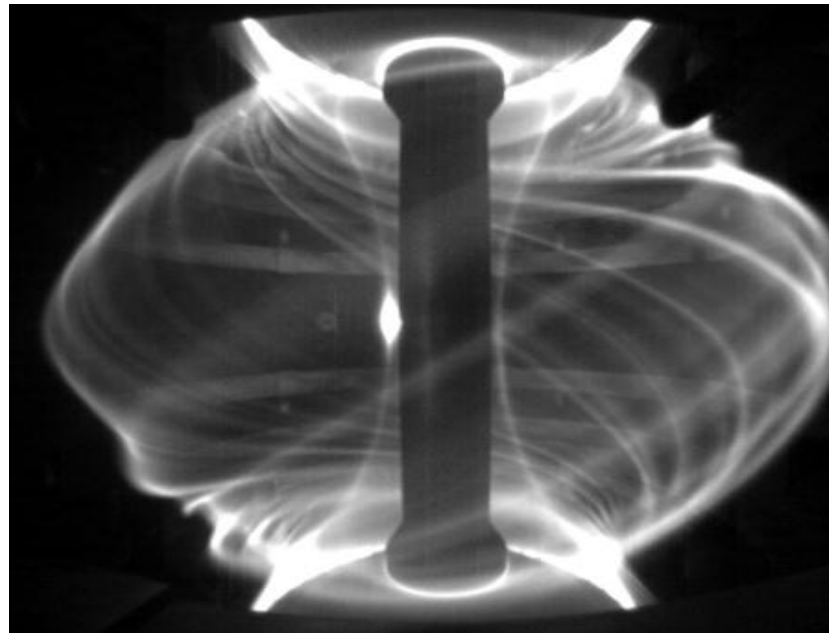


# Gyrokinetic Instabilities near an Evolving Tokamak H-Mode Pedestal



C M Roach, D Dickinson, S Saarelma,  
R Scannell, A Kirk and H R Wilson

Acknowledgements:

J W Connor, R J Hastie + computer access to HECToR, HPC-FF and Helios.

1. Need for Gyrokinetics to Improve Pedestal Models
2. Plasma Profile Evolution between Type I ELMs in MAST
3. Local GK analysis of ELM cycle,  $k_y \rho_i \sim O(1)$ 
  - microtearing (MTM) and kinetic ballooning (KBM)
4. MTM/KBM Transition at Pedestal Top
  - inward advance of pedestal?
5. Drive Mechanism for Microtearing at MAST Edge
6. Conclusions

# 1. Need for Gyrokinetics in Pedestal Models

## Understanding the Edge Pedestal will help:

- optimise confinement in the core
- develop strategies to tame the ELM

## State-of-the Art Model is EPED: [1]

- kinetic ballooning+MHD peeling ballooning  $\Rightarrow$  predicts  $P_{\text{ped}}$ ,  $\Delta_{\text{ped}}$  prior to ELM
- EPED agrees with many measurements from prior to type-I ELMs
- EPED does NOT describe:
  - full details of how pedestal profiles evolve
  - $T_{\text{ped}}$ ,  $n_{\text{ped}}$  as required by core transport models

## More Complete Model:

- must describe all edge transport processes

## Role for Gyrokinetics:

- unveil microinstability mechanisms influencing pedestal evolution
- determine turbulent fluxes

[1] P B Snyder et al, Phys. Plasmas **16**, 056118 (2009)

# 1. Gyrokinetics at Edge is Challenging

Extensive physics required for high fidelity in edge GK:

- $\delta\mathbf{B}$  , collisions, strong shaping, impurities, flow

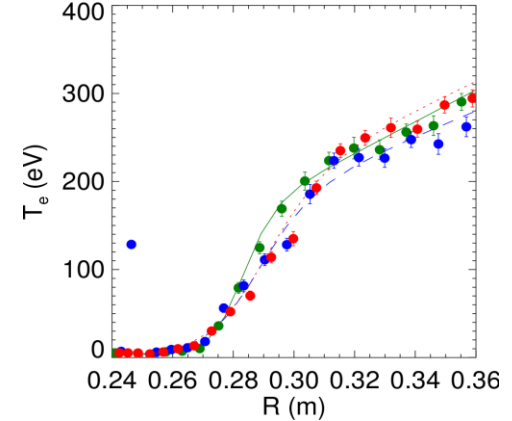
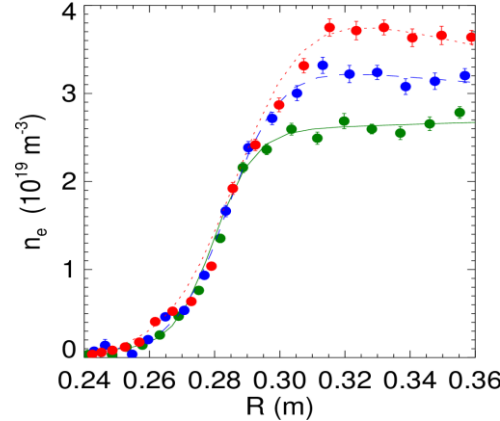
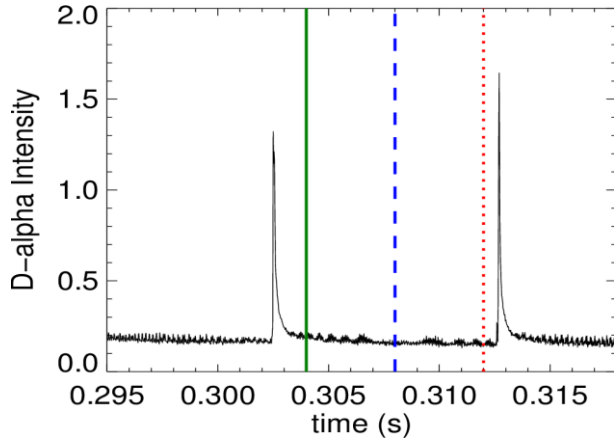
GK expansion parameter  $\rho_i/L_{eq}$  larger than in core, i.e. weak separation between turbulence and equilibrium length scales

...

$L_{eq}$  varies across radial turbulence correlation lengths  
⇒ global simulations desirable

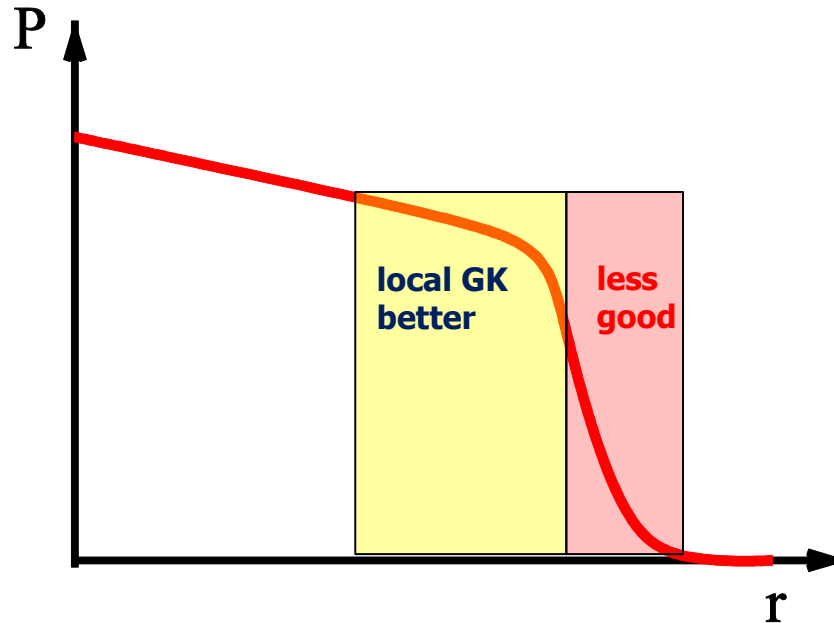
Neutrals influence edge plasma, and not included in GK.

# 1. MAST Plasma Evolution Measured over ELM cycle



\* More MAST edge TS data in **R Scannell et al, EX/P7-22 (Friday)**

“What can we learn by Pushing Local GK to the Limit?”



# 2: MAST ELM cycle Profile Evolution: low $T_e^{\text{ped}}$

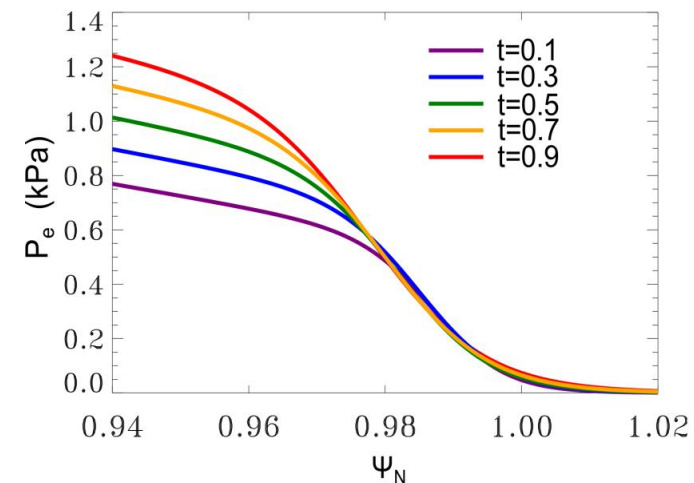
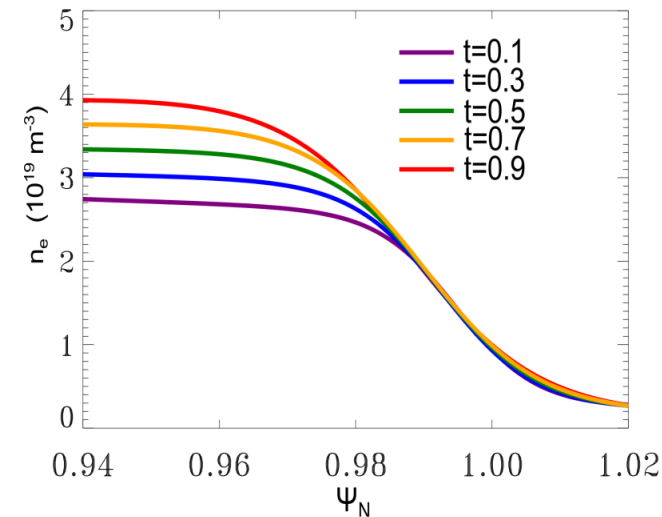
50 TS profiles from reproducible MAST discharges with periodic type I ELMs

