

Formation of Transport Barrier

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ABSTRACT

- We analyzed evolution of corrugated structures using gyrofluid code developed by Yagi[1].
- From the simple calculation using model equations and traffic jam model [2], spatial scale and the life time of corrugated structures are affected by collisional diffusion and neoclassical poloidal flow.
- Our simulation results reproduce the tendency suggested by our calculation and traffic jam model.

BACKGROUND

- Recent experiments in KSTAR have exhibited the evidence of the non-diffusive avalanche-like electron heat transport events without MHD instabilities[3].
- Also, gyrokinetic simulations showed corrugated structures of δT and correlated $E \times B$ staircase structures [4,5].
- Theories explaining the profile corrugation :
 - 1) Vorticity mixing based on Self-Organized Criticality (SOC) dynamics[6]
 - 2) Traffic jam model [2]
- Based on traffic jam model, with

$$\partial_t \delta T + \lambda \delta T \partial_x \delta T = \chi_2 \partial_x^2 \delta T - \chi_4 \partial_x^4 \delta T - \tau \partial_t^2 \delta T$$

$$\text{scale length of the structure is } \Delta_{max}^2 = \frac{2\sqrt{\chi_2 \chi_4}}{\lambda \delta T_0} \text{ and } \gamma_{max} = \frac{\lambda \delta T_0}{2\sqrt{\chi_2 \tau}}$$

Model equation and primary analysis

3-field gyrofluid equations used in code [1]

- Ion continuity equation

$$\Rightarrow \frac{dW}{dt} + \kappa_n \frac{1}{r} \frac{\partial \Phi}{\partial \theta} + A \nabla_{\parallel} V = \epsilon \widehat{\omega}_d F + \rho_* \frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{q}{\epsilon} \mu_{nc} U_P \right) - \rho_*^2 \mu \nabla_{\perp}^4 F \quad (1)$$

- Ion parallel velocity equation

$$\Rightarrow \frac{dV}{dt} = -A \nabla_{\parallel} F + 4\mu \nabla_{\perp}^2 V - \mu_{nc} U_P - A \sqrt{\frac{1}{\tau} \frac{2}{5} \sqrt{\pi} |\nabla_{\parallel} V|} + \frac{2}{5} A \nabla_{\parallel} T \quad (2)$$

- Ion thermal equation

$$\Rightarrow \frac{3}{2} n_0(r) \left(\frac{dT}{dt} + \kappa_T \frac{1}{r} \frac{\partial \Phi}{\partial \theta} \right) - T_i(r) \left(\frac{dn}{dt} + \kappa_n \frac{1}{r} \frac{\partial \Phi}{\partial \theta} \right) = \frac{5}{2\tau} \epsilon \widehat{\omega}_d T - \frac{9}{5\sqrt{\pi}} A |\nabla_{\parallel} V| T + \frac{2}{5} A \nabla_{\parallel} V + \chi_{\perp} \nabla_{\perp}^2 T + S_T \quad (3)$$

$W = n - \nabla_{\perp}^2 F$: generalized vorticity $F = \phi + p/\tau$: generalized potential

$U_P = V + \rho_* \frac{q}{\epsilon} \left(\frac{\partial F}{\partial r} - \kappa_{nc} \frac{dT}{dr} \right)$: poloidal velocity

$$\kappa_{nc} = \frac{1}{1 + v_{*i}^2 \epsilon^3} \left(\frac{1.17 - 0.35 v_{*i}^{1/2}}{1 + 0.7 v_{*i}^{1/2}} - 2.1 v_{*i}^2 \epsilon^3 \right)$$

Primary analysis based on traffic jam model

For (0,0) mode, assume $V_{\parallel} \sim 0$ and high aspect ratio limit.

