Predictions of alpha-particle and neutral-beam heating and transport in ITER scenarios

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Acknowledgements: G. M. Staebler (GA), He Sheng (PKU)

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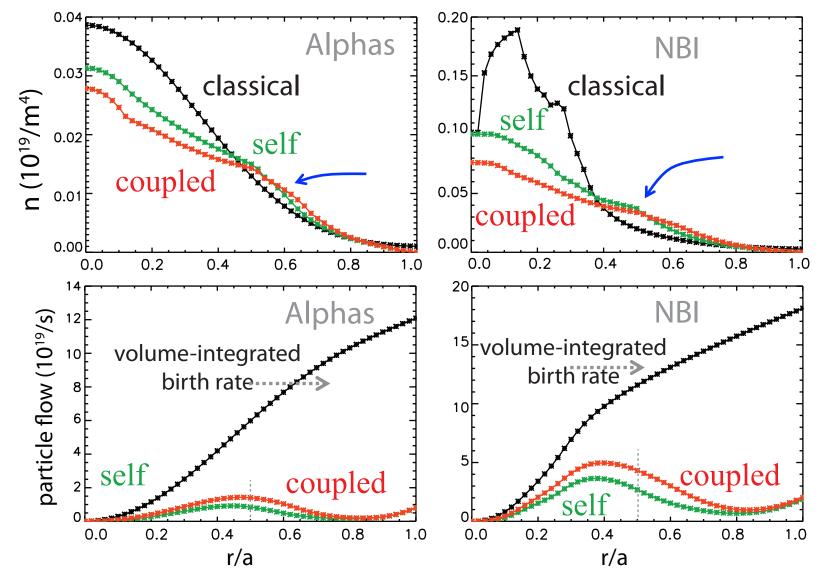


Outline

- I. Introduction: Energetic Particle (EP) transport by Alfvén eigenmodes (AEs) and the need for reduced models
- II. TGLFEP + ALPHA code: A flexible and inexpensive 1D EP transport model
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Main takeaway: The local critical-gradient model (CGM) of AE transport of EPs shows redistribution from mid to outer core in ITER



Mid-core AEs redeposit EPs to the outer radii where their energy is absorbed.

Time-averaged EP density profile corresponds directly to the heating profile.

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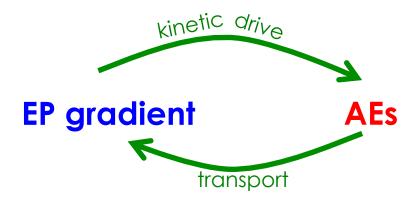
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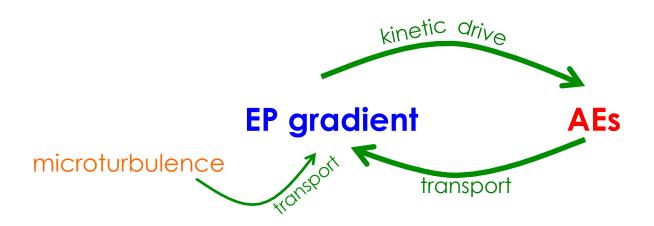
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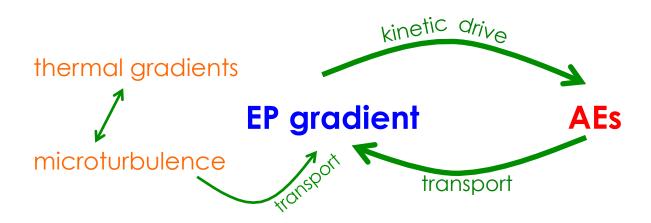
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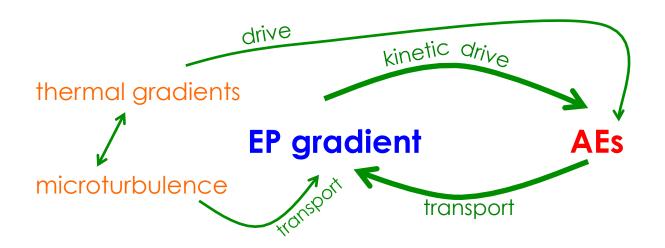
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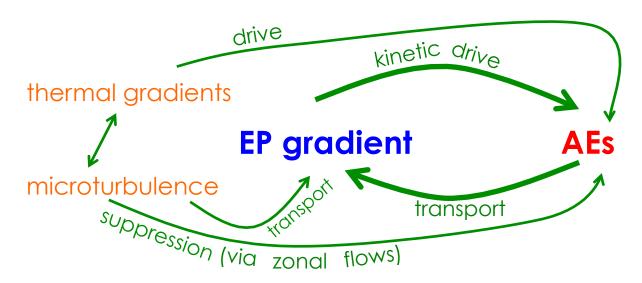
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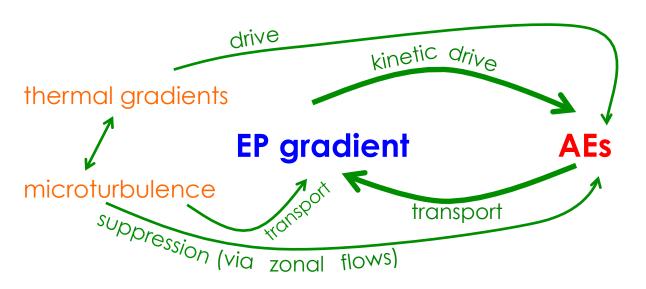
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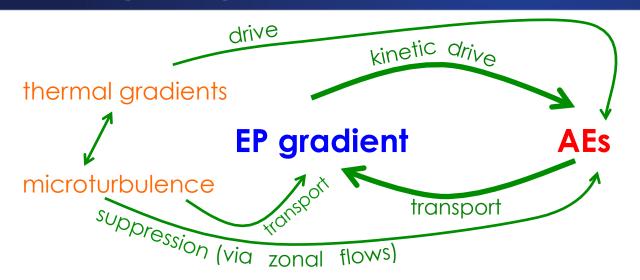
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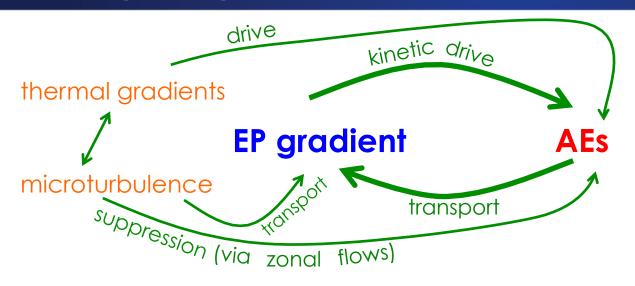
Alfvén eigenmodes. Alfvén frequency MHD modes. EP kinetic drive and transport. Different flavors (RSAE, TAE, BAE, BAAE, EPM, etc.), don't matter here.



AEs drive most EP transport, mainly in the particle channel (i.e. transport is convective).

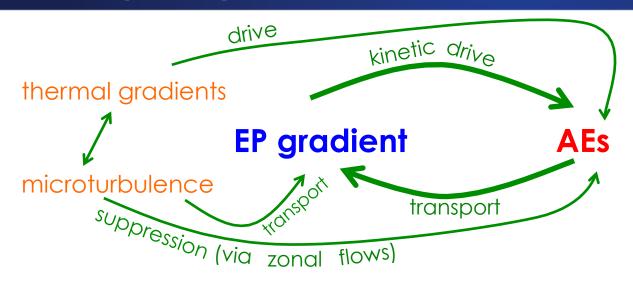


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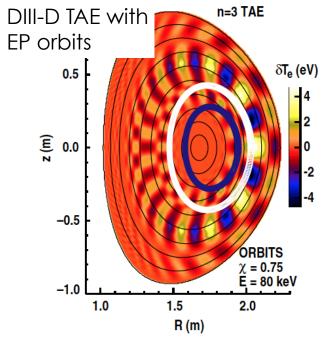
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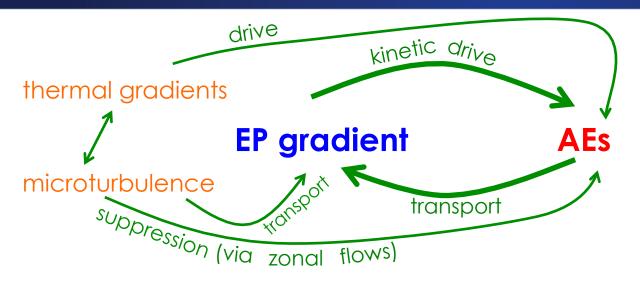
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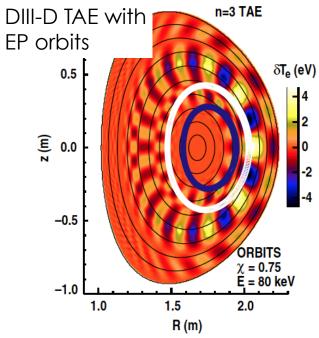


