beta_{\rm N} \sim 2., \overline{n}_{\rm e} = 3.3 \times 10^{19} \, {\rm m}^{-3}.$$

- ✓ Stable ELM suppression entry at  $I_{\rm RMP} \ge 3.5$  kA.
- ✓ Simulation with x10 larger neoclassical resistivity due to numerical reasons.
- ✓ Simulation with  $I_{\rm RMP} = 4$ kA.



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## RMP response is the kink-tearing response which can contribute to the enhanced convective/conductive pedestal transport

- Kink tearing responses by RMP
  - ✓ Kink + tearing response (KTM).
- Kink  $\{\checkmark$  Edge localized perturbation.
- Tearing  $\int V_{\perp e} = 0$  layer and finite resistivity.  $\checkmark$  Field penetration into the pedestal.



- $\checkmark V_{\rm E \times B}$  and stochastic layer in the pedestal.
- $\checkmark\,$  Degradation of the mean pedestal.
- ✓ Increased radial flux due to
  - $\Gamma_{\mathrm{E} imes \mathrm{B} \perp}$  convection (Mainly  $n_{\mathrm{e}}$ ).
  - Island and stochastic layer ( $n_{
    m e}$  and T).





## Plasma response causes NTV particle transport, resulting in further pedestal degradation, partially explaining pump-out

- NTV induced by plasma response
  - ✓ Plasma displacement ( $\xi_{\perp}$ ) induced by RMPs.
  - ✓ Resulted NTV fluxes.
    - Torque  $au_{
      m NTV}$
    - Particle flux  $\Gamma_{NTV}$
- Effect of NTV transport
  - ✓ Further degradation of  $n_{\rm e}$  pedestal by  $\Gamma_{\rm NTV}$ ✓ Kink + NTV (40% of Exp.).
    - → Considerable effect of kink and NTV on pump-out.



### MHD modeling with NTV explains pedestal degradation to some extent, but additional mechanism has to be introduced for full explanation

- Net decrease in pedestal gradient
  - Pedestal degradation by plasma response
     + NTV transport.
  - ✓ ~40% decrease in pressure gradient (close to Experimental level).



[Decreased pressure gradient by RMP]

- Additional pump-out mechanisms
  - ✓ RMP induced micro-instabilities [R. Hager 2020].
  - ✓ Particle transport by polarization drift [Q. Hu 2019].
    - $\rightarrow$  They will be needed to fully explain the pump-out.

ExB convection and NTV flux largely contribute to the pump-out, but full explanation requires additional transport mechanisms.

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### Natural ELM simulation (without RMPs) shows good agreement with experimental observations

- Linear ELM simulation
  - ✓ Consistent dominant  $n_{\rm ELM} = 12$ .
  - ✓ Consistent poloidal velocity  $V_{\theta,\text{ELM}}$ ~3 km/s.
  - ✓  $V_{\theta,\text{ELM}} \approx V_{\theta,\text{E}\times\text{B}}$  (ion diamagnetic) [1,2].
- Nonlinear phase
  - $\checkmark\,$  Mode crash during nonlinear phase.
  - $\checkmark \Delta W_{\rm ELM,sim} \approx 8 \, {\rm kJ} \, (\Delta W_{\rm ELM,exp} \approx 7 \pm 4 \, {\rm kJ}).$
  - → Experimentally relevant ELM is obtained. ( $V_{\theta,\text{ELM}} \approx V_{\theta,\text{E}\times\text{B}}$ )





<sup>[</sup>Mode amplitude in NL phase]

[1] M. Becoulet M. et al, NF (2017), 116059[2] J. Morales, POP (2016), 042513

# ELM crash suppression by experimentally relevant RMP configuration is successfully reproduced in the simulation

- RMP-driven ELM crash suppression
  - ✓ Strongly suppressed mode amplitude.
  - ✓ Disappeared bursty nonlinear mode crash.



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  - ✓ Disappeared bursty nonlinear mode crash.
  - ✓ Existing filament structures in suppression case.
  - ✓ Spatially locked structure [J. Lee 2019].
    - → ELM is nonlinearly saturated rather than linearly stabilized, so filament can remain.



[Nonlinear evolution of ELM]



[Filament motions]

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- Suppression above RMP threshold
  - ✓ Mitigated with small RMP amplitude.
  - ✓ Fully suppressed at  $I_{\rm RMP}$  > 3 kA.

 $\rightarrow$  It is consistent to experimental level (~4kA).



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## Degraded pedestal and RMP-ELM mode coupling make ELM crash suppression, but they must participate simultaneously

• Effect of degraded pedestal on ELM stability

✓ ~40% decreased pedestal gradient by RMPs.

✓ ~65% decreased growth rate.

Coupling between RMP and ELM harmonics



**Degraded pedestal** 

RMP-ELM coupling

- No crash suppression without coupling effect.
   (Even with decreased growth rate)
- ✓ ELM crash suppression by combined two effects.