Then, model equation becomes

$$\mu_{nc} U_P = 0, \delta F = \kappa_{nc} \delta T \text{ or } \delta n = \delta \phi = \left(\kappa_{nc} - \frac{1+\tau}{\tau} \right) \delta T$$

$$\frac{d}{dt} (\delta n - \rho_*^2 \nabla_{\perp}^2 \kappa_{nc} \delta T) = -\rho_*^2 \mu \nabla_{\perp}^4 \kappa_{nc} \delta T$$

$$\frac{3}{2} n_0 \frac{d\delta T}{dt} - T_0 \frac{d\delta n}{dt} = \chi_{\perp} \nabla_{\perp}^2 \delta T$$

$$\Rightarrow \frac{3}{2} \frac{n_0}{T_0} \frac{d\delta T}{dt} = \frac{\chi_{\perp}}{T_0} \nabla_{\perp}^2 \delta T - \rho_*^2 \mu \kappa_{nc} \nabla_{\perp}^4 \delta T - \frac{\rho_*^2 \kappa_{nc}}{\chi_{\perp}} \left(\frac{3}{2} n_0 + \left(\frac{1+\tau}{\tau} - \kappa_{nc} \right) T_0 \right) \frac{d^2 \delta T}{dt^2}, \quad (4)$$

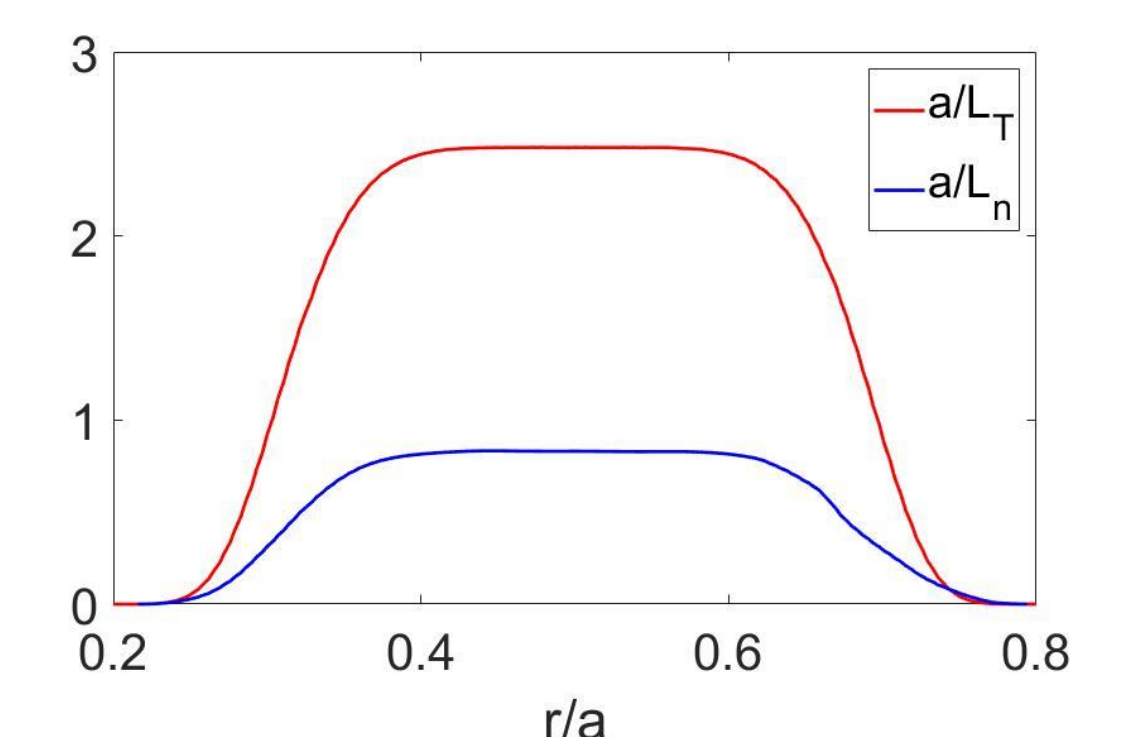
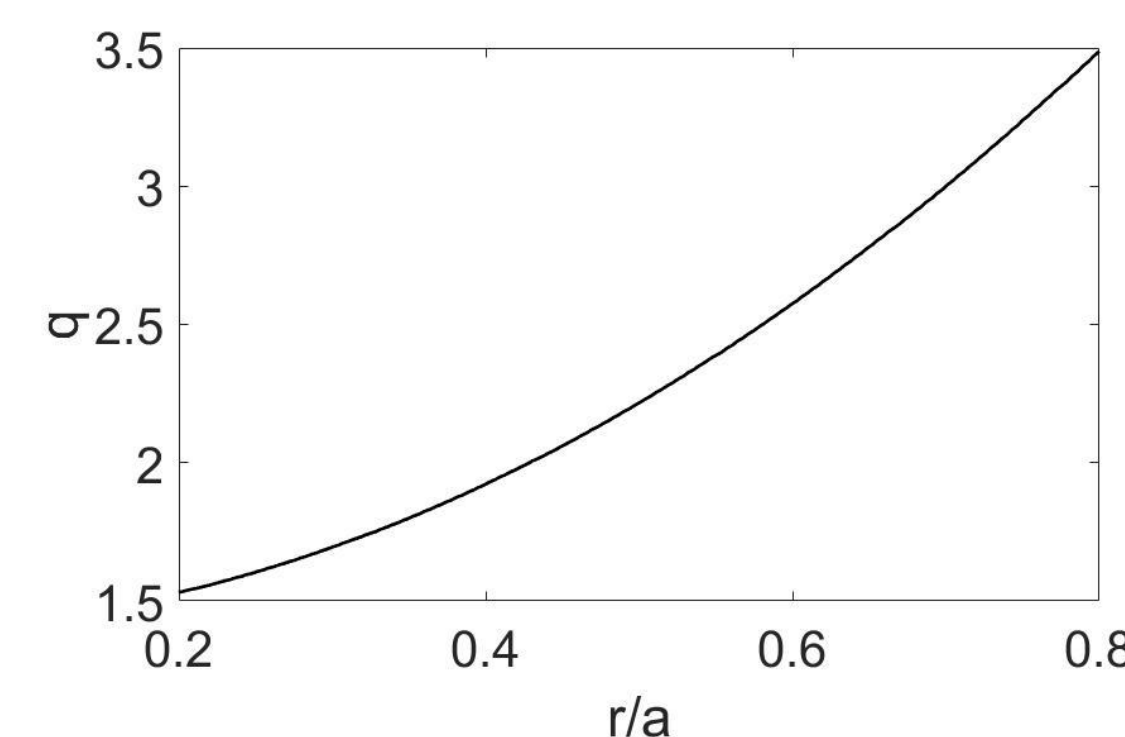
which is similar to traffic jam model [2].