- sort profiles in elapsed time since last ELM  
 $t = (\text{time} - \text{time}_{\text{lastELM}}) / \tau_{\text{ELM}}$
- 5 bins:  $t=0-0.2$ ,  $0.2-0.4$ ,  $0.4-0.6$ ,  $0.6-0.8$ ,  $0.8-1.0$
- fit mean binned profiles (mtanh)

Evolution over ELM cycle:

- $n_e$ ,  $P_e$  have similar evolution
  - $T_e$  evolution modest
- high  $dP_e/dr$ ,  $dn_e/dr$  at separatrix after ELM then expand inwards with  $\text{Max}(\text{gradient})$  staying  $\sim$ constant

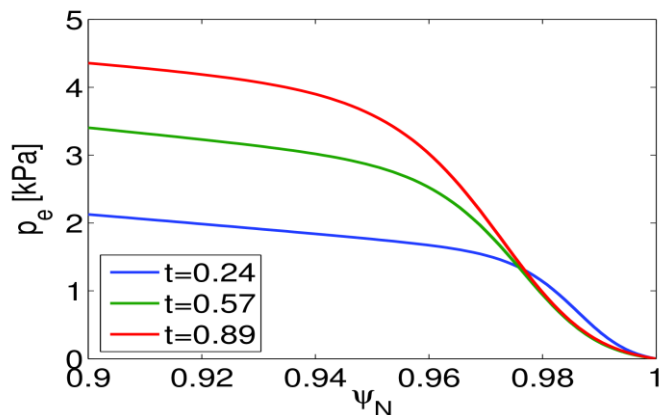
$T_e^{\text{ped}} \sim 150\text{eV}$   
 $v_{*e}(\psi_N=0.94) \sim 1.1$



[1] Dickinson et al, PPCF **53**, 115010 (2011)

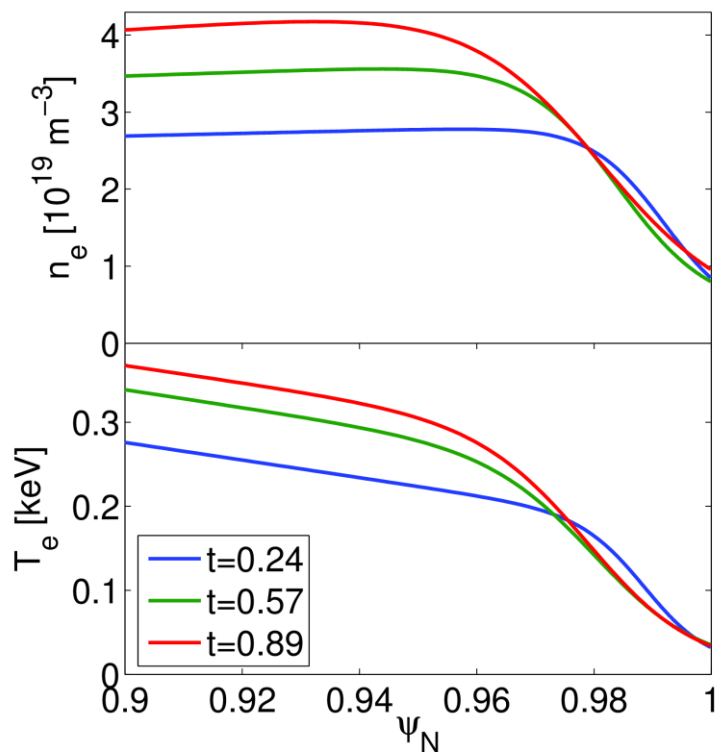
# 2: Profiles during MAST ELM cycle: high $T_e^{\text{ped}}$

$T_e^{\text{ped}} \sim 300\text{eV}$   
 $v_{*e}(\psi_N=0.94) \sim 0.5$



Lower gas puff:

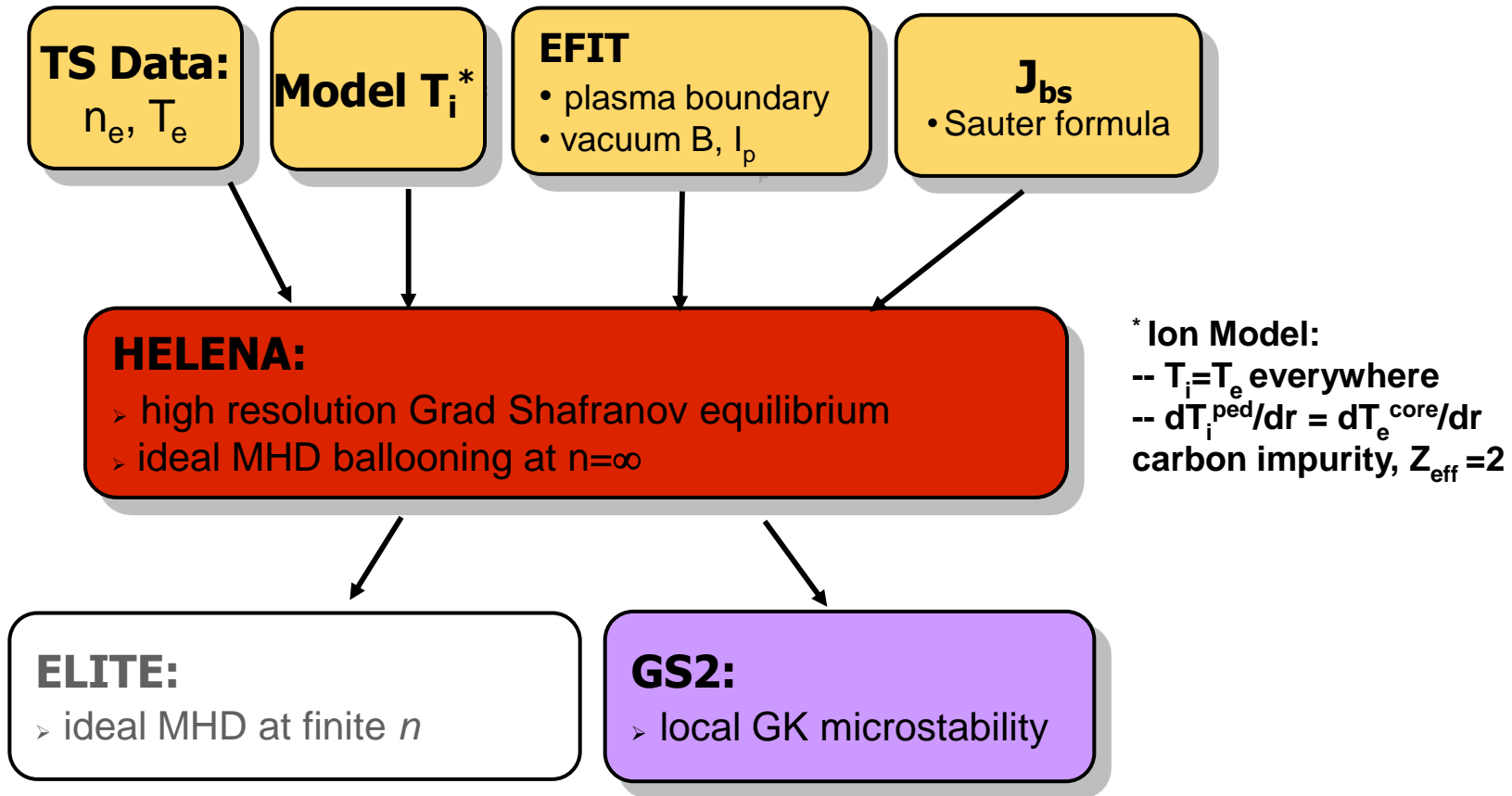
- reduces collisionality in edge



ELM cycle profile evolution similar to low  $T_e^{\text{ped}}$  :

- pedestal in  $T_e$  also expands inwards

# 2: MAST Equilibria for Stability Analysis



Equilibria +MHD analysis for **low  $T_e^{ped}$**  discussed in **[1]**

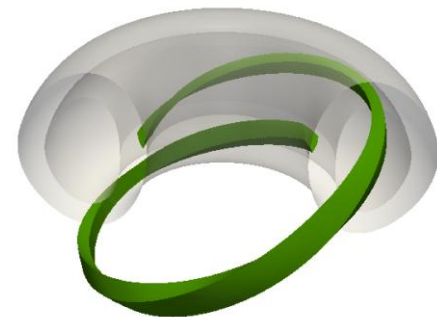
[1] Dickinson et al, PPCF **53**, 115010 (2011)



# 2: Local GK Analysis

Local linear GK analysis using GS2 [1]

- full  $\delta\mathbf{B}$ , general shaping, collisions [2]
- neglect flow (may be important in pedestal)