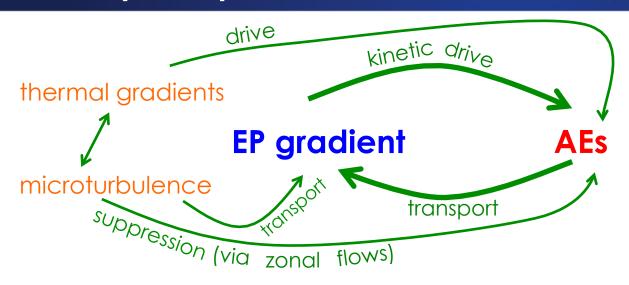


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Sparse spectrum and high coherency:

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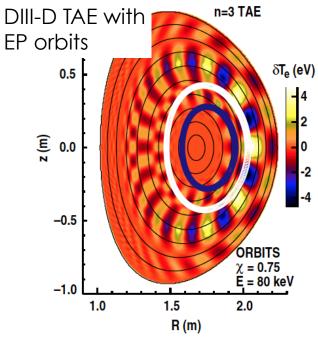


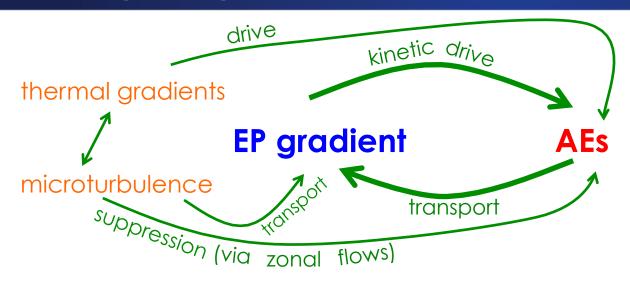


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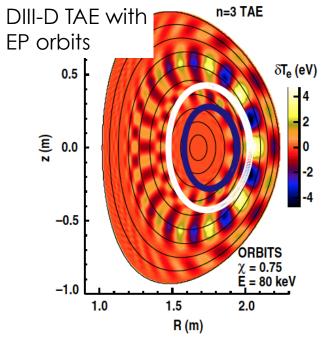


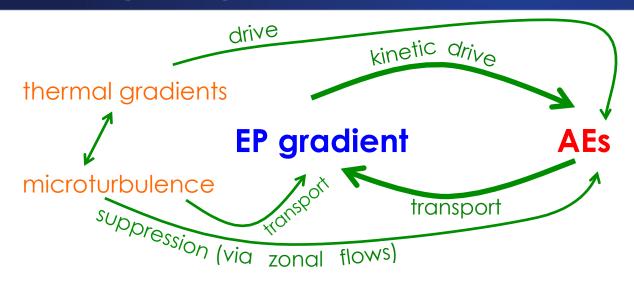
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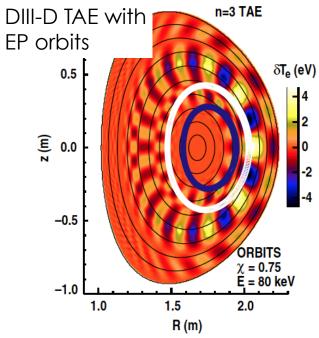


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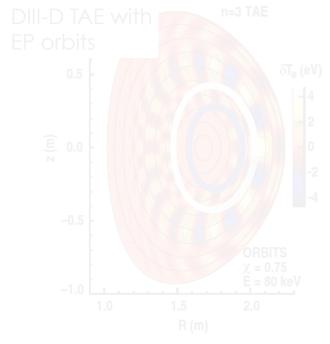


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So how dangerous are EP-driven AEs in ITER and other devices?

It's complicated!

Sparse spectrum and high coherency:

We need reduced models to get useful transport estimates.

- Saturation sensitive to stochastic processes (e.g., collisions, microturbulence)
- Here, we focus on the ALPHA critical-gradient model, probably the simplest and most nimble in use.

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ALPHA transport EP continuity equation

$$\frac{\partial n_{EP}}{\partial t} = S \left(1 - \frac{n_{EP}}{n_{SD}} \right) - \nabla \cdot \Gamma_{EP} \longrightarrow 0$$

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ALPHA code provides source parameters and finds time-invariant solution.

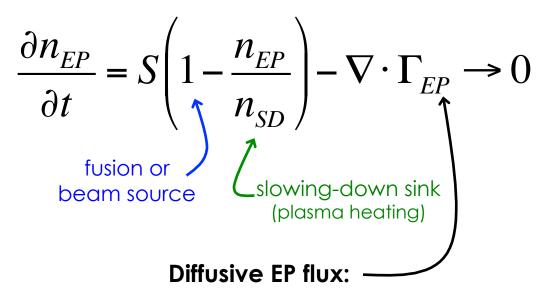
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$$n_{SD} = \int_0^\infty \frac{S\tau_s}{2} \frac{\Theta(E_\alpha - E)}{E_c^{3/2} + E^{3/2}} E^{1/2} dE$$

classical slowing-down density Gaffey 1976

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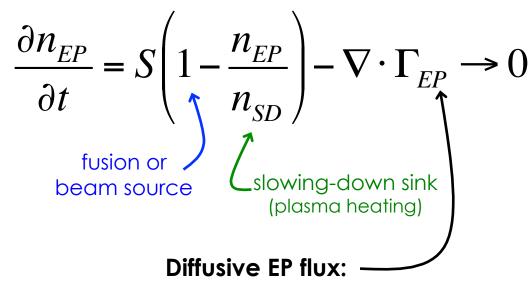
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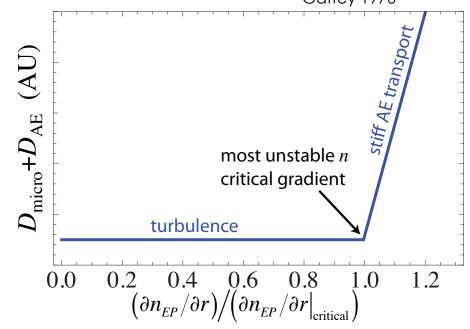
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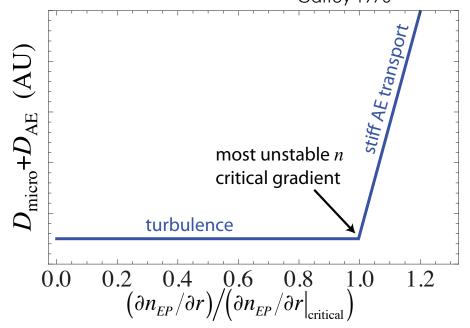
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fusion or beam source
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Diffusive EP flux:

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 $D_{
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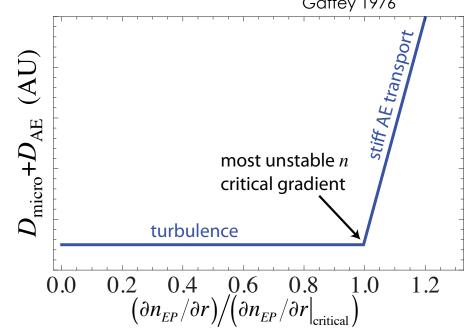
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Critical gradient as a function of r determined by TGLFEP, the **crucial input**.

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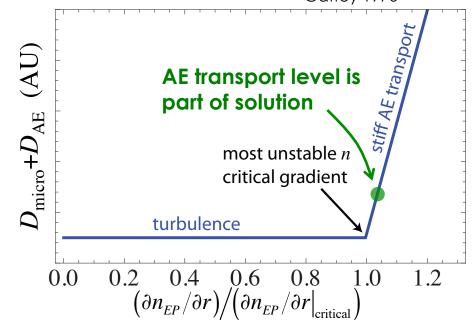
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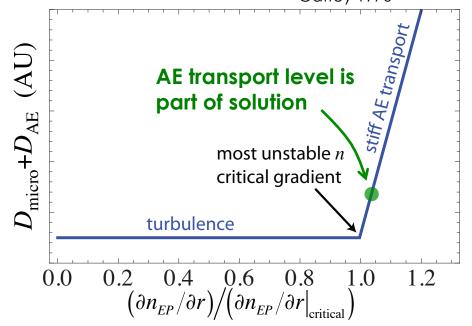
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Boundary condition: Edge $n_{\rm EP}$ is set to zero (pessimistic edge loss estimate).