## RMP-ELM coupling further degrades the pedestal by increasing transport, resulting in the reduced ELM instability

- Enhanced pedestal transport by coupling effect
  - ~15% increased radial perturbed fields by coupling effect. (Tearing component)
  - $\checkmark$  Enhanced pedestal transport with increased island width.
  - $\checkmark\,$  Further decrease of pedestal gradient.

→ Reduced ELM instability source



## **RMP-ELM coupling results in broad mode spectrum and increased interactions between ELM harmonics, preventing unstable ELM crash**

- Enhanced harmonic interactions by coupling effect
  - ✓ Unlike ELMy, enhanced energy correlation among harmonics. [J. Kim NF 2019]
  - ✓ Broadened mode spectrum.
  - ✓ Large growth of unstable harmonic: ELM crash
  - ✓ Prevented mode crash due to broad spectrum and mode interactions. [P. W. Xi, PRL 2014]
  - ✓ Therefore, nonlinearly saturated ELMs by



✓ Important quantities for RMP-ELM coupling?





**time** [Mode spectrum vs time]

# Overlap of magnetic islands near the pedestal top can be important to RMP-ELM coupling and ELM suppression

- Spatial overlap of harmonics
  - ✓ Overlap of harmonics: Favorable to their couplings [Rhee POP2015].
  - ✓ Existing harmonics,
    - ELM harmonics
    - RMP-Kink (peeling)  $\rightarrow$  Localized to LCFS.
    - RMP-Tearing (island) → Wide radial range.
- Island overlap near the pedestal top
  - $\checkmark$  I<sub>RMP</sub> scan to adjust island width near pedestal top.
  - ✓ ELM suppression entry where island overlap starts.
     (Chiricov S = 1 between 8/2+9/2)
- → Overlap of RMP-induced islands can be advantageous for RMP-ELM coupling and suppression.



n=2 Island overlap



Slow poloidal rotation of ELM structure can be advantageous for enhancing the RMP-ELM interaction and achieving ELM suppression

- Poloidal mode rotation and RMP-ELM coupling
  - ✓ Well sustained mode overlap: Favorable to coupling.
  - ✓ Sustained spatial overlap ( $|V_{\theta,ELM} V_{\theta,RMP}| \approx 0$ ). → Stationary phase difference ( $\delta$ ) of RMP and ELM.



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  - ✓ Static RMP, V<sub>θ,RMP</sub> = 0.
     →V<sub>θ,ELM</sub> ≈ 0 to make stationary δ.



**Time** [*Time evolution of*  $\cos \delta$ ]



<sup>[</sup>Filament motions]

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  - ✓ Sustained spatial overlap ( $|V_{\theta,ELM} V_{\theta,RMP}| \approx 0$ ). → Stationary phase difference ( $\delta$ ) of RMP and ELM.
  - ✓ Static RMP,  $V_{\theta,RMP} = 0$ . → $V_{\theta,ELM} \approx 0$  to make stationary δ.
- Small  $V_{\theta, E \times B}$  for RMP-ELM interaction
  - ✓  $V_{\theta,\text{ELM}} \approx V_{\theta,\text{E}\times\text{B}}$  [1, 2] at pedestal. →  $V_{\theta,\text{E}\times\text{B}} \approx 0$  is favorable.
  - ✓ No suppression with <u>large</u>  $V_{\theta,E\times B}$  at pedestal top.
    - → Small  $V_{\theta,\text{ELM}}$  (or  $V_{\theta,\text{E}\times\text{B}}$ ) be advantageous for RMP-ELM coupling and suppression.





1.0



Oscillatory  $V_{\theta,\text{ELM}} \gg 0$ 

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4000

### **Summary**

- n=2 RMP-driven pedestal degradation and ELM suppression
  - ✓ Pedestal degradation by RMP response and NTV, explaining the experiment to some extent.
  - ✓ Numerical reproduction of nonlinearly saturated ELM suppression.
    - Reduced pedestal gradient.
    - Mode coupling between RMP and ELM.

### RMP-ELM coupling contributes to the ELM-crash suppression

- ✓ Further decreasing pedestal gradient.  $\rightarrow$  ELM driving source ↓
- $\checkmark$  Enhanced interactions between ELM harmonics.  $\rightarrow$  Prevent NL mode crash

### Favorable conditions for RMP-ELM coupling

- ✓ Overlap of RMP-induced islands near the pedestal top.
- ✓ Small rotation of ELM structure or  $V_{\theta,E\times B} \approx 0$  at the pedestal.



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## **Thank You**





### Backup – Plasma displacement from JOREK perturbation

• Approximated displacement from nonlinear perturbation



- ✓  $T_{n=0}$  is dominant.
- $\checkmark$  Uniformity of T on the flux surface due to large parallel heat conduction.
- ✓ Therefore,  $\xi_{\perp,n,m} \sim -\delta T_{n,m} / \nabla T_{n'=0}$
- ✓ Less accurate under the presence of stochastic layer.
- ✓ No  $\delta B_{\parallel}$  component in reduced MHD.
- ✓  $\xi_{\parallel}$  derived from linearized force balance equation ( $\delta F(\xi_{\perp}, \xi_{\parallel}) = 0$ ).