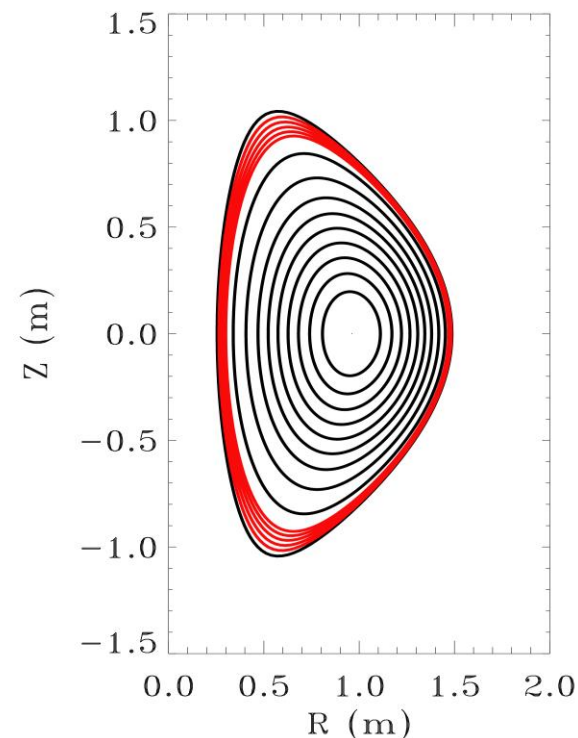


[1] Kotschenreuther *et al*, *Comp Phys Comm* **88** 128 (1995)

[2] Barnes *et al*, *Phys Plasmas* **16** 072107 (2009)

Microstability analysis on surfaces spanning plateau/pedestal:

- focus on ion scales:  $0.1 < k_y \rho_i < 5$

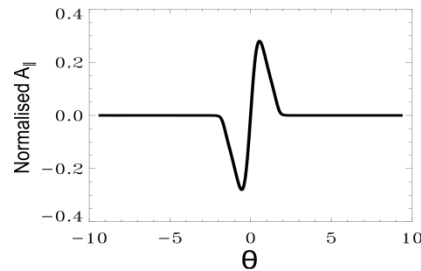


# 3: Local GK Results at Low $T_e^{\text{ped}}$

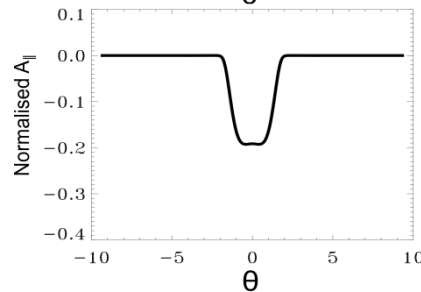
[1],[2]

$\delta B$  crucial for dominant microinstabilities ( $\beta$  scans)

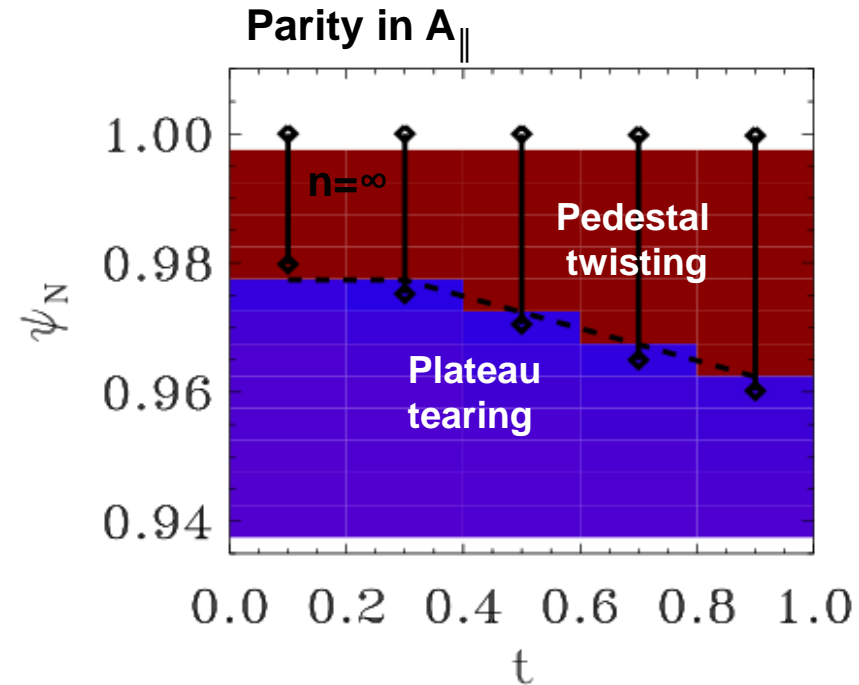
$A_{\parallel}$  eigenfunctions in ballooning space.



$A_{\parallel}$  odd, twisting  
( $k_y \rho_i = 0.22$ ,  $\psi_n = 0.98$ ,  $t = 0.5$ )



$A_{\parallel}$  even, tearing  
( $k_y \rho_i = 3.3$ ,  $\psi_n = 0.95$ ,  $t = 0.5$ )



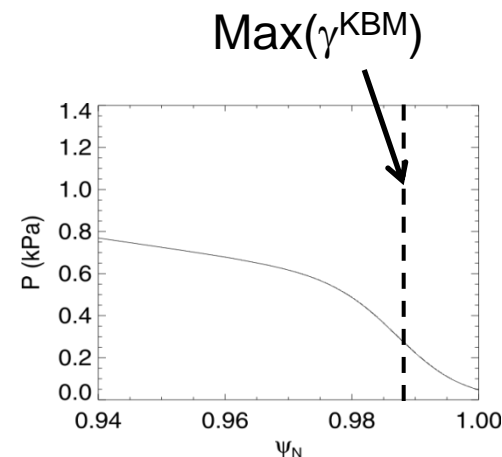
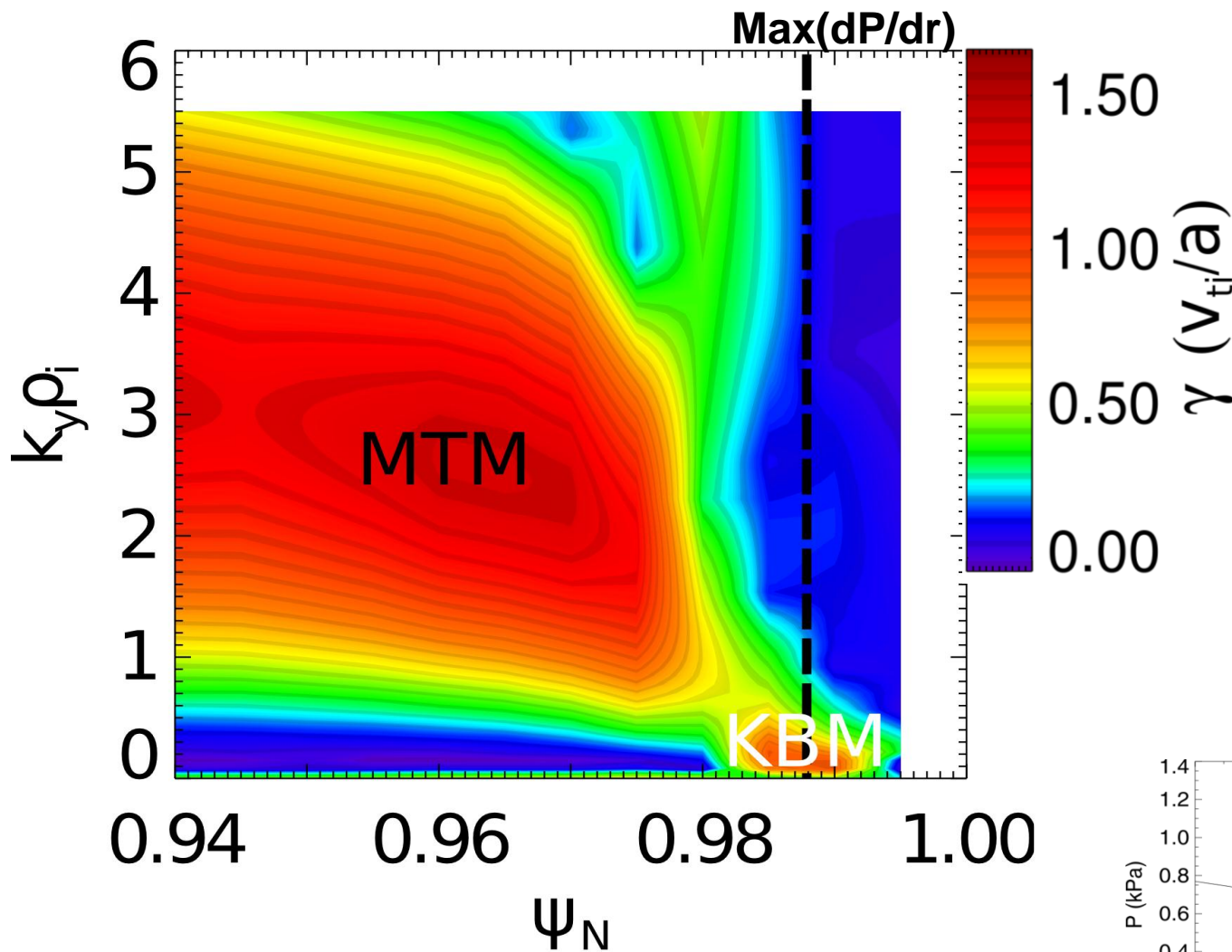
- **Pedestal: Kinetic ballooning modes (KBMs)** ( $k_y \rho_i < 1$ ,  $\omega > 0$ )
  - › NB ideal MHD  $n = \infty$  ballooning modes also unstable
- **Plateau: Microtearing modes (MTMs)** \* ( $k_y \rho_i > 1$ ,  $\omega < 0$ )

\* similar MTMs unstable in JET plateau  
**Saarelma et al, TH/P3-10 (Wednesday)**

[1] Dickinson et al, PPCF **53**, 115010 (2011)