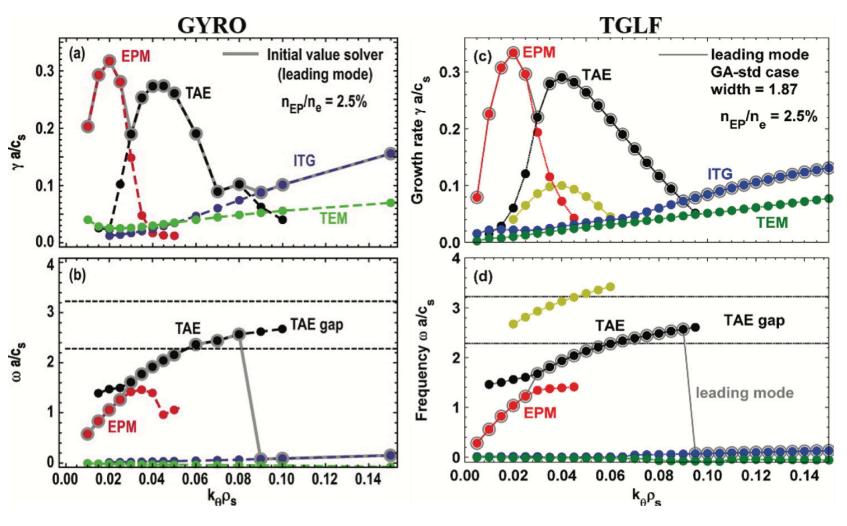
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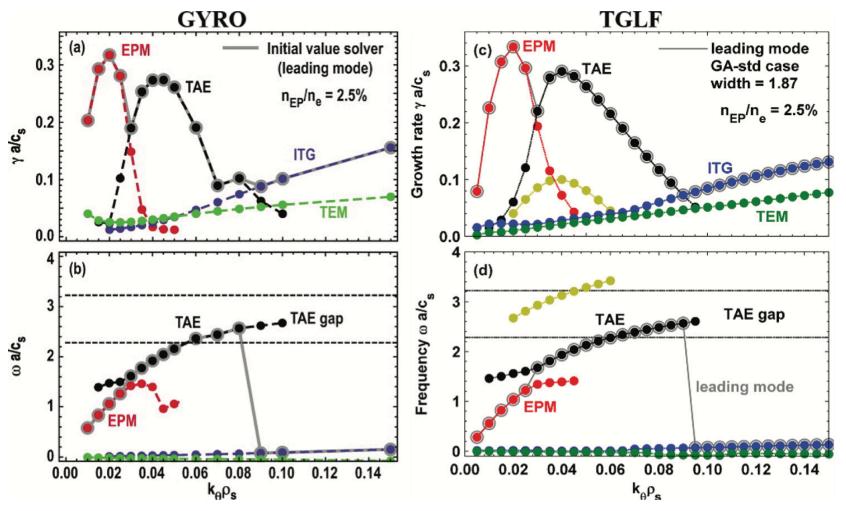
TGLFEP code uses the gyro-Landau fluid TGLF model to find the AE-EP critical gradient where $\gamma_{AF} \rightarrow 0$



Using a high-temperature equivalent Maxwellian, TGLF (gyro-Landau fluid) matches GYRO (gyrokinetic) AE growth rates well, but is >100 times cheaper.

EM Bass/IAEA-FEC/October. 2018 Bass, E.M. Slide 34

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TGLFEP¹: A parallelized wrapper that searches across mode number and drive strength for the critical gradient.

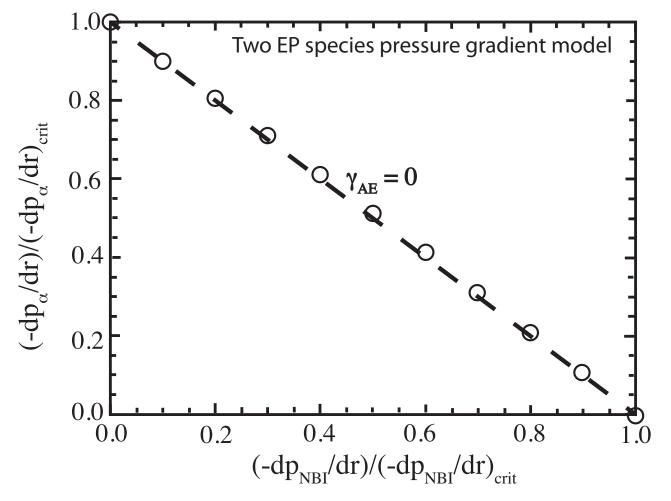
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The model is extended to include simultaneous drive of multiple EP species

The multi-species criticality condition (in terms of each EP pressure p_i) appears as a weighted sum.

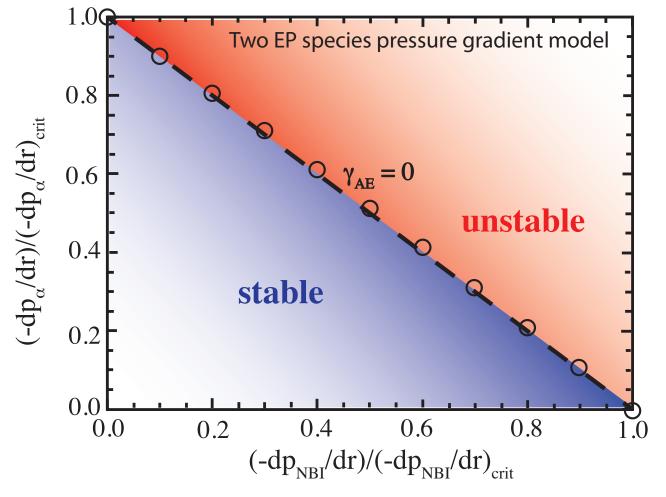
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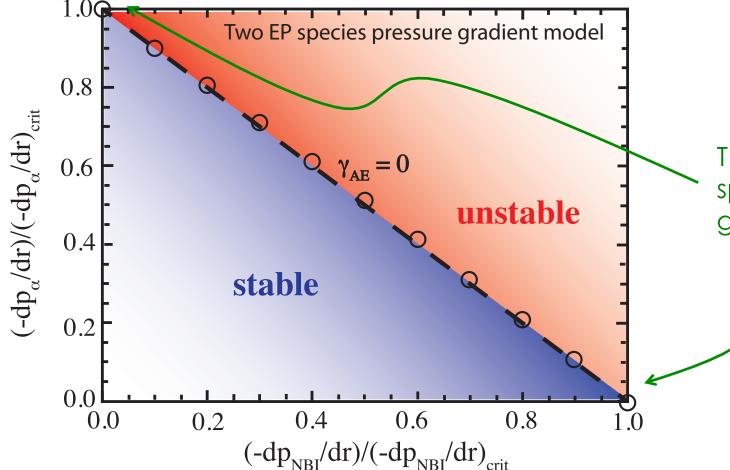
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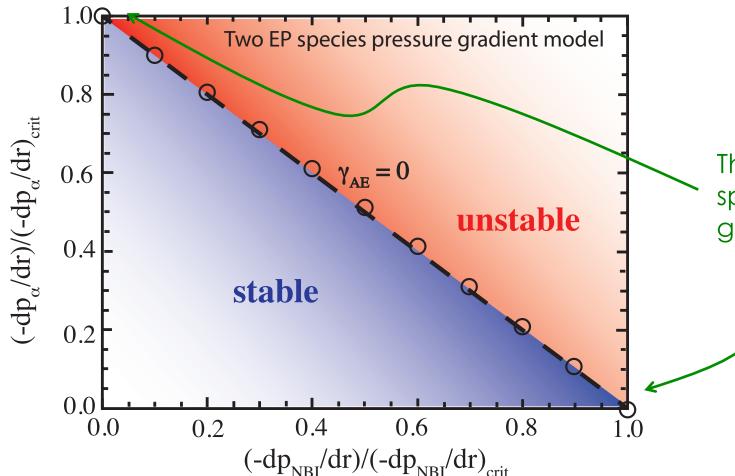


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The two isolated critical gradients specify the two-species critical gradient for **coupled transport**.