# Backup - In summary, RMP-ELM coupling can contribute to ELM crash suppression in two aspects

• Role of RMP-ELM coupling in ELM crash suppression

### **ELM Crash Suppression**



Important quantities for RMP-ELM coupling?

Spatial overlap between RMP-induced modes and ELM harmonics seems to be important.

### Numerical setup

- ✓ Neoclassical constraint ( $V_{neo}$ ) is applied to construct the ion-poloidal flow.
- $\checkmark V_{\theta, E \times B}$  in the pedestal region is in the <u>ion-diamagnetic</u> direction.
- $\checkmark T_i = T_e$  is assumed.
- ✓ Adaptive diffusive profile and source are used to sustain the  $\rho$ , T,  $v_{\phi}$  profiles.
- ✓ x10 resistivity (x40 spitzer) and braginskii parallel conductivity are used.



# Backup - Coupling simulation shows experimentally reasona ble results

- Code coupling test
  - ✓ Well reconstructed  $\xi_{\perp}$  including kink and partial tearing component.
  - ✓ Successful calculation of NTV-driven particle flux and torque.
  - ✓ A reasonable value from code coupling.



### **Backup – tearing response**

### Tearing response

40

20

-20

0.8

 $v_{\perp}$  [km/s]

- ✓ Perturbed current shields the external field.
- $\checkmark v_{\perp e} pprox 0$  layer and finite resistivity in the edge weaken the field shielding.
- $\checkmark$  Field penetration occurs in the pedestal region.

 $2\pi$ 

 $heta_{
m geo}$ 

0.8

1.1

✓ As a result, stochastic layer is formed.

 $v_{\perp,e} = 0$ 

1.0

 $\psi_{\rm N}$ 

[Perpendicular flow profile]



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0.9

 $v_{\perp, E imes B}$ 

 $v_{\perp.e}$ 

### Backup – profile comparison (kink-tearing only)

- Pedestal profile degradation
  - ✓ Radial transport increases due to
    - $v_{\mathrm{E} imes \mathrm{B} \perp}$  convection (Kink).
    - Stochastic layer (Tearing).
  - ✓ Pedestal profile (n=0) is degraded.
  - ✓ Density pedestal is governed by  $v_{E \times B, \perp}$ .
  - ✓ It is consistent with the trend that pump-out increases with kink response [1,2].
  - ✓ T pedestal shows a similar tendency in the experiment and simulation.





[1] Y. Liu et al., PPCF 58 (2016), 114005[2] C. Paz-Soldan et al., Nucl. Fusion (2016), 056001

### **Backup – Vorticity and ExB profiles**

• Vorticity and ExB profiles in the simulation



- $\checkmark$  Reduced vorticity  $U_{00}$  during ELM suppression
  - Possibility of evenly distributed energy among harmonics [H. Jhang 2017].

- ✓ ExB radial profile comparison
  - $V_{\theta, E \times B}$  is increased from 3 to 15 km/s.
  - Decoupling of  $V_{\theta,E\times B}$  and  $V_{\theta,ELM}$  can occur in very nonlinear case.

## Backup - RMP-ELM interaction can increase spectral transfer and broaden mode spectrum of ELM, preventing crash of unstable ELM

Increased spectral energy transfer by RMP-ELM coupling



- ✓ Enhanced interaction between ELM harmonics with RMP [M. Becoulet 2014].
  - Amplified energy transfer between harmonics and broadened spectrum
- ✓ Prevented catastrophic growth and crash of unstable mode [P. Xi 2014].
- $\checkmark$  Participation of both tearing and twisting parity modes in the mode coupling.
  - Both kink and tearing part by RMP mediates the mode interactions.

# Backup - Both kink and tearing response by RMP have to spatialy cover pedestal to mediate interactions between ELM



 $\checkmark\,$  Covering the pedestal and overlapping of RMP mode to mediate interactions.

- Kink-peeling → Overlap is easy, but localized to LCFS.
- Tearing  $\rightarrow$  Wide radial range, but sufficient island width needed for overlap.

✓ Chiricov parameter (> 1) near the <u>pedestal top</u> ( $S_{89}$ ).

- $n = n_{\text{RMP}}$  island overlap to couple with higher n's.
- ELM suppression as island overlap occurs.

Position of rational surfaces and island width are important.

## Backup - Importance of RMP-ELM coupling addresses required or advantageous conditions for RMP-driven ELM crash suppression

- Conditions for the interactions between RMP and ELM
  - ✓ Kink-peeling favorable MP configuration.
  - Rational surface ( $q = m/n_{\rm RMP}$ ) near the pedestal top.
    - Island to cover the entire pedestal and dominant ELMs.
  - $\checkmark$  Chiricov parameter (S > 1) near the pedestal top.
    - $n = n_{\text{RMP}}$  island overlap to couple with higher n's.
  - $\checkmark V_{\theta,\text{ELM}} \approx 0$  before RMP application.
    - Favorable to the locking of ELM.