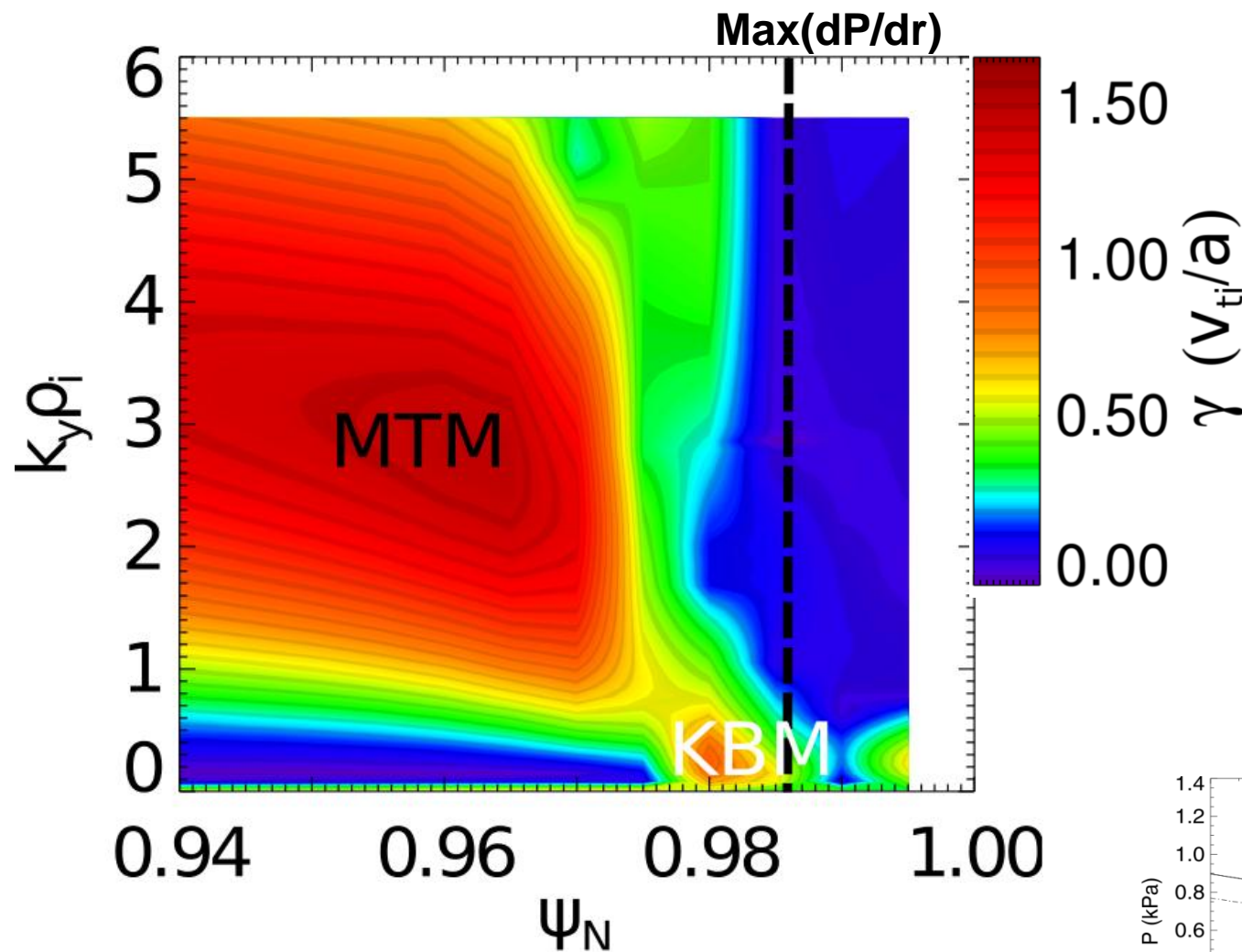
[2] Dickinson et al, PRL **108**, 135002 (2012)

# 3: Microinstability Evolution Low $T_e^{\text{ped}}$ $t=0.1$

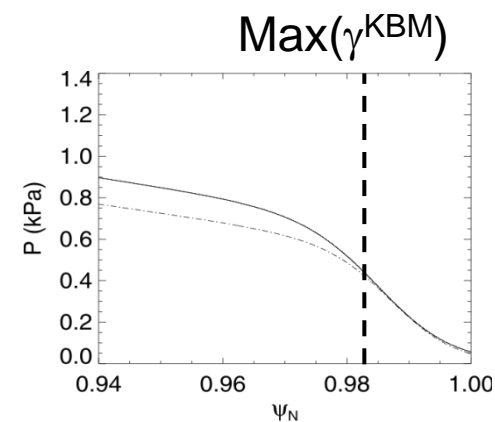


**$\text{Max}(\gamma_{\text{KBM}})$  initially close to  $\text{Max}(dP/dr)$**

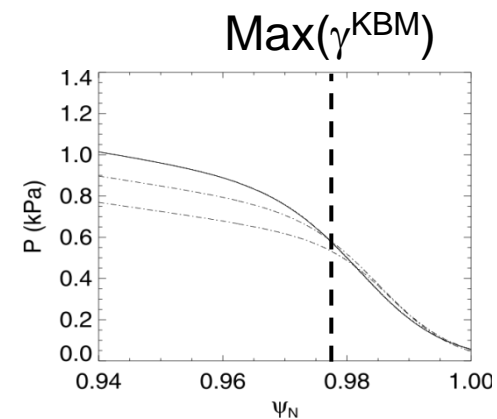
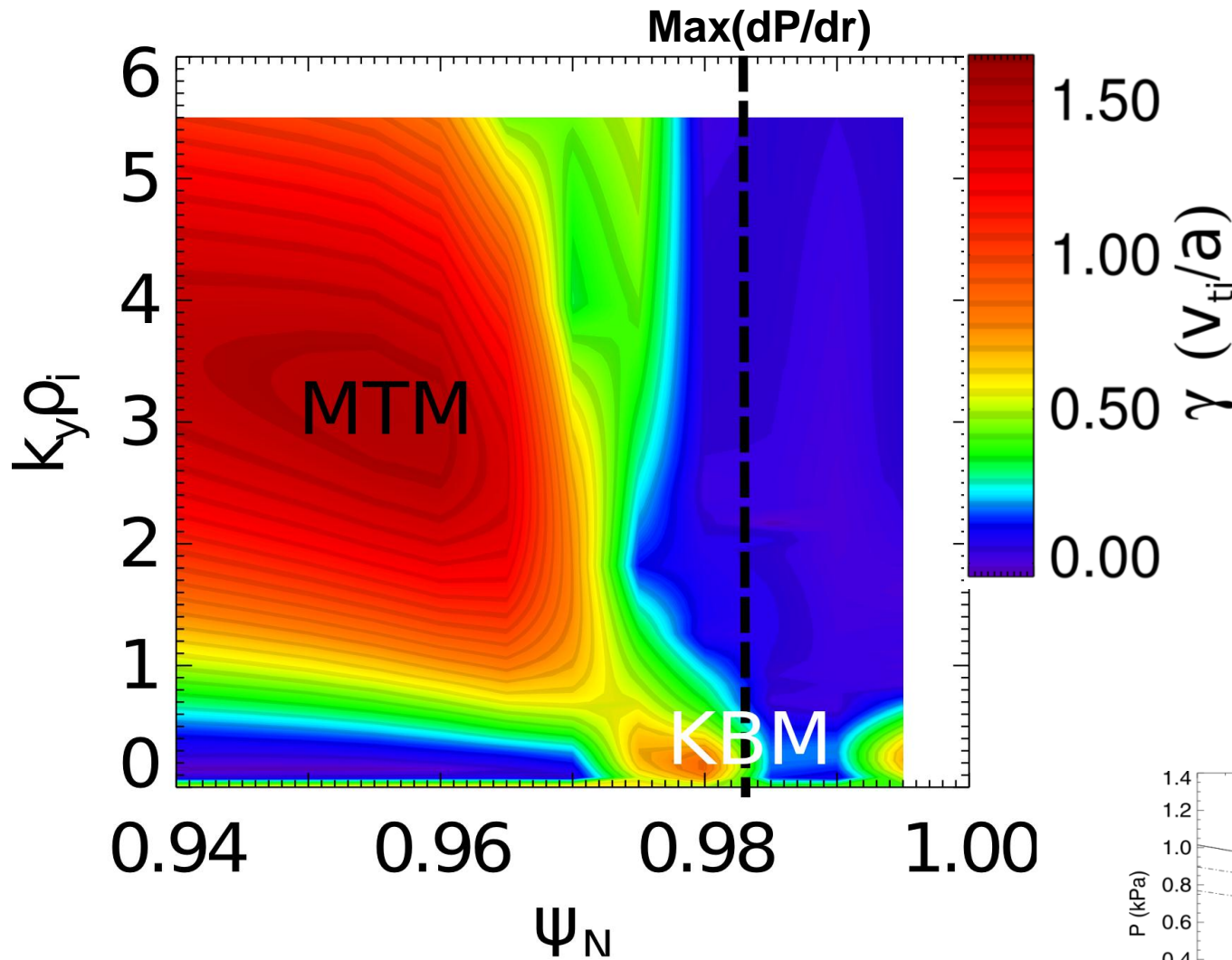
# 3: Microinstability Evolution Low $T_e^{\text{ped}}$ $t=0.3$



$\gamma_{\text{KBM}}$  increases at  $\psi_N=0.98$  as joins pedestal.