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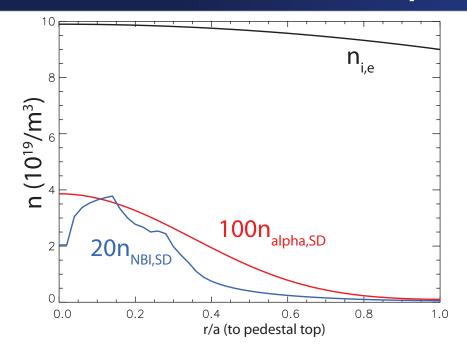
In other words: AEs driven by NBI ions drive additional alpha particle transport, and vice versa.

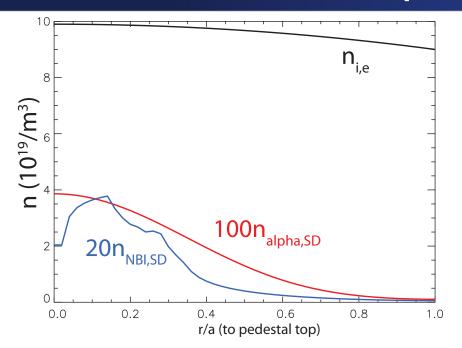
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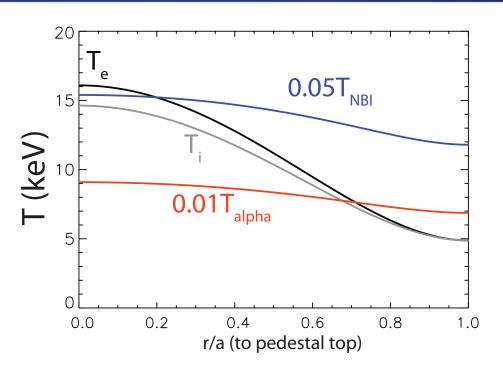
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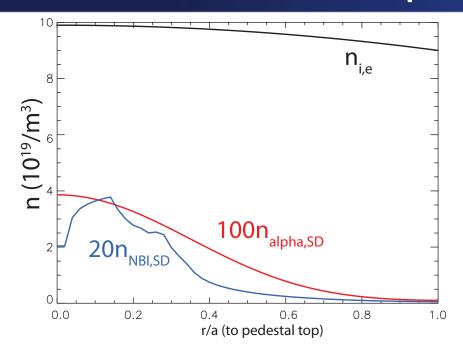
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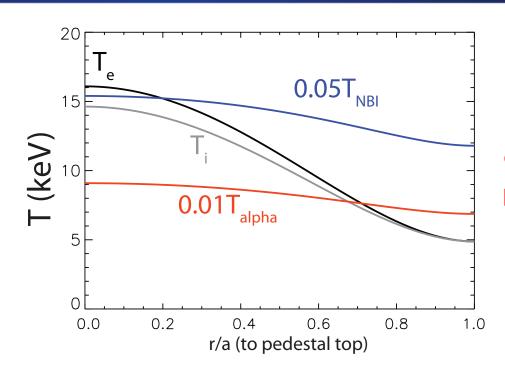
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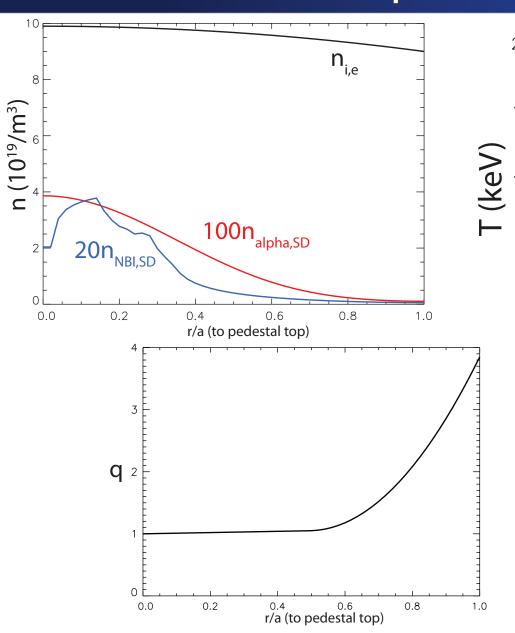


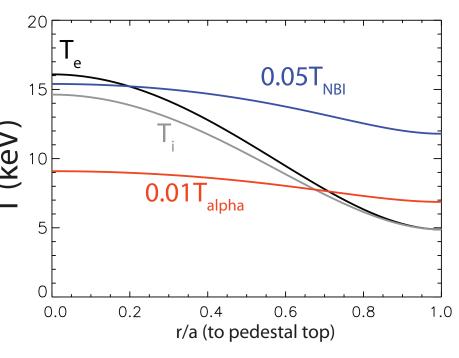






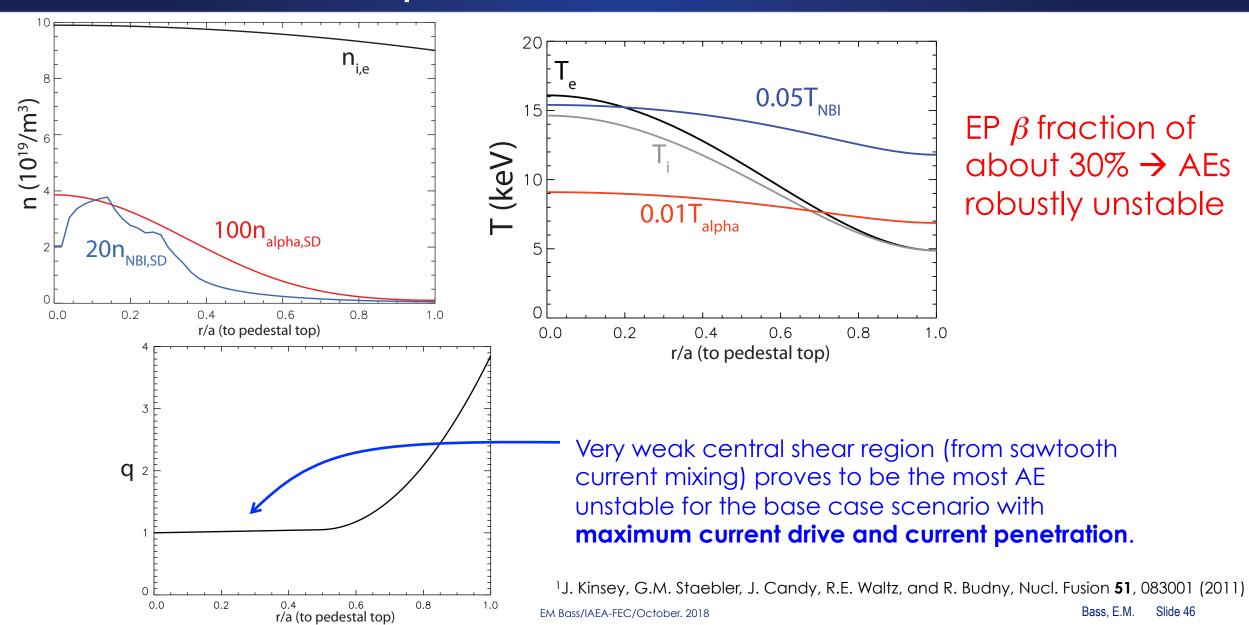
EP β fraction of about 30% \rightarrow AEs robustly unstable

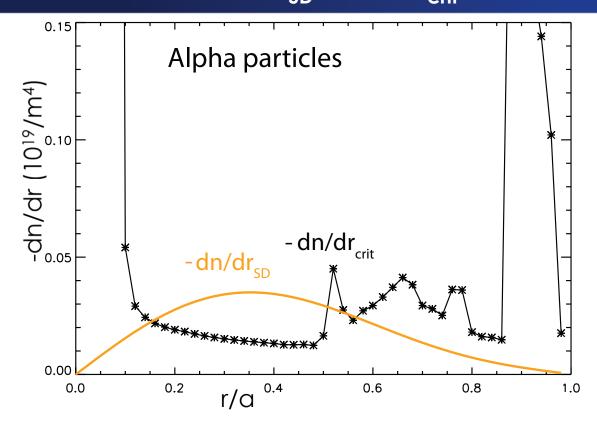




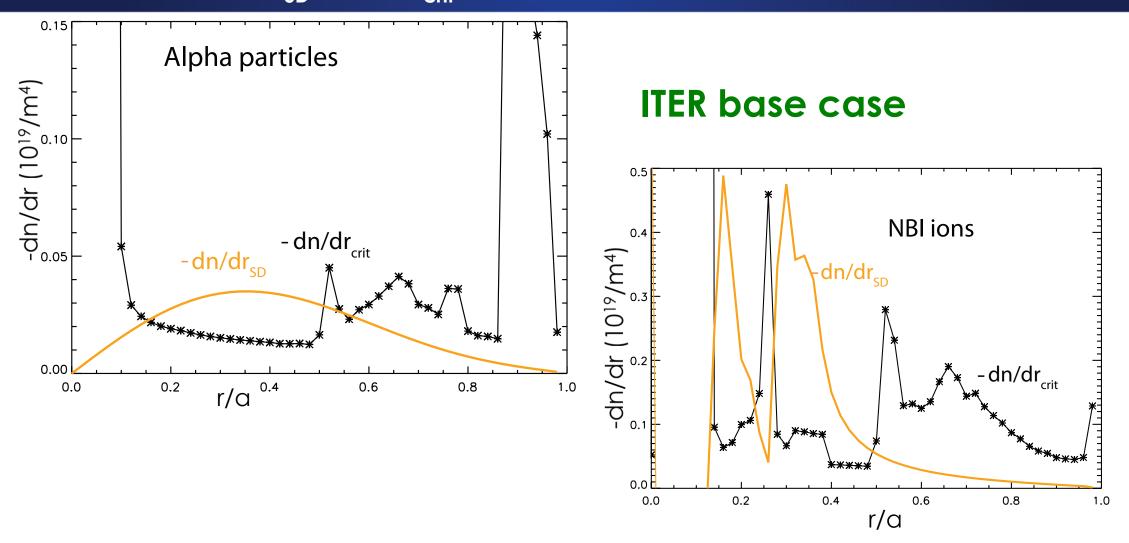
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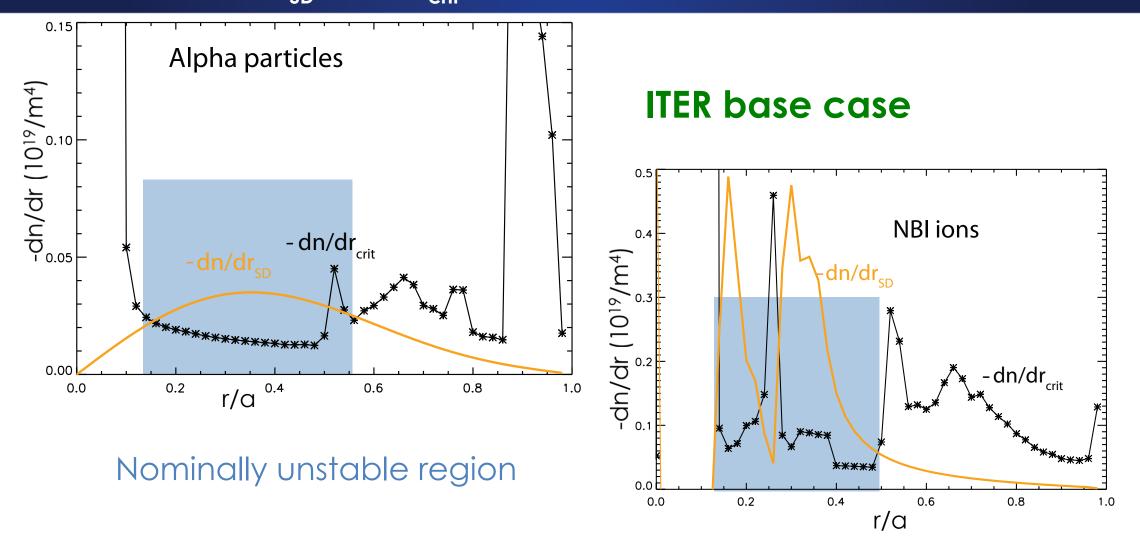
¹J. Kinsey, G.M. Staebler, J. Candy, R.E. Waltz, and R. Budny, Nucl. Fusion **51**, 083001 (2011)

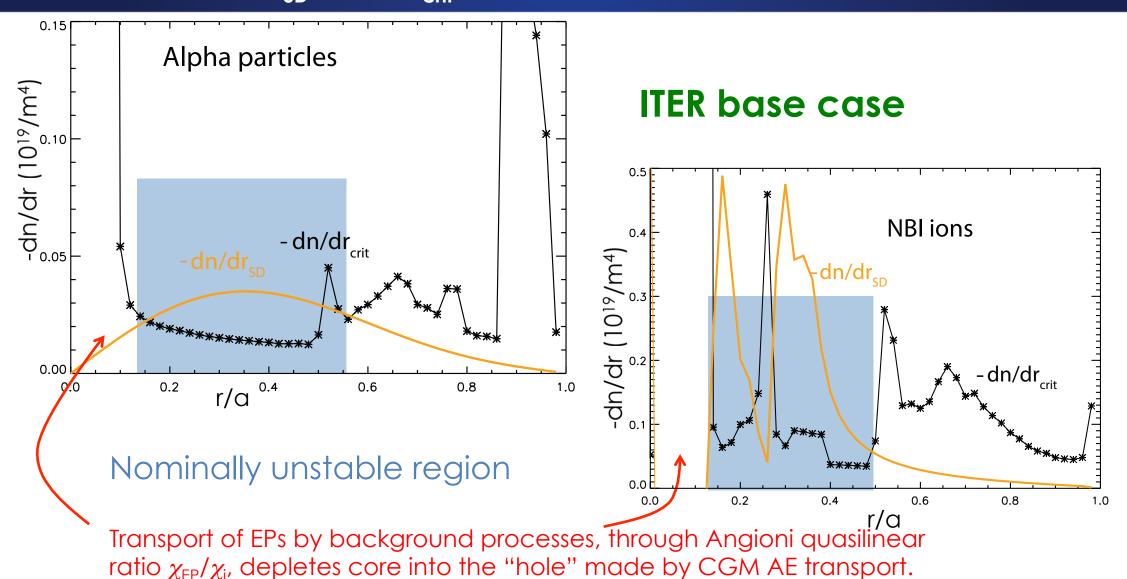




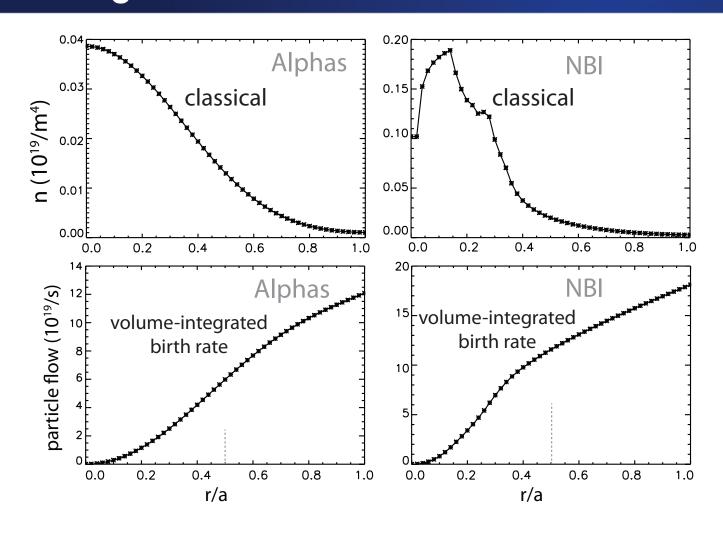
ITER base case

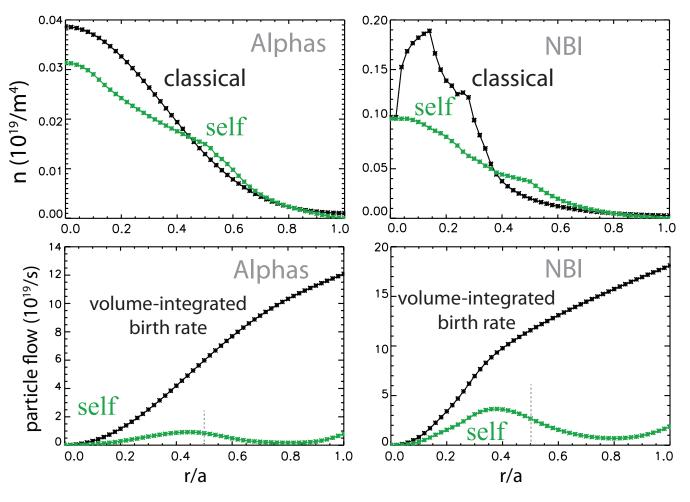




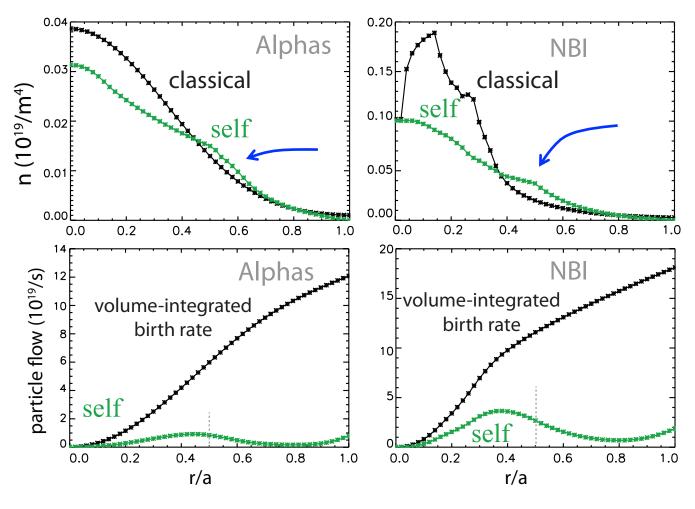


¹R.E. Waltz, E.M. Bass, W.W. Heidbrink, and M.A. VanZeeland, Nucl. Fusion **55**, 123012 (2011)