Based on simple analysis, as κ_{nc} , μ and χ_{\perp} increase, spatial scale of corrugated structure increases but its growth rate decreases.

Thus, structures won't sustain for longer time.

Initial setup

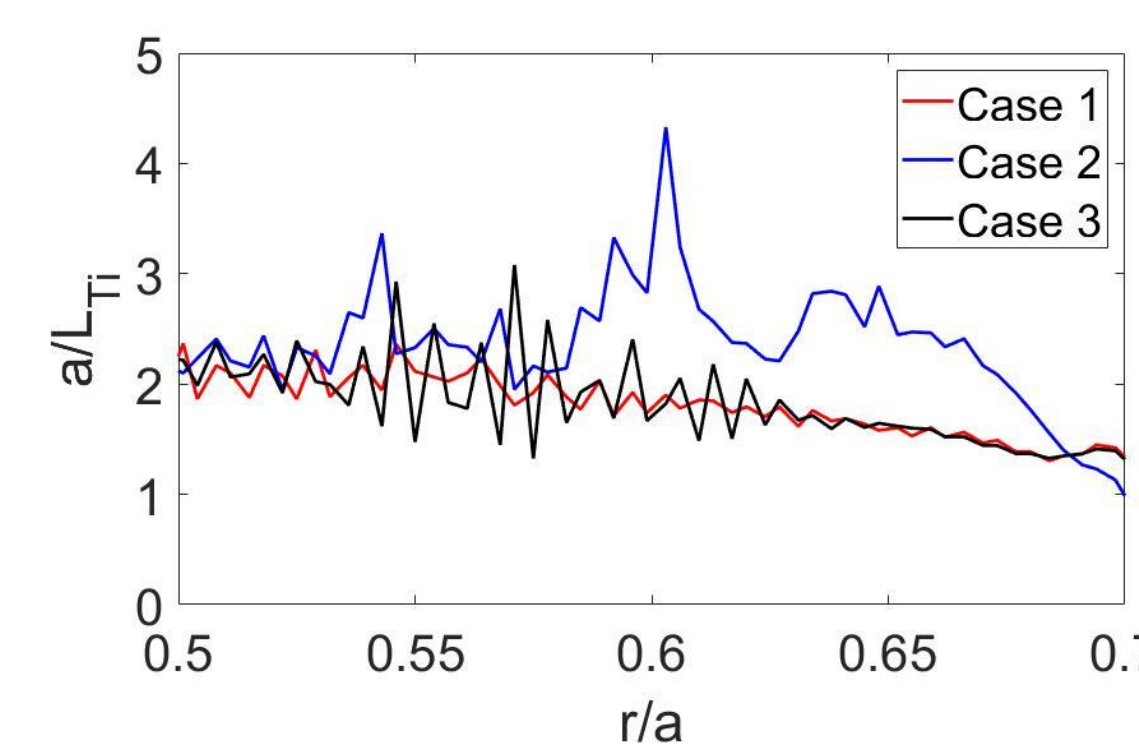
- $R=1.8\text{m}$, $a=0.67\text{m}$, $B_T = 2.5\text{T}$
- Shaping effects are considered ($\Delta = 0.1$, $\kappa = 1.5$, $\delta = 0.3$)
- Profile is fixed by external heat source.