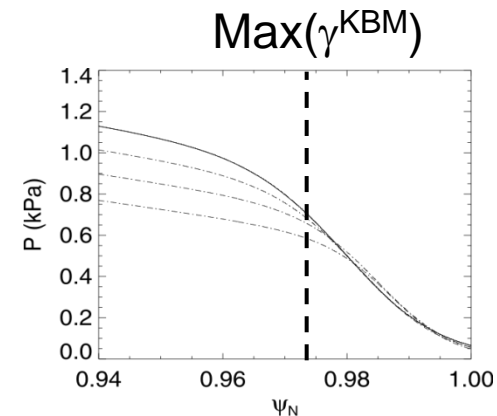
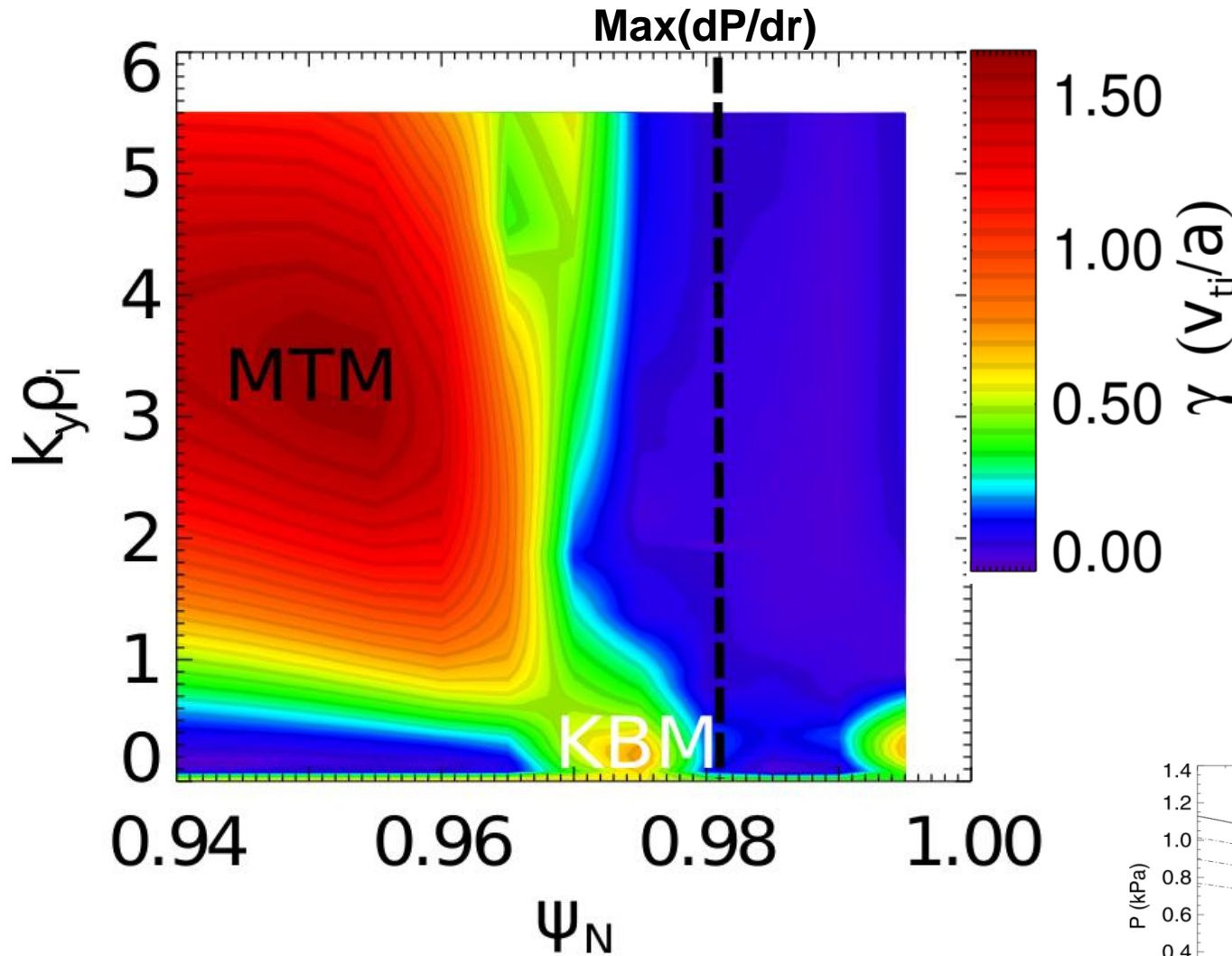


# 3: Microinstability Evolution Low $T_e^{\text{ped}}$ $t=0.5$



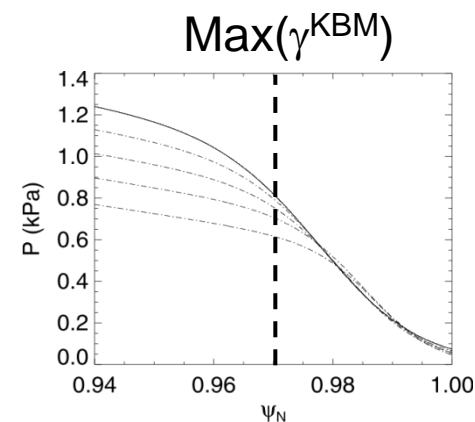
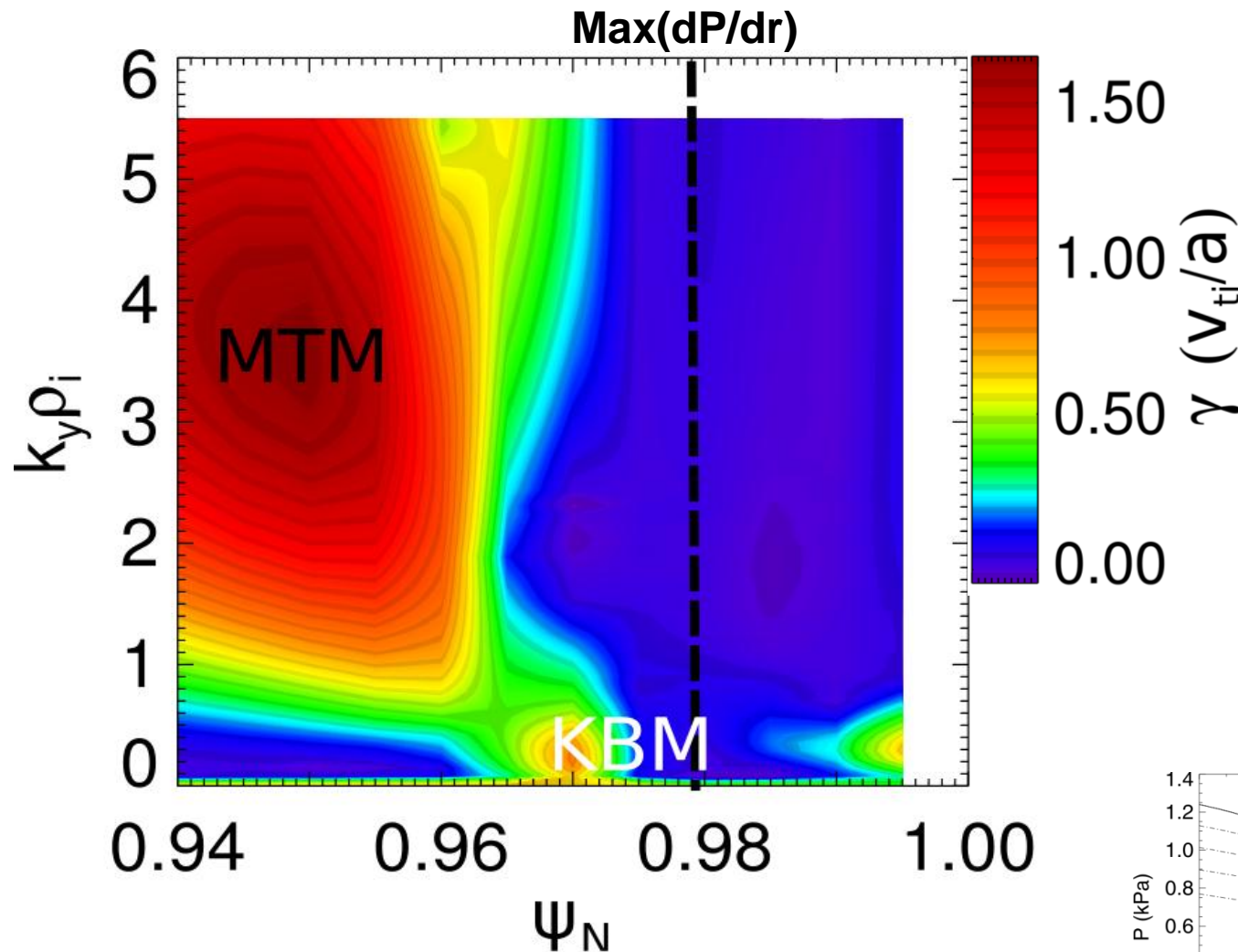
$\gamma_{\text{KBM}}$  falls at heart of the pedestal, e.g.  $\psi_N \sim 0.985$ .

# 3: Microinstability Evolution Low $T_e^{\text{ped}}$ $t=0.7$



MTM stabilised at  $\psi_N=0.97$  on joining pedestal

# 3: Microinstability Evolution Low $T_e^{\text{ped}}$ $t=0.9$



$\text{Max}(\gamma_{\text{KBM}})$  increasingly inboard of  $\text{Max}(dP/dr)$

# 3: Microinstability Evolution at High $T_e^{\text{ped}}$

MTMs dominate plateau

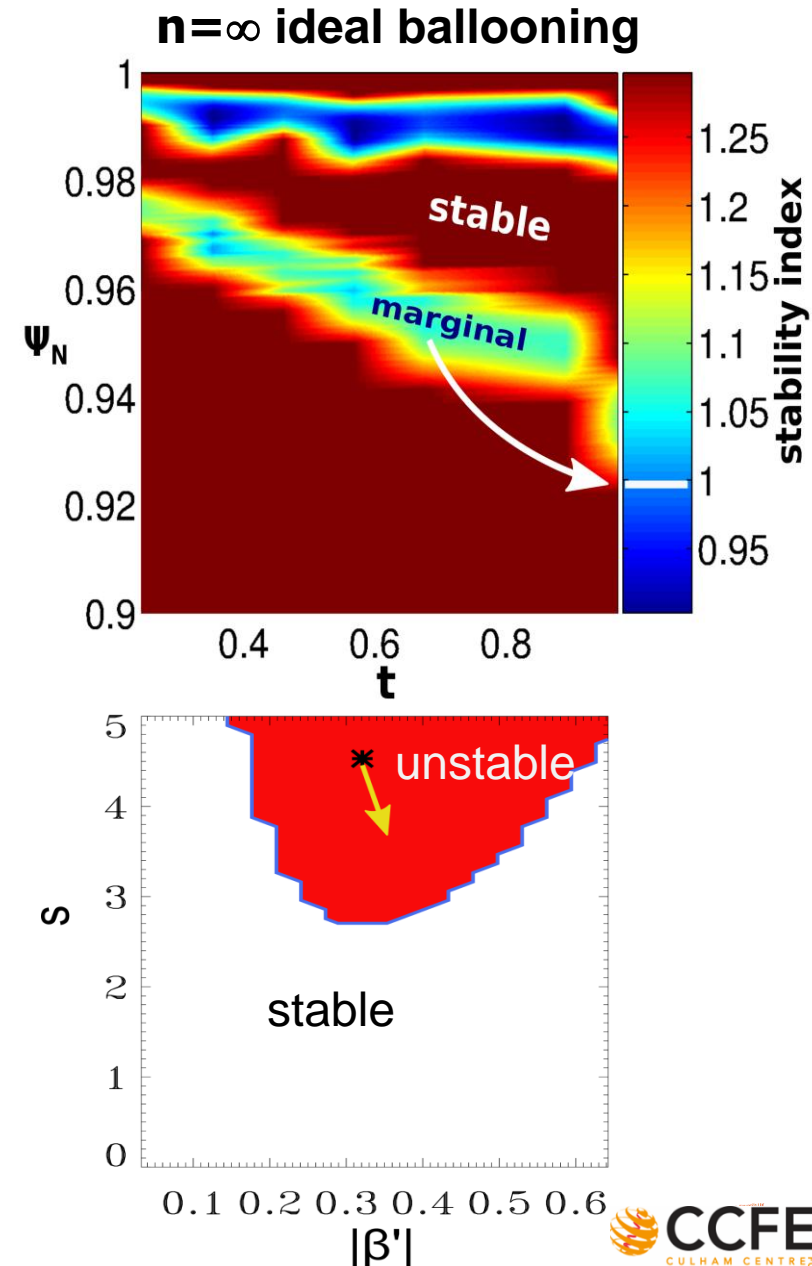
- $\gamma^{\text{MTM}} \uparrow \uparrow$  through ELM cycle.

KBMs at marginal stability on knee of P(r)

- **stable** in high  $T_e^{\text{ped}}$  pedestal

KBMs more stable in pedestal because:

- $J_{bs} \uparrow \Rightarrow$  magnetic shear  $s \downarrow$   
 $\Rightarrow$  approach/access 2<sup>nd</sup> stability
- high  $T_e^{\text{ped}}$  has stronger stabilisation as higher  $J_{bs}$  at lower collisionality

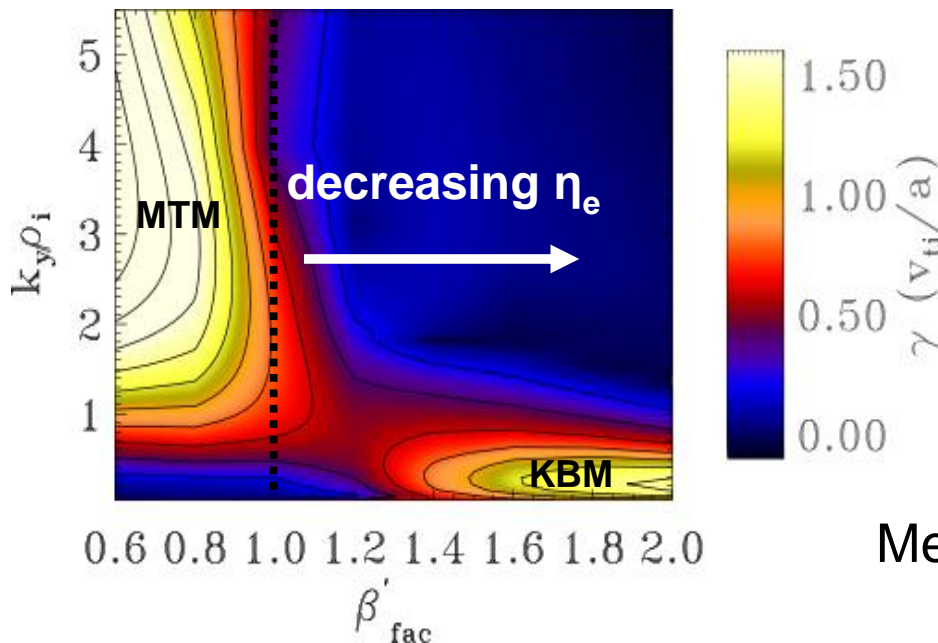
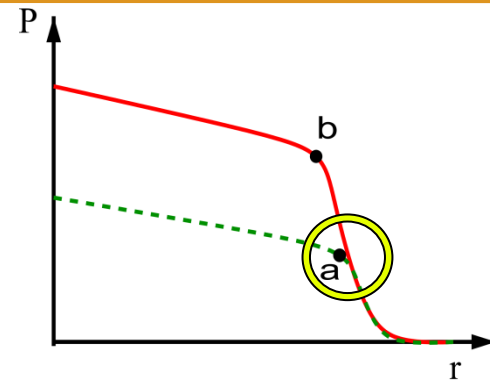




# 4. Why does Pedestal Expand Inwards?

Artificial scan to mimic pedestal advance on **a**

⇒ scale  $[\beta', R/L_{ne}]$  by  $\beta'_{fac}$  at fixed  $[n_e, T_{e,i}, R/L_{Te,i}]$   
 (motivated by measured profile evolution at **low  $T_e^{ped}$** )



MTMs stabilised by

- $R/L_{ne} \uparrow$  (disrupts MTM phases)
- $\beta' \uparrow$  (favourable drifts)

until....

- KBMs unstable at high  $\beta'_{fac}$

Mechanism may assist pedestal advance

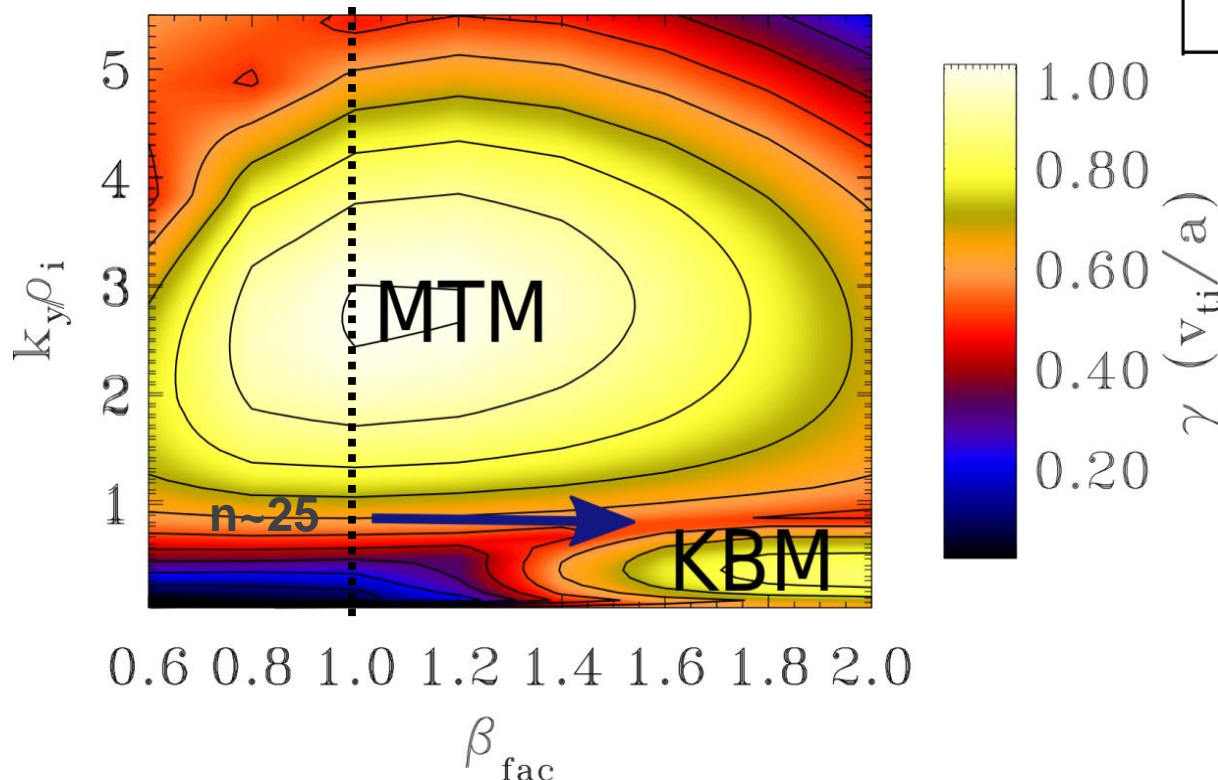
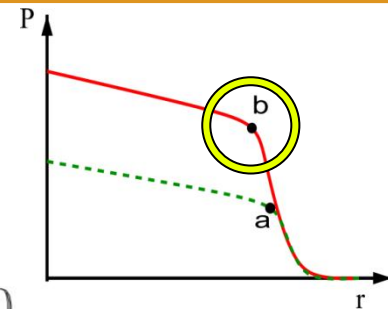
- $q_e^{MTM} \downarrow$ , allowing  $dP_e/dr \uparrow$

NB similar MTM/KBM transition also in **high  $T_e^{ped}$**

# 4. Limits to Inwards Pedestal Expansion?

Scans around **b** seek “equilibria” with interesting  $\mu$  stability

- scale [  $\beta$ ,  $n_e$  ] by  $\beta_{fac}$ , at fixed [  $dn_e/dr$ ,  $T_{e,i}$ ,  $R/L_{Te,i}$ ,  $v_e$  ]



Fully developed pedestal close to threshold where **KBM**s + **MTM**s are simultaneously strongly unstable over broad  $k_y$  range.

- breaching this limit would cause large change in edge transport.

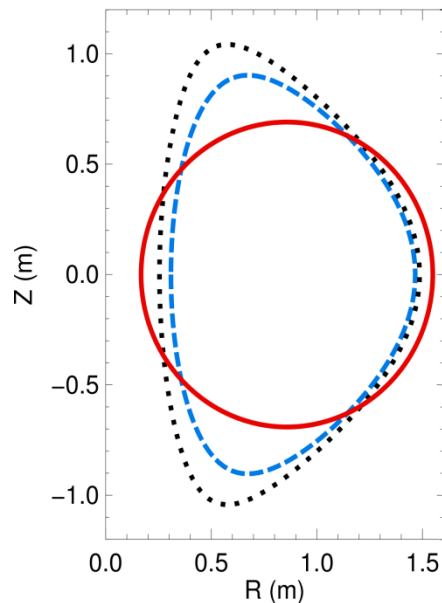
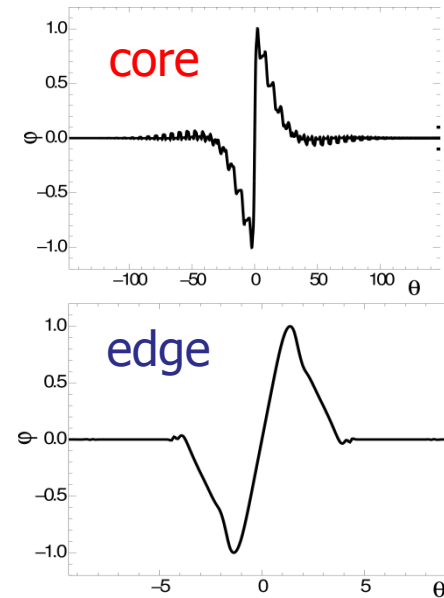
# 5. Exploring Mechanism for Edge MTMs

MTMs previously reported in **core** of STs, conceptual high performance devices, and conventional devices [1-6]

- drive mechanism poorly understood [1]

Investigate **edge** MTM to improve understanding [7]

- **edge** MTM  $\Phi$  efunc. less extended in  $\theta$ .



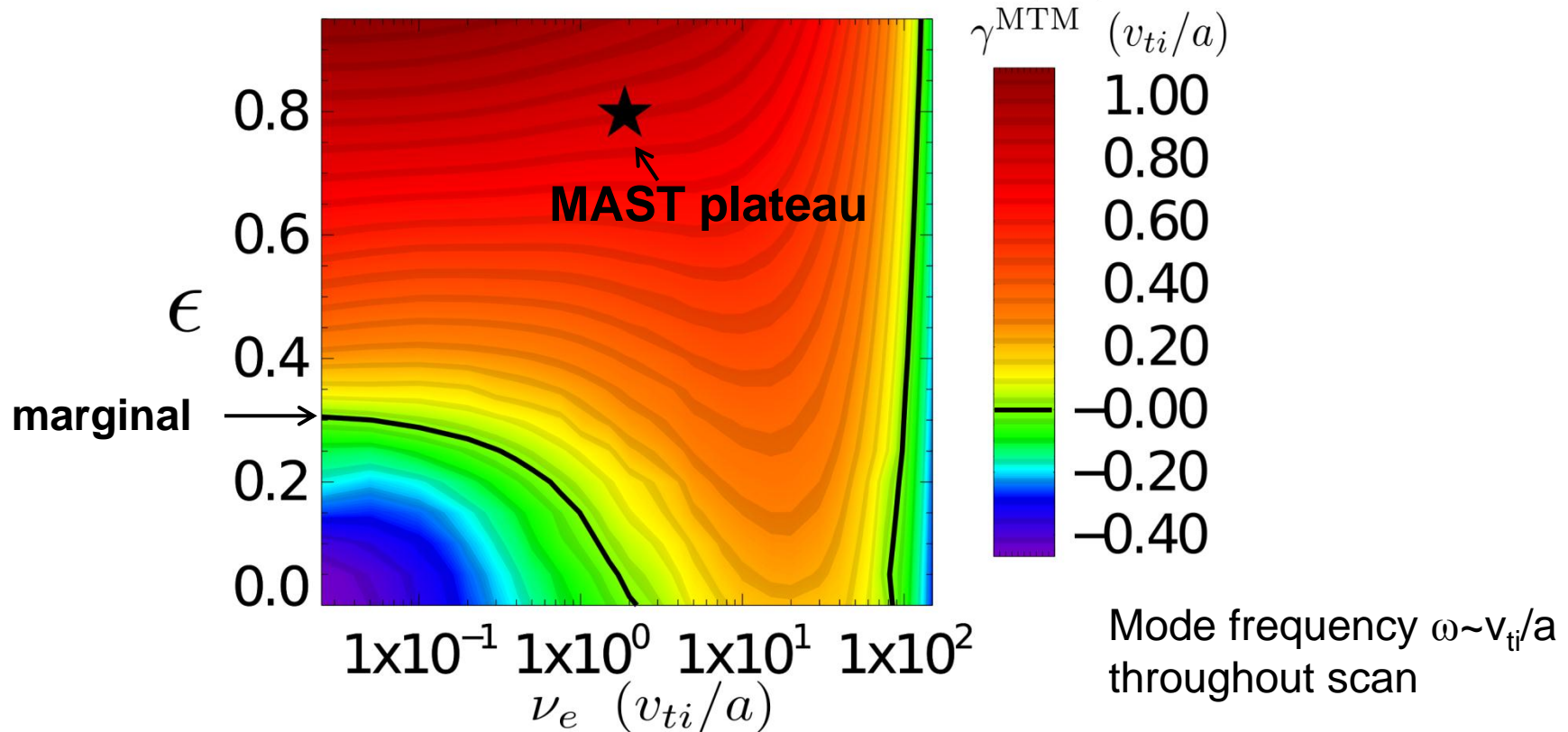
Circular  $s$ - $\alpha$  model fit to MAST edge

- unstable to similar MTMs
- convenient reference to study **edge MTM**

[1] Applegate *et al*, PPCF **19**, 1113, (2007) [4] Kotschenreuther *et al*, NF **40**, 677, (2000) [7] Dickinson *et al*, submitted to PPCF (2012) <http://arxiv.org/abs/1209.3695>  
[2] Applegate *et al*, PoP **11**, 5085, (2004) [5] Wilson *et al*, NF **44**, 917, (2004)  
[3] Wong *et al*, PoP **15**, 056108, (2008) [6] Told *et al*, PoP **15**, 102306, (2008)

# 5. Influence of Trapping and Collisions

Growth rate at peak of MTM spectrum,  $\gamma^{\text{MTM}}$ , versus  $\epsilon$ ,  $\nu_e$



High  $\epsilon$  (trapped fraction) is destabilising.

At **low**  $\epsilon$ ,  $\gamma^{\text{MTM}}$  peaks at **finite**  $\nu_e$ , and MTM **stable** at low  $\nu_e$

At **high**  $\epsilon$ ,  $\gamma^{\text{MTM}}$  **peaks** at low  $\nu_e$

Collisions not essential to **edge MTM** drive.

NB leading analytic theories require **finite**  $\nu_e$  [1,2] [1] Catto *et al*, Phys Fluids **24**, 243, (1981) [2] Drake *et al*, Phys Fluids **20**, 1341, (1977)

# 5. For More on Drive Study

See:

- Dickinson *et al*, submitted to PPCF (2012)  
<http://arxiv.org/abs/1209.3695>
- Poster TH5-1, Tomorrow am (Friday)

# 6. Conclusions

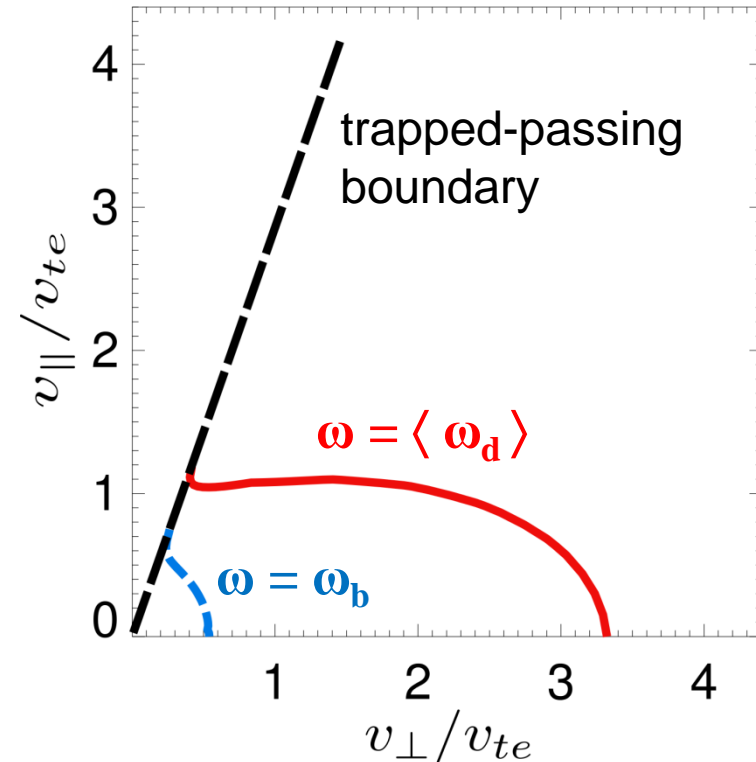
- Plasma profile evolution measured in MAST over ELM cycle:
  - steep  $dP/dr$ ,  $dn_e/dr^*$  form rapidly after ELM near separatrix, then advance into core \*and  $dT_e/dr$  at high  $T_e^{ped}$
- Local GK reveals corresponding microstability evolution,  $k_y \rho_i \sim O(1)$ 
  - MTMs dominate in plateau
  - KBMs most unstable near knee of pressure profile  
more stable\* in pedestal due to  $J_{bs}$  \*stable at high  $T_e^{ped}$
- MTM/KBM transition at knee
  - MTM stabilised by  $dn_e/dr \uparrow + dP/dr \uparrow$  until... KBM unstable.
  - transition may assist inwards advance of pedestal
  - knee of fully developed pedestal close to threshold where MTMs+KBMs are strongly unstable over broad  $k_y$  range
- Edge MTMs studied in simplified circular s- $\alpha$  model equilibrium
  - large  $\epsilon$  (or trapped fraction) is destabilising
  - at large  $\epsilon$  MTMs do not need finite  $v_e$



# 5. Comparing Frequencies\*

Mode frequency,  $\omega$ , compared with:

- trapped e bounce frequency,  $\omega_b$
- trapped e precession frequency,  $\langle \omega_d \rangle$

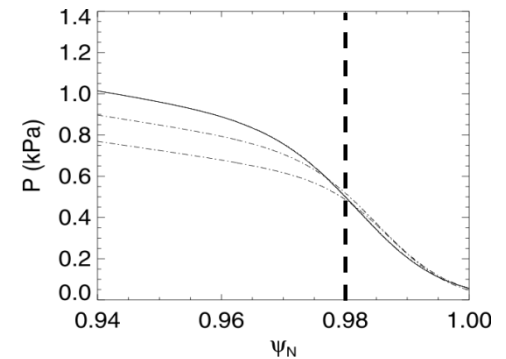


- $\omega \sim \langle \omega_d \rangle$  for thermal trapped electron  
 $\Rightarrow$  drift resonance?
- $\omega \sim O(\omega_b)$   
 $\Rightarrow$  bounce averaging unsuitable for trapped particle response



# Dominant Modes in Pedestal: KBMs

Consider dominant mode at  $t=0.5$ ,  $\Psi_n=0.98$ ,  
 $k_y \rho_i=0.218$

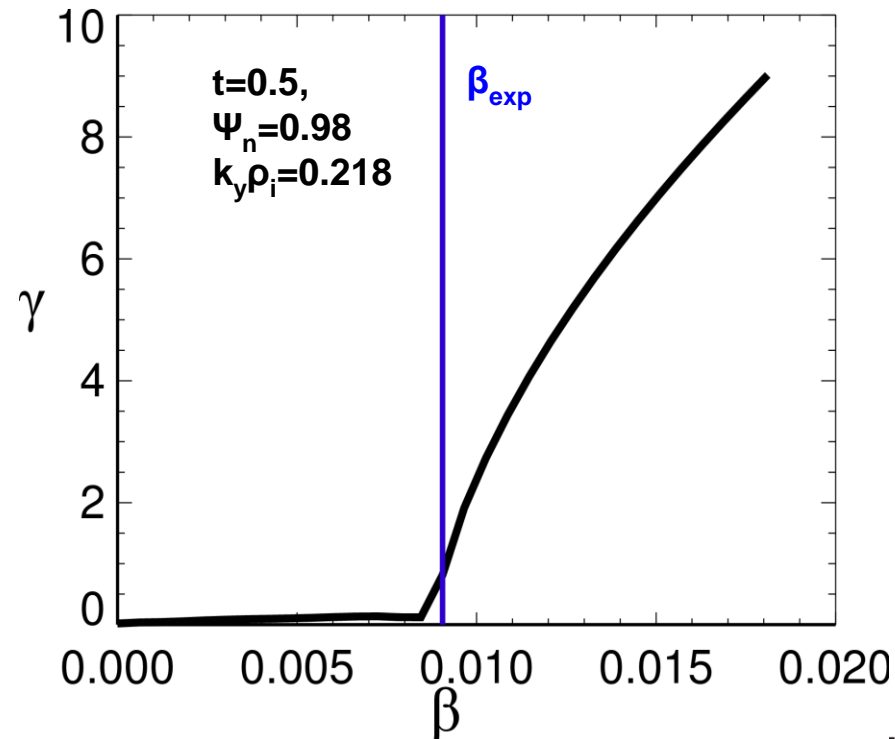


$\beta$  scan shows classic KBM signature

- $\beta_{\text{exp}} > \beta_{\text{crit}}$
- $\delta \mathbf{B}$  essential
- (electrostatic mode at low  $\beta$ )

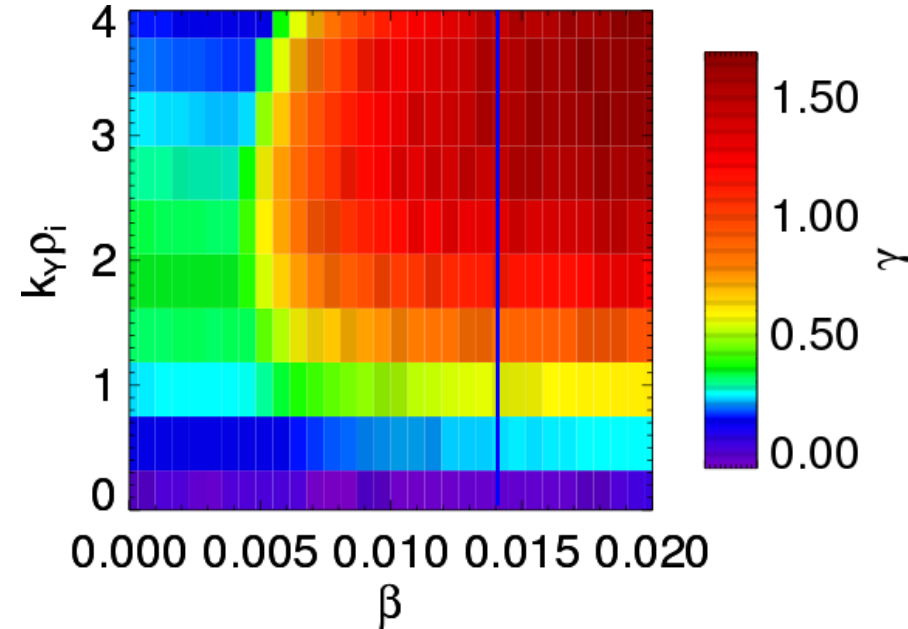
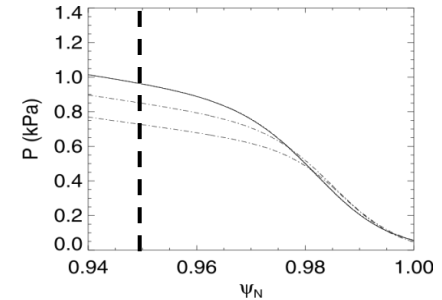
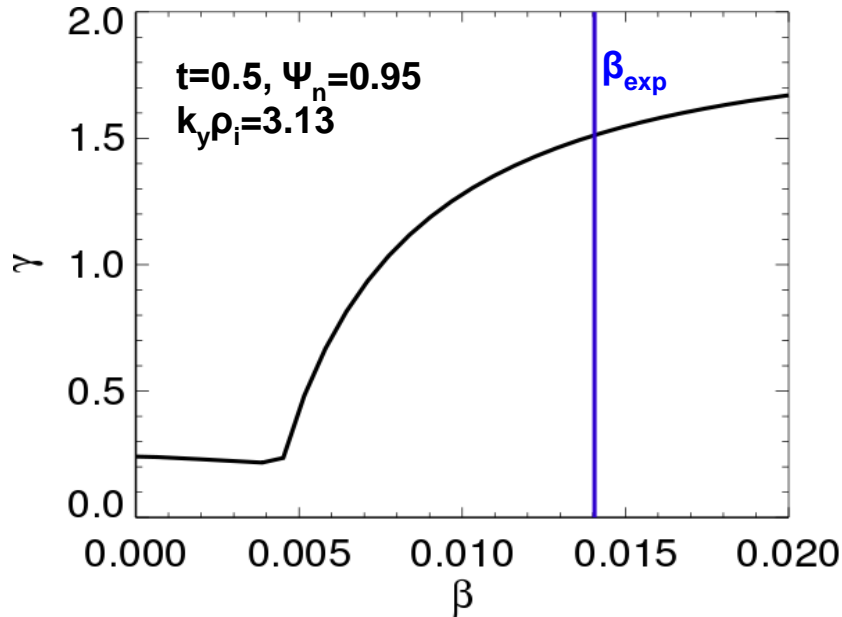
KBM driven by any source of  $dP/dr$ :

- $R/L_n$ ,  $R/L_{Te}$ ,  $R/L_{ti}$
- $\Rightarrow$  transport in all channels



# Dominant Modes in Plateau: MTMs

Consider dominant mode at  $t=0.5$ ,  $\Psi_n=0.95$ ,  $k_y\rho_i \sim 3$



$\beta$  scan reveals

- EM mode,  $\beta_{\text{exp}} \gg \beta_{\text{crit}}$
- (electrostatic mode at low  $\beta$ )

MTMs driven by  $R/L_{Te}$

- mainly electron heat transport

# Evolution of $\gamma$ Spectrum on Surfaces