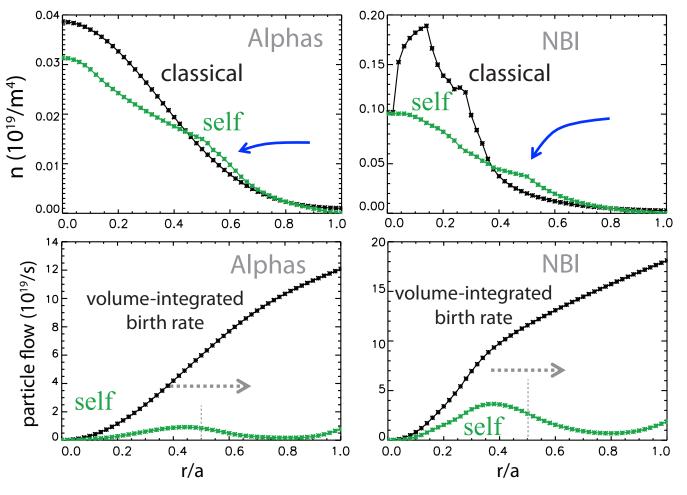


self: Each EP species drives only its own transport



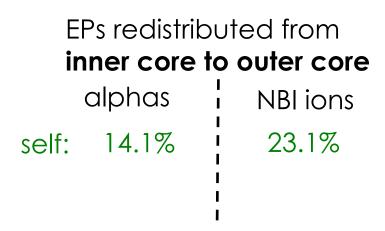
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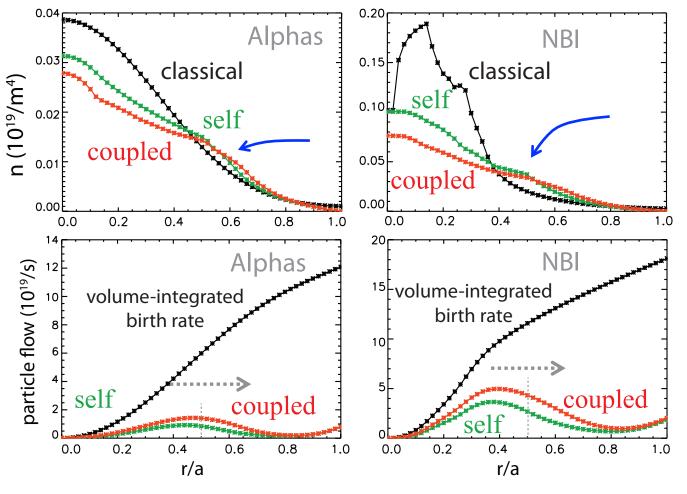
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Mid-core AEs redeposit EPs outward

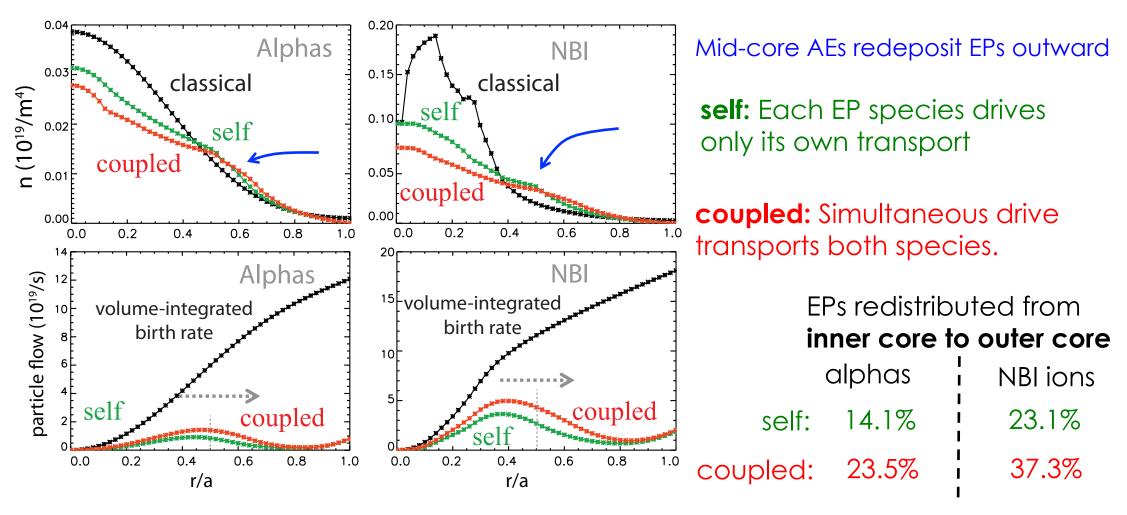
self: Each EP species drives only its own transport

coupled: Simultaneous drive transports both species.

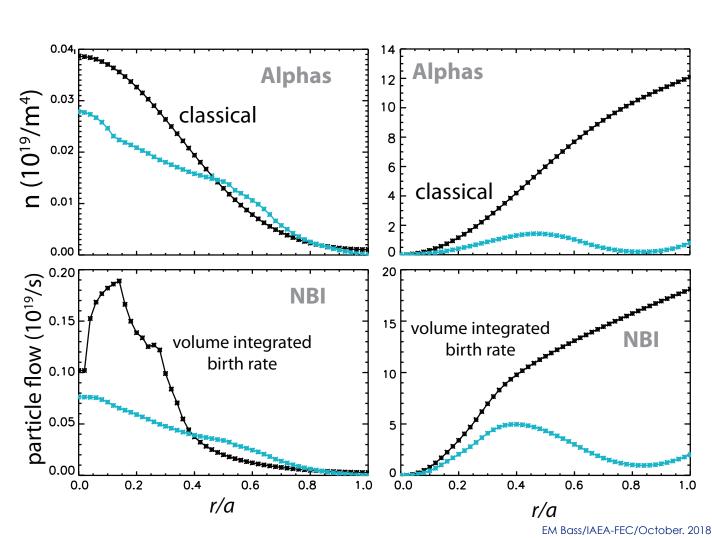
EPs redistributed from				
inner core to outer core				
alphas	NRLions			

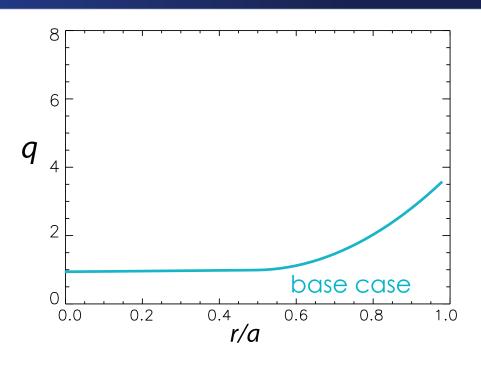
	3	•	1 10110113
		ı	
self:	14.1%	l I	23.1%

coupled: 23.5% 37.3%



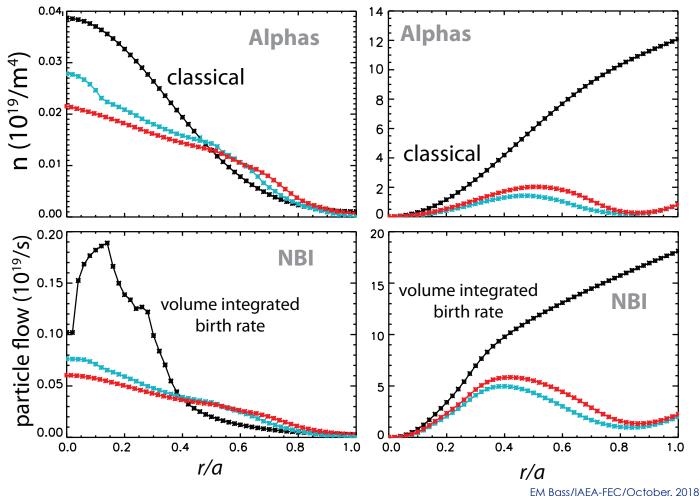
Outside AE-unstable region (center and edge) flux comes from background transport component.

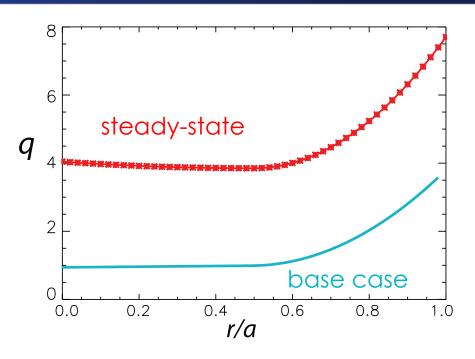




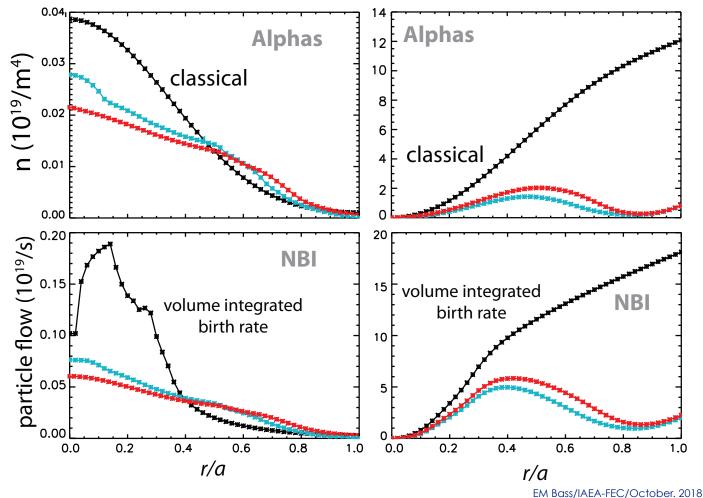
Bass. E.M.

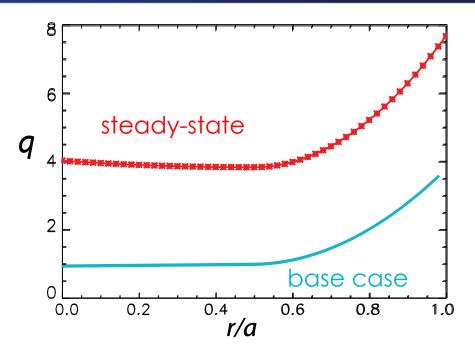
Steady-state (non-inductive current drive) case has 7.5 MA (half base-case value) current and weak penetration.





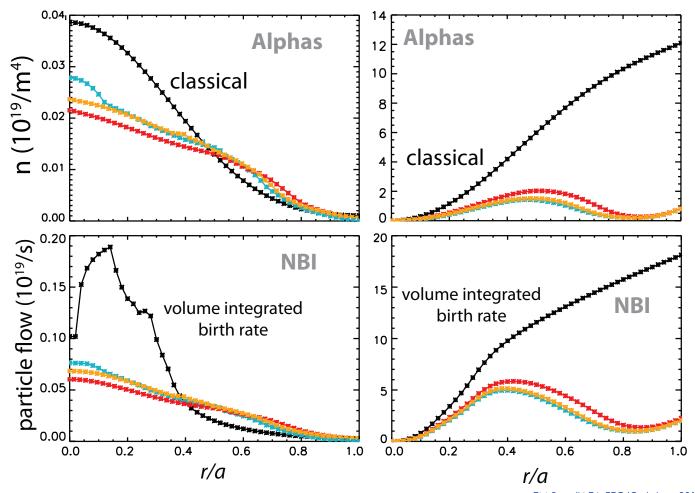
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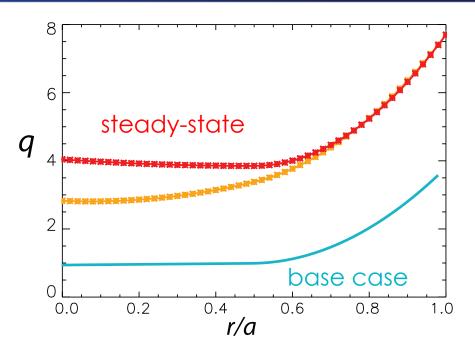




Low shear hurts both the steady-state and base cases.

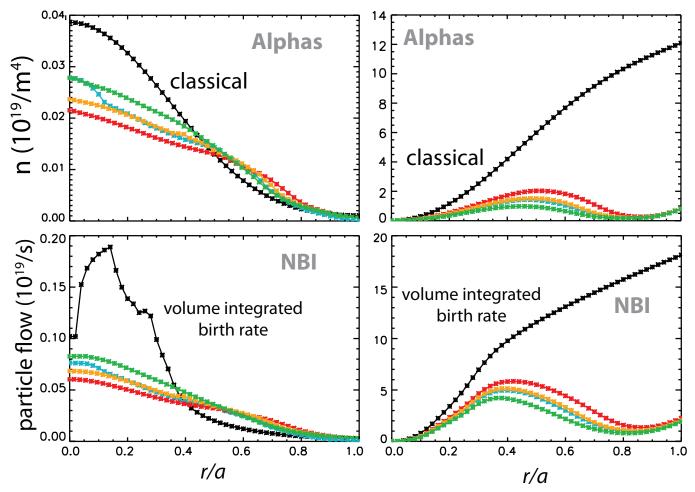
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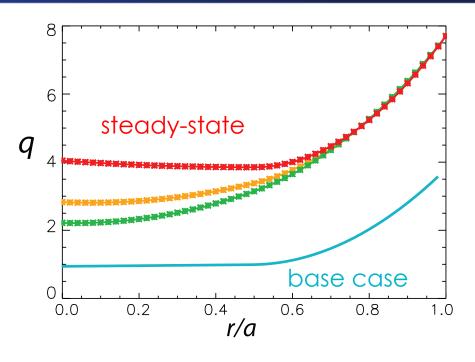




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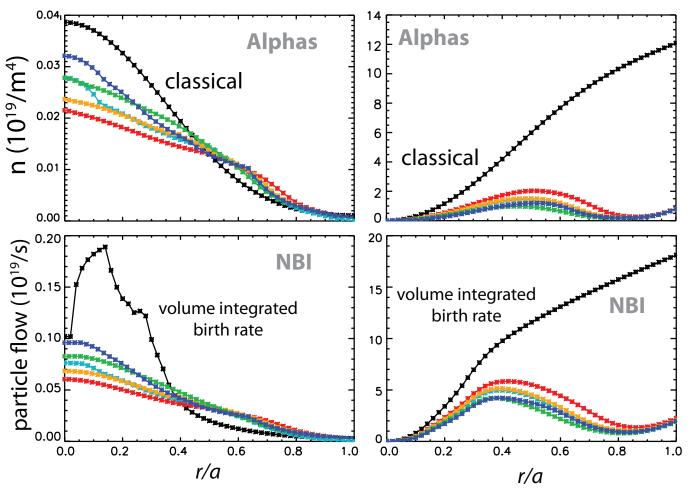
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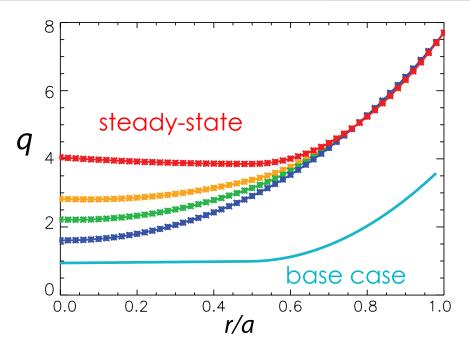




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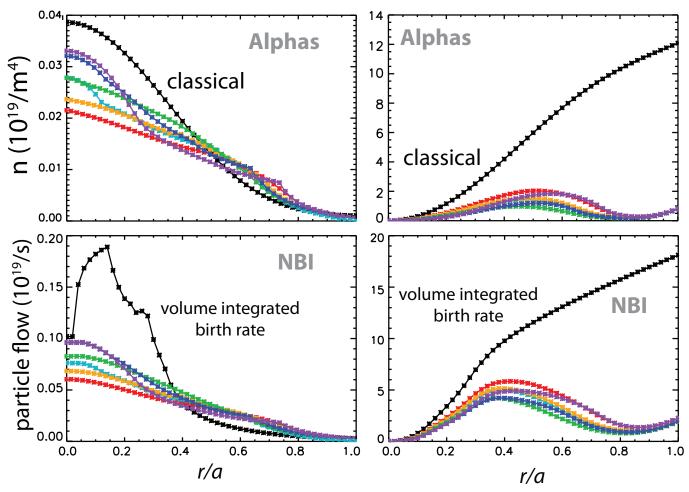
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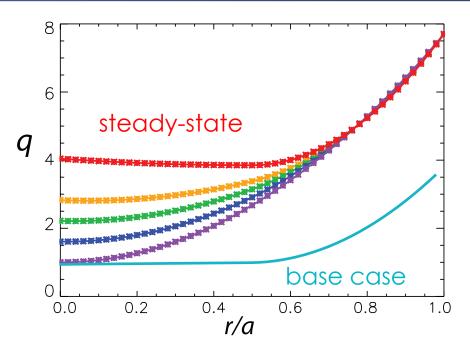




Low shear hurts both the steady-state and base cases.

Steady-state (non-inductive current drive) case has 7.5 MA (half base-case value) current and weak penetration.





Low shear hurts both the steady-state and base cases.

Outline

- I. Introduction: Energetic Particle (EP) transport by Alfvén eigenmodes (AEs) and the need for reduced models
- II. TGLFEP + ALPHA code: A flexible and inexpensive 1D EP transport model
- III. Predictions for ITER scenarios for burninig plasmas with beam heating

IV. Summary

Summary: TGLFEP+ALPHA reduced model code ITER predictions

- The TGLFEP+ALPHA reduced model robustly predicts **EP redistribution from the mid core to the outer core**, but with minimal net edge loss.
- Reductions in ITER current (increased q) or current penetration (increased q_{min} with lower core shear) increase mid-core confinement loss.
- Tailoring the current profile to raise central-core shear offers a promising control knob for reducing AEdriven mid-core EP confinement losses in ITER.

Going forward:

- Estimation of mode intermittency, needed to predict peak heat flux (instead of time average)
- Deploy TGLFEP+ALPHA model into the AToM2 whole-device modeling project for use by broader community
- Adjust inputs considering broadened heating and current deposition profiles in an integrated modeling feedback loop

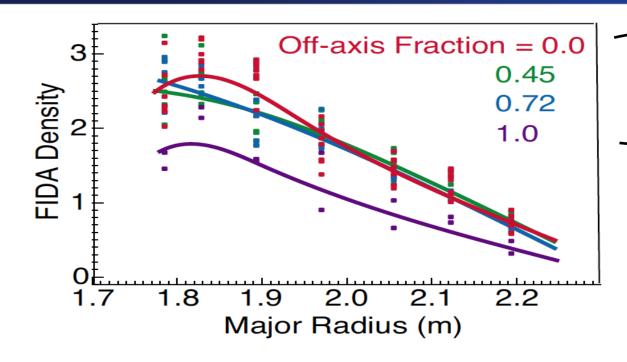
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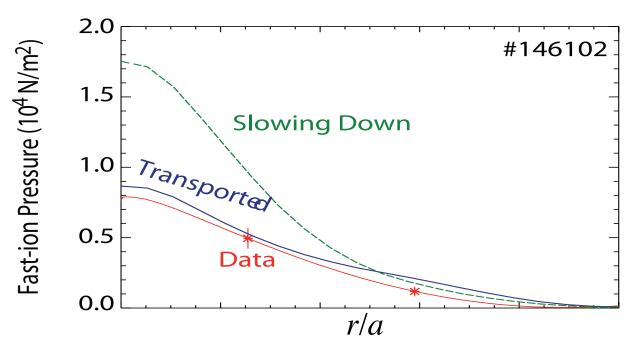
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The ALPHA model neglects much physics but retains experimental relevance



EP pressure profile prediction from the ALPHA critical-gradient model is well validated by experiment¹ and verified against nonlinear GYRO simulations².

¹R.E. Waltz and E.M. Bass, Nucl. Fusion **55** 123012 (2015) ²E.M. Bass and R.E. Waltz, Phys. Plasmas **24**, 122302 (2017) A DIII-D tilted NBI experiment¹ moving the NBI from on-axis to off-axis had virtually **no effect** on the measured beam ion profile.



The AE stiff-transport critical gradient can be identified with a simple linear stability condition

A careful nonlinear, gyrokinetic study (using GYRO) of DIII-D discharge 146102 shows runaway over a critical EP gradient¹.

YAE-ITG/TEM

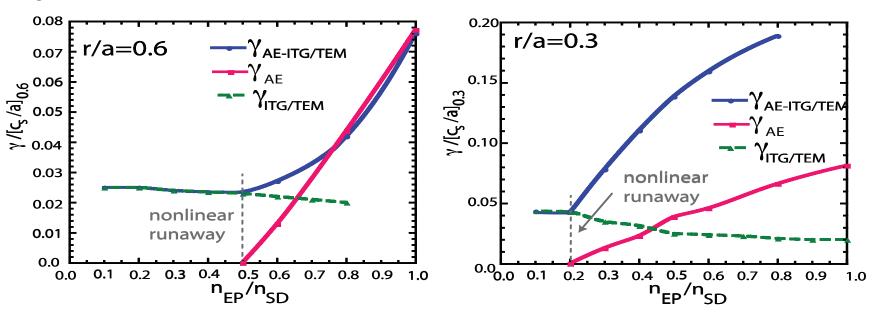
EP+thermal drive on AEs

YAE

only EP drive on AEs

YITG/TEM

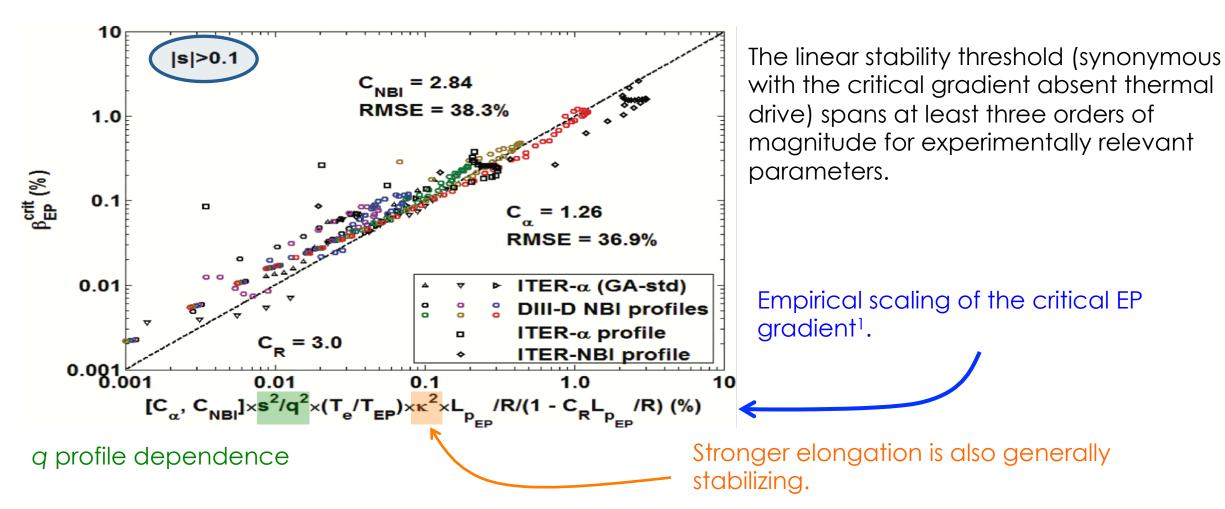
leading microturbulent growth rate



Runaway onset at $\gamma_{AE+ITG/TEM} = \gamma_{ITG/TEM}$ is due to suppression of AEs by microturbulence-driven zonal flows.

By luck, the **much simpler condition** γ_{AE} =0 works just as well, allowing us to take microturbulence out of the critical gradient analysis (but not transport).

Inexpensive, automated TGLFEP confirms shear and elongation are stabilizing, higher q is destabilizing



But... Most transport occurs at very low shear, where q scaling is much weaker. We will see that the q profile matters surprisingly little in practice.