Results & analysis

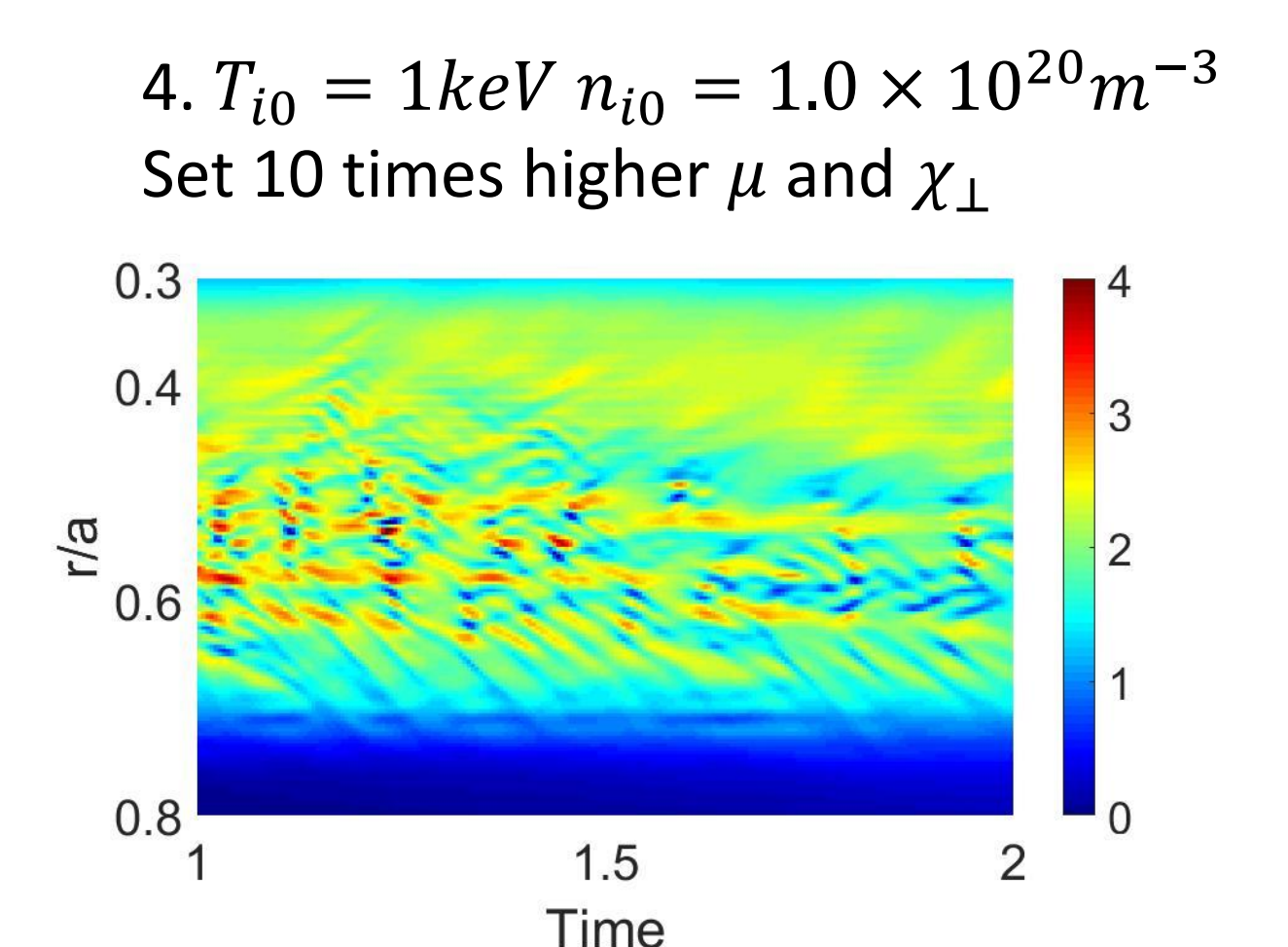
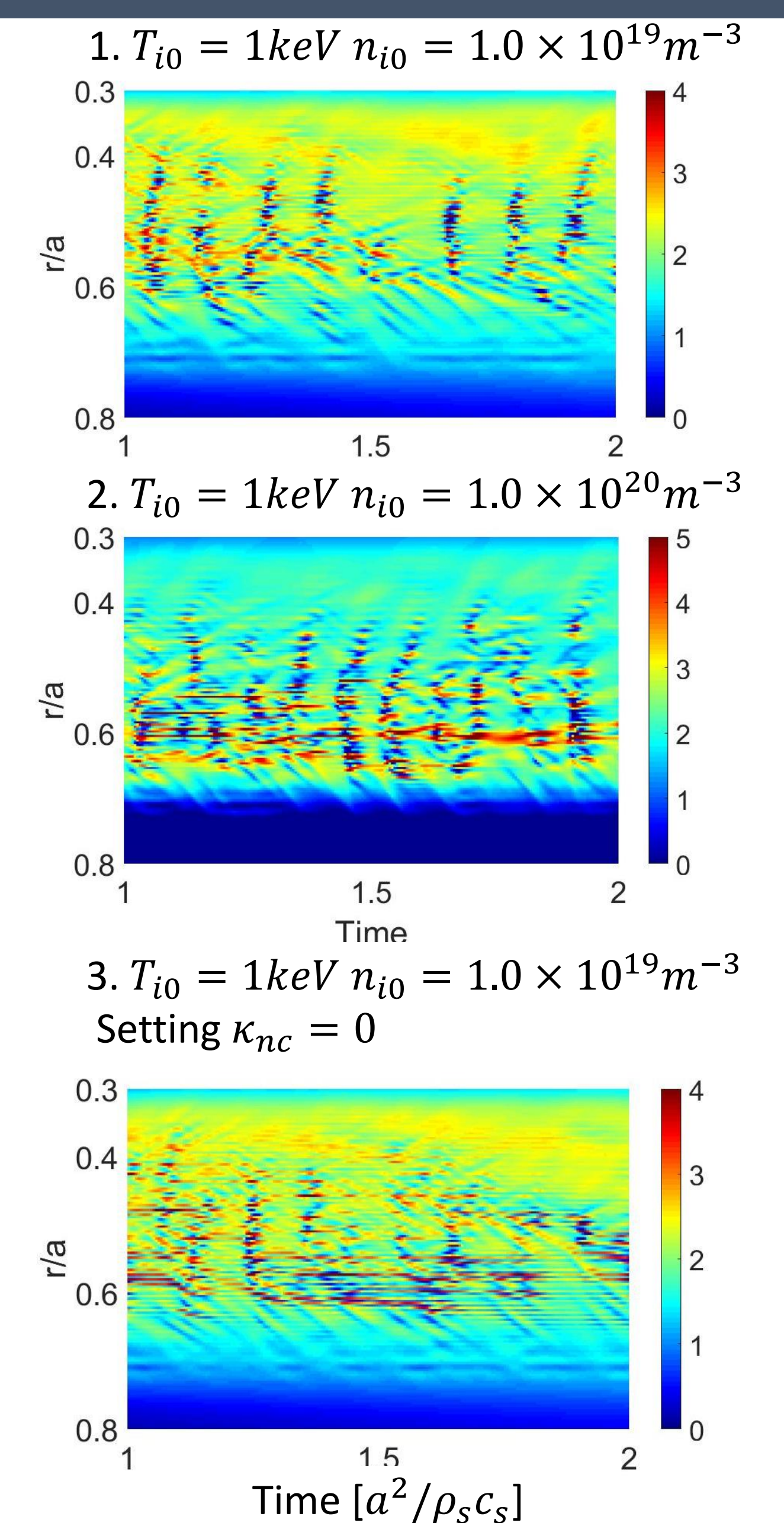
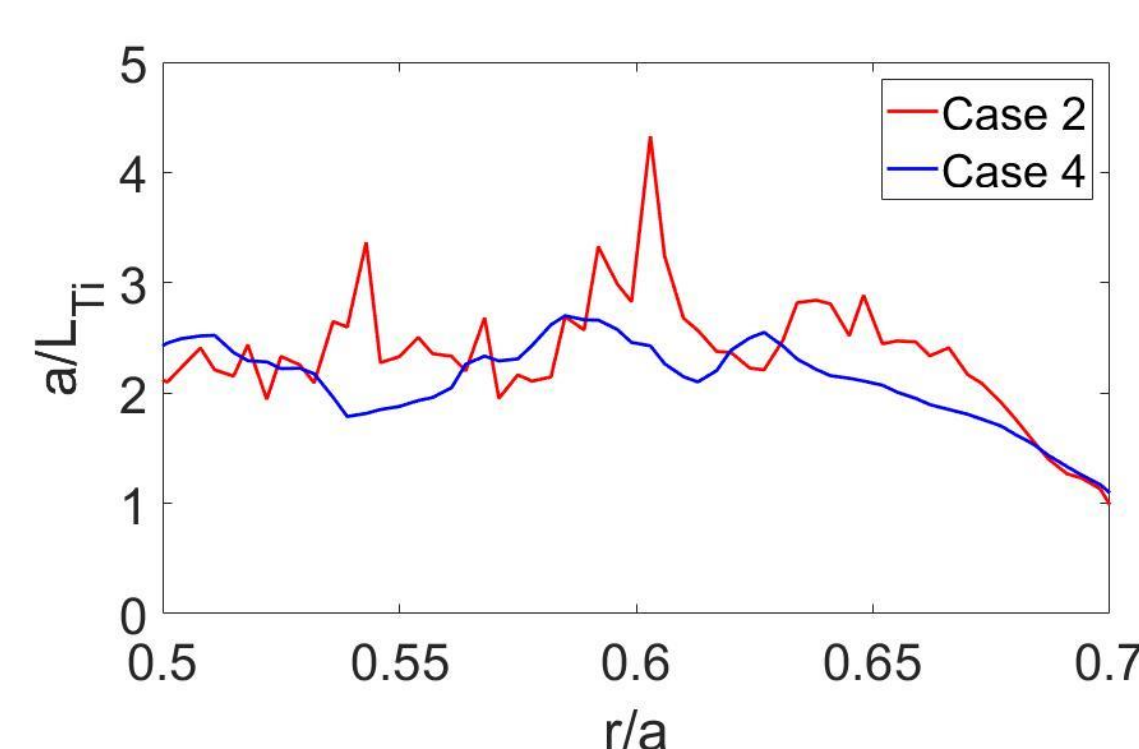
Check the effects of κ_{nc}

- Above 3 figures contour plot of a/L_{Ti}
- Linear growth rate of ITG instability is the same.
- Corrugated structures sustain for a longer time for lower κ_{nc} cases.
- Below figure : time averaged ($t=1-2$) a/L_{Ti}
- Scale length of structures : Case2 > Case 1 > Case 3



Check the effects of μ and χ_{\perp}

- Similar analysis based on Eq. (4) is adjustable.



CONCLUSION & Future Work

- Corrugated structures of a/L_{Ti} are observed in gyrofluid simulations.
- Their tendency follows the prediction by primary analysis using model equations and traffic jam model.
- In the future, radial correlation length and correlation time will be calculated and check the tendency based on our analysis.

ACKNOWLEDGEMENTS / REFERENCES